

PV System

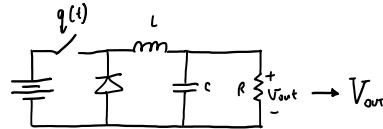
Thursday, March 7, 2024 4:04 PM

RECAP DC-DC power converters — L.C. switches

$$\langle V_L \rangle = 0$$

$$\langle i_C \rangle = 0$$

• DC-DC Buck Converter



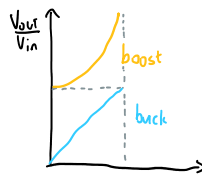
$$\text{SWITCH ON: } V_L(t) = V_{in} - V_{out} \geq 0 \rightarrow i_L(t) \uparrow$$

$$\text{SWITCH OFF: } V_L(t) = -V_{out} \leq 0 \rightarrow i_L(t) \downarrow$$

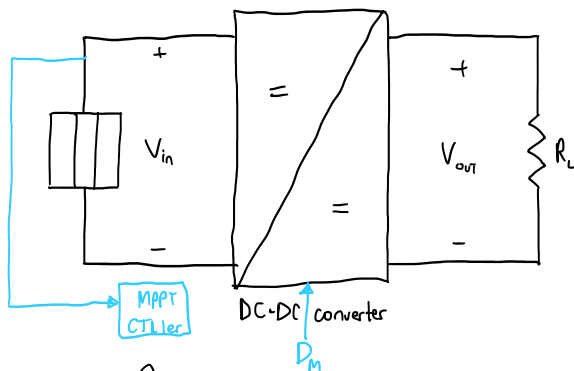
$$\langle V_L(t) \rangle = 0 \rightarrow V_{out} = D V_{in}, \quad 0 \leq D \leq 1$$

• DC-DC Boost Converter

$$V_{out} = \frac{1}{1-D} V_{in}$$



How do converters fit into PV systems?



$$V_{out} = f(D) V_{in}$$

Also, if 100% efficient:

$$I_{out} = \frac{1}{f(D)} I_{in}$$

Example Resistive load $V_{out} = I_{out} R$

$$f(D) V_{in} = \frac{1}{f(D)} I_{in} R$$

Denote by D_m as duty cycle that ensures $V_{in} = V_m, I_{in} = I_m$

$$(f(D))^2 = \frac{I_{in}}{V_{in}} R = \frac{R}{R_m} \quad \text{where } R_m = \frac{V_m}{I_m}$$

$$(*) D_m = f^{-1}\left(\sqrt{\frac{R}{R_m}}\right)$$

For buck: $f(D) = D$

For boost: $f(D) = \frac{1}{1-D}$

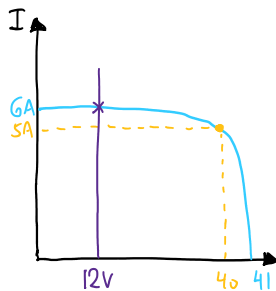
For buck: $D^2 = \frac{I_m}{V_m} R = \frac{R}{R_m}$
 $D_m = \sqrt{\frac{R}{R_m}}$

For boost: $\left(\frac{1}{1-D}\right)^2 = \frac{R}{R_m}$
 \dots Solve for D to get D_m

Determine D_m such that (*) is satisfied.

* MPPT determines R_m (or V_m and I_m) to give to converter

Example PV module with following specifications: $V_{oc} = 41\text{ V}$, $I_{sc} = 6\text{ A}$, $V_m = 40\text{ V}$, $I_m = 5\text{ A}$



Want to deliver power to charge a 12V battery

Want to use a DC-DC converter to extract maximum power from module

1) Topology \rightarrow Buck converter because $V_{out} < V_{in}$

2) Duty Cycle $\rightarrow V_{out} = D V_{in}$

$$12 = D \cdot 40 \rightarrow D = 0.3$$

3) If solar irradiance increases, would the required duty cycle increase or decrease?

$$\text{solar irradiance} \uparrow \rightarrow I_{sc} \uparrow \rightarrow V_m = ?$$

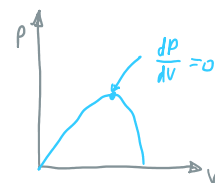
$$I = I_{sc} - I_o \left(e^{\frac{qV}{kT}} - 1 \right) \quad \text{ideal equivalent circuit model}$$

$$P = VI = VI_{sc} - VI_o \left(e^{\frac{qV}{kT}} - 1 \right)$$

$$\frac{dP}{dV} = I_{sc} - I_o \left(e^{\frac{qV}{kT}} - 1 \right) - VI_o \frac{q}{kT} e^{\frac{qV}{kT}} = 0$$

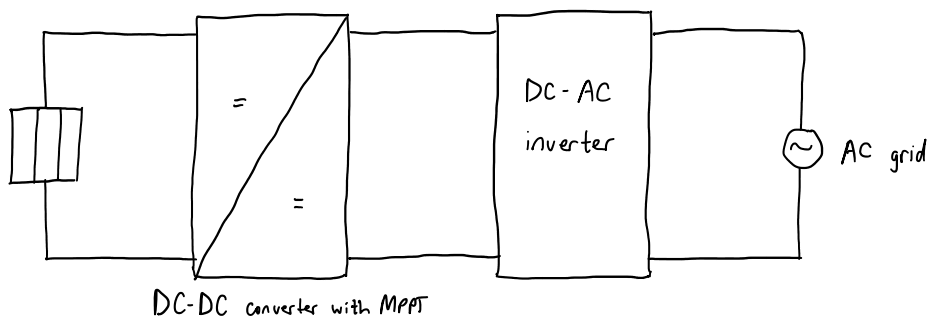
$$0 = I_{sc} - I_o e^{\frac{qV}{kT}} + I_o - VI_o \frac{q}{kT} e^{\frac{qV}{kT}}$$

$$I_{sc} = I_o e^{\frac{qV}{kT}} \left(1 + \frac{qV}{kT} \right) - I_o$$

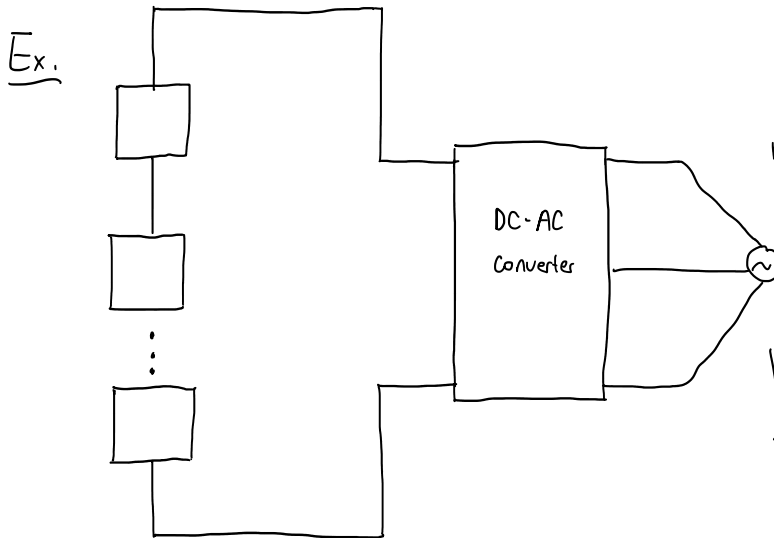


$$I_{sc} \uparrow \rightarrow V_m \uparrow \rightarrow D \downarrow$$

Grid Interface (DC-AC Inverter)



Design considerations:
 > losses, cost, footprint, power ratings, power density, harmonics



Suppose that the inverter input voltage is rated for 1000V.

What is the maximum number of modules that can be connected in series?

Idea: maximum number of modules in series = $\left\lceil \frac{1000}{V_{oc}} \right\rceil$ → We know voltage will be less than V_{oc}
 $= \left\lceil \frac{1000}{67.9} \right\rceil = 14$
 ↳ from spec sheet

NOT the whole story, spec sheet data is obtained at STC (25°C , AM 1.5, 1 kW/m^2)

Say the module will be installed at a location where ambient temperature can be as low as -10°C .

How does V_{oc} change with temperature?

$$\frac{dV_{oc}}{dT} = -167.4 \text{ mV}/^\circ\text{C}$$

$$\text{At } -10^\circ\text{C}, V_{oc}' = V_{oc} + \frac{dV_{oc}}{dT} \Delta T$$

$$= 67.9 + (-0.1674)(-10 - 25)$$

$$= 73.8 \text{ V}$$

$$\longrightarrow T \downarrow \rightarrow V_{oc} \uparrow$$

Now Maximum number of modules in series = $\left\lceil \frac{1000}{73.8} \right\rceil = 13!$

- Micro inverters — embed MPPT

- increase reliability

- easier to repair/maintain

- flexible footprint



- could be more expensive ^{\$\$}