# SC-2 Electric Boogalo

Regression on the Irish datset agregated by class

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### Contents

1	Cle	aning the Data	1	
	1.1	Data overview	]	
	1.2	Loading and Structure	2	
	1.3	Feature engineering	2	
		1.3.1 Temperature	2	
		1.3.2 Day of the week	•	
		1.3.3 Fourier terms		
	1.4	Social class	•	
<b>2</b>	Sim	aple Regression	4	
	2.1	Theory	4	
	2.2	Model		
	2.3	Implementation	4	
3	$\operatorname{Rid}$	ge Regression	4	
	3.1	Theory	4	
	3.2	Model	4	
	3.3	Implementation	4	
4	Gaussian Process Regression			
	4.1	Theory	4	
	4.2	Model	4	
	4.3	Implementation	4	
5	Res	m sults	4	

## 1 Cleaning the Data

#### 1.1 Data overview

We are analyzing a set of Irish household electricity demand available from the electBook package. We have three datasets:

- indCons: 16799 x 2672 matrix of individual household electricity consumption. Each column corresponds to a household and each row to a time point. Demand is observed every half hour, so there are 48 observations per day per household.
- survey: 2672 row dataframe of household survey data. This dataset contains household level data on variables such as social class, renting vs. owning, appliances, etc.
- extra: 16799 row dataframe of time-related variables. This dataset contains the date-time of each demand observation, time of year, day of week, time of day, whether the day was a holiday, and external temperature.

```
# Extract individual dataframes
library(electBook)
library(tidyverse)
data(Irish)
indCons <- Irish[["indCons"]]
survey <- Irish[["survey"]]
extra <- Irish[["extra"]]</pre>
```

## 1.2 Loading and Structure

```
# Aggregate total
# Frequency is 30 minutes, so each day has 48 ticks
agg <- rowSums(indCons)</pre>
```

## 1.3 Feature engineering

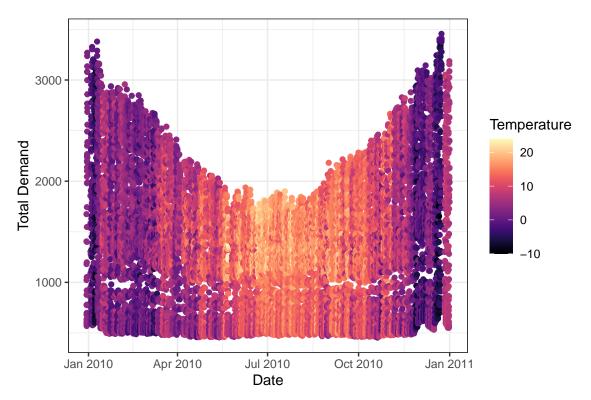
Based on exploratory data analysis, we created some features from the dataset to model demand.

### 1.3.1 Temperature

We can visualize the relationship between temperature and the aggregate demand over time across all households:

```
temp_demand <- data.frame(demand = agg) %>%
  bind_cols(Irish[["extra"]])

ggplot(temp_demand, aes(x = dateTime, y = demand, color = temp)) +
  geom_point() +
  viridis::scale_color_viridis(option = "magma") +
  labs(x = "Date", y = "Total Demand", color = "Temperature") +
  theme_bw()
```



We can see that during the warmer summer months, demand dips, although the pattern is messy. We included linear and quadratic terms for temperature in our models.

### 1.3.2 Day of the week

Since we have the categorical variable day of the week for each date, we used one-hot encoding to include this information in our models.

### 1.3.3 Fourier terms

We used Fourier terms to capture the patterns of seasonality in the data. Fourier terms are a set of sine and cosine functions with different frequencies that can be used to model periodic patterns. For a given period P, the Fourier terms are defined as follows:

$$\sin_k(t) = \sin\left(\frac{2\pi kt}{P}\right), \quad \cos_k(t) = \cos\left(\frac{2\pi kt}{P}\right)$$

where k is the frequency and t is the time.

We used Fourier terms to model the daily and annual seasonality in the data.

#### 1.4 Social class

We wanted to investigate demand patterns across different social classes. The dataset includes 5 social classes, defined by the occupation of the head of household:

- AB: managerial roles, administrative or professional
- C1: supervisory, clerical, junior managerial
- C2: skilled manual workers
- DE: semi-skilled and unskilled manual workers, state pensioners, casual workers
- F: farmers

<sup>\*\*</sup> Insert plot of demand patterns for different classes \*\*

We modeled the average demand for each social class separately.

## 2 Simple Regression

- 2.1 Theory
- 2.2 Model
- 2.3 Implementation

## 3 Ridge Regression

### 3.1 Theory

Ridge regression is a method for penalized regression. Consider the model

$$Y_i^0 = \alpha + \beta x_i^0 + \epsilon_i, \quad i = 1, ..., n$$

where  $\beta \in \mathbb{R}^p$ ,  $\alpha \in \mathbb{R}$ , and for all  $i, l \in \{1, ..., n\}$ ,  $\mathbb{E}[\epsilon_i] = 0$  and  $\mathbb{E}[\epsilon_i \epsilon_l] = \sigma^2 \delta_{il}$  for some  $\sigma^2 > 0$ . Then the ridge regression estimator is defined as the minimizer of the following objective function:

$$(\hat{\alpha}_{\lambda},\hat{\beta}_{\lambda}) = \operatorname{argmin}_{\alpha \in \mathbb{R}, \beta \in \mathbb{R}^p} \|y^0 - \alpha - X^0 \beta\|_2^2 + \lambda \|\beta\|_2^2$$

where  $\lambda > 0$  is a tuning parameter and  $\|\cdot\|_2$  denotes the Euclidean norm. Ridge regression is thus imposing a penalty on the size of  $\beta$ , with the strength of that penalty determined by the choice of  $\lambda$ . The coefficients will be shrunk towards zero, but will not be set to zero (as opposed to in lasso regression).

### 3.2 Model

### 3.3 Implementation

## 4 Gaussian Process Regression

### 4.1 Theory

A gaussian process is a collection of random variables, which have a joint Gaussian distribution. A Gaussian process is completely specified by its mean function and covariance function. We build the following model:

Let  $y_i = f(x_i) + \varepsilon_i$ , where  $f(x) \sim \text{GP}(0, k(x, x'))$  and  $\varepsilon_i \sim N(0, \sigma^2)$ . Then we can find the posterior distribution of  $f(x_*)$  given y as:

$$f(x_*)|y \sim N(\mu(x_*), \sigma^2(x_*))$$

where  $\mu(x_*) = k(x_*,x)^T(K+\sigma^2I)^{-1}y$  and  $\sigma^2(x_*) = k(x_*,x_*) - k(x_*,x)^T(K+\sigma^2I)^{-1}k(x_*,x)$ . In practice, to find the posterior distribution, we maximise the marginal log-likelihood.

#### 4.2 Model

### 4.3 Implementation

### 5 Results