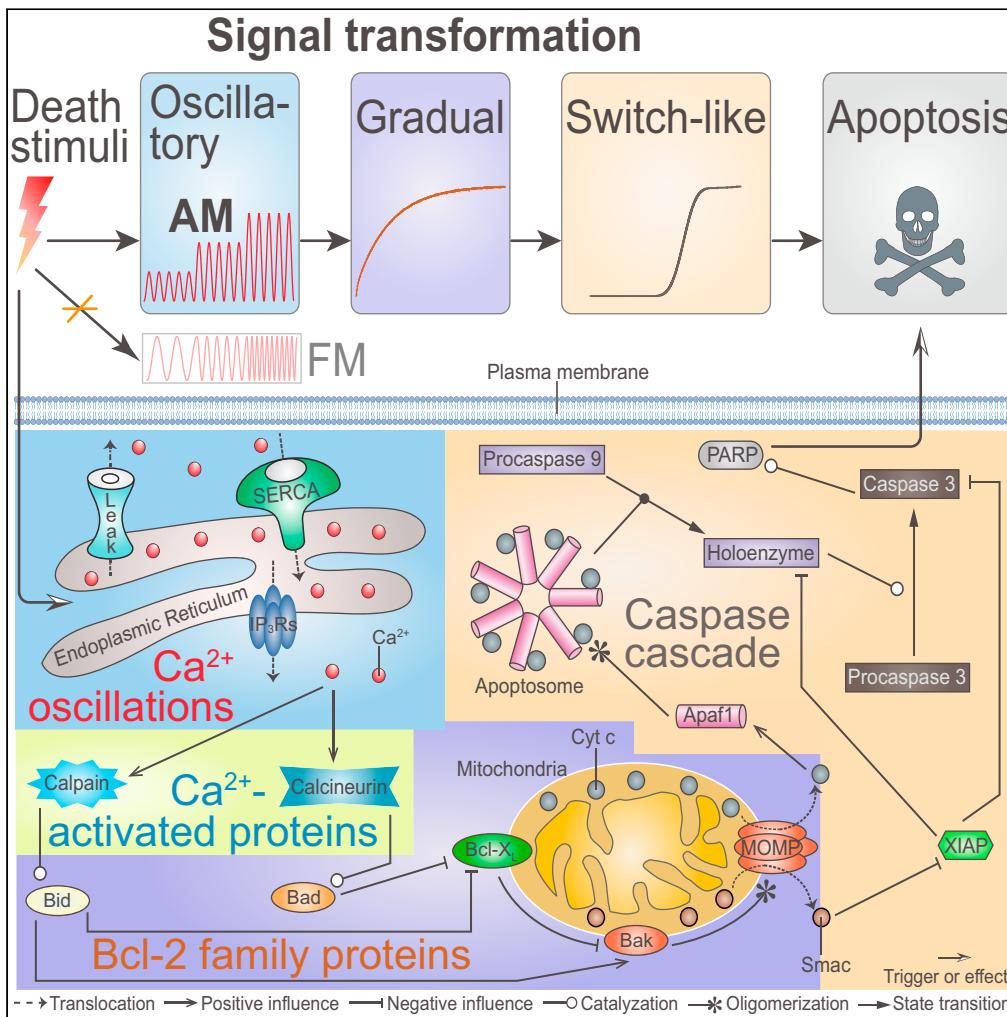


## Article

## The Oscillation Amplitude, Not the Frequency of Cytosolic Calcium, Regulates Apoptosis Induction



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**HIGHLIGHTS**  
A signaling network of cytosolic Ca<sup>2+</sup>-induced apoptosis is constructed

The network is converted into a mathematical model composed of four modules

Oscillatory signals first transform into gradual ones and then into switch-like ones

Ca<sup>2+</sup> regulates apoptosis mainly via amplitude, rather than frequency, modulation

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## Article

## The Oscillation Amplitude, Not the Frequency of Cytosolic Calcium, Regulates Apoptosis Induction

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## SUMMARY

Although a rising concentration of cytosolic  $\text{Ca}^{2+}$  has long been recognized as an essential signal for apoptosis, the dynamical mechanisms by which  $\text{Ca}^{2+}$  regulates apoptosis are not clear yet. To address this, we constructed a computational model that integrates known biochemical reactions and can reproduce the dynamical behaviors of  $\text{Ca}^{2+}$ -induced apoptosis as observed in experiments. Model analysis shows that oscillating  $\text{Ca}^{2+}$  signals first convert into gradual signals and eventually transform into a switch-like apoptotic response. Via the two processes, the apoptotic signaling pathway filters the frequency of  $\text{Ca}^{2+}$  oscillations effectively but instead responds acutely to their amplitude. Collectively, our results suggest that  $\text{Ca}^{2+}$  regulates apoptosis mainly via oscillation amplitude, rather than frequency, modulation. This study not only provides a comprehensive understanding of how oscillatory  $\text{Ca}^{2+}$  dynamically regulates the complex apoptotic signaling network but also presents a typical example of how  $\text{Ca}^{2+}$  controls cellular responses through amplitude modulation.

## INTRODUCTION

Calcium ion ( $\text{Ca}^{2+}$ ) is one of the most versatile and universal signaling agents to translate extra- and intracellular information into specific cellular outcomes (Berridge et al., 1998; Giorgi et al., 2018a). Upon stimulation,  $\text{Ca}^{2+}$  is released from the endoplasmic reticulum (ER) into the cytosol through inositol 1,4,5-trisphosphate receptor ( $\text{IP}_3\text{R}$ ) channels. Changes in cytosolic  $\text{Ca}^{2+}$  concentration ( $[\text{Ca}^{2+}]$ ) of a moderate level can govern a myriad of vital cell functions, including fertilization, proliferation, and differentiation, and are essential for cell survival (Berridge et al., 2003). However, excessive elevations of  $[\text{Ca}^{2+}]$  typically result in cell death, including apoptosis (Orrenius et al., 2003).

A cytosolic  $\text{Ca}^{2+}$  overload initiates the mitochondrial apoptotic pathway as follows.  $\text{Ca}^{2+}$  can activate calpain and calcineurin, causing the activation of BH3-only proteins (Chen et al., 2001; Wang et al., 1999). This results in the sequestering of anti-apoptotic Bcl-2 proteins and the activation of the pro-apoptotic effectors Bax and Bak (Czabotar et al., 2014; Youle and Strasser, 2008). These interaction patterns among Bcl-2 protein family culminate in Bax and Bak oligomerization and mitochondrial outer membrane permeabilization (MOMP) (Tait and Green, 2010). Subsequently, several apoptogenic factors are released from the mitochondrial intermembrane space, particularly cytochrome c (Cyt c) (Ow et al., 2008). In the cytosol, Cyt c engages Apaf1 and forms the apoptosome, which recruits caspase 9 and promotes caspase 3 activation. Active caspase 3 cleaves several hundred proteins, resulting in apoptosis (Shi, 2004). In addition, mitochondria retain cytosolic  $\text{Ca}^{2+}$  and this massive mitochondrial  $\text{Ca}^{2+}$  accumulation causes the opening of mitochondrial permeability transition pore, which leads to the Cyt c release and cell death (Qi and Shuai, 2016). Despite this detailed characterization of the molecular sequence of events, we still lack a comprehensive understanding of how  $\text{Ca}^{2+}$  dynamics control this complex apoptosis signaling network.

Differential equation modeling can simulate the dynamic output of individual proteins and can identify critical players in a signaling network, thus often providing novel insights to our understanding of cellular dynamics (Spencer and Sorger, 2011; Yao et al., 2016). Such modeling efforts have been devoted to understand intracellular  $\text{Ca}^{2+}$  dynamics (Dupont and Sneyd, 2017; Goldbeter et al., 1990; Li and Rinzel, 1994; Qi et al., 2015; Shuai and Jung, 2003; Sneyd et al., 2017) and the mechanistic details of the apoptotic pathway (Albeck et al., 2008; Anderson et al., 2019; Legewie et al., 2006; Qi et al., 2018; Rehm et al.,

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2006; Santos et al., 2019; Spencer and Sorger, 2011; Yin et al., 2017; Zhao et al., 2015). However, so far,  $\text{Ca}^{2+}$  signaling has not been mathematically integrated into models of apoptosis yet.

Two major types of  $\text{Ca}^{2+}$  temporal profiles have been reported in apoptotic cells, including a high plateau and oscillations (Boehning et al., 2003; Lee et al., 2010; Garcia et al., 2017). Oscillations of  $[\text{Ca}^{2+}]$  in individual cells often occur as repetitive spikes or sinusoid-like oscillations (Berridge, 1990; Oancea and Meyer, 1998). In our study, we focused on investigating how cytosolic  $\text{Ca}^{2+}$  oscillations, especially sinusoidal oscillations, regulate apoptosis from a network dynamics perspective.

Typically,  $\text{Ca}^{2+}$  oscillations occur with periods from seconds to minutes (Uhlén and Fritz, 2010), whereas the apoptotic program normally takes between a few and several tens of hours (Garcia et al., 2017; Márquez-Jurado et al., 2018). Owing to technical limitations in producing distinct long-term  $\text{Ca}^{2+}$  oscillations in experimental setups of apoptotic processes, the switch from a fast oscillatory  $\text{Ca}^{2+}$  signal to a switch-like apoptotic response with a long latency remains unclear.

$\text{Ca}^{2+}$  oscillations contain information in their amplitude and frequency, thus providing two ways to selectively activate downstream signaling pathways (Berridge, 1997; Parekh, 2011). It has been shown that some gene expression events (Li et al., 1998) and the activations of CaMKII (De Koninck and Schulman, 1998), PKC (Oancea and Meyer, 1998), and Ras (Kupzig et al., 2005), as well as ATP production (Hajnóczky et al., 1995), are regulated by the frequency of  $\text{Ca}^{2+}$  oscillations. These experimental observations, together with a well-known engineering principle that frequency modulation (FM) signaling is more precise than amplitude modulation (AM) signaling, have led to the prevailing view that  $\text{Ca}^{2+}$  controls cellular functions typically by an FM mode (Dupont and Combettes, 2016; Dupont and Sneyd, 2017; Goldbeter et al., 1990; Smedler and Uhlén, 2014). We have decided to investigate whether this is also the case during  $\text{Ca}^{2+}$ -induced apoptosis.

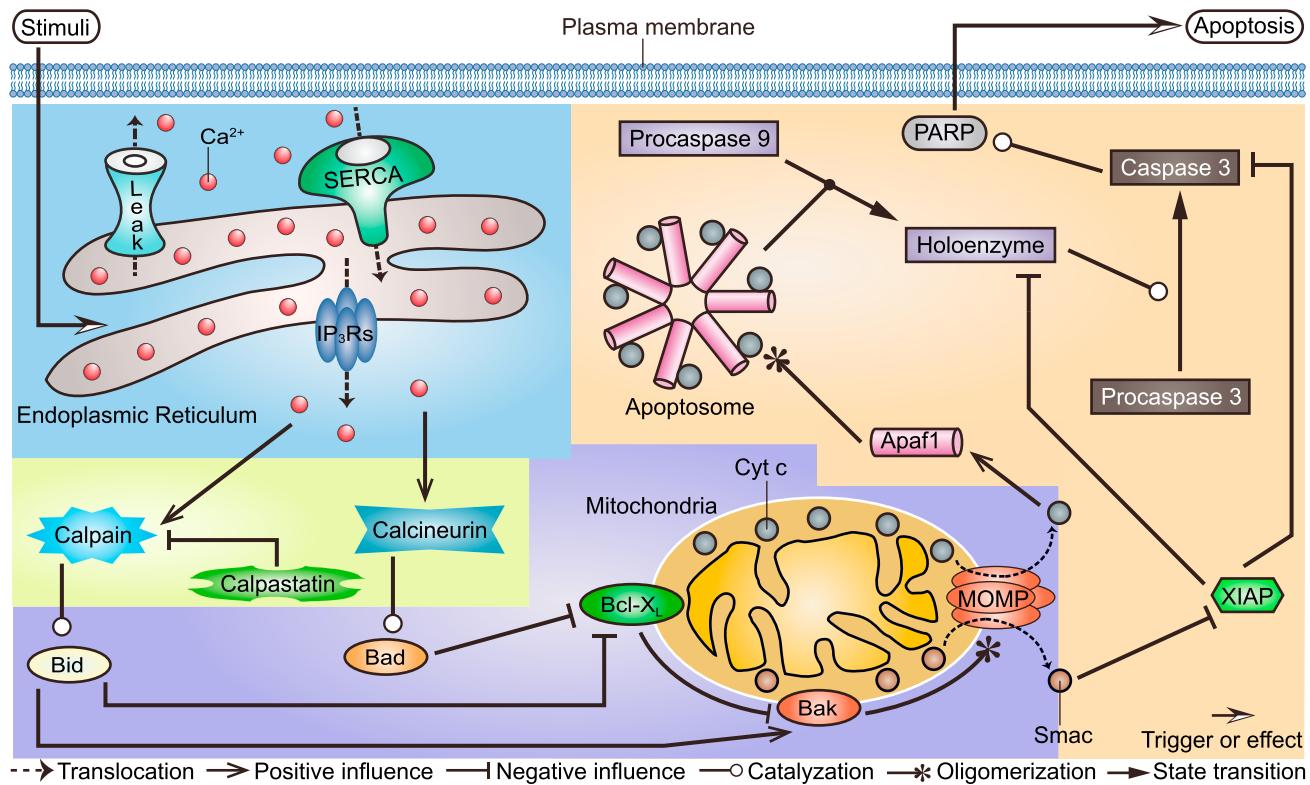
To solve these two basic issues, we constructed a four-module network model, including  $\text{Ca}^{2+}$  oscillations,  $\text{Ca}^{2+}$ -activated proteins, Bcl-2 family proteins, and Cyt c-induced caspase cascade. We transformed the biochemical reactions of the network into a set of ordinary differential equations (ODEs). The simulation results reveal that oscillatory  $\text{Ca}^{2+}$  signals will be first converted into gradual signals, i.e., the slowly and monotonically changed signals, and then be transformed into a switch-like apoptotic response. Furthermore, our results show that, with such converting processes,  $\text{Ca}^{2+}$  regulates apoptosis mainly through an AM mode, rather than through an FM mode. Our work provides crucial insight in the understanding of the modulatory role of  $\text{Ca}^{2+}$  signals on the apoptotic process.

## RESULTS

### Model Construction

A complete picture of the role of  $\text{Ca}^{2+}$  as a mechanistic trigger of apoptosis is still missing. Based on previous works (Albeck et al., 2008; Rehm et al., 2006) and our recent studies (Qi et al., 2018; Qi and Shuai, 2016; Yin et al., 2017), we developed an integrative signaling network comprising four modules (Figure 1): (1) ER-involved  $\text{Ca}^{2+}$  oscillations, (2)  $\text{Ca}^{2+}$ -activated proteins, (3) MOMP controlled by Bcl-2 family proteins on mitochondria, and (4) Cyt c-induced caspase cascade. The brief descriptions of each module are presented below (see details in *Supplemental Information*).

Extracellular stimuli result in the formation of  $\text{IP}_3$  (inositol 1,4,5-trisphosphate), which binds to the  $\text{IP}_3$  receptors ( $\text{IP}_3\text{Rs}$ ) to release  $\text{Ca}^{2+}$  from the ER. Cytosolic  $\text{Ca}^{2+}$  oscillations derive from three mechanisms of ions exchange between the ER and the cytoplasm:  $\text{IP}_3\text{Rs}$ -mediated  $\text{Ca}^{2+}$  release from the ER into the cytosol, SERCA (sarco/ER  $\text{Ca}^{2+}$ -ATPase)-dependent  $\text{Ca}^{2+}$  uptake from the cytosol into the ER, and  $\text{Ca}^{2+}$  leakage from the ER into the cytosol (Shuai and Jung, 2003). An important machinery linking cytosolic  $\text{Ca}^{2+}$  signal and apoptosis is the activation of two  $\text{Ca}^{2+}$ -regulated enzymes, i.e., calpain and calcineurin. In the presence of high  $[\text{Ca}^{2+}]$ , calcineurin dephosphorylates Bad, thus allowing Bad to inhibit the anti-apoptotic Bcl-X<sub>L</sub> (Wang et al., 1999). Calpain, which is normally inhibited by calpastatin (Hanna et al., 2008), cleaves Bid to form truncated Bid (tBid), which in turn can directly activate Bak or inhibit Bcl-X<sub>L</sub> that then indirectly activates Bak (Chen et al., 2001). Active Bak monomers form oligomers to trigger MOMP. Following MOMP, Smac and Cyt c are released from the mitochondria into the cytosol. In the cytosol, Cyt c binds Apaf1 to form the heptameric apoptosome, which interacts with procaspase 9 to induce the formation of holoenzyme, thereby triggering caspase 3 activation (Li et al., 2017). Caspase 3 can cleave a series of substrates



**Figure 1. Model Topology Scheme**

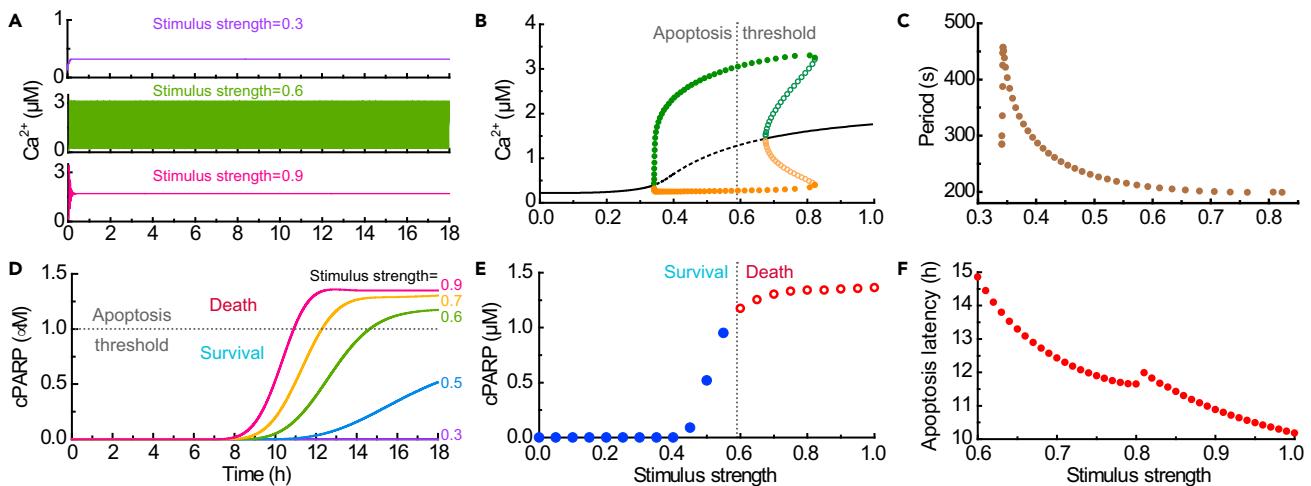
The four modules are highlighted by different background colors. The blue region is for the module of  $\text{Ca}^{2+}$  oscillations, the green for the module of  $\text{Ca}^{2+}$ -activated proteins, the purple for the module of MOMP controlled by Bcl-2 family proteins, and the yellow for the module of the Cyt c-induced caspase cascade. More details can be found in the main text.

(a process represented in the model by cleavage of PARP to form cPARP [Albeck et al., 2008]) and orchestrate the demolition of the cell. Smac assists this function by neutralizing the caspase inhibitor XIAP.

Using well-established kinetics approaches (Anderson et al., 2019; Qiao et al., 2019; Zhang et al., 2011), we translated these biochemical processes into a set of ODEs. Every variable represents the amount or concentration of a molecular species, which is dynamically controlled by the combination of all processes that increase and decrease the level of that particular molecular species. Each process is described by chemical kinetics, i.e., the mass action law or Hill function. The ODEs are numerically solved and the total simulation time was set to 18 h, the typical length of cell cycle (Spiller et al., 2010), reflecting the fact that a cell ultimately adopts one of two fates, either to survive by cell division or to die by apoptosis at the end of 18 h. In our model we assumed that the cell fate depends on the concentration of cleaved PARP ( $[\text{cPARP}]$ ) within 18 h. A detailed description of all biochemical reactions, ODEs, and parameters is provided in [Transparent Methods](#).

### Dynamics of $\text{Ca}^{2+}$ and cPARP

The simulation results we obtained are qualitatively consistent with the reported dynamics of  $\text{Ca}^{2+}$  (Dupont and Goldbeter, 1993; Gerasimenko et al., 2002; Jacob et al., 1988; Scorrano et al., 2003) and cPARP (Albeck et al., 2008; Rehm et al., 2006; Spencer and Sorger, 2011) upon incubation with apoptotic triggers. In many cell types,  $\text{Ca}^{2+}$  oscillations occur within an appropriate range of stimulus levels (Dupont and Goldbeter, 1993; Jacob et al., 1988). The time course plot (Figure 2A) and bifurcation diagram, i.e., the maximal and minimal value of  $\text{Ca}^{2+}$  oscillations (Figure 2B) show that, as the stimulus strength increases, the cytosolic  $\text{Ca}^{2+}$  changes from a stationary to an oscillatory behavior, before returning to a stationary state. The oscillation period is about 200 s (Figure 2C), as seen both in healthy and apoptotic cells (Gerasimenko et al., 2002; Scorrano et al., 2003). To define the apoptotic cell from the healthy cell, we proposed that apoptosis occurs when  $[\text{cPARP}]$  is above the apoptosis threshold of  $1.02 \mu\text{M}$ , a value that corresponds to 60% substrate cleavage (dotted line in Figure 2D). This result agrees with the experimental result that apoptosis



**Figure 2. The Dynamical Behavior of  $\text{Ca}^{2+}$  and cPARP at Different Stimulus Strengths**

- (A) Different kinetic behaviors of  $\text{Ca}^{2+}$  in response to different stimuli lasting for 18 h.
- (B) Bifurcation diagram of  $\text{Ca}^{2+}$  in response to different stimuli. Solid/dashed lines represent stable/unstable fixed point; filled/empty circles represent minimal (orange) and maximal (green)  $[\text{Ca}^{2+}]$  during a stable/unstable oscillation.
- (C) Periods of  $\text{Ca}^{2+}$  oscillations within the stable oscillation range.
- (D) The kinetic behavior of cPARP responding to different stimuli.
- (E and F) The final [cPARP] (E) and the apoptosis latency (F) at different stimulus strengths. The dotted lines in (B), (D), and (E) depict the apoptosis threshold.

is triggered only when the level of substrate cleavage exceeds a high value (Rehm et al., 2006). Accordingly, when the multiple maximal concentration of sustained  $\text{Ca}^{2+}$  oscillations exceeds a critical threshold of about 3  $\mu\text{M}$  (Figure 2B), apoptosis is initiated, which is compatible with the experimental observation for  $[\text{Ca}^{2+}]$  under resting conditions and after stimulation (Giorgi et al., 2018b). Figure 2D also shows that the latency from the exposure to the apoptotic stimulus to the actual initiation of apoptosis is about 10 h, but the cleavage of PARP is sudden and switch-like, again in agreement with experimental observation (Albeck et al., 2008; Spencer and Sorger, 2011). The reasons for the selection of critical threshold of  $[\text{Ca}^{2+}]$  and [cPARP] are detailed in [Supplemental Information](#).

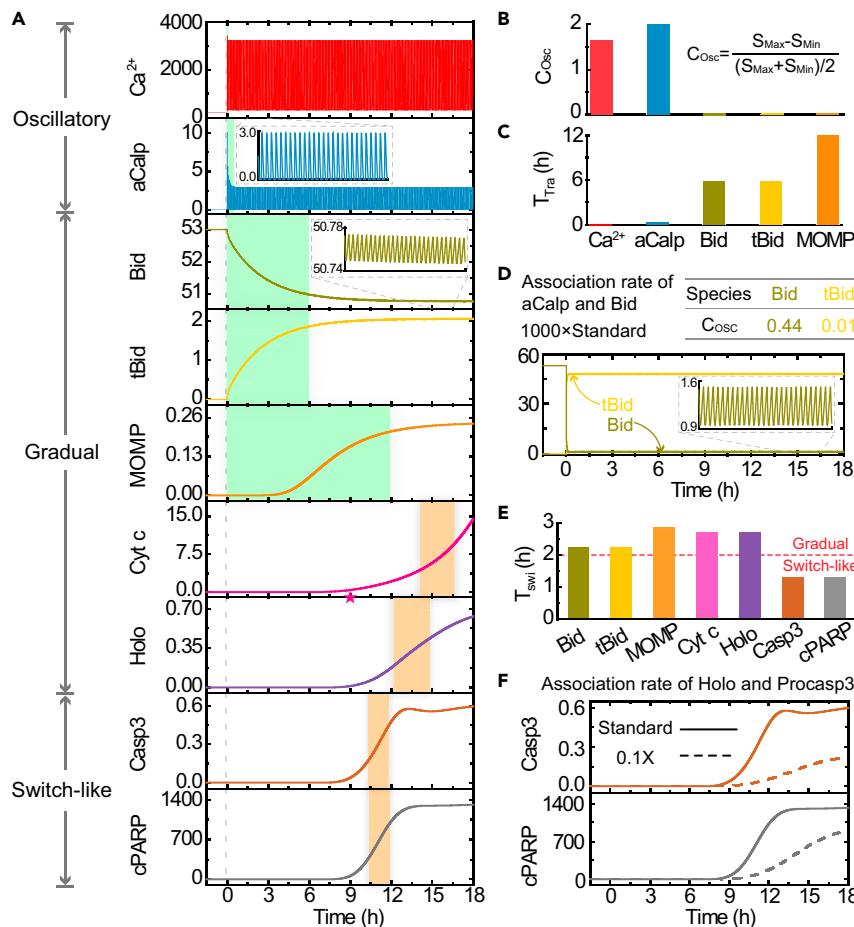
It should be pointed out that, in order to provide a global view of the dynamical behavior of the system, the bifurcation diagram of  $\text{Ca}^{2+}$  is obtained mathematically with the steady states of the system (Figure 2B). However, considering the biological fact that a cell ultimately commits to apoptosis or to division at a limited time duration, we simply limited the discussion of the cell fate within 18 h for all the simulation results.

### Two Indexes for Apoptosis

The relationship between the stimulus strength and the corresponding final [cPARP] yields an ultrasensitive signal-response curve (Figure 2E). Here [cPARP] at 18 h is defined as the final [cPARP], which is used as an index for cell fate. In detail, the fate of a cell is survival if the final [cPARP] < 1.02  $\mu\text{M}$ ; otherwise, the apoptosis process is initiated. This result is insensitive to the variations in the cell cycle, i.e., total simulation time (Figure S2C). If apoptosis is triggered, another index, i.e., the apoptosis latency is introduced to evaluate how quickly apoptosis can be induced. In other words, it measures the interval between the time when the stimulus is applied and the time when the increasing [cPARP] crosses the apoptosis threshold of 1.02  $\mu\text{M}$ . As shown in Figure 2F, the stronger the stimulus intensity is, the shorter the apoptosis latency becomes.

### Signal Transduction

Given the different dynamics of  $\text{Ca}^{2+}$  and cPARP (Figures 2A and 2D), it is curious how the fast oscillatory  $\text{Ca}^{2+}$  signal is converted into a slow but switch-like apoptotic signal. To address this question, we analyzed the time series of the main reaction species along the reaction pathway (Figure 3A). These species include  $\text{Ca}^{2+}$ , aCalp (activated calpain), Bid, tBid, MOMP, Cyt c, holoenzyme, caspase 3, and cPARP. According to the kinetic patterns of these species, we observed that the oscillatory patterns starting with  $\text{Ca}^{2+}$  signal first become gradual for proteins such as Bid, and then become switch-like for proteins such as caspase 3.



**Figure 3. Transition from Oscillatory to Switch-like Kinetics**

(A) Time courses of the main species in the signaling network. The vertical dashed line indicates the time at which the stimulus (strength = 0.73) is introduced. The green and orange shaded regions denote the transient time and the switch time, respectively. The time at which mitochondrial Cyt c begins to release into the cytosol is marked by an asterisk. (B and C) (B) Oscillation coefficient ( $C_{Osc}$ ) and (C) transient time ( $T_{Tra}$ ) of five upstream species.  $S_{Max}$  and  $S_{Min}$  are the maximal and minimal concentrations of a certain species at the steady state, respectively. (D) Time series and  $C_{Osc}$  of Bid and tBid with the association rate of aCalp and Bid increased by 1,000-fold. (E) Switch time ( $T_{Swi}$ ) of gradual and switch-like signals. The horizontal dashed line at 2 h is applied to distinguish the switch-like signals from the gradual ones. (F) Time series of Casp3 and cPARP when the association rate of holoenzyme and procaspase 3 is decreased by 10% (broken lines). The results obtained under standard parameter are the same as in (A) and are shown to facilitate comparison. The insets in (A) and (D) show representative time courses of 1.5 h. The units of y axes in (A), (D), and (F) are nM. Abbreviation: aCalp, activated calpain; Holo, holoenzyme; Casp3, caspase 3.

As shown in Figure 3A, the transition from oscillatory to gradual pattern involves two changes. First, the oscillation amplitudes of the upstream species become successively smaller. In detail, it is about 3,000 nM for  $\text{Ca}^{2+}$ , nearly 3 nM for aCalp, only 0.03 nM for Bid and tBid, and barely perceptible for MOMP. To compare the oscillation strength among different species with a uniform standard, an oscillation coefficient, which is the ratio of oscillation amplitude to mean (looks like the deterministic version of the coefficient of variation), is calculated (Figure 3B). As a consequence, the oscillation coefficients of  $\text{Ca}^{2+}$  and aCalp are far larger than those of Bid, tBid, and MOMP. Here we define a signal as oscillatory if the oscillation coefficient of a species is larger than 0.1. Accordingly, the signals of Bid, tBid, and MOMP are not considered oscillatory. Second, upon stimulation, the system transitions from a resting steady state to a new equilibrium state, generating a transient time, which is defined as the time required for oscillatory species to reach steady oscillation or for other species to reach 90% of their peaks. As a result, the transient times for  $\text{Ca}^{2+}$ , aCalp, Bid, tBid, and MOMP are about 0.1, 0.5, 6, 6, and 12 h, respectively (Figure 3C), becoming successively longer. Compared with the length of cell cycle (18 h), a transient

time longer than 6 h is a duration that is not negligible. Therefore, we suggest that such a non-oscillatory signal with long transient time should be labeled as gradual. According to the oscillation coefficient and transient time, we therefore classify  $\text{Ca}^{2+}$  and aCalp as oscillatory signals and Bid, tBid, and MOMP as gradual signals.

Obviously the most dramatic change in the kinetics from  $\text{Ca}^{2+}$  to MOMP occurs upon the truncation of Bid by aCalp. The result of parameter sensitivity analysis also shows that this step indeed exerts a substantial influence on the output of the system (Figure S2B). Interestingly, the kinetics of Bid owns two distinct timescales. On the one hand, Bid oscillates at a fast timescale of around 200 s. On the other hand, a gradually decreasing trend occurs for Bid in a slower timescale of about 6 h as a transient process (Figure 3A). Meanwhile, the oscillation amplitude is far smaller than the mean value of its steady oscillations. This is mainly due to the slow truncation reaction of Bid by aCalp, which directly results in a long transient time and also generates a small oscillation amplitude for Bid by averaging aCalp over a long duration with slow association rate of aCalp with Bid ( $5 \times 10^{-6} \text{ nM}^{-1}\text{s}^{-1}$ ). If this rate is increased 1,000-fold, Bid will achieve its new equilibrium very quickly and its oscillation coefficient will be 0.44 (Figure 3D), thus becoming an oscillatory signal. The slow truncation of Bid by aCalp, therefore, plays a significant role to convert the oscillatory signals to gradual signals in this pathway.

The kinetics from Bid to cPARP (Figure 3A) shows a transition from a gradual pattern to a switch-like pattern. Here, we distinguish a switch-like signal from gradual signal according to their switch time, which is defined as the time it takes to progress from a 30% to a 70% final concentration of any reaction species. If its switch time is longer than 2 h, it is labeled a gradual signal; otherwise, it is labeled a switch-like signal. According to this classification, Bid, tBid, MOMP, Cyt c, and holoenzyme are gradual signals, whereas caspase 3 and cPARP are switch-like signals (Figure 3E). If the switch time is defined as the time for a signal to increase from 20% to 80% of its final value, similar results are obtained, albeit with a longer switch time.

As a gradual signal, the MOMP-released Cyt c leads to a gradual accumulation of the apoptosome and thus the holoenzyme. In detail, before MOMP accumulates to reach a threshold, Cyt c cannot be released, thus maintaining Cyt c and downstream signals in an "off" state. After MOMP reaches the threshold at about 9 h (marked by asterisk in Figure 3A), the Cyt c-induced holoenzyme assembly ensures the downstream signals switch to an "on" state.

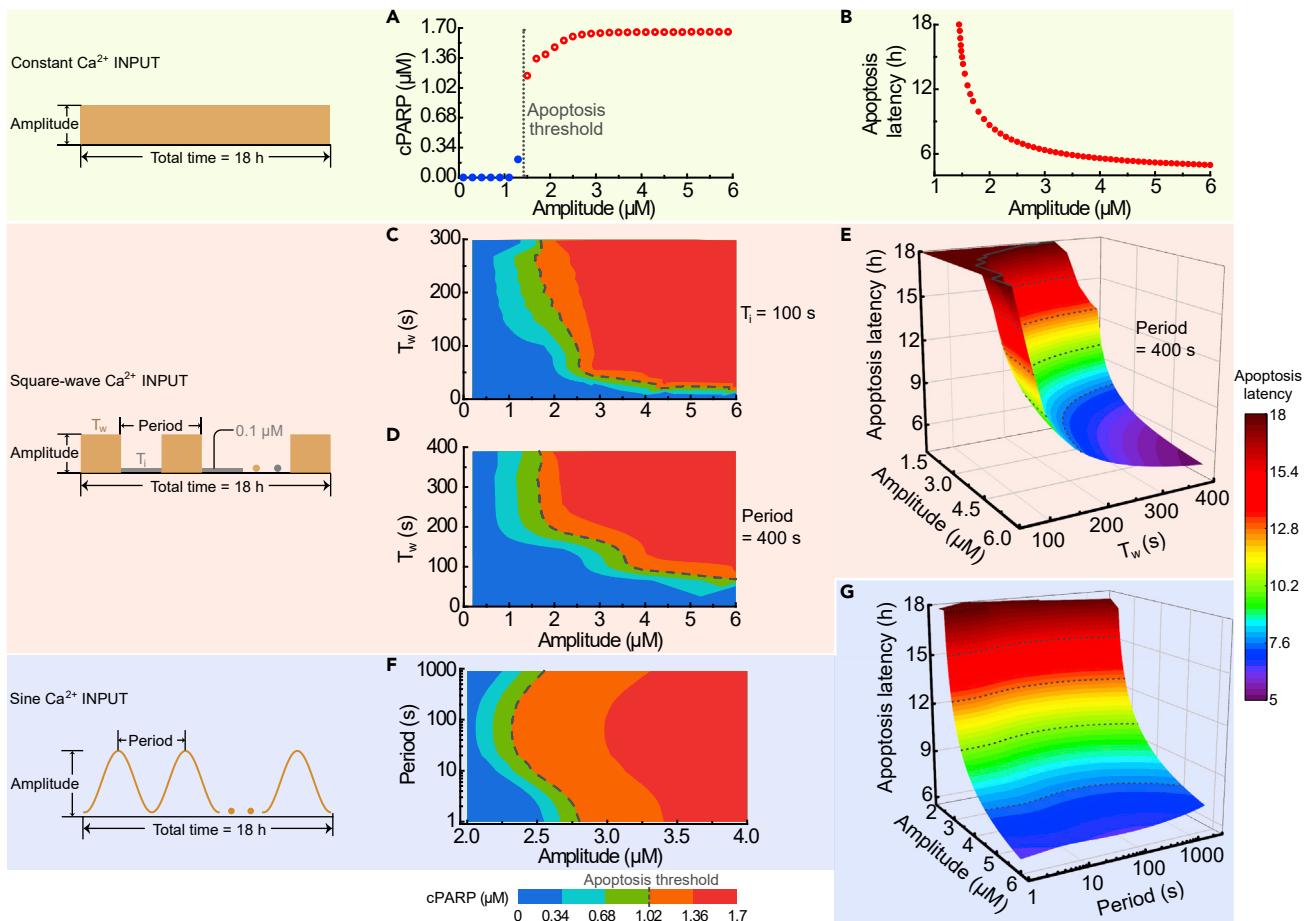
The conversion from gradual to switch-like signals is regulated by multiple reactions, including the mechanics of MOMP assembly, mitochondria-to-cytosol translocation of Smac and Cyt c (Albeck et al., 2008), the direct repression of holoenzyme and caspase 3 by XIAP (Figure S3), and holoenzyme-mediated activation of caspase 3. As seen in Figure 3A, holoenzyme activation results in a sudden and rapid cleavage of caspase 3 and thus the processing of PARP into cPARP, suggesting that the conversion from gradual to switch-like signals is strongly influenced by the interaction between holoenzyme and pro caspase 3. If the association rate of holoenzyme and pro caspase 3 ( $1.0 \mu\text{M}^{-1}\text{s}^{-1}$ ) is decreased to 10%, the original switch-like signals, i.e., caspase 3 and cPARP, will become gradual signals (Figure 3F). Thus, the holoenzyme-mediated activation of caspase 3 has a crucial influence on the conversion from gradual into switch-like signals.

### Three Ideal $\text{Ca}^{2+}$ Inputs

Since both the amplitude and frequency of the ER-involved  $\text{Ca}^{2+}$  oscillations largely increase with stimulus strength (Figures 2B and 2C), it is hard to dissect the individual contributions of amplitude and frequency to apoptosis. To explore whether amplitude or frequency of  $\text{Ca}^{2+}$  oscillations is the critical determinant for  $\text{Ca}^{2+}$ -induced apoptosis, three ideal  $\text{Ca}^{2+}$  waveforms and their effects on the two indexes for evaluating apoptosis are presented in Figure 4.

First a constant  $\text{Ca}^{2+}$  input is imposed to assess its efficacy in triggering apoptosis. Figure 4A shows that, as the amplitude of the constant  $\text{Ca}^{2+}$  increases, the final [cPARP] exhibits an almost all-or-none pattern. When the amplitude increases beyond an apoptotic threshold, the apoptosis latency decreases first rapidly and then slowly approaches 5 h (Figure 4B). Different from the high amplitude threshold of  $3 \mu\text{M} [\text{Ca}^{2+}]$  for apoptosis with an oscillatory  $\text{Ca}^{2+}$  signal, a small  $[\text{Ca}^{2+}]$  threshold of  $1.5 \mu\text{M}$  is obtained with constant  $\text{Ca}^{2+}$  input for apoptosis. These results suggest that  $\text{Ca}^{2+}$  amplitude alone is sufficient to cause a low or high final [cPARP], corresponding to survival or apoptosis of cells.

Second, we used a square-wave  $\text{Ca}^{2+}$  input to investigate the roles of its amplitude and frequency in regulating apoptosis. For such a pulsating  $\text{Ca}^{2+}$  signal, besides the amplitude, we can define the wave width ( $T_w$ )



**Figure 4. Three Ideal  $\text{Ca}^{2+}$  Inputs and Their Impact on Apoptosis**

(A and B) The final [cPARP] (A) and apoptosis latency (B) as a function of the amplitude of constant  $\text{Ca}^{2+}$  input. (C) The final [cPARP] in response to the amplitude and period (varying  $T_w$  with the unchanged  $T_i$ ) of square-wave  $\text{Ca}^{2+}$  input. (D and E) The final [cPARP] (D) and apoptosis latency (E) in response to the amplitude and  $T_w$  with the fixed period of square-wave  $\text{Ca}^{2+}$  input. (F and G) The dependence of the final [cPARP] (F) and apoptosis latency (G) on the amplitude and period of sinusoidal  $\text{Ca}^{2+}$  input. (C), (D), and (F) have the same color bar at the bottom, whereas (E) and (G) share the same color bar on the right.

and inter-wave interval ( $T_i$ ), which can be varied separately, as well as the period ( $T_w + T_i$ ). Such type of signal has been used experimentally (De Koninck and Schulman, 1998) and in mathematical models (Marhl et al., 2006; Salazar et al., 2008). In the case of varied wave width but fixed inter-wave interval, the contour map in Figure 4C shows that the final [cPARP] mainly depends on the  $\text{Ca}^{2+}$  amplitude but not on the wave width and of course not on its period. Figure 4D shows the dependence of final [cPARP] on the  $\text{Ca}^{2+}$  amplitude and wave width, while keeping the period constant. From the apoptosis threshold (dashed line) shown in Figure 4D, one can see that the final [cPARP] is high when the  $\text{Ca}^{2+}$  amplitude is large ( $>1.5 \mu\text{M}$ ) and the wave width is long ( $>75 \text{ s}$ ). Thus, the  $\text{Ca}^{2+}$  amplitude is the dominant pro-apoptotic factor.

The comparison of the results in Figures 4C and 4D reveals that the final [cPARP] depends less on oscillation period than on its wave width. Next, we examined the influence of the  $\text{Ca}^{2+}$  amplitude and wave width on apoptosis latency. The result plotted in Figure 4E indicates that apoptosis latency is less sensitive to wave width than to wave amplitude. A similar but more obvious trend for apoptosis latency can be found when comparing  $\text{Ca}^{2+}$  amplitude and period (Figure S4). Together, the results obtained in Figures 4C–4E and S4 indicate that apoptosis is mainly modulated by amplitude, rather than frequency of a square-wave  $\text{Ca}^{2+}$  input.

Third we used sinusoidal  $\text{Ca}^{2+}$  input to further strengthen the conclusion that apoptosis depends more on amplitude than on frequency. The sinusoidal input mimics more closely biological  $\text{Ca}^{2+}$  oscillations, and its

oscillation amplitude and period can be varied separately. [Figure 4F](#) shows that the final [cPARP] exhibits only a modest response to the change of  $\text{Ca}^{2+}$  oscillation period but a pronounced sensitivity to the change of oscillation amplitude. Notably, a cell remains alive when its  $\text{Ca}^{2+}$  amplitude is small but undergoes apoptosis when the amplitude is large, regardless of the oscillation period. This result holds true when the top two most sensitive parameters are varied in a limited range ([Figures S5](#)). In addition, the change in  $\text{Ca}^{2+}$  amplitude significantly influences apoptosis latency, whereas its period does not ([Figure 4G](#)). These results reveal that AM is the dominant mechanism for  $\text{Ca}^{2+}$ -regulated apoptosis.

In summary, by virtue of three ideal  $\text{Ca}^{2+}$  waveforms, we demonstrated that cytosolic  $\text{Ca}^{2+}$  regulates apoptosis mainly via AM but not via FM. Although the  $\text{Ca}^{2+}$  amount or average  $\text{Ca}^{2+}$  and action time of  $\text{Ca}^{2+}$  input also have impacts on apoptosis ([Figures S6](#) and [S7](#)), these factors appear insignificant.

### Signal Transduction of Sinusoidal $\text{Ca}^{2+}$ Input

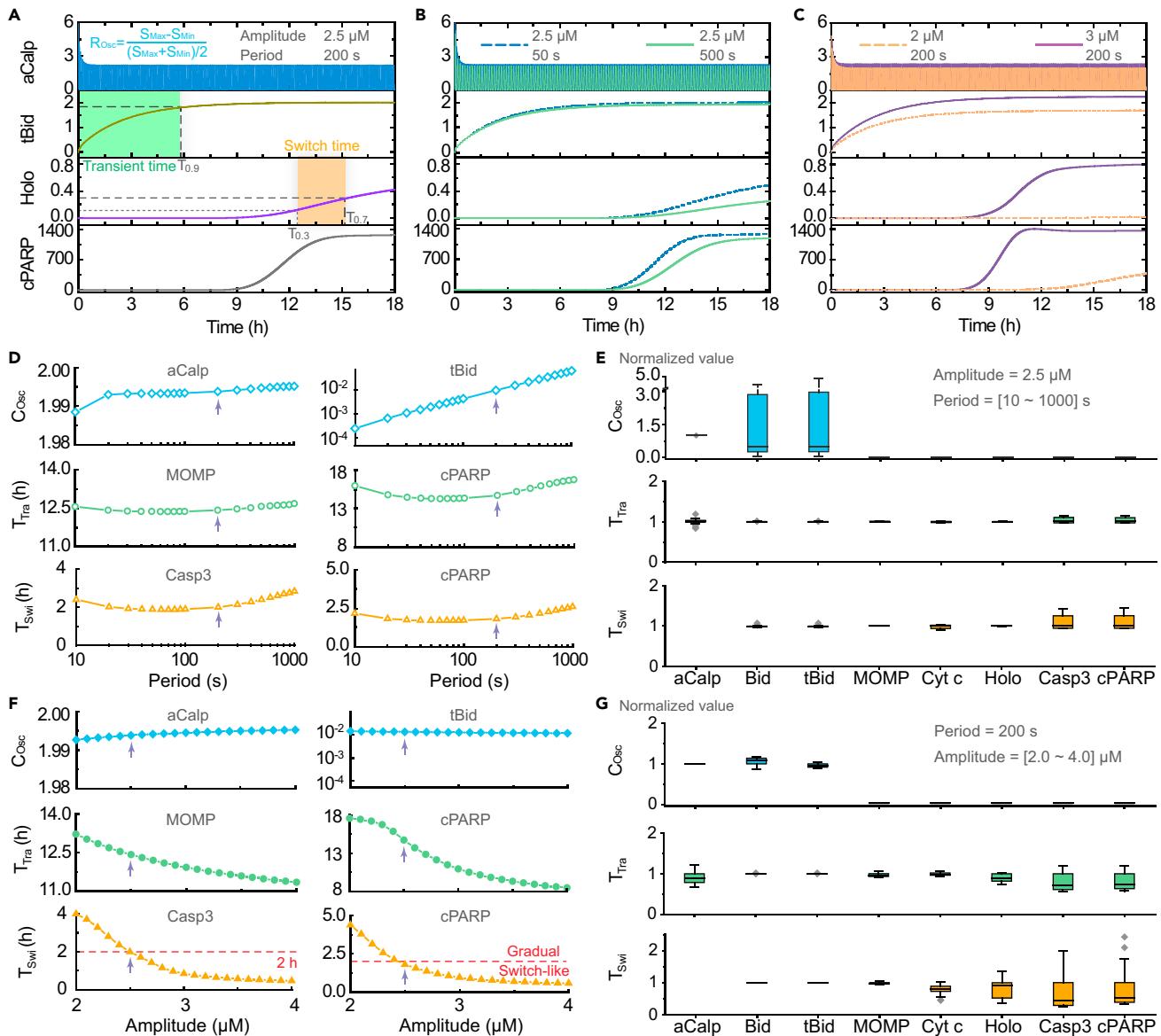
Given that sinusoidal  $\text{Ca}^{2+}$  oscillations can mimic one of the two biologically oscillatory patterns (the sinusoid-like oscillations and the repetitive spikes) *in vivo* ([Berridge, 1990](#); [Putney and Bird, 1993](#)), we explored the roles of amplitude and frequency of sinusoidal  $\text{Ca}^{2+}$  oscillations in the apoptotic signal transduction pathway. [Figure 5A](#) presents the temporal evolution of four key species in the signal transduction process where the  $\text{Ca}^{2+}$  amplitude is  $2.5 \mu\text{M}$  and its period is 200 s. Here, aCalp is an oscillatory signal, tBid and holoenzyme are gradual signals, and cPARP is a switch-like signal, which are almost the same as those induced by the ER-involved  $\text{Ca}^{2+}$  oscillations ([Figure 3A](#)).

If the period of sinusoidal  $\text{Ca}^{2+}$  input becomes significantly shorter or longer, i.e., 50 s or 500 s, the kinetics of the four species change slightly ([Figure 5B](#)). The frequency information carried in  $\text{Ca}^{2+}$  oscillations becomes largely suppressed within the gradual signal of tBid. In contrast, if the amplitude of sinusoidal  $\text{Ca}^{2+}$  input becomes smaller or bigger, i.e., 2 or  $3 \mu\text{M}$ , the kinetics of the four species change significantly, especially for the holoenzyme and cPARP ([Figure 5C](#)). A decreased amplitude causes the original switch-like cPARP signal to become a gradual signal, and the eventual cell fate changes from apoptosis to survival. An increased amplitude transforms the original gradual holoenzyme signal into a switch-like signal, and the apoptosis latency becomes dramatically shorter. The time course study suggests that the signal transduction from  $\text{Ca}^{2+}$  to tBid acts as a frequency filter of the  $\text{Ca}^{2+}$  oscillation information. Moreover, the information of the  $\text{Ca}^{2+}$  amplitude is important to determine the final intensity of the gradual signals, which is in turn crucial to determine the curve pattern of cPARP.

To gain further insights into these mechanisms, we analyzed how the changes in the period and amplitude of a sinusoidal  $\text{Ca}^{2+}$  input affect the oscillation coefficient, transient time, and switch time of the key species.

First, we considered the situation where the sinusoidal  $\text{Ca}^{2+}$  period changes from 10 to 1,000 s, while keeping the amplitude constant at  $2.5 \mu\text{M}$ . [Figure 5D](#) depicts the change of the oscillation coefficients of aCalp and tBid, the transient times of MOMP and cPARP, and the switch times of caspase 3 and cPARP against the sinusoidal  $\text{Ca}^{2+}$  period. In order to clearly describe the process of information transformation, [Figure S8A](#) shows the distribution of the values of the three characteristic times of all key species. To accommodate the wide range of values, these values are normalized with respect to the corresponding value at period = 200 s, and each box plot in [Figure 5E](#) exhibits the distribution of the normalized values. Then, we considered the situation where the sinusoidal  $\text{Ca}^{2+}$  amplitude varies from 2 to  $4 \mu\text{M}$ , while keeping the period constant at 200 s. [Figures 5F](#), [5G](#), and [S8B](#) are the counterparts of [Figures 5D](#), [5E](#), and [S8A](#), respectively.

[Figures 5D](#) and [5F](#) show that the oscillation coefficient of aCalp is far larger than that of tBid, which indicates that the frequency attribute of  $\text{Ca}^{2+}$  oscillations is only well retained in the aCalp signal, whereas it is largely lost in the gradual signals. When comparing [Figures 5E](#) and [5G](#), it is evident that the change in the period of a sinusoidal  $\text{Ca}^{2+}$  input only significantly affects the oscillation coefficients of the two upstream gradual signals, i.e., Bid and tBid, whereas the change in the  $\text{Ca}^{2+}$  amplitude dramatically modulates both the transient times and switch times of the downstream species, especially for the switch-like signals, i.e., caspase 3 and cPARP. Together, these results imply that the  $\text{Ca}^{2+}$ -regulated apoptotic transduction pathway is capable of efficiently filtering the frequency attribute during the transformation from oscillatory signals to gradual signals but capable of sensitively responding to the amplitude attribute of the  $\text{Ca}^{2+}$  oscillations.



**Figure 5. Effects of Amplitude and Period of Sinusoidal  $\text{Ca}^{2+}$  Input on Signal Transduction**

(A-C) Time series of representative species such as aCalp, tBid, Holo, and cPARP (A) at amplitude = 2.5  $\mu\text{M}$  and period = 200 s, (B) at amplitude = 2.5  $\mu\text{M}$  and period = 50 s or 200 s, and (C) at period = 200 s and amplitude = 2  $\mu\text{M}$  or 3  $\mu\text{M}$ . The units of y axes are nM.

(D) Oscillation coefficient ( $C_{\text{osc}}$ ) of aCalp and tBid, transient time ( $T_{\text{tra}}$ ) of MOMP and cPARP, and switch time ( $T_{\text{swi}}$ ) of Casp3 and cPARP, keeping the amplitude constant at 2.5  $\mu\text{M}$  and changing the period.

(E)  $C_{\text{osc}}$ ,  $T_{\text{tra}}$ , and  $T_{\text{swi}}$  of the main species are normalized to the corresponding value at amplitude = 2.5  $\mu\text{M}$  and period = 200 s, as indicated by the arrows in (D).

(F and G) (F) and (G) are the counterparts of (D) and (E), respectively, but at fixed period of 200 s and varying amplitude. In the box plot, the middle line denotes the median; the top and bottom of the box denote 75th and 25th percentiles, respectively; whiskers denote 1.5×interquartile range; and diamonds denote outliers. Abbreviation: aCalp, activated calpain; Holo, holoenzyme; Casp3, caspase 3.

Hence, the results here reveal the underlying mechanism that  $\text{Ca}^{2+}$  signal regulates apoptosis mainly via the  $\text{Ca}^{2+}$  oscillation amplitude, rather than via its frequency.

## DISCUSSION

Given the difficulties of experimentally tracking long-term  $\text{Ca}^{2+}$  signaling dynamics simultaneously with apoptotic protein processing, it is currently unknown how a fast and oscillatory  $\text{Ca}^{2+}$  signal transforms

into a slow but switch-like apoptotic response. How  $\text{Ca}^{2+}$  signaling regulates apoptosis has also remained elusive because the amplitude and period of  $\text{Ca}^{2+}$  oscillations cannot be manipulated independently within a biological system. We address these two fundamental questions with a mathematical model for deciphering the mechanism underlying  $\text{Ca}^{2+}$ -induced apoptosis.

Our results indicate that the conversion of an oscillatory  $\text{Ca}^{2+}$  signal into a switch-like apoptotic signal requires two steps. In the first step, oscillatory signals transform into gradual signals during which the oscillation amplitudes of the upstream species in signal cascade decrease successively, meanwhile their transient times to the new equilibrium increase successively. During this transformation, the slow truncation of Bid by aCalp plays a significant role. In the second step, gradual signals are converted into switch-like signals, during which the switch times of the downstream species in the apoptotic signaling pathway decrease dramatically. This process critically depends on the fast activation of caspase 3 by the holoenzyme.

Cellular information can be encoded in the amplitude and frequency of  $\text{Ca}^{2+}$  oscillations, and that information can then be decoded by distinct downstream effectors to achieve different cellular outcomes (Berridge, 1997; Monteith et al., 2017). The predominant view is that the cellular function is determined by the frequency of  $\text{Ca}^{2+}$  oscillations (Dupont and Combettes, 2016; Dupont and Sneyd, 2017; Goldbeter et al., 1990; Smedler and Uhlén, 2014). In contrast, our results show that the amplitude of  $\text{Ca}^{2+}$  oscillations is primarily used to modulate apoptosis in three different systems, that is, in the constant, square-wave, and sinusoidal  $\text{Ca}^{2+}$  input systems. Of note, the elucidation in the last system is compelling not only because sinusoidal  $\text{Ca}^{2+}$  input has separable amplitude and period but also because it can largely mimic the biologically oscillatory pattern observed in cells. Strikingly, by employing sinusoidal  $\text{Ca}^{2+}$  input, we revealed that the frequency property of  $\text{Ca}^{2+}$  oscillations is filtered but the amplitude property is retained during the apoptotic signal transduction process. During the process to translate these oscillatory signals into gradual signals, the oscillatory  $\text{Ca}^{2+}$  signal is converted into a non-oscillatory signal by filtering out the frequency information. Thus, the amplitude, other than the frequency, of  $\text{Ca}^{2+}$  oscillations, functions as the more important attribute for apoptosis induction.

The mechanisms by which cells encode the dynamic properties of oscillatory signaling (e.g., amplitude and/or frequency) into their decision-making processes are the subject of very intense investigation (Benzinger and Khammash, 2018; Cai et al., 2008; Hannanta-anan and Chow, 2016; Hansen and O'Shea, 2015). For a  $\text{Ca}^{2+}$  signal, it is generally believed that AM is less reliable than FM, owing to the difficulty of distinguishing small  $\text{Ca}^{2+}$  changes from the background noise level (Berridge et al., 1998). However, the fidelity of apoptotic  $\text{Ca}^{2+}$  signal can be guaranteed through AM mode because the apoptotic  $\text{Ca}^{2+}$  levels are much higher than those produced by spontaneous fluctuation. Indeed, a recent experiment revealed that individual cells exhibit high amplitude  $\text{Ca}^{2+}$  release events but significant heterogeneity in the frequency of these events after treatment with apoptosis-inducing drugs (Garcia et al., 2017). In addition, Monteith et al. recently proposed that it is the amplitude of  $\text{Ca}^{2+}$  oscillations that controls cell fate (e.g., proliferation or cell death), whereas it is their frequency that controls gene transcription (Monteith et al., 2017). Our finding demonstrates that  $\text{Ca}^{2+}$ -regulated apoptosis is a typical example of AM fashion, which is a key perspective in the field of  $\text{Ca}^{2+}$  signaling.

### Limitations of the Study

Although  $\text{Ca}^{2+}$  oscillations are intrinsically stochastic because of stochastic  $\text{IP}_3\text{R}$  channel dynamics (Powell et al., 2020; Thul, 2014; Thurley et al., 2012), the  $\text{Ca}^{2+}$  oscillations at the cellular level can be effectively treated as deterministic (Cao et al., 2014; Sneyd et al., 2017; Voorsluys et al., 2019). As a result, we only used the two-variable Li-Rinzel model as the simplest but useful model to produce  $\text{Ca}^{2+}$  oscillations. The focus of this work is on cytosolic  $\text{Ca}^{2+}$ -induced apoptosis, and for simplicity, we did not take mitochondrial  $\text{Ca}^{2+}$  into account. In addition, the prediction of AM given in the paper largely depends on a sinusoidal type of  $\text{Ca}^{2+}$  oscillations. Thus, whether our prediction can be generalized to other types of  $\text{Ca}^{2+}$  oscillations such as repetitive spikes remains an open question for future study. Furthermore, the test of this prediction will rely on the experimental design that can compare directly the effects of the amplitude and period of cytosolic  $\text{Ca}^{2+}$  oscillations on the apoptosis.

### Resource Availability

#### Lead Contact

Jianwei Shuai

### Materials Availability

This study did not generate new unique reagents.

### Data and Code Availability

All data needed to evaluate the conclusions in the paper are present in the paper and/or the [Supplemental Information](#). The code related to this paper may be requested from the authors.

### Methods

All methods can be found in the accompanying [Transparent Methods supplemental file](#).

## SUPPLEMENTAL INFORMATION

Supplemental Information can be found online at <https://doi.org/10.1016/j.isci.2020.101671>.

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## AUTHOR CONTRIBUTIONS

H.Q. and J.S. designed research; H.Q. and X.L. performed research; X.L., Z.J., and T.S. analyzed data; H.Q., T.S., and J.S. wrote the paper.

## DECLARATION OF INTERESTS

The authors declare no conflict of interest.

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## **Supplemental Information**

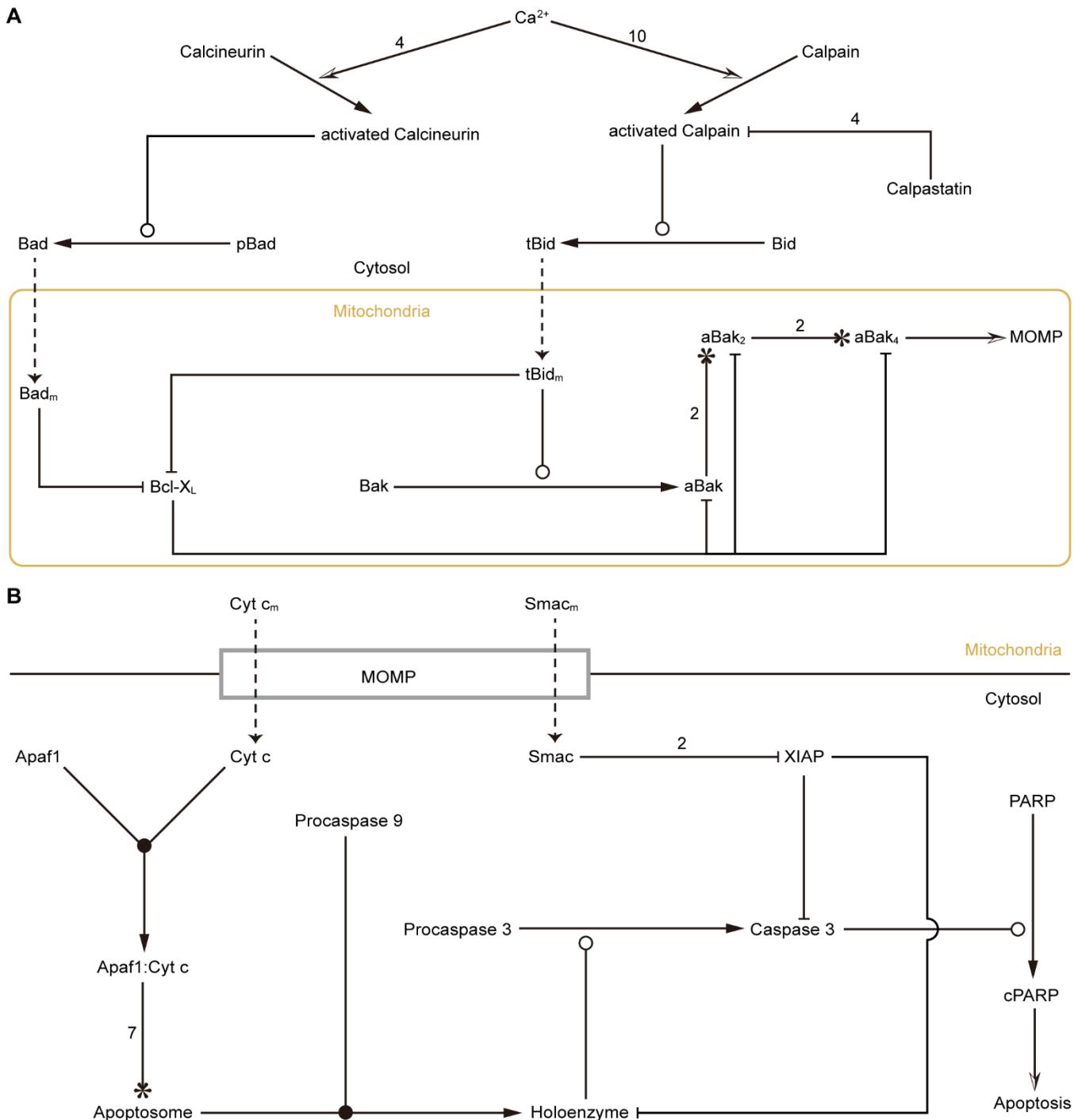
**The Oscillation Amplitude,  
Not the Frequency of Cytosolic Calcium,  
Regulates Apoptosis Induction**

**Hong Qi, Xiang Li, Zhen Jin, Thomas Simmen, and Jianwei Shuai**

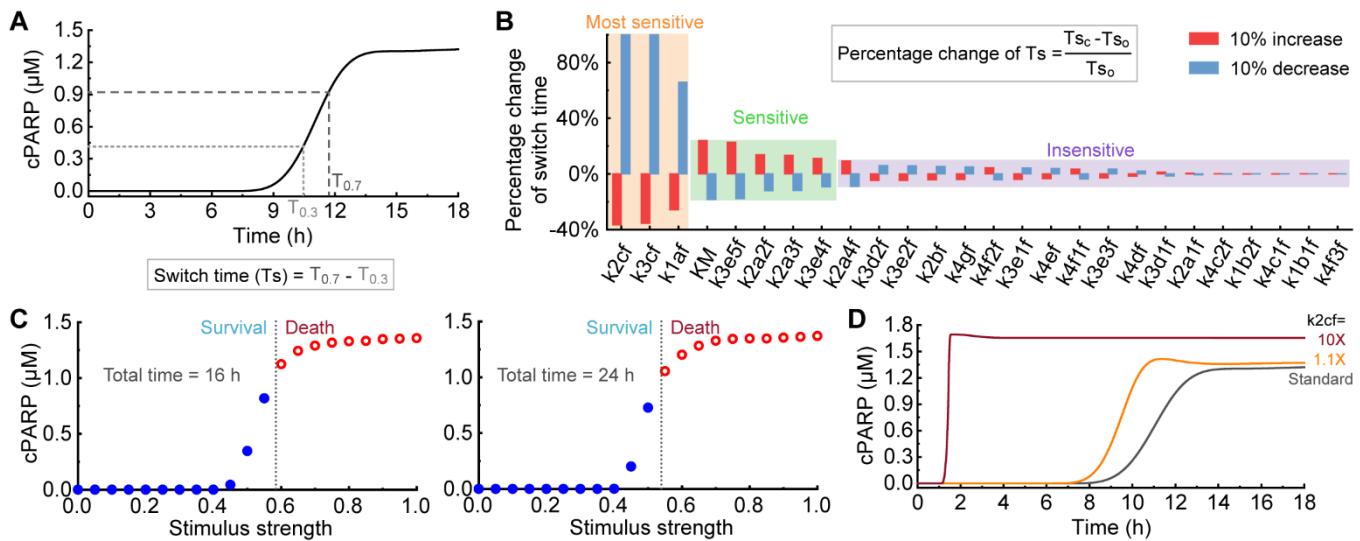
## Supplementary Information

### **The Oscillation Amplitude, Not the Frequency of Cytosolic Calcium Regulates Apoptosis Induction**

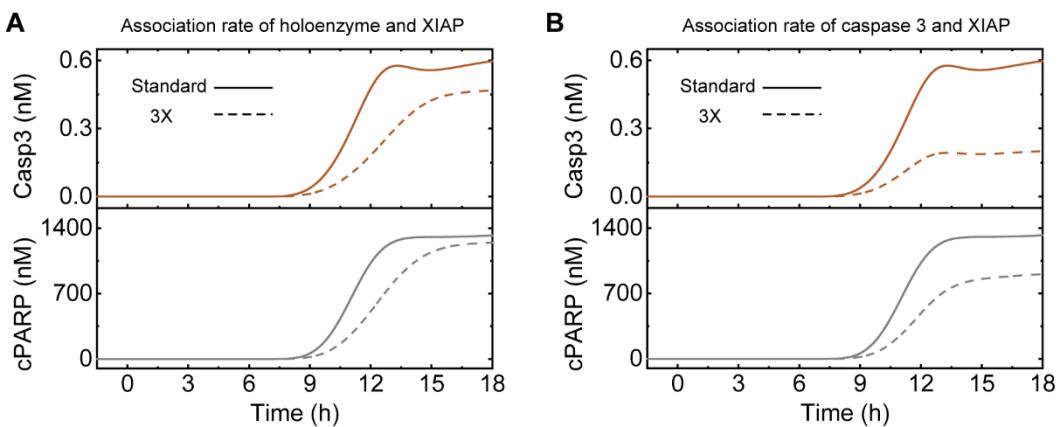
**Hong Qi, Xiang Li, Zhen Jin, Thomas Simmen, and Jianwei Shuai**



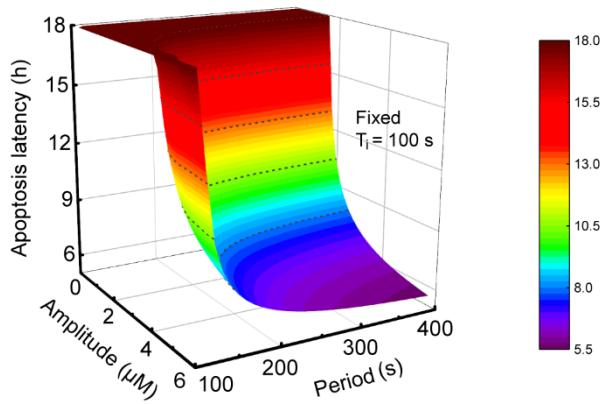
**Figure S1. The detailed scheme of the last three modules, related to Figure 1.** (A) Module of  $\text{Ca}^{2+}$ -activated proteins (top) and MOMP controlled by Bcl-2 protein family (bottom). (B) Module of Cyt c-induced caspase cascade. The graphical notations are the same as in Figure 1. The numbers beside the arrows refer to the stoichiometric number of the corresponding reaction.



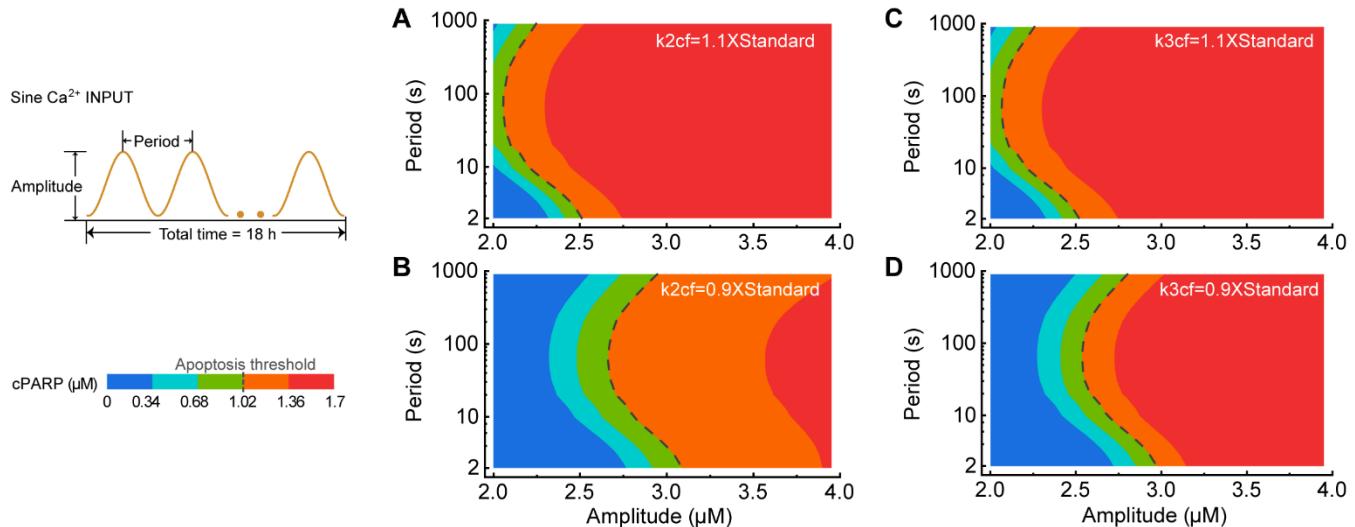
**Figure S2. Parameter sensitivity analysis, related to Figures 2 and 3.** (A) Illustration of the definition of switch time ( $T_{\text{swi}}$ , the time for cPARP to increase from 30 to 70% of its final concentration). (B) Percentage change of the switch time in response to 10% increase or decrease of each parameter.  $T_0$  is the switch time obtained under standard parameter conditions, and  $T_c$  is the one under changed parameter settings. See Table S3 for details of the meanings of parameters. (C) The final [cPARP] at different stimulus strengths when the total simulation time is 16 h (left) and 24 h (right), respectively. The dotted lines depict the apoptosis threshold. (D) Time series of cPARP when the association rate of aCalp and Bid ( $k_{2cf}$ ) is increased by 10% and 10-fold. Stimulus strength=0.73.



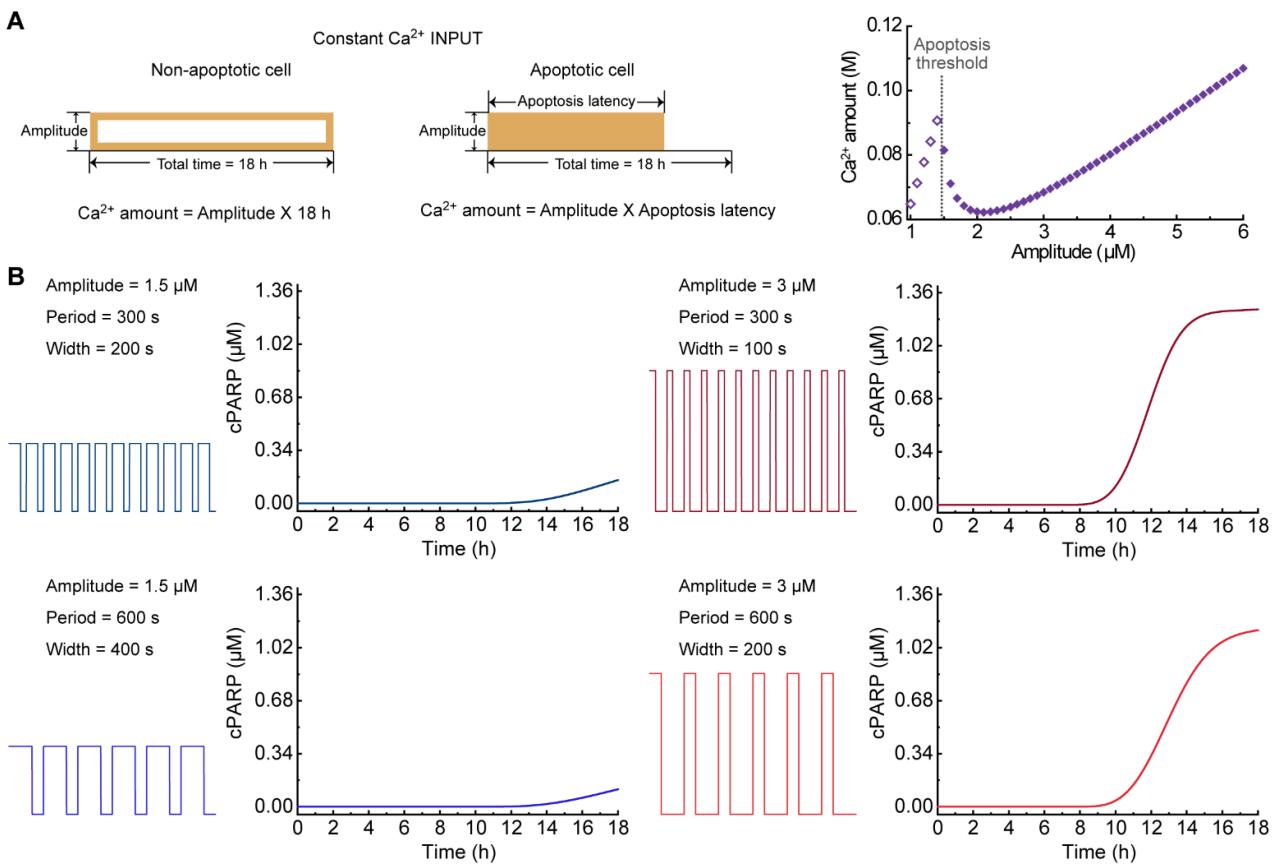
**Figure S3. Influence of repression of holoenzyme and caspase 3 by XIAP on signal conversion, related to Figure 3.** Time series of Casp3 and cPARP when the association rate of holoenzyme (or caspase 3) and XIAP is increased to 3-fold (broken lines). The curves obtained by the standard parameter value are shown in solid lines. Casp3, caspase 3.



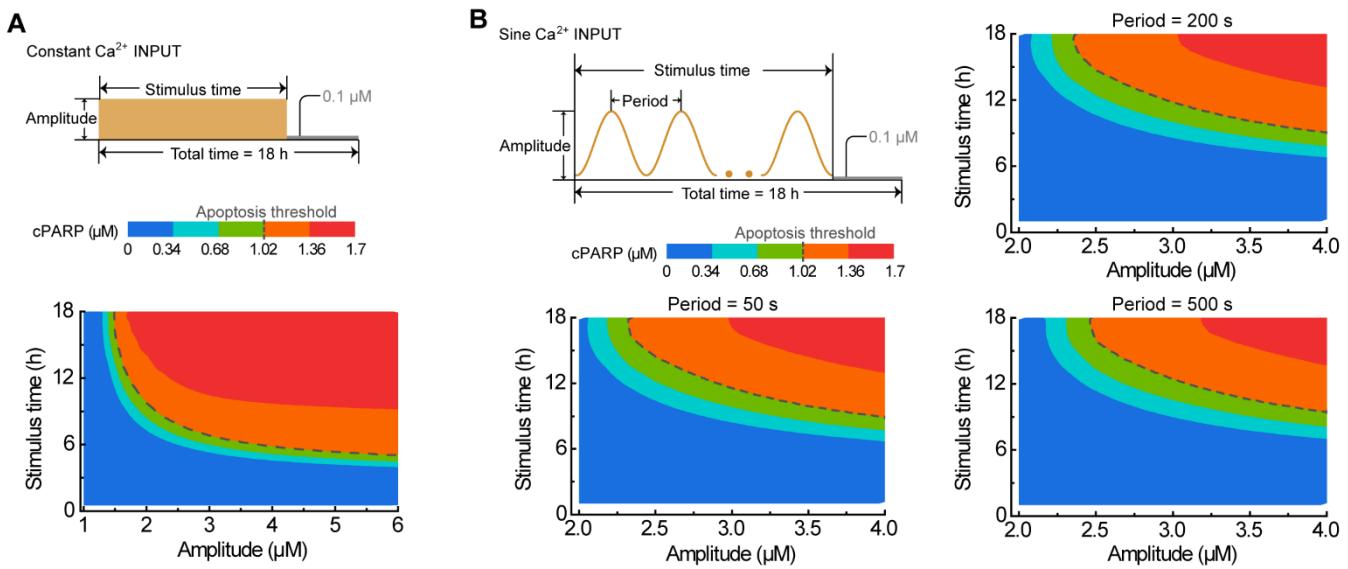
**Figure S4. Apoptosis latency mainly depends on  $\text{Ca}^{2+}$  amplitude, but not on the period of square-wave  $\text{Ca}^{2+}$  input, related to Figure 4.** The apoptosis latency in response to the amplitude and period with the fixed inter-wave interval ( $T_i$ ) of square-wave  $\text{Ca}^{2+}$  input.



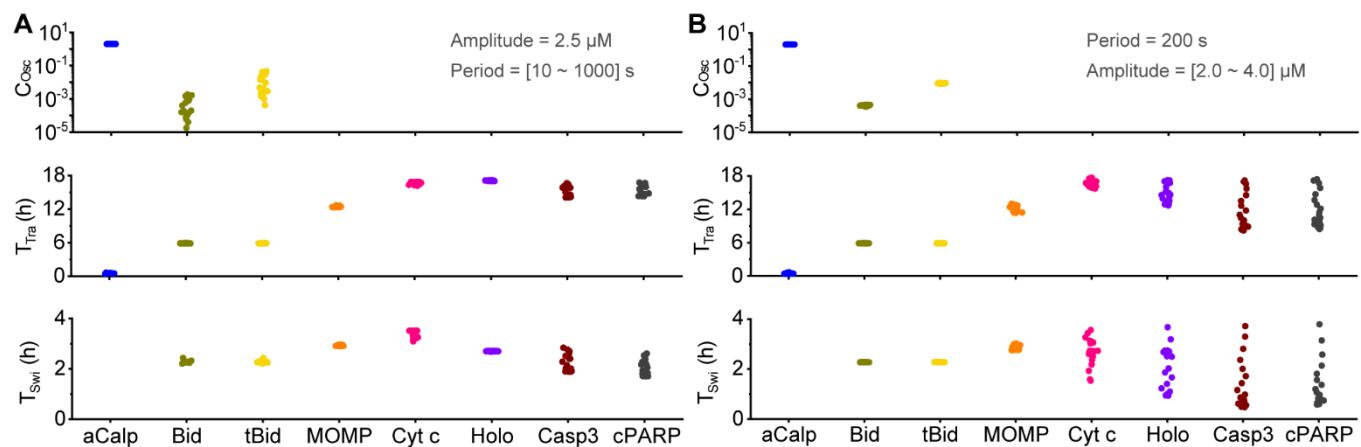
**Figure S5. The robustness of the conclusion that  $\text{Ca}^{2+}$  regulates apoptosis mainly via AM, but not via FM, related to Figures 4 and S2.** The final [cPARP] in response to the amplitude and period of sinusoidal  $\text{Ca}^{2+}$  input when the two most sensitive parameters,  $k_{2\text{cf}}$  and  $k_{3\text{cf}}$ , are varied  $\pm 10\%$ .



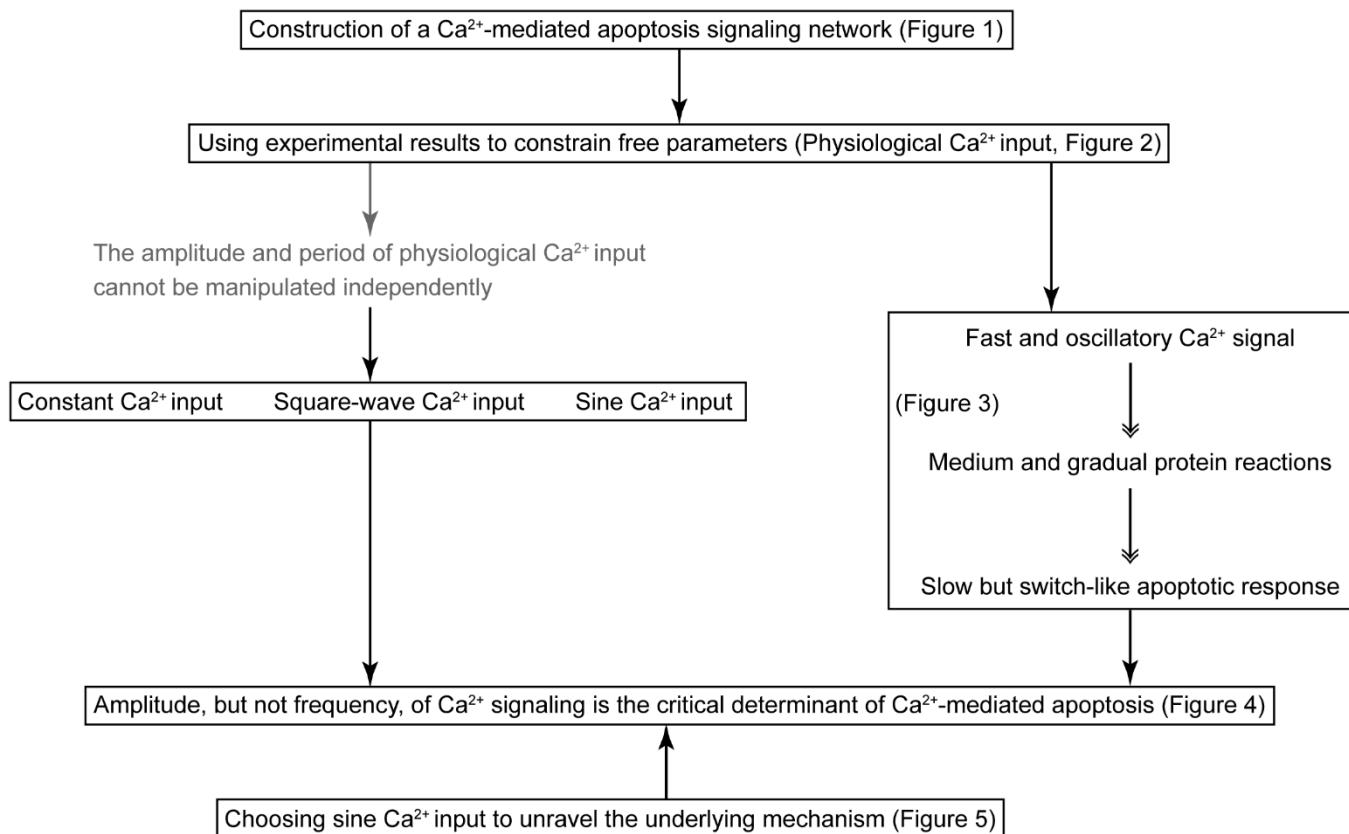
**Figure S6. Effect of  $\text{Ca}^{2+}$  amount or average  $\text{Ca}^{2+}$  on the apoptosis, related to Figure 4.** (A)  $\text{Ca}^{2+}$  amount as a function of the amplitude of constant  $\text{Ca}^{2+}$  input. Survival and death are corresponding to the left and right region of the apoptosis threshold, respectively. (B) The time series of [cPARP] with different square-wave  $\text{Ca}^{2+}$  input. Despite the waveforms of the  $\text{Ca}^{2+}$  input are different, their total  $\text{Ca}^{2+}$  amounts per hour (and thus the average  $\text{Ca}^{2+}$ ) are identical.



**Figure S7. Effect of stimulus time on the apoptosis, related to Figure 4.** (A) Dependence of the final [cPARP] on independent amplitude and stimulus time with constant  $\text{Ca}^{2+}$  input. (B) Under sinusoidal  $\text{Ca}^{2+}$  input, the final [cPARP] in response to the amplitude and stimulus time with fixed period of 50 s, 200 s, and 500 s, respectively.



**Figure S8. Distribution of three characteristic times, related to Figure 5.** (A) Oscillation coefficient ( $C_{osc}$ ), transient time ( $T_{tra}$ ), and switch time ( $T_{swi}$ ) of the main species in the signaling pathway, keeping the amplitude constant at 2.5  $\mu$ M and changing the period from 10 to 1000 s. (B)  $C_{osc}$ ,  $T_{tra}$ , and  $T_{swi}$  of the main species in the signaling pathway, keeping the period constant at 200 s and changing the amplitude from 2 to 4  $\mu$ M.



**Figure S9. Workflow of the present work, related to Figures 1-5.**

## Transparent Methods

### Detailed description of the model

In vertebrates, apoptosis typically proceeds through two main pathways: the extrinsic pathway and the intrinsic pathway. We primarily focus our attention on the latter due to the importance of cytosolic  $\text{Ca}^{2+}$  in the regulation of the intrinsic pathway (Harr and Distelhorst, 2010). To qualitatively study this process, we constructed a model comprised of four functional modules (Figure 1 and Figure S1), which are described in detail in following.

#### i. ER-involved $\text{Ca}^{2+}$ oscillations

Under resting conditions, cytosolic  $\text{Ca}^{2+}$  concentration ( $[\text{Ca}^{2+}]$ ) is maintained at low levels, while  $[\text{Ca}^{2+}]$  in the endoplasmic reticulum (ER) is very high. Their homeostasis is dynamically regulated by active  $\text{Ca}^{2+}$  uptake through sarco/endoplasmic reticulum  $\text{Ca}^{2+}$ -ATPase (SERCA) and passive  $\text{Ca}^{2+}$  leak from the ER (Chang et al., 2014). Upon stress stimuli,  $\text{IP}_3$  (inositol 1,4,5-trisphosphate) forms and binds to  $\text{IP}_3$  receptors ( $\text{IP}_3\text{Rs}$ ) to release  $\text{Ca}^{2+}$  from the ER, producing the upstroke of a  $\text{Ca}^{2+}$  oscillation. The SERCA then pumps the cytosolic  $\text{Ca}^{2+}$  back into the ER, completing the  $\text{Ca}^{2+}$  oscillation.

The  $\text{Ca}^{2+}$  oscillation module (blue region of Figure 1) is described by the two-variable Li-Rinzel model, which is simple but has a significant ability to reproduce experimental observations. In contrast to the original model (De Pitta et al., 2008), we made two modifications: a. for correlating the different stimulus strengths with different levels of  $\text{IP}_3$ , the production and degradation of  $\text{IP}_3$  are considered additionally; b. the amplitude and period of  $\text{Ca}^{2+}$  oscillations are rescaled with the modified model parameters to better fit the  $\text{Ca}^{2+}$  oscillation patterns observed in experiment (Giorgi et al., 2018; Scorrano et al., 2003).

#### ii. $\text{Ca}^{2+}$ -activated proteins

An important machinery linking cytosolic  $\text{Ca}^{2+}$  and apoptosis is the activation of two  $\text{Ca}^{2+}$ -regulated enzymes, calpain and calcineurin. The key mechanism for guarding against inappropriate activation of the two proteases is their weak affinity for  $\text{Ca}^{2+}$ . Calpain and calcineurin are activated by tens-of-micromolar and micromolar concentrations of  $\text{Ca}^{2+}$ , respectively.

Calcineurin has four  $\text{Ca}^{2+}$  binding sites: sites 1 and 2 with dissociation constants in the micromolar range, whereas sites 3 and 4 with dissociation constants in the nanomolar range (Li et al., 2011). Fully activated calpain needs to bind ten  $\text{Ca}^{2+}$  ions (Moldoveanu et al., 2008), but the activation mechanisms remain poorly

understood (Campbell and Davies, 2012). Here we made three simplifications and assumptions: a.  $\text{Ca}^{2+}$  ions bind calpain one by one; b. all binding sites have the same dissociation constant for  $\text{Ca}^{2+}$ ; c. calpain is activated because of its vicinity to microdomains of high  $[\text{Ca}^{2+}]$  ( $[\text{Ca}^{2+}]_{\text{Mic}}$ ) (Hanna et al., 2007), which is 5- to 10-fold higher than in the bulk cytosol (Giacomello et al., 2010). For simplicity, we assumed that  $[\text{Ca}^{2+}]_{\text{Mic}}$  is 7.5-fold higher than cytosolic  $[\text{Ca}^{2+}]$  ( $[\text{Ca}^{2+}]_{\text{Cyt}}$ ), the latter being determined by the modified Li-Rinzel model mentioned above. Calpastatin, an endogenous inhibitor of calpain, is capable of neutralizing four molecules of activated calpain (Hanna et al., 2008; Moldoveanu et al., 2008).

### iii. MOMP controlled by Bcl-2 protein family

The activated calcineurin dephosphorylates the phosphorylated Bad into Bad (Wang et al., 1999). Activated calpain cleaves Bid into truncated Bid, tBid (Chen et al., 2001). Both Bad and tBid then migrate into the mitochondria and mediate mitochondrial outer membrane permeabilization (MOMP). In detail, tBid on the mitochondria directly activates Bak. Active Bak (aBak) monomers first form dimers and then tetramers, causing MOMP. Bcl-X<sub>L</sub> is able to bind and antagonize all the active forms of Bak. Bad and tBid on the mitochondria can both bind to Bcl-X<sub>L</sub> and release active forms of Bak to promote MOMP.

### iv. Cyt c-induced caspase cascade

Following MOMP, mitochondrial intermembrane space proteins such as cytochrome c (Cyt c) and second mitochondria-derived activator of caspases (Smac) are released into the cytosol. In the cytosol, Cyt c engages apoptotic protease-activating factor-1 (Apaf1), and together form the heptameric apoptosome, which interacts with procaspase 9 to induce the formation of holoenzyme, thereby triggering caspase 3 activation. Caspase 3 in turn cleaves a series of substrates, including PARP, and ultimately leads to apoptosis. Smac facilitates apoptosis by neutralizing the holoenzyme and caspase inhibitor X-linked inhibitor of apoptosis protein (XIAP).

We used the mathematical model of apoptosis from (Albeck et al., 2008b) and (Rehm et al., 2006) as a template to construct the biochemical reactions of the last two modules, but two modifications have been made in our model. Since MOMP is a pore, and thus the drive force for the release of Cyt c and Smac via the MOMP is the concentration difference between two compartments (i.e., intermembrane space of mitochondria and cytosol). In the model we used a Hill function to model the release kinetics of Cyt c and Smac through the MOMP. In addition, our recent study proposed that there are 2047 pathways for the assembly of apoptosome (Qi et al., 2018). To avoid combinatorial complexity, we chose an optimal pathway in the current model.

### Limitation of the model

The main purpose of the paper is to explore which characteristic of cytosolic  $\text{Ca}^{2+}$  oscillations regulates apoptosis, so three simplifications were made to reduce complexity of the problem without significantly affecting our result. First, although  $\text{Ca}^{2+}$  oscillations are mainly from the periodic release of  $\text{Ca}^{2+}$  within the ER in many cell types, the ER-to-mitochondria  $\text{Ca}^{2+}$  transfer, the mitochondria-to-cytosol  $\text{Ca}^{2+}$  transport and the  $\text{Ca}^{2+}$  exchange through the plasma membrane also impact  $\text{Ca}^{2+}$  oscillations. However, they are not considered in the current model. Second, it should be noted that mitochondria can sequester cytosolic  $\text{Ca}^{2+}$  and excessive  $\text{Ca}^{2+}$  accumulation within mitochondria causes the opening of mitochondrial permeability transition pore in the inner mitochondrial membrane, which results in increased mitochondrial permeability to ions and solutes, followed by organelle swelling and the rupture of the outer mitochondrial membrane, and thus the release of Cyt c, leading to apoptosis. Obviously, the consideration of mitochondrial  $\text{Ca}^{2+}$  in our model will make the situation very complex and therefore it has not been considered. Third, there may be complicated pathways for the long-duration  $\text{Ca}^{2+}$  oscillations to induce apoptosis. The long-duration  $\text{Ca}^{2+}$  oscillations may cause other sources of stress or lead to the transformation of  $\text{Ca}^{2+}$  oscillations into a sustained  $\text{Ca}^{2+}$  response to finally induce apoptosis. With a mathematic model, we are not trying to discuss various possible mechanisms of long-duration  $\text{Ca}^{2+}$  oscillations induced apoptosis, which can make the results simpler to interpret.

### Rationality of parameter selection

In our model, the output of the  $\text{Ca}^{2+}$ -induced apoptosis system is regarded as cPARP, a switch-like signal. Accordingly, we performed parameter sensitivity analysis for 26 key parameters to identify their influence on the switch time of cPARP (Figure S2B). On each trial only one parameter is increased or decreased by 10% with respect to its standard value, while the others remain at their standard values. According to the result of k-means clustering, if the percentage change of the corresponding switch time is smaller than 10%, it is classified as an insensitive parameter, otherwise it is classified as a sensitive parameter; and if the percentage change is larger than 20%, it is regarded as a most sensitive parameter.

Approximately 70% of the parameters are insensitive, which are mostly related to the two downstream modules, i.e., MOMP controlled by Bcl-2 protein family and Cyt c-induced caspase cascade. The three most sensitive parameters are associated with the upstream reactions of signaling network, i.e., activation of calpain by  $\text{Ca}^{2+}$ , cleavage of Bid into tBid by aCalp, and tBid-mediated activation of Bak. The considerable influence of  $k_{2cf}$  (the association rate of aCalp and Bid) on the switch-like response suggests that it is the rate-limiting step in the signal transduction.

Giorgi et al. summarized that under resting conditions  $[Ca^{2+}]$  is maintained at about 0.1  $\mu M$ , while after stimulation it can reach 0.2~5  $\mu M$  (Giorgi et al., 2018). Although the critical  $[Ca^{2+}]$  threshold for apoptosis depends on the cell type and apoptotic stimuli, we must select a fixed one for the deterministic model to evaluate its correlation with the cell fate. Viewed in this perspective, we chose 3  $\mu M$   $[Ca^{2+}]$  as a critical threshold to initiate apoptosis. Similarly, Rehm et al. found that 25% substrate cleavage does not elicit apoptosis, while cells that exhibits 65% substrate cleavage undergo apoptosis (Rehm et al., 2006). Since the total [PARP] is 1.7  $\mu M$ , we chose 60% substrate cleavage, i.e. 1.02  $\mu M$  [cPARP] as a critical threshold to initiate apoptosis. As seen in Figure 2 in the main text, a stimulus strength of 0.6 promotes the peak of  $[Ca^{2+}]$  above 3  $\mu M$ , which in turn results in [cPARP] more than 1.02  $\mu M$ , inducing apoptotic cell death. We should stress that although choosing these two critical values is to some extent arbitrary, the current model is only qualitative, and thus these precise values in the model have little qualitative influence on the conclusion. Likewise, the conclusion is also robust to the detailed selection of the cell cycle, i.e. total simulation time (Figure S2C, compared to Figure 2E).

In addition, cells exposed to the same apoptotic stimulus always have different apoptosis latency. This is due to the intrinsic and extrinsic noise existed in the cells (Flusberg and Sorger, 2015), which can be reflected by variations of the parameter values of the model. Here we used  $k_{2cf}$  as an example to illustrate how its variation can influence the apoptosis latency (Figure S2D). If  $k_{2cf}$  is increased by 10%, the apoptosis latency is less than 8 h; and if  $k_{2cf}$  is increased by 10-fold, it becomes less than 2 h.

### **Influence of repression of holoenzyme and caspase 3 by XIAP on signal conversion**

If the association rate of holoenzyme and XIAP is increased to 3-fold, the original switch-like signals, i.e. caspase 3 and cPARP, will become gradual signals (Figure S3A). If the association rate of caspase 3 and XIAP is increased to 3-fold, caspase 3 and cPARP will become lower (Figure S3B).

### **Apoptosis latency in response to amplitude and period of square-wave $Ca^{2+}$ input**

For the square-wave  $Ca^{2+}$  input, if the wave width is varied with the inter-wave interval fixed, the period of  $Ca^{2+}$  input varies with the wave width. The contour map in Figure S4 displays that apoptosis latency is significantly sensitive to wave amplitude, but slightly to period. This result indicates that the apoptosis latency is mainly dependent on the  $Ca^{2+}$  amplitude, but not on its period.

### **Apoptosis is not dependent on the $Ca^{2+}$ amount or average $Ca^{2+}$**

A recent study found a strategy called signal integration in the decision-making system for cell cycle (Liu et

al., 2015). To determine whether apoptosis is primarily a result of an integrator of cumulative  $\text{Ca}^{2+}$  load, we assess the amount of  $\text{Ca}^{2+}$  over 18 h to see whether apoptosis only occurs when  $\text{Ca}^{2+}$  amount reaches a certain threshold by imposing constant  $\text{Ca}^{2+}$  input. In detail, if the cell is still survival at the end of 18 h, the  $\text{Ca}^{2+}$  amount is equal to the total amount during the past 18 h. However, if the cell becomes death within 18 h, the  $\text{Ca}^{2+}$  amount is defined as the total amount accumulated in the period of apoptosis latency. From Figure 4A in the main text we can see that a plot of the final [cPARP] versus  $\text{Ca}^{2+}$  amplitude shows a monotonic relationship. In detail, the final [cPARP] is low if the  $\text{Ca}^{2+}$  amplitude is smaller than a threshold amplitude of 1.5  $\mu\text{M}$ , while it is high if the  $\text{Ca}^{2+}$  amplitude is greater than the threshold amplitude. However, the amounts of  $\text{Ca}^{2+}$  around this threshold amplitude display a peak (Figure S6A). This clearly excludes the possibility of signal integration in our  $\text{Ca}^{2+}$ -apoptosis system.

Average  $\text{Ca}^{2+}$  maybe another factor to influence the apoptosis. We designed four different square-wave  $\text{Ca}^{2+}$  inputs: they have different amplitudes, periods, or wave widths, albeit with the same average  $\text{Ca}^{2+}$  level, i.e. 1  $\mu\text{M/s}$ . The results in Figure S6B show that despite that period and wave width have a certain effect on the outcome (the final [cPARP]), amplitude is still the dominant factor. This demonstrates that  $\text{Ca}^{2+}$  amplitude is important even for a fixed average  $\text{Ca}^{2+}$ .

### Effect of $\text{Ca}^{2+}$ action time on the apoptosis

We need to point out that the stimulating duration of high  $\text{Ca}^{2+}$  signal may not be always 18 h in the apoptosis process. An experiment revealed that the  $\text{Ca}^{2+}$  release events last more than 10 h (Garcia et al., 2017). In addition,  $\text{Ca}^{2+}$  ions not only stimulate proapoptotic pathways, but also activate prosurvival pathways, and so cell fate is decided by the balance between survival and apoptotic pathways. We thus chose 18 h, i.e., the length of cell cycle, as the stimulus time in our standard procedure. Next we explored the model dynamics with constant and sinusoidal  $\text{Ca}^{2+}$  input to verify the robustness of our conclusions under the condition of varying stimulus time.

Constant  $\text{Ca}^{2+}$  input is the simplest input and is easy to illustrate the effect of stimulus time on cell fate. Here the total running time is still 18 h. As illustrated in Figure S7A, a high constant  $[\text{Ca}^{2+}]$  is added as a stimulus for a certain stimulus time, after which  $[\text{Ca}^{2+}]$  is set to 0.1  $\mu\text{M}$ . The corresponding result indicates that a stimulus time of 6 h is enough to cause apoptosis, presumably as the minimal response time for the  $\text{Ca}^{2+}$ -induced apoptotic cascade in our model.

Sinusoidal  $\text{Ca}^{2+}$  input is employed to demonstrate that it is not the frequency of the  $\text{Ca}^{2+}$  oscillations, but

rather the amplitude, that dominates the extent of apoptotic response. In [Figure S7B](#) the abilities to induce apoptosis for  $\text{Ca}^{2+}$  inputs that have fixed period but with distinct amplitudes are compared. It is shown that apoptosis can be induced only when the stimulus time is longer than 9 h, depending mainly on the  $\text{Ca}^{2+}$  amplitude. Even though the periods of  $\text{Ca}^{2+}$  input are different, the response patterns of apoptosis to  $\text{Ca}^{2+}$  amplitude are similar. As a result, the conclusion that apoptosis acts primarily as a  $\text{Ca}^{2+}$  amplitude-selective, rather than a  $\text{Ca}^{2+}$  frequency-selective decoder, is not critically dependent on the duration of stimulus time.

## Parameters, biochemical reactions, and ordinary differential equations

The principles of parameter selection are detailed in following paragraphs. The parameters of  $\text{Ca}^{2+}$  dynamics module, protein synthesis and degradation rates, and the kinetic rate parameters of other three modules, are summarized in [Table S1](#), [S2](#), and [S3](#), respectively. Biochemical reactions and corresponding reaction rates are given in [Table S4](#), and the resulting ordinary differential equations are listed in [Table S5](#).

### i. Choice of model parameters

Parameter selection is based on the following criteria:

- a. Parameters are preferentially taken from the combined experimental and theoretical studies, then from experimental studies, and lastly from the preceding modeling studies.
- b. Although measuring the cellular kinetic parameters is extremely difficult, most of the dissociation constants can be obtained from the literatures. So we can estimate the association rate constant by fixing the dissociation rate constant.
- c. The unknown parameters are determined mainly by fitting the dynamics of  $\text{Ca}^{2+}$  and cPARP to the experimental measurements.

### ii. Geometric parameters

The diameter of human cell is in the range of 5~100  $\mu\text{m}$  ([Ginzberg et al., 2015](#)). Here we assumed that the cell is a sphere of radius 10  $\mu\text{m}$ , giving the cell volume about 4190  $\mu\text{m}^3$ . Given the mean mitochondrial volume is 0.5  $\mu\text{m}^3$  ([Morigi et al., 2015](#)) and each cell contains hundreds of mitochondria, we estimated the total mitochondrial volume of a cell is about 300  $\mu\text{m}^3$ . So the cytosolic volume is 3890  $\mu\text{m}^3$ , and the mitochondria-to-cytosol volume ratio is 0.077. If we assume that the mitochondrial intermembrane space occupies 10% of the mitochondrial volume, then the intermembrane space-to-cytosol volume ratio is 0.0077. The ER-to-cytosol volume ratio is assumed to be 0.185, which indicates that the ER accounts for approximately 15% of the total cell volume.

### iii. Protein synthesis and degradation rate

Because we consider the dynamical behavior of the system within 18 h, the synthesis and degradation of proteins must be included. To reduce the number of free parameters, we assumed the same protein degradation rate for all molecular species, a procedure that was used in (Zhao et al., 2015). The only exception is the complex between XIAP and caspase 3. This is because XIAP-mediated degradation of caspase 3 is involved in restraining caspase 3 catalytic activity (Albeck et al., 2008a), and we consider an additional degradation rate for this complex. Protein synthesis rate can be obtained by the product of degradation rate and steady-state concentration of a certain protein.

Since  $\text{Ca}^{2+}$  is not created or destroyed or converted into an inactive metabolite (Monteith et al., 2017), in addition to the  $\text{Ca}^{2+}$  flux between the ER and cytosol,  $[\text{Ca}^{2+}]$  in the cytosol changes only due to the association and dissociation reactions between  $\text{Ca}^{2+}$  and  $\text{Ca}^{2+}$ -binding proteins. When  $\text{Ca}^{2+}$ -binding proteins are degraded, the  $\text{Ca}^{2+}$  ions that bind with them release into the cytosol.

**Table S1. Parameters in the  $\text{Ca}^{2+}$  dynamics module, related to Figure 1.**

Parameter	Description	Value (Unit)	Reference <sup>1</sup>
$C_0$	Total $[\text{Ca}^{2+}]$ in terms of cytosolic volume	9.4 ( $\mu\text{M}$ )	Rescaled
$c_1$	ER-to-cytosol volume ratio	0.185	(De Pitta et al., 2008)
$v_1$	Maximum $\text{IP}_3\text{R}$ channel flux	0.4286 ( $\text{s}^{-1}$ )	Rescaled
$v_2$	$\text{Ca}^{2+}$ leak flux constant	0.0078 ( $\text{s}^{-1}$ )	Rescaled
$v_3$	Maximum SERCA pump rate	0.151 ( $\mu\text{M s}^{-1}$ )	Rescaled
$K_3$	Activation constant for SERCA	0.235 ( $\mu\text{M}$ )	Rescaled
$d_1$	$\text{IP}_3\text{R}$ dissociation constant for $\text{IP}_3$ sites A	0.13 ( $\mu\text{M}$ )	(De Pitta et al., 2008)
$d_2$	$\text{IP}_3\text{R}$ dissociation constant for $\text{Ca}^{2+}$ -inhibition sites	2.4651 ( $\mu\text{M}$ )	Rescaled
$d_3$	$\text{IP}_3\text{R}$ dissociation constant for $\text{IP}_3$ sites B	0.9434 ( $\mu\text{M}$ )	(De Pitta et al., 2008)
$d_5$	$\text{IP}_3\text{R}$ dissociation constant for $\text{Ca}^{2+}$ -activation sites	0.47 ( $\mu\text{M}$ )	Rescaled
$a_2$	$\text{IP}_3\text{R}$ binding rate constant for $\text{Ca}^{2+}$ -inhibition sites	0.006 ( $\mu\text{M}^{-1} \text{s}^{-1}$ )	Rescaled
$p_{\text{IP}_3}$	Maximum $\text{IP}_3$ synthesis rate	0.18 ( $\mu\text{M s}^{-1}$ )	Adjusted
$k_{\text{IP}_3}$	Activation constant for $\text{IP}_3$ synthesis	0.6	Adjusted
$d_{\text{IP}_3}$	$\text{IP}_3$ degradation rate	0.14 ( $\text{s}^{-1}$ )	(Brown et al., 2008)

1. Rescaled means that the parameters from (De Pitta et al., 2008) are rescaled to yield appropriate amplitude and period of  $\text{Ca}^{2+}$  oscillations.

Adjusted means that these parameters are adjusted by correlating the level of  $\text{IP}_3$  with the stimulus strength between 0 to 1.

**Table S2. Protein synthesis and degradation rates, related to Figure 1.**

Parameter	Description	Value (Unit)	Reference
$k_{\text{Calp}}$	Synthesis rate of Calpain (Calp)	$5.0 \times 10^{-6}$ ( $\mu\text{M/s}$ )	(Hanna et al., 2008)
$k_{\text{Calc}}$	Synthesis rate of Calcineurin (Calc)	$5.0 \times 10^{-6}$ ( $\mu\text{M/s}$ )	(Bornhop et al., 2007)
$k_{\text{Cals}}$	Synthesis rate of Calpastatin (Cals)	$1.25 \times 10^{-6}$ ( $\mu\text{M/s}$ )	1/4 of Calp
$k_{\text{Bid}}$	Synthesis rate of Bid	$5.3 \times 10^{-6}$ ( $\mu\text{M/s}$ )	(Ballesta et al., 2013)
$k_{\text{pBad}}$	Synthesis rate of phosphorylated Bad (pBad)	$1.0 \times 10^{-5}$ ( $\mu\text{M/s}$ )	(Hekman et al., 2006)
$k_{\text{Bak}}$	Synthesis rate of Bak	$1.0 \times 10^{-4}$ ( $\mu\text{M/s}$ )	(Lindner et al., 2013)
$k_{\text{BclxL}}$	Synthesis rate of Bcl-X <sub>L</sub>	$2.5 \times 10^{-5}$ ( $\mu\text{M/s}$ )	1/4 of Bak
$k_{\text{Cytcm}}$	Synthesis rate of Cyt c	$1.3 \times 10^{-1}$ ( $\mu\text{M/s}$ )	Deduced from (Rehm et al., 2006)
$k_{\text{Smacm}}$	Synthesis rate of Smac	$1.6 \times 10^{-3}$ ( $\mu\text{M/s}$ )	Deduced from (Rehm et al., 2006)
$k_{\text{Apaf}}$	Synthesis rate of Apaf-1	$3.72 \times 10^{-5}$ ( $\mu\text{M/s}$ )	(Rehm et al., 2006)
$k_{\text{pcasp9}}$	Synthesis rate of Procaspsase 9	$3.0 \times 10^{-6}$ ( $\mu\text{M/s}$ )	(Rehm et al., 2006)
$k_{\text{pcasp3}}$	Synthesis rate of Procaspsase 3	$1.2 \times 10^{-5}$ ( $\mu\text{M/s}$ )	(Rehm et al., 2006)
$k_{\text{XIAP}}$	Synthesis rate of XIAP	$6.3 \times 10^{-6}$ ( $\mu\text{M/s}$ )	(Rehm et al., 2006)
$k_{\text{PARP}}$	Synthesis rate of PARP	$1.7 \times 10^{-4}$ ( $\mu\text{M/s}$ )	(Rehm et al., 2006)
$k_d$	Degradation rate of all proteins and complexes	$1.0 \times 10^{-4}$ (1/s)	(Eden et al., 2011)

**Table S3. Kinetic rate parameters, related to Figure 1.**

Parameter	Description <sup>1</sup>	Value <sup>2</sup>	Corresponding reaction	Reference <sup>3</sup>
$k_{1af}/k_{1ar}$	Association / Dissociation rate of $\text{Ca}^{2+}$ and Calp	0.1 / 3.0	1~10	4
$k_{1bf}/k_{1blr}$	Association / Dissociation rate of $\text{Ca}^{2+}$ and Calc (the first two sites)	0.2 / 1.0	11, 12	5
$k_{1b2f}/k_{1b2r}$	Association / Dissociation rate of $\text{Ca}^{2+}$ and Calc (the last two sites)	200.0 / 1.0	13, 14	5
$k_{2a1f}/k_{2a1r}$	Association / Dissociation rate of aCalp and Cals (the first site)	$20.0 / 9.0 \times 10^{-5}$	15	6
$k_{2a2f}/k_{2a2r}$	Association / Dissociation rate of aCalp and Cals (the second site)	3.0 / 0.01	16	6
$k_{2a3f}/k_{2a3r}$	Association / Dissociation rate of aCalp and Cals (the third site)	5.0 / 0.003	17	6
$k_{2a4f}/k_{2a4r}$	Association / Dissociation rate of aCalp and Cals (the fourth site)	$6.0 / 3.0 \times 10^{-4}$	18	6
$k_{2bf}/k_{2br}$	Association / Dissociation rate of aCalc and pBad	0.005 / 0.001	19	Adjusted
$k_{2beat}$	Transition rate for Bad	1.0	19	7
$k_{2cf}/k_{2cr}$	Association / Dissociation rate of aCalp and Bid	0.005 / 0.001	20	Adjusted
$k_{2ccat}$	Transition rate for tBid	1.0	20	7
$k_{3cf}/k_{3cr}$	Association / Dissociation rate of tBid and Bak on the Mt	0.015 / 0.001	23	Adjusted
$k_{3ccat}$	Transition rate for aBak	1.0	23	7
$k_{3d1f}/k_{3d1r}$	Association / Dissociation rate of aBak dimer on the Mt	0.6 / 0.001	24	7
$k_{3d2f}/k_{3d2r}$	Association / Dissociation rate of two aBak dimers on the Mt	0.6 / 0.001	25	7
$k_{3e1f}/k_{3e1r}$	Association / Dissociation rate of tBid and Bcl-X <sub>L</sub> on the Mt	0.125 / 0.001	26	8
$k_{3e2f}/k_{3e2r}$	Association / Dissociation rate of Bad and Bcl-X <sub>L</sub> on the Mt	0.05 / 0.001	27	8
$k_{3e3f}/k_{3e3r}$	Association / Dissociation rate of aBak and Bcl-X <sub>L</sub> on the Mt	0.125 / 0.001	28	8
$k_{3e4f}/k_{3e4r}$	Association / Dissociation rate of aBak dimer and Bcl-X <sub>L</sub> on the Mt	0.125 / 0.001	29	8
$k_{3e5f}/k_{3e5r}$	Association / Dissociation rate of aBak tetramer and Bcl-X <sub>L</sub> on the Mt	0.125 / 0.001	30	8
$v_{rel}$	Maximum release rate of Cyt c and Smac from Mt	50000.0	31, 32	Adjusted
$k_M$	Release threshold of Cyt c and Smac	0.025	31, 32	Adjusted
$p$	Hill coefficient	5	31, 32	Adjusted
$k_{4c1f}/k_{4c1r}$	Association / Dissociation rate of Apaf-1 and Cyt c	0.04 / 0.001	33	9
$k_{4c2f}/k_{4c2r}$	Association / Dissociation rate of Apaf-1:Cyt c oligomers	10.0 / 0.001	34~37	9
$k_{4df}/k_{4dr}$	Association / Dissociation rate of Apoptosome and Procaspsase 9	0.01 / 0.001	38	9
$k_{4dcat}$	Transition rate for Holoenzyme	1.0	38	7
$k_{4ef}/k_{4er}$	Association / Dissociation rate of Holoenzyme and Procaspsase 3	1.0 / 0.001	39	10
$k_{4ecat}$	Transition rate for Caspase 3	0.17	39	10
$k_{4flf}/k_{4flr}$	Association / Dissociation rate of Holoenzyme and XIAP	1.0 / 0.001	40	9
$k_{4f2f}/k_{4f2r}$	Association / Dissociation rate of Caspase 3 and XIAP	1.0 / 0.001	41	9
$k_{4f2cat}$	XIAP-mediated destruction rate of Caspase 3	0.001	42	11
$k_{4f3f}/k_{4f3r}$	Association / Dissociation rate of Smac and XIAP	3.0 / 0.001	43	12
$k_{4gff}/k_{4gr}$	Association / Dissociation rate of Caspase 3 and PARP	0.6 / 0.01	44	7
$k_{4gcat}$	Transition rate for cPARP	1.0	44	7
$k_{ctm}$	Translocate rate for proteins from cytosol to Mt	0.01	21, 22	13
$k_{mtc}$	Translocate rate for proteins from Mt to cytosol	0.13	21, 22	13

1. Mt, mitochondria. Other abbreviations see Table S2.

2. All units are defined with respect to the cytosolic volume. Due to limited space, they are not listed here.

3. Adjusted means that these parameters are adjusted by matching the timescale of apoptosis to the experimental observations.

4. (Campbell and Davies, 2012); 5. (Li et al., 2011); 6. (Hanna et al., 2007); 7. (Albeck et al., 2008b); 8. (Ku et al., 2010); 9. (Würstle and Rehm, 2014); 10. (Pop et al., 2006); 11. (Albeck et al., 2008a); 12. (Huang et al., 2003); 13. (Aldridge et al., 2011).

**Table S4. Biochemical reactions and corresponding reaction rates, related to Figure 1.**

Number	Reaction	Reaction rate
1	$\text{Calp} + \text{Ca}_{\text{Mic}}^{2+} \xrightleftharpoons[k_{1\text{ar}}]{k_{1\text{af}}} \text{Calp1Ca}$	$J_{1\text{a}1} = 10k_{1\text{af}}[\text{Calp}][\text{Ca}_{\text{Mic}}^{2+}] - k_{1\text{ar}}[\text{Calp1Ca}]$
2~9	$\text{CalpmCa} + \text{Ca}_{\text{Mic}}^{2+} \xrightleftharpoons[k_{1\text{ar}}]{k_{1\text{af}}} \text{CalpnCa}$ ( $m = 1 \sim 8, n = m + 1$ )	$J_{1\text{a}n} = (11-n)k_{1\text{af}}[\text{CalpmCa}][\text{Ca}_{\text{Mic}}^{2+}] - k_{1\text{ar}}[\text{CalpnCa}]$
10	$\text{Calp9Ca} + \text{Ca}_{\text{Mic}}^{2+} \xrightleftharpoons[k_{1\text{ar}}]{k_{1\text{af}}} \text{aCalp}$	$J_{1\text{a}10} = k_{1\text{af}}[\text{Calp9Ca}][\text{Ca}_{\text{Mic}}^{2+}] - k_{1\text{ar}}[\text{aCalp}]$
11	$\text{Calc} + \text{Ca}_{\text{Cyt}}^{2+} \xrightleftharpoons[k_{1\text{b}1\text{r}}]{k_{1\text{b}1\text{f}}} \text{Calc1Ca}$	$J_{1\text{b}1} = 2k_{1\text{b}1\text{f}}[\text{Calc}][\text{Ca}_{\text{Cyt}}^{2+}] - k_{1\text{b}1\text{r}}[\text{Calc1Ca}]$
12	$\text{Calc1Ca} + \text{Ca}_{\text{Cyt}}^{2+} \xrightleftharpoons[k_{1\text{b}1\text{r}}]{k_{1\text{b}1\text{f}}} \text{Calc2Ca}$	$J_{1\text{b}2} = k_{1\text{b}1\text{f}}[\text{Calc1Ca}][\text{Ca}_{\text{Cyt}}^{2+}] - k_{1\text{b}1\text{r}}[\text{Calc2Ca}]$
13	$\text{Calc2Ca} + \text{Ca}_{\text{Cyt}}^{2+} \xrightleftharpoons[k_{1\text{b}2\text{r}}]{k_{1\text{b}2\text{f}}} \text{Calc3Ca}$	$J_{1\text{b}3} = 2k_{1\text{b}2\text{f}}[\text{Calc2Ca}][\text{Ca}_{\text{Cyt}}^{2+}] - k_{1\text{b}2\text{r}}[\text{Calc3Ca}]$
14	$\text{Calc3Ca} + \text{Ca}_{\text{Cyt}}^{2+} \xrightleftharpoons[k_{1\text{b}2\text{r}}]{k_{1\text{b}2\text{f}}} \text{aCalc}$	$J_{1\text{b}4} = k_{1\text{b}2\text{f}}[\text{Calc3Ca}][\text{Ca}_{\text{Cyt}}^{2+}] - k_{1\text{b}2\text{r}}[\text{aCalc}]$
15	$\text{Cals} + \text{aCalp} \xrightleftharpoons[k_{2\text{a}1\text{r}}]{k_{2\text{a}1\text{f}}} \text{Cals:aCalp}$	$J_{2\text{a}1} = k_{2\text{a}1\text{f}}[\text{Cals}][\text{aCalp}] - k_{2\text{a}1\text{r}}[\text{Cals:aCalp}]$
16	$\text{Cals:aCalp} + \text{aCalp} \xrightleftharpoons[k_{2\text{a}2\text{r}}]{k_{2\text{a}2\text{f}}} \text{Cals:aCalp}_2$	$J_{2\text{a}2} = k_{2\text{a}2\text{f}}[\text{Cals:aCalp}][\text{aCalp}] - k_{2\text{a}2\text{r}}[\text{Cals:aCalp}_2]$
17	$\text{Cals:aCalp}_2 + \text{aCalp} \xrightleftharpoons[k_{2\text{a}3\text{r}}]{k_{2\text{a}3\text{f}}} \text{Cals:aCalp}_3$	$J_{2\text{a}3} = k_{2\text{a}3\text{f}}[\text{Cals:aCalp}_2][\text{aCalp}] - k_{2\text{a}3\text{r}}[\text{Cals:aCalp}_3]$
18	$\text{Cals:aCalp}_3 + \text{aCalp} \xrightleftharpoons[k_{2\text{a}4\text{r}}]{k_{2\text{a}4\text{f}}} \text{Cals:aCalp}_4$	$J_{2\text{a}4} = k_{2\text{a}4\text{f}}[\text{Cals:aCalp}_3][\text{aCalp}] - k_{2\text{a}4\text{r}}[\text{Cals:aCalp}_4]$
19	$\text{aCalc} + \text{pBad} \xrightleftharpoons[k_{2\text{br}}]{k_{2\text{bf}}} \text{aCalc:pBad}$ $\xrightarrow{k_{2\text{beat}}} \text{aCalc} + \text{Bad}$	$J_{2\text{b}} = k_{2\text{bf}}[\text{aCalc}][\text{pBad}] - k_{2\text{br}}[\text{aCalc:pBad}]$ $J_{2\text{beat}} = k_{2\text{beat}}[\text{aCalc:pBad}]$
20	$\text{aCalp} + \text{Bid} \xrightleftharpoons[k_{2\text{cr}}]{k_{2\text{cf}}} \text{aCalp:Bid}$ $\xrightarrow{k_{2\text{ccat}}} \text{aCalp} + \text{tBid}$	$J_{2\text{c}} = k_{2\text{cf}}[\text{aCalp}][\text{Bid}] - k_{2\text{cr}}[\text{aCalp:Bid}]$ $J_{2\text{ccat}} = k_{2\text{ccat}}[\text{aCalp:Bid}]$
21	$\text{tBid} \xrightleftharpoons[k_{\text{mtc}}]{k_{\text{ctm}}} \text{tBid}_m$	$J_{3\text{atran}} = k_{\text{ctm}}[\text{tBid}] - k_{\text{mtc}}[\text{tBid}_m]$
22	$\text{Bad} \xrightleftharpoons[k_{\text{mtc}}]{k_{\text{ctm}}} \text{Bad}_m$	$J_{3\text{btran}} = k_{\text{ctm}}[\text{Bad}] - k_{\text{mtc}}[\text{Bad}_m]$
23	$\text{tBid}_m + \text{Bak} \xrightleftharpoons[k_{3\text{er}}]{k_{3\text{cf}}} \text{tBid}_m:\text{Bak}$ $\xrightarrow{k_{3\text{ccat}}} \text{tBid}_m + \text{aBak}$	$J_{3\text{c}} = k_{3\text{cf}}/\text{V}[\text{tBid}_m][\text{Bak}] - k_{3\text{er}}[\text{tBid}_m:\text{Bak}]$ $J_{3\text{ccat}} = k_{3\text{ccat}}[\text{tBid}_m:\text{Bak}]$
24	$2\text{aBak} \xrightleftharpoons[k_{3\text{dlr}}]{k_{3\text{dlf}}} \text{aBak}_2$	$J_{3\text{d}1} = k_{3\text{dlf}}/\text{V}[\text{aBak}]^2 - k_{3\text{dlr}}[\text{aBak}_2]$
25	$2\text{aBak}_2 \xrightleftharpoons[k_{3\text{d2r}}]{k_{3\text{d2f}}} \text{aBak}_4$	$J_{3\text{d}2} = k_{3\text{d2f}}/\text{V}[\text{aBak}_2]^2 - k_{3\text{d2r}}[\text{aBak}_4]$
26	$\text{tBid}_m + \text{Bcl-X}_L \xrightleftharpoons[k_{3\text{elr}}]{k_{3\text{elf}}} \text{tBid}_m:\text{Bcl-X}_L$	$J_{3\text{e}1} = k_{3\text{elf}}/\text{V}[\text{tBid}_m][\text{Bcl-X}_L] - k_{3\text{elr}}[\text{tBid}_m:\text{Bcl-X}_L]$
27	$\text{Bad}_m + \text{Bcl-X}_L \xrightleftharpoons[k_{3\text{e2r}}]{k_{3\text{e2f}}} \text{Bad}_m:\text{Bcl-X}_L$	$J_{3\text{e}2} = k_{3\text{e2f}}/\text{V}[\text{Bad}_m][\text{Bcl-X}_L] - k_{3\text{e2r}}[\text{Bad}_m:\text{Bcl-X}_L]$
28	$\text{Bcl-X}_L + \text{aBak} \xrightleftharpoons[k_{3\text{e3r}}]{k_{3\text{e3f}}} \text{Bcl-X}_L:\text{aBak}$	$J_{3\text{e}3} = k_{3\text{e3f}}/\text{V}[\text{Bcl-X}_L][\text{aBak}] - k_{3\text{e3r}}[\text{Bcl-X}_L:\text{aBak}]$

29	$Bcl-X_L + aBak_2 \xrightleftharpoons[k_{3e4r}]{k_{3e4f}} Bcl-X_L:aBak_2$	$J_{3e4} = k_{3e4f} / V[Bcl-X_L][aBak_2] - k_{3e4r}[Bcl-X_L:aBak_2]$
30	$Bcl-X_L + aBak_4 \xrightleftharpoons[k_{3e5r}]{k_{3e5f}} Bcl-X_L:aBak_4$	$J_{3e5} = k_{3e5f} / V[Bcl-X_L][aBak_4] - k_{3e5r}[Bcl-X_L:aBak_4]$
31	$Cyt\ c_m \rightarrow Cyt\ c$	$J_{4atran} = v_{rel} \frac{[MOMP]^p}{k_M^p + [MOMP]^p} ([Cyt\ c_m] - [Cyt\ c])$
32	$Smac_m \rightarrow Smac$	$J_{4btran} = v_{rel} \frac{[MOMP]^p}{k_M^p + [MOMP]^p} ([Smac_m] - [Smac])$
33	$Apaf+Cyt\ c \xrightleftharpoons[k_{4c1r}]{k_{4c1f}} Apaf:Cyt\ c\ (AC)$	$J_{4c1} = k_{4c1f}[Apaf][Cyt\ c] - k_{4c1r}[AC]$
34	$AC+AC \xrightleftharpoons[k_{4c2r}]{k_{4c2f}} AC_2$	$J_{4c2} = k_{4c2f}[AC]^2 - k_{4c2r}[AC_2]$
35	$AC+AC_2 \xrightleftharpoons[k_{4c2r}]{k_{4c2f}} AC_3$	$J_{4c3} = k_{4c2f}[AC][AC_2] - k_{4c2r}[AC_3]$
36	$AC+AC_3 \xrightleftharpoons[k_{4c2r}]{k_{4c2f}} AC_4$	$J_{4c4} = k_{4c2f}[AC][AC_3] - k_{4c2r}[AC_4]$
37	$AC_3+AC_4 \xrightleftharpoons[k_{4c2r}]{k_{4c2f}} Apop$	$J_{4c5} = k_{4c2f}[AC_3][AC_4] - k_{4c2r}[Apop]$
38	$Apop+pCasp9 \xrightleftharpoons[k_{4dr}]{k_{4df}} Apop:pCasp9$ $\xrightarrow{k_{4dcat}} Holo$	$J_{4d} = k_{4df}[Apop][pCasp9] - k_{4dr}[Apop:pCasp9]$ $J_{4dcat} = k_{4dcat}[Apop:pCasp9]$
39	$Holo+pCasp3 \xrightleftharpoons[k_{4er}]{k_{4ef}} Holo:pCasp3$ $\xrightarrow{k_{4ecat}} Holo+Casp3$	$J_{4e} = k_{4ef}[Holo][pCasp3] - k_{4er}[Holo:pCasp3]$ $J_{4ecat} = k_{4ecat}[Holo:pCasp3]$
40	$XIAP+Holo \xrightleftharpoons[k_{4flr}]{k_{4flf}} XIAP:Holo$	$J_{4fl} = k_{4flf}[XIAP][Holo] - k_{4flr}[XIAP:Holo]$
41	$XIAP+Casp3 \xrightleftharpoons[k_{4f2r}]{k_{4f2f}} XIAP:Casp3$	$J_{4f2} = k_{4f2f}[XIAP][Casp3] - k_{4f2r}[XIAP:Casp3]$
42	$XIAP:Casp3 \xrightarrow{k_{4f2cat}} \emptyset$	$J_{4f2cat} = k_{4f2cat}[XIAP:Casp3]$
43	$2Smac+XIAP \xrightleftharpoons[k_{4f3r}]{k_{4f3f}} Smac_2:XIAP$	$J_{4f3} = k_{4f3f}[Smac]^2[XIAP] - k_{4f3r}[Smac_2:XIAP]$
44	$Casp3+PARP \xrightleftharpoons[k_{4gr}]{k_{4gf}} Casp3:PARP$ $\xrightarrow{k_{4gcat}} Casp3+cPARP$	$J_{4g} = k_{4gf}[Casp3][PARP] - k_{4gr}[Casp3:PARP]$ $J_{4gcat} = k_{4gcat}[Casp3:PARP]$

**Table S5. Ordinary differential equations, related to Figure 1.**

Number	ODE
1	$\dot{[Calp]} = k_{Calp} - J_{1a1} - k_d [Calp]$
2	$\dot{[Calp1Ca]} = J_{1a1} - J_{1a2} - k_d [Calp1Ca]$
3	$\dot{[Calp2Ca]} = J_{1a2} - J_{1a3} - k_d [Calp2Ca]$
4	$\dot{[Calp3Ca]} = J_{1a3} - J_{1a4} - k_d [Calp3Ca]$
5	$\dot{[Calp4Ca]} = J_{1a4} - J_{1a5} - k_d [Calp4Ca]$
6	$\dot{[Calp5Ca]} = J_{1a5} - J_{1a6} - k_d [Calp5Ca]$
7	$\dot{[Calp6Ca]} = J_{1a6} - J_{1a7} - k_d [Calp6Ca]$
8	$\dot{[Calp7Ca]} = J_{1a7} - J_{1a8} - k_d [Calp7Ca]$
9	$\dot{[Calp8Ca]} = J_{1a8} - J_{1a9} - k_d [Calp8Ca]$
10	$\dot{[Calp9Ca]} = J_{1a9} - J_{1a10} - k_d [Calp9Ca]$
11	$\dot{[aCalp]} = J_{1a10} - J_{2a1} - J_{2a2} - J_{2a3} - J_{2a4} - J_{2c} + J_{2ccat} - k_d [aCalp]$
12	$\dot{[Calc]} = k_{Calc} - J_{1b1} - k_d [Calc]$
13	$\dot{[Calc1Ca]} = J_{1b1} - J_{1b2} - k_d [Calc1Ca]$
14	$\dot{[Calc2Ca]} = J_{1b2} - J_{1b3} - k_d [Calc2Ca]$
15	$\dot{[Calc3Ca]} = J_{1b3} - J_{1b4} - k_d [Calc3Ca]$
16	$\dot{[aCalc]} = J_{1b4} - J_{2b} + J_{2bcat} - k_d [aCalc]$
17	$\dot{[Cals]} = k_{Cals} - J_{2a1} - k_d [Cals]$
18	$\dot{[Cals:aCalp]} = J_{2a1} - J_{2a2} - k_d [Cals:aCalp]$
19	$\dot{[Cals:aCalp_2]} = J_{2a2} - J_{2a3} - k_d [Cals:aCalp_2]$
20	$\dot{[Cals:aCalp_3]} = J_{2a3} - J_{2a4} - k_d [Cals:aCalp_3]$
21	$\dot{[Cals:aCalp_4]} = J_{2a4} - k_d [Cals:aCalp_4]$
22	$\dot{[pBad]} = k_{pBad} - J_{2b} - k_d [pBad]$
23	$\dot{[aCalc:pBad]} = J_{2b} - J_{2bcat} - k_d [aCalc:pBad]$

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- 24  $\dot{[Bad]} = J_{2bcat} - J_{3btran} - k_d [Bad]$
- 25  $\dot{[Bad_m]} = J_{3btran} - J_{3e2} - k_d [Bad_m]$
- 26  $\dot{[Bid]} = k_{Bid} - J_{2c} - k_d [Bid]$
- 27  $\dot{[aCalp:Bid]} = J_{2c} - J_{2ccat} - k_d [aCalp:Bid]$
- 28  $\dot{[tBid]} = J_{2ccat} - J_{3atran} - k_d [tBid]$
- 29  $\dot{[tBid_m]} = J_{3atran} - J_{3c} + J_{3ccat} - k_d [tBid_m]$
- 30  $\dot{[Bak]} = k_{Bak} - J_{3c} - k_d [Bak]$
- 31  $\dot{[tBid_m:Bak]} = J_{3c} - J_{3ccat} - k_d [tBid_m:Bak]$
- 32  $\dot{[aBak]} = J_{3ccat} - 2J_{3d1} - J_{3e3} - k_d [aBak]$
- 33  $\dot{[aBak_2]} = J_{3d1} - 2J_{3d2} - J_{3e4} - k_d [aBak_2]$
- 34  $\dot{[aBak_4]} = J_{3d2} - J_{3e5} - k_d [aBak_4]$
- 35  $\dot{[Bcl-X_L]} = k_{Bcl-X_L} - J_{3e1} - J_{3e2} - J_{3e3} - J_{3e4} - J_{3e5} - k_d [Bcl-X_L]$
- 36  $\dot{[tBid_m:Bcl-X_L]} = J_{3e1} - k_d [tBid_m:Bcl-X_L]$
- 37  $\dot{[Bad_m:Bcl-X_L]} = J_{3e2} - k_d [Bad_m:Bcl-X_L]$
- 38  $\dot{[Bcl-X_L:aBak]} = J_{3e3} - k_d [Bcl-X_L:aBak]$
- 39  $\dot{[Bcl-X_L:aBak_2]} = J_{3e4} - k_d [Bcl-X_L:aBak_2]$
- 40  $\dot{[Bcl-X_L:aBak_4]} = J_{3e5} - k_d [Bcl-X_L:aBak_4]$
- 41  $\dot{[Cyt\,c_m]} = k_{Cyt\,c_m} - J_{4atran} - k_d [Cyt\,c_m]$
- 42  $\dot{[Smac_m]} = k_{Smac_m} - J_{4btran} - k_d [Smac_m]$
- 43  $\dot{[Cyt\,c]} = VDV * J_{4atran} - J_{4c1} - k_d [Cyt\,c]$
- 44  $\dot{[Smac]} = VDV * J_{4btran} - 2J_{4f3} - k_d [Smac]$
- 45  $\dot{[Apaf]} = k_{Apaf} - J_{4c1} - k_d [Apaf]$
- 46  $\dot{[AC]} = J_{4c1} - 2J_{4c2} - J_{4c3} - J_{4c4} - k_d [AC]$
- 47  $\dot{[AC_2]} = J_{4c2} - J_{4c3} - k_d [AC_2]$
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48	$\dot{[AC_3]} = J_{4c3} - J_{4c4} - J_{4c5} - k_d [AC_3]$
49	$\dot{[AC_4]} = J_{4c4} - J_{4c5} - k_d [AC_4]$
50	$\dot{[Apop]} = J_{4c5} - J_{4d} - k_d [Apop]$
51	$\dot{[pCasp9]} = k_{pCasp9} - J_{4d} - k_d [pCasp9]$
52	$\dot{[Apop:pCasp9]} = J_{4d} - J_{4dcat} - k_d [Apop:pCasp9]$
53	$\dot{[Holo]} = J_{4dcat} - J_{4e} + J_{4ecat} - J_{4f1} - k_d [Holo]$
54	$\dot{[pCasp3]} = k_{pCasp3} - J_{4e} - k_d [pCasp3]$
55	$\dot{[Holo:pCasp3]} = J_{4e} - J_{4ecat} - k_d [Holo:pCasp3]$
56	$\dot{[Casp3]} = J_{4ecat} - J_{4f2} - J_{4g} + J_{4gcat} - k_d [Casp3]$
57	$\dot{[XIAP]} = k_{XIAP} + J_{4f2cat} - J_{4f1} - J_{4f2} - J_{4f3} + J_{4f2cat} - k_d [XIAP]$
58	$\dot{[XIAP:Holo]} = J_{4f1} - k_d [XIAP:Holo]$
59	$\dot{[XIAP:Casp3]} = J_{4f2} - J_{4f2cat} - k_d [XIAP:Casp3]$
60	$\dot{[Smac:XIAP]} = J_{4f3} - k_d [Smac:XIAP]$
61	$\dot{[PARP]} = k_{PARP} - J_{4g} - k_d [PARP]$
62	$\dot{[Casp3:PARP]} = J_{4g} - J_{4gcat} - k_d [Casp3:PARP]$
63	$\dot{[cPARP]} = J_{4gcat} - k_d [cPARP]$
64	$\dot{[IP3]} = p_{IP3} \frac{Stimulus^2}{k_{IP3}^2 + Stimulus^2} - d_{IP3} [IP3]$
65	$\dot{h} = \alpha_h (1-h) - \beta_h h$
66	$\dot{[Ca\_cyt]} = (J_{IP3R} + J_{Leak} - J_{SERCA}) - \sum_1^{10} J_{1ai} - \sum_1^4 J_{1bj}$ $+ k_d \sum_1^9 m [CalpmCa] + 10 k_d [aCalp]$ $+ k_d \sum_1^3 n [CalcnCa] + 4 k_d [aCalc]$ $+ 10 k_d (\sum_1^4 q [Cals:aCalp_q] + [aCalp:Bid])$ $+ 4 k_d [aCalc:pBad]$

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