Exam 2: CS 6364 Fall 2015

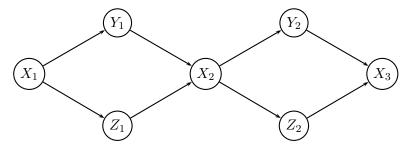
The exam is open book (Russell and Norvig, third edition) but not open notes/tablet/laptop. Answer the questions in the space provided on the question sheets. If you run out of room for an answer, use an additional sheet (available from the instructor) and staple it to your exam.

• NAME		
• UTD-ID if known		

Question	Points	Score
Bayesian Networks: Representation	10	
Bayesian Networks: Inference	10	
Particle Filtering and Bayes net Sampling	10	
Naive Bayes	10	
Perceptron	10	
Total:	50	

Question 1: Bayesian Networks: Representation (10 points)

Consider the Bayesian network given below:

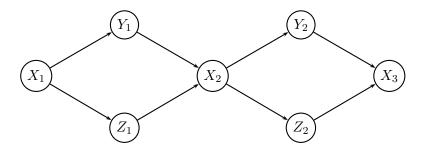


(a) (5 points) Is X_3 conditionally independent of X_2 given Y_2 ? Explain your answer. No credit without a correct explanation.

(b) (5 points) Is X_1 conditionally independent of X_3 given X_2 ? Explain your answer. No credit without a correct explanation.

Question 2: Bayesian Networks: Inference (10 points)

Consider the Bayesian network given below:



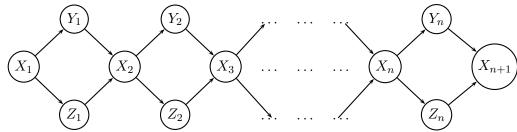
Assuming that all variables take values from the domain $\{0,1\}$, the conditional probability tables are given below:

	_						X_{i+1}	Y_i	Z_i	$P(X_{i+1} Y_i,Z_i)$	
$ Y_* P(Y_*) $	Y_i	X_i	$P(Y_i X_i)$	Z_i	X_i	$P(Z_i X_i)$	0	0	0	0.4	
$A_1 \mid I(A_1)$	0	0	0.3	0	0	0.2	0	0	1	0.1	
0 0.8	0	1	0.6	0	1	0.5	0	1	0	0.8	
$\begin{array}{c c c} X_1 & P(X_1) \\ \hline 0 & 0.8 \end{array}$	•		'	•	•		0	1	1	0.2	

where $i \in \{1,2\}$, which means that the CPT of $P(Y_2|X_2)$ is qualitatively equivalent to $P(Y_1|X_1)$, $P(Z_2|X_2)$ is qualitatively equivalent to $P(X_1|X_1)$ and $P(X_3|Y_2,Z_2)$ is qualitatively equivalent to $P(X_2|Y_1,Z_1)$.

(a) (5 points) Compute $P(X_1 = 1 | X_2 = 0)$ using the variable elimination algorithm. Show your work.

(b) (3 points) Consider the following generalization of the Bayesian network. For this question, assume that each variable can take d values.



What is the **optimal elimination order** for computing $P(X_1|X_{n+1}=x_{n+1})$ (here X_{n+1} is an evidence variable). Recall that an elimination order o is optimal if there does not exist an order o' such that running variable elimination along o' has smaller time and space complexity than running it along o.

(c) (2 points) What is the **time and space complexity** of variable elimination along the order you provided in your answer to the previous question. Assume that there are d values in the domain of each variable.

Question 3: Particle Filtering and Bayes net Sampling (10 points)

Consider the Bayesian network given below. The domains of the variables X, Y, Z and W are $\{+x, -x\}$, $\{+y, -y\}$, $\{+z, -z\}$ and $\{+w, -w\}$ respectively.



Let the CPTs be defined as follows:

ĺ	V	P(X)	X	Y	P(Y X)	Y	Z	P(Z Y)	W	Z	P(W Z)	
_	$\frac{\Lambda}{-x}$	$\frac{1}{3/4}$	-x	-y	2/3	-y	-z	1/4	-z	-w	1/8	1
l	-x	3/4	+x	-y	4/5	+y	-z	1/2	+z	-w	5/6	!

You are given the following 8 samples:

(a) (2 points) Assume that these samples came from performing **Prior Sampling**, and calculate the sample estimate of P(+w).

(b) (2 points) Now we will estimate P(+z|+x,-w). In the samples given above, clearly cross out the samples that would not be used when doing **Rejection Sampling** for this task, and write down the sample estimate of P(+z|+x,-w) below.

(c) (2 points) Now, we will use likelihood weighting to estimate P(-x|+y,-w). Suppose that the following samples are generated. Fill in the weight of each sample in the corresponding row.

1. Sample:
$$-x, +y, +z, -w$$
 Weight =

2. Sample:
$$+x, +y, +z, -w$$
 Weight =

3. Sample:
$$+x, +y, -z, -w$$
 Weight =

4. Sample:
$$-x, +y, -z, -w$$
 Weight =

(d) (2 points) From the weighted samples in the previous question, estimate P(-x|+y,-w).

(e) (2 points) Which query is better suited for likelihood weighting, P(W|X) or P(X|W)? Justify your answer in one sentence.

Question 4: Naive Bayes (10 points)

Consider the training data given below. Each feature F1, F2, F3 can take three values: $\{a, b, c\}$. The class variable (that you have to predict) can take two values $\{+, -\}$.

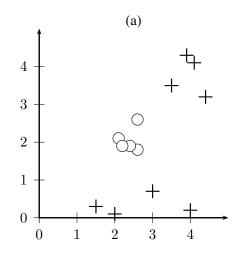
F	1	F2	F3	Class
á	ı	c	a	+
(2	a	c	+
	ı	a	c	_
ł)	c	a	_
(2	c	b	_

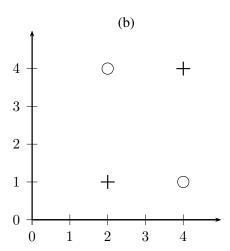
(a) (7 points) Build a Naive Bayes classifier for the above training data. **Use 1-laplace smoothing**. Precisely, show the structure of the network and the CPTs.

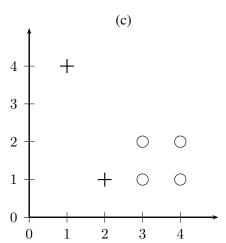
(b) (3 points) How would your Naive Bayes classifier classify the test example: (F1=a,F2=c,F3=b). Be sure to show your work.

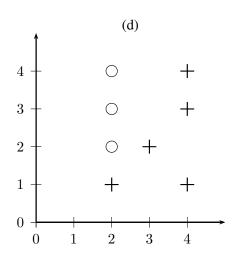
Question 5: Perceptron (10 points)

(a) (8 points) For each of the following four datasets, indicate whether a perceptron will have zero training error on the dataset. Also, explain why in one sentence or explain by drawing a decision boundary. No credit if the explanation is incorrect. The features are the x and y co-ordinates and the classes are indicated by " \circ " (negative class) and "+" (positive class) respectively.









- Explanation for (a):
- Explanation for (b):
- Explanation for (c):
- Explanation for (d):

(b) (2 points) Recall that the perceptron is an error-driven classifier while Naive Bayes is a probabilistic classifier. Given this, will the perceptron always have smaller training error as compared with the Naive Bayes classifier. True or False. Explain your answer.