

# Quiz Week 6

## Part 1.

1. F    2. F    3. T    4. F    5. T

6. F    7. F

## Part 2.

8. C.    9. B, D.

## Part 3.

10. (1).

Aliasing occurs when the sampling rate is insufficient to capture the high-frequency details of a scene, leading to artifacts such as jagged edges or moiré patterns.

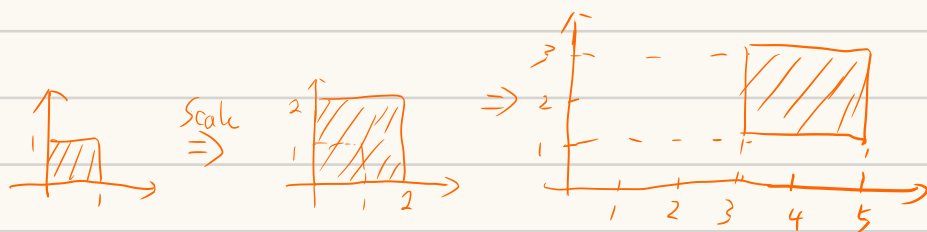
(2), Increase resolution: Higher resolution can reduce the visibility of aliasing by sampling more points

Pre filtering: Applying low-pass filter before sampling to smooth out high-frequency components.

Post filtering: Applying smoothing filter after sampling to reduce visible artifacts like jagged edges.

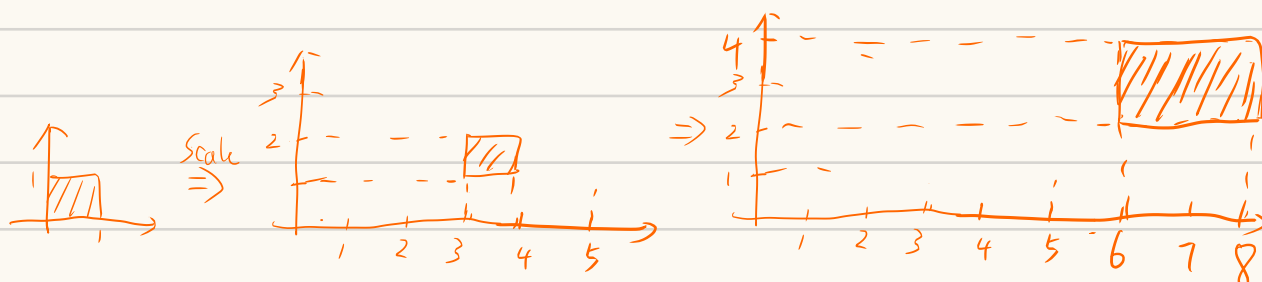
11.

(1)



$$(x, y) \rightarrow (2x, 2y) \rightarrow (2x+3, 2y+1)$$

(2).



$$(x, y) \rightarrow (x+3, y+1) \rightarrow (2x+6, 2y+2)$$

12.

Algebraic Surfaces : use  $\bar{f}(x, y, z) = 0$  to define surfaces

Level Sets : store a grid of values approximating function

Distance Functions : use  $f(x)$  to define distance

Fractals : a geometric shape containing detailed structure at arbitrarily small scales

NeRF : volumetric representation using neural network

13, Obviously,  $T = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$ ,

Let  $M = \begin{bmatrix} \frac{3\sqrt{2}}{2}, -\frac{3\sqrt{2}}{2} & 0 \\ \frac{5\sqrt{2}}{2}, \frac{5\sqrt{2}}{2} & 0 \\ 0 & 0 & 7 \end{bmatrix}$ , Say  $M = S_0 R_0$   
 $\Rightarrow MM^T = S_0 S_0^T$

$MM^T = \begin{bmatrix} 9 & 0 & 0 \\ 0 & 25 & 0 \\ 0 & 0 & 49 \end{bmatrix} \Rightarrow S_0 = \begin{bmatrix} 3 & & \\ & 5 & \\ & & 7 \end{bmatrix}$

$R_0 = S_0^{-1} M = \begin{bmatrix} \frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2} & 0 \\ \frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2} & 0 \\ 0 & 0 & 1 \end{bmatrix}$

Hence  $S = \begin{bmatrix} 3 & & \\ & 5 & \\ & & 7 \end{bmatrix}$   $R = \begin{bmatrix} \frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2} & & \\ \frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2} & & \\ & & 1 \end{bmatrix}$

14.  $R = \begin{bmatrix} \frac{3}{4} + \frac{\sqrt{2}}{8} & \frac{3}{4} - \frac{\sqrt{6}}{8} & \frac{\sqrt{2}}{4} \\ \frac{\sqrt{3}}{4} & \frac{\sqrt{6}}{8} & -\frac{\sqrt{6}}{4} \\ -\frac{\sqrt{2}}{4} & \frac{\sqrt{6}}{4} & \frac{\sqrt{2}}{2} \end{bmatrix}$   $\theta = \cos^{-1}\left(\frac{\text{trace } R - 1}{2}\right) = 45^\circ$   
 $n = \frac{(R_{21} - R_{12}, R_{02} - R_{20}, R_{10} - R_{01})}{2 \sin \theta}$

Rotate about  $n = \begin{bmatrix} \frac{\sqrt{6}}{4} \\ \frac{\sqrt{2}}{4} \\ 0 \end{bmatrix}$  with  $45^\circ$ .

15.  $T(x, y, z) = (x+2, 2y+10, 2z+12)$

$T\left(\frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{3}}\right) = \left(2 + \frac{\sqrt{3}}{3}, \frac{2\sqrt{3}}{3} + 10, \frac{2\sqrt{3}}{3} + 12\right)$

$n' = \frac{(A^{-1})^T n}{\|(A^{-1})^T n\|} = \frac{(1, \frac{1}{2}, \frac{1}{3})}{\|(1, \frac{1}{2}, \frac{1}{3})\|} = \left(\frac{6}{7}, \frac{3}{7}, \frac{2}{7}\right)$