

# CS156 Assignment 6: LBA - Dimensionality Reduction, Compression and Reconstruction of Pictures

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For this assignment I took 46 pictures of Berlin's Fernsehturm (Television Tower) over the course of 4 hours and ten minutes at an approximate pace of one picture every 5 minutes, from a tripod in a café in Alexanderplatz. I only purchased two cups of coffee and a slice of cake throughout that period, and recieved 14 scornful looks from the staff, and 3 questions about my interest in "anything else?".

The principal component analysis of my pictures shows that two components can explain over 87% of the variation in the data. This doesn't surprise me, since aiming the camera to the sky not many features vary over time. Visualizing the principal components it's clear that they mostly deal with formations of clouds, and their correlation with the lights on the tower tip.

The components in the 2D compressed space follow a gentle curve, with sequential points very close to one another. One component varies almost perfectly linearly with time, which makes sense since prominent features like the color of the sky and the tower lights vary linearly with time. The other variable follows a sinusoidal curve, which requires further investigation. Varying each component individually to reveal the derivative effects on the picture, it becomes clear that the linearly varying component really corresponds to sky color and tower lights. The sinusoidal varying component seems to govern the way the tower is lit from the outside, which is a feautre influenced by the clouds (which could have come and gone in a nice sinusoidal curve) and by the external lighting, which turns on at one point and becomes more visible as the sky darkens.

Overall, reconstructing all pictures, they seem to represent the originals very accurately, with few visual artifacts, and with natural time progression. Points taken far from the curve appear quite normal, sadly. However, points taken outside the bounds of known examples are far more interesting.

I've dedicated a simple cell to emphasize the compression power of PCA and this example specifically. 87% of the variance was explained by 2 dimensions, for data that was previously stored in  $512 \times 288 \times 3 = 442,368$  dimensions, with pictures still reconstructed accurately, with the only extra requirement that the PCA component matrix is also stored (and a bit of computing time). The reconstructed pictures are also generally compressed more efficiently by other algorithms (jpg in this case), but I cannot explain why.

In [1]:

```
1 # Imports
2 from os import listdir, stat
3 from PIL import Image, ImageFile
4 import numpy as np
5 from sklearn.decomposition import PCA
6 import matplotlib.pyplot as plt
7 import math
```

In [2]:

```
1 # Loading pictures
2 # already converted to 512*288 (16:9 ratio)
3 directory = listdir("Tower")
4 data = []
5 for image in directory:
6     imagepath = "Tower/" + image
7     img = Image.open(imagepath)
8     img_arr = np.frombuffer(img.tobytes(), dtype=np.uint8)
9     data.append(img_arr)
10    img.close()
```

In [4]:

```
1 # Function to reconstruct images from bytes
2 def reconstruct(array):
3     template = np.zeros((288, 512, 3), dtype=np.uint8)
4     for j,val in enumerate(array):
5         pxl = math.floor(j/3)
6         clr = j%3
7         row = math.floor(pxl/512)
8         col = pxl%512
9         template[row][col][clr] = val
10    return Image.fromarray(template, 'RGB')
```

In [10]:

```
1 # Function to plot gallery
2 def plot_gallery(title, images, n_row, n_col, scale, cmap=plt.cm.gray):
3     plt.figure(figsize=(16 * scale * n_col, 9 * scale * n_row))
4     plt.suptitle(title, size=70*scale)
5     for i, comp in enumerate(images):
6         plt.subplot(n_row, n_col, i + 1)
7         plt.imshow(comp, cmap=cmap, interpolation='nearest')
8         plt.xticks(())
9         plt.yticks(())
```

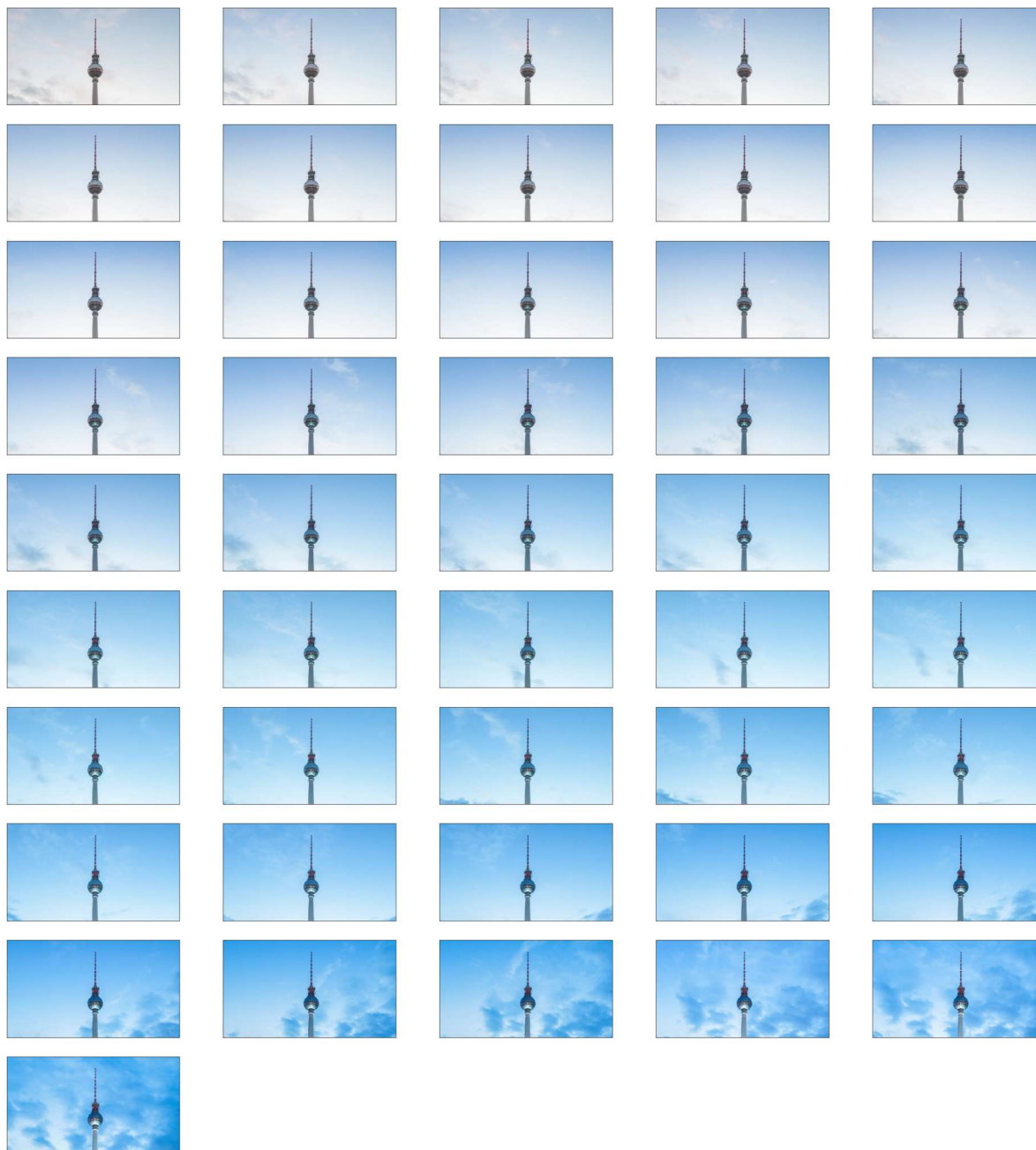
In [9]:

```
1 # Plot original
2 images0=[]
3 for i in range(46):
4     images0.append(reconstruct(data[i]))
```

In [11]:

```
1 plot_gallery("Original Pictures",images0,10,5,0.5)
```

Original Pictures

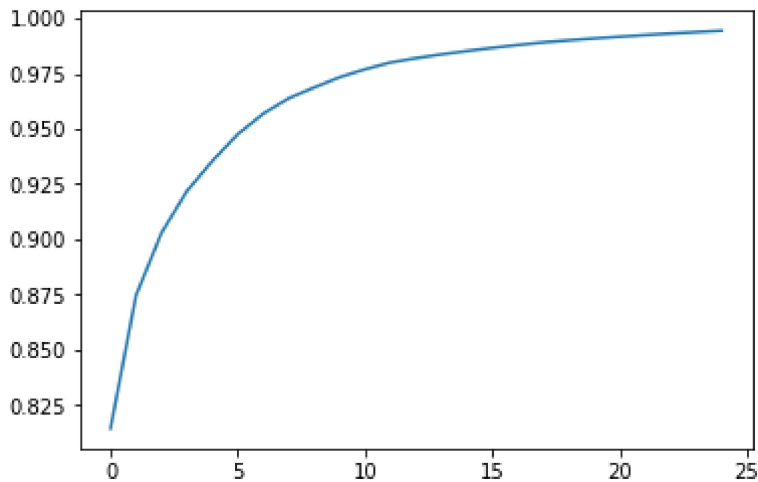


In [12]:

```
1 # Perform PCA
2 pca_check = PCA()
3 pca_check.fit(data);
```

In [13]:

```
1 # Plot explained variance over n_components
2 plt.plot(np.cumsum(pca_check.explained_variance_ratio_[:25]))
3 plt.show()
4 print("Variance explained by the first two principal components: " \
5       + str(np.sum(pca_check.explained_variance_ratio_[:2]))) + "%.")
```



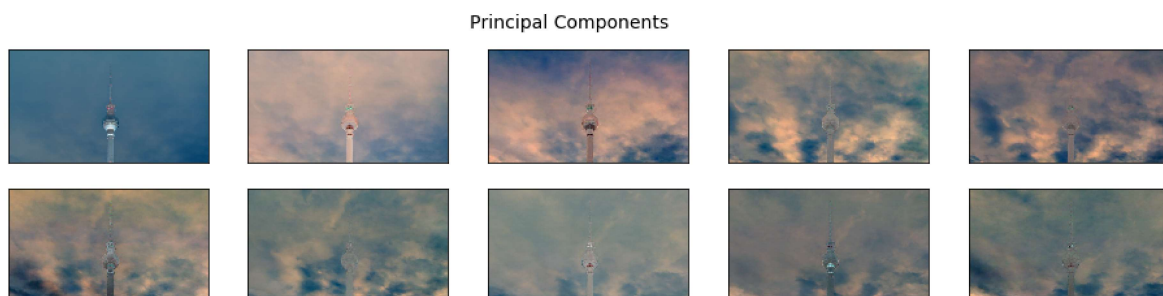
Variance explained by the first two principal components: 0.8746034979479546%.

In [14]:

```
1 # Visualize the principal components
2 images = []
3 for i in range(10):
4     a = pca_check.components_[i,:]
5     images.append(reconstruct(np.interp(a, (a.min(), a.max()), (0, 255))))
```

In [15]:

```
1 plot_gallery("Principal Components", images, 2, 5, 0.2)
```

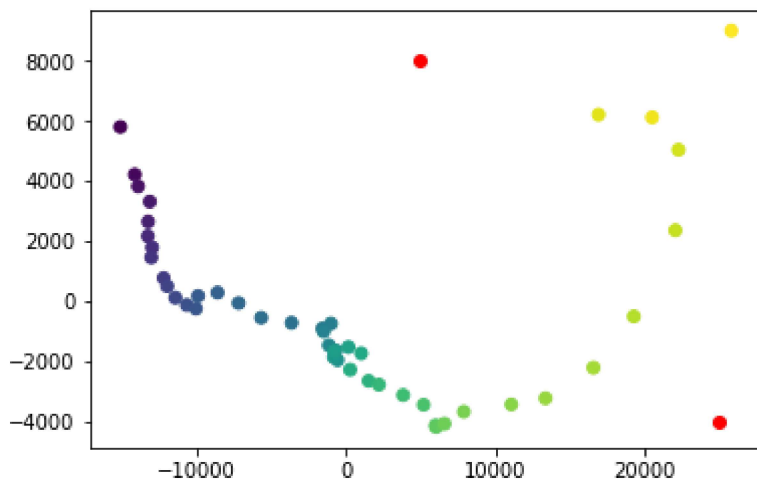


In [16]:

```
1 # Using n=2
2 pca = PCA(n_components=2)
3 pca.fit(data)
4 pca_data = pca.transform(data)
```

In [20]:

```
1 # Plot images by principal components
2 # Color corresponds to time to verify continuity
3 plt.scatter(*zip(*pca_data),c=np.arange(46))
4 # Plotting far points I plot later
5 plt.scatter([5000,25000],[8000,-4000],c="red")
6 plt.show()
```



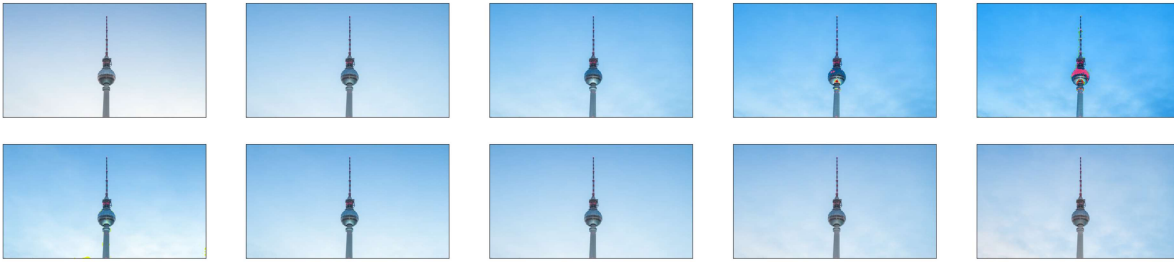
In [22]:

```
1 # Visualizing derivative
2 images2 = []
3 # Component 1
4 for i in range(5):
5     images2.append(reconstruct(pca.inverse_transform([-10000+i*10000,0])))
6 # Component 2
7 for i in range(5):
8     images2.append(reconstruct(pca.inverse_transform([0,-6000+i*3000])))
```

In [24]:

```
1 plot_gallery("Derivative with Respect to the Components", images2, 2, 5, 0.5)
```

Derivative with Respect to the Components



In [21]:

```
1 # Reconstruct data
2 recons = pca.inverse_transform(pca_data)
```

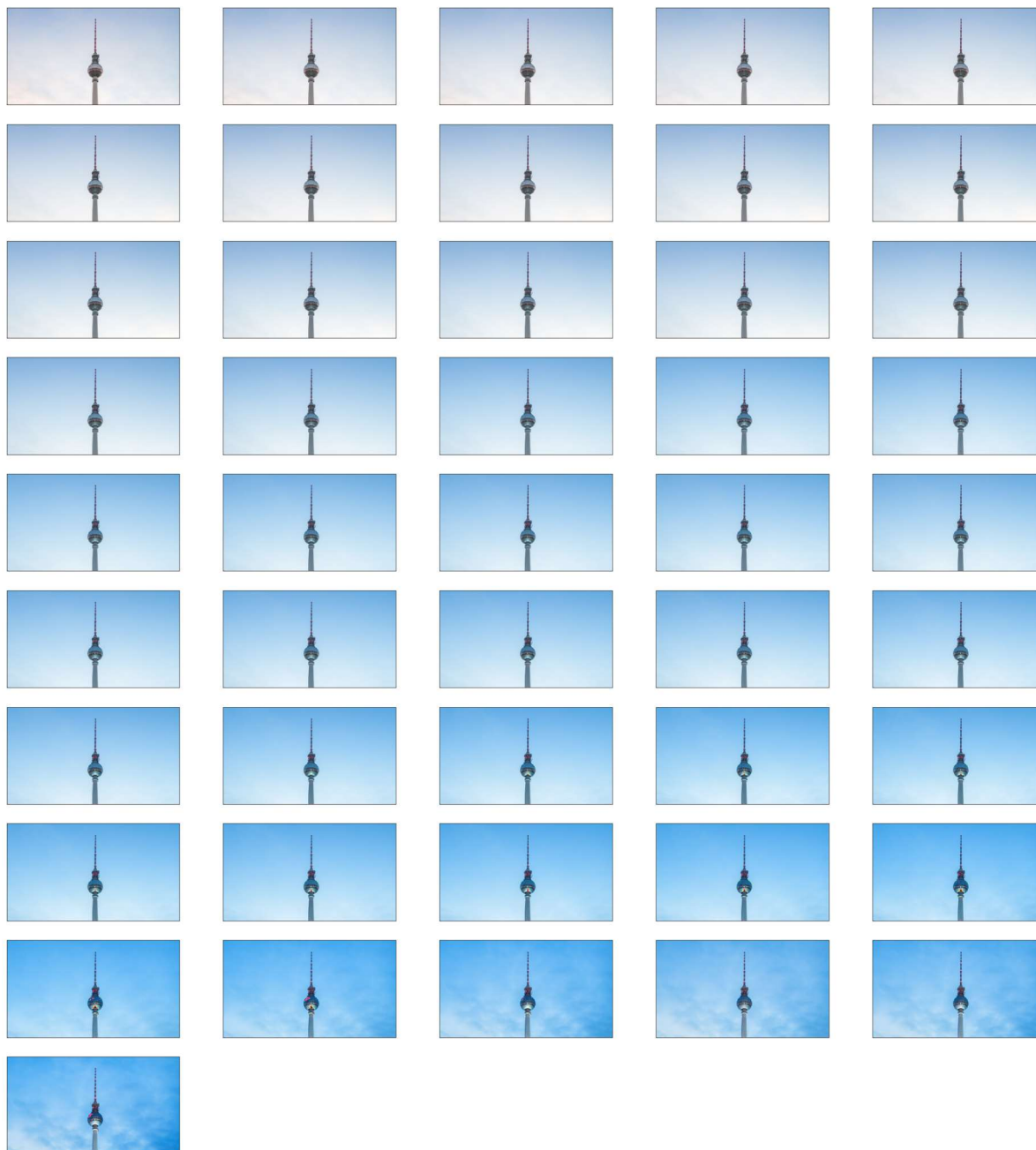
In [28]:

```
1 # Reconstruct pictures
2 images1 = []
3 for i in range(46):
4     images1.append(reconstruct(recons[i]))
```

In [29]:

```
1 plot_gallery("Reconstructions of Original Pictures",images1,10,5,0.5)
```

Reconstructions of Original Pictures





In [30]:

```
1 # Visualizing points far from the curve
2 far1 = reconstruct(pca.inverse_transform([8000,5000]))
3 far2 = reconstruct(pca.inverse_transform([-4000,25000]))
4 images = [far1,far2]
5 plot_gallery("Reconstructions of Original Pictures",images,1,2,1)
```

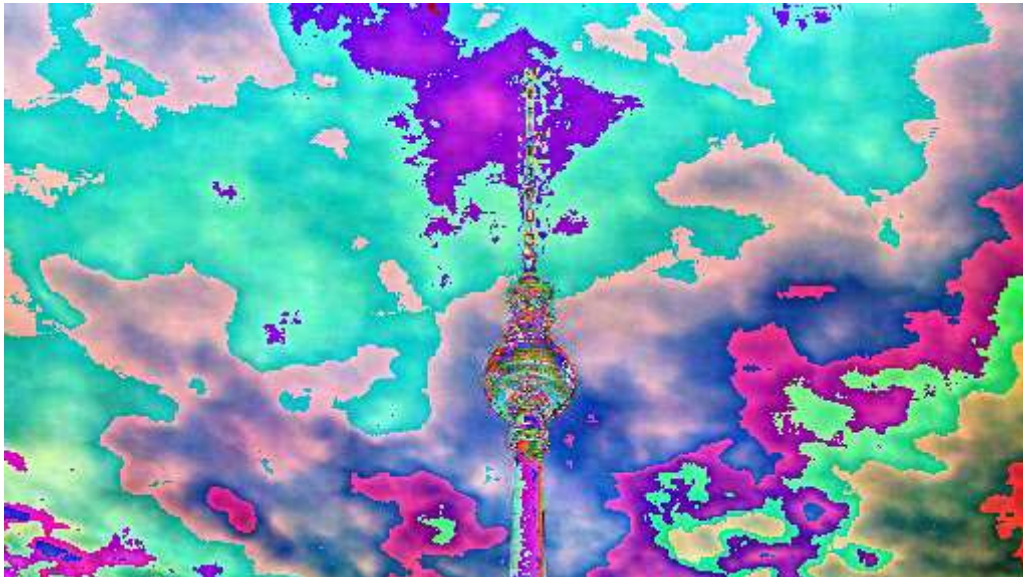
## Reconstructions of Original Pictures



In [31]:

```
1 # Visualizing point REALLY far from the curve
2 # (outside of range)
3 recon_far = pca.inverse_transform([20000,100000])
4 reconstruct(recon_far)
```

Out[31]:





In [32]:

```
1 # Compare file sizes
2 uncompressed = reconstruct(data[6])
3 uncompressed.save('uncompressed.jpg')
4 compressed = reconstruct(pca_data[6])
5 compressed.save('reconstructed.jpg')
6 print("Uncompressed dimensionality: " + str(len(data[6])))
7 print("Compressed dimensionality: " + str(len(pca_data[6])))
8 print("Uncompressed size: " + str(stat('uncompressed.jpg').st_size) + " bytes")
9 print("Reconstructed size: " + str(stat('compressed.jpg').st_size) + " bytes")
```

Uncompressed dimensionality: 442368

Compressed dimensionality: 2

Uncompressed size: 6310 bytes

Reconstructed size: 2950 bytes