

Solar Spectrum

Tuesday, January 30, 2024 4:06 PM

Solar Energy Conversion System

↳ Converting the sun's energy into electrical power

• Insolation

↳ Incident Solar Radiation [W/m^2]

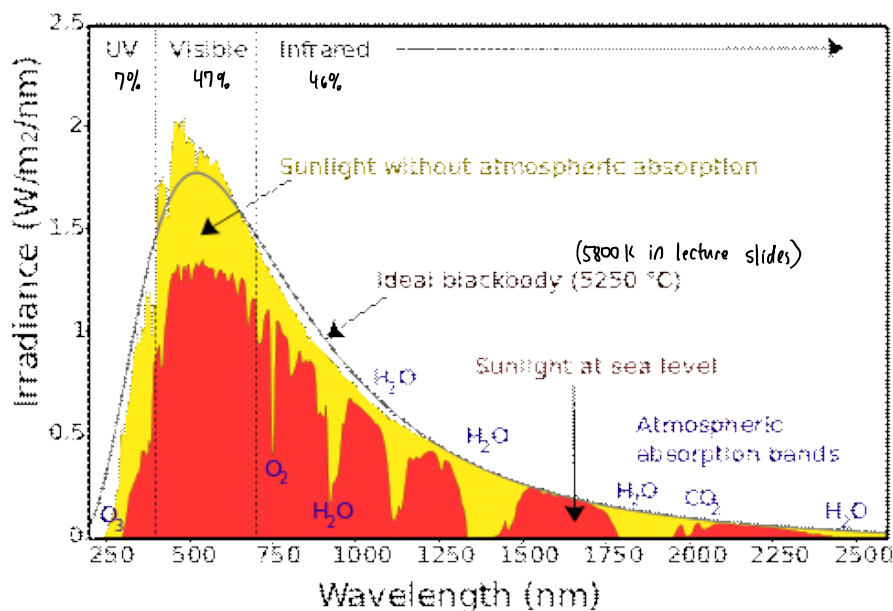
• Goal: • Determine insolation for a particular location

on " " day

at " " time

• Choose good locations and tilt angles for solar panels

Spectrum of Solar Radiation (Earth)

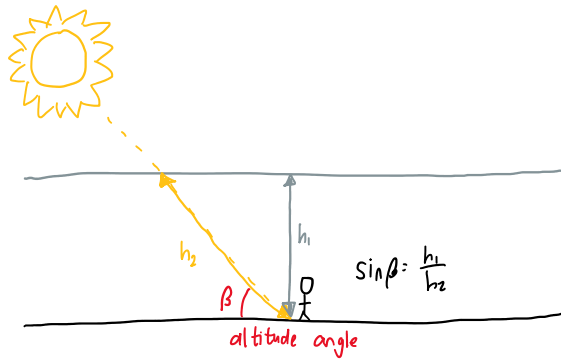


• Area under curve = solar insolation just under Earth's atmosphere [W/m^2]
= 1.37 kW/m^2

• As solar radiation makes its way to Earth's surface, it has to pass some distance thru Earth's atmosphere

↳ Attenuation occurs, but by how much?

• Simplifying Assumption: Earth is flat (!)

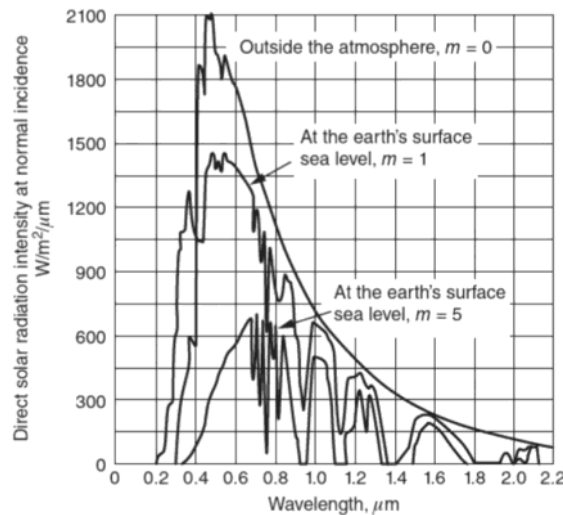


Air Mass Ratio

$$m = \frac{h_2}{h_1} = \frac{1}{\sin \beta}$$

↳ AM 0 → extra-terrestrial solar spectrum

↳ AM 1.5 → average



• As m increases, spectrum attenuation overall

• Also, shift towards longer wavelength

$$E = \frac{hc}{\lambda} \quad \text{photon energy}$$

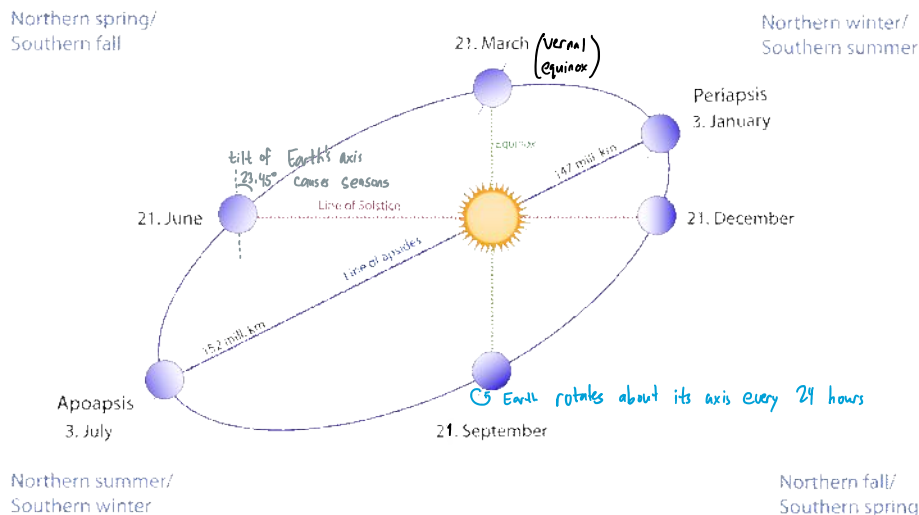


• This is why sunsets look red

• To compute m without the flat earth assumption, need to know more about Earth's orbit

Earth's Orbit

• Elliptical orbit around the sun 365.25 days/yr



• Variation in distance:

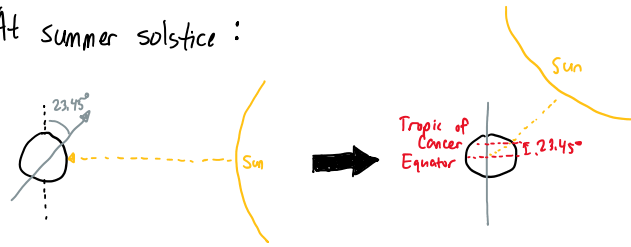
$$d = 1.5 \times 10^8 \left(1 + 0.017 \sin \left(\frac{360(n-93)}{365} \right) \right) \quad [\text{km}]$$

↗ day number. {Jan 1 = 1, ..., Dec 31 = 365}
↘ in degrees
↖ distance away from the sun

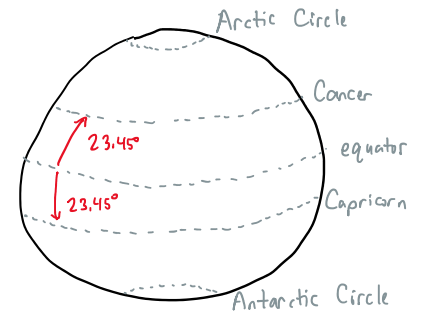
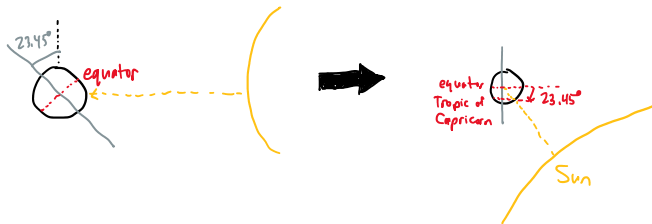
- Sun rises in the East, sets in the West

- Try alternate frame of reference (stationary Earth)

- At summer solstice:



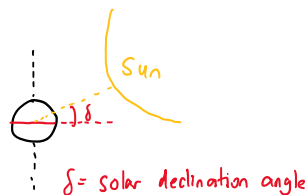
- At winter solstice:



Can we use this information to find a good tilt angle for solar collector?
See next lecture

- In this new frame of reference, the sun moves around!

In general:



Solar Declination Angle (δ)

• angle formed between plane of equator and line drawn from centre of the sun

$$\delta = 23.45^\circ \sin\left(\frac{360}{365} (n - 81)\right)$$

\nearrow day number

$$\delta \in [-23.45^\circ, +23.45^\circ]$$

winter solstice summer solstice

$$\frac{360}{365} (n - 81) = 0^\circ \text{ or } 180^\circ \rightarrow \delta = 0$$

\uparrow day $n = 81$ \uparrow day $n = 264$
 Spring equinox fall equinox