Exercises given with a numbering are from  $Basic\ Analysis:\ Introduction\ to\ Real\ Analysis\ (Vol\ I)$  by J. Lebl.

## Reading Sections 0.3, 1.1, 1.2

## Exercises

- 1. Exercise 1.1.1
- 2. Exercise 1.1.2
- 3. Exercise 1.1.5
- 4. Exercise 1.1.6
- 5. Exercise 1.2.7
- 6. Exercise 1.2.9
- 7. Let

$$E = \{x \in \mathbb{R} : x > 0 \text{ and } x^3 < 2\}.$$

- (a) Prove that E is bounded above.
- (b) Let  $r = \sup E$  (which exists by part (a)). Prove that r > 0 and  $r^3 = 2$ . Hint: Adapt the proof used in Example 1.2.3.

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