

Tutorial Week 10

Questions

1. Is the Diffie-Hellman algorithm a public key encryption algorithm? If not, what is it?
2. 133 is the product of two primes. What are they?
3. RSA and Diffie-Hellman can generate very large numbers that require their modulus to be calculated. Fortunately, modulo arithmetic is associative and commutative. That is:

$$a^{p+q+r} \bmod N = (a^p \bmod N) (a^q \bmod N) (a^r \bmod N) \bmod N$$

For example

$$\begin{aligned} 3^6 \bmod 5 \\ &= (3^2 \bmod 5) (3^2 \bmod 5) (3^2 \bmod 5) \bmod 5 \\ &= (9 \bmod 5)(9 \bmod 5)(9 \bmod 5) \bmod 5 \\ &= 4^3 \bmod 5 = 64 \bmod 5 = 4 \end{aligned}$$

Try this approach with $5^5 \bmod 23$

4. What key do Alice and Bob come to agree upon using the Diffie-Hellman algorithm using the following values?

Alice chooses $a = 3$, Bob chooses $b = 4$, $p = 17$ and $g = 3$.

5. The following is a public/private key pair.

$[33,3]$ and $[33,7]$

Use the keys and RSA to encrypt and decrypt '2'.

6. Generate a public / private key using the prime numbers 3 and 11.