Biomedical Data Science - Assignment 2

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2022/3/26

Assignment 2

Biomedical Data Science

Due on Tuesday 5th April 2022, 5:00pm

The assignment is marked out of 100 points, and will contribute to 30% of your final mark. Please knit this document in PDF format and submit using the gradescope link on Learn. If you can't knit to PDF directly, knit it to word and you should be able to either convert to PDF or print it and scan to PDF using a scanning app on your phone. If you have any code that doesn't run you won't be able to knit the document so comment it as you might still get some grades for partial code. Clear and reusable code will be rewarded so pay attention to indentation, choice of variable identifiers, comments, error checking, etc. An initial code chunk is provided after each subquestion but create as many chunks as you feel is necessary to make a clear report. Add plain text explanations in between the chunks as and when required and any comments necessary within code chunks to make it easier to follow your code/reasoning.

Problem 1 (27 points)

File wdbc2.csv (available from the accompanying zip folder on Learn) refers to a study of breast cancer where the outcome of interest is the type of the tumour (benign or malignant, recorded in column "diagnosis"). The study collected 30 imaging biomarkers on 569 patients.

Problem 1.a (7 points)

Using package caret, create a data partition so that the training set contains 70% of the observations (set the random seed to 984065 beforehand). Fit both a ridge regression model and a lasso model which uses cross-validation on the training set to diagnose the type of tumour from the 30 biomarkers. Then use a plot to help identify the penalty parameter λ that maximizes the AUC. Note: There is no need to use the prepare.glmnet() function from lab 4, using as.matrix() with the required columns is sufficient.

Solution:

After reading the dataset into R, we find that response variable diagnosis consists of strings. Though glmnet() function can deal with strings in diagnosis, glm() function failed to fit regressions on the response variable with strings in 1.c. Therefore, before any further handling, we encoded diagnosis with 0 and 1, where 0 represents "malignant" and 1 represents "benign".

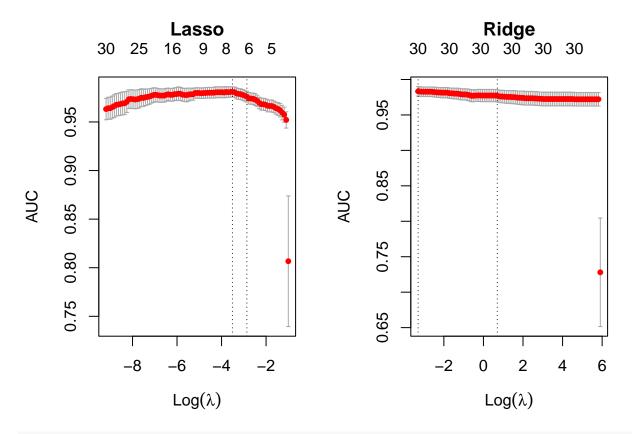
We use package caret to create training and testing sets with a ratio of 7:3. For model reproducibility and comparison, we set the random seed to 984065 beforehand. Since glmnet() function requires matrix as

input rather than data tables, we use as.matrix() function to transform data tables for 30 biomarkers to matrices.

After data pre-processing, we fit a Ridge regression and a Lasso regression which use cross-validation on the training data. To identify the optimal penalty parameter which maximises the AUC for each model, for each model, we make an auxiliary plot which display the AUC in red with bars corresponding to standard errors. The leftmost dotted line in each plot corresponds to the λ that maximises AUC, i.e. lambda_min in the regression object. The right dotted line corresponds to the largest value of λ such that the error is within one standard error from the minimum, i.e. lambda_1se in the fitted object.

Finally, we report the optimal λ s which maximise the AUC for two models.

```
# Read dataset into R
wdbc <- fread("assignment2/wdbc2.csv")</pre>
# convert strings in 'diagnosis' to numeric
wdbc$diagnosis <- ifelse(wdbc$diagnosis == 'malignant', 1, 0)</pre>
# set random seed beforehand
set.seed(984065)
# create training and testing sets
train.idx <- createDataPartition(y = wdbc$diagnosis, p = 0.7)$Resample1</pre>
train.wdbc <- wdbc[train.idx, -c(1)]</pre>
test.wbdc <- wdbc[-train.idx, -c(1)]</pre>
# define x and y matrices in the regression function
train.x <- train.wdbc[, -c(1)]</pre>
test.x <- test.wbdc[, -c(1)]</pre>
train.x.mat <- as.matrix(train.x)</pre>
test.x.mat <- as.matrix(test.x)</pre>
train.y.mat <- train.wdbc$diagnosis</pre>
test.y.mat <- test.wbdc$diagnosis</pre>
# fit a Ridge regression and a Lasso regression using CV on training set
set.seed(984065)
fit.cv.lasso <- cv.glmnet(train.x.mat, train.y.mat,</pre>
                            family = "binomial", type.measure = "auc")
fit.cv.ridge <- cv.glmnet(train.x.mat, train.y.mat, alpha = 0,</pre>
                            family = "binomial", type.measure = "auc")
# make plots to find the optimal lambdas that maximise the AUC
par(mfrow = c(1,2), mar = c(4,4,5,2))
plot(fit.cv.lasso, main = "Lasso")
plot(fit.cv.ridge, main = "Ridge")
```



```
# the values of optimal lambdas
cat("The optimal lambda in Lasso regression: ", fit.cv.lasso$lambda.min, "\n")
```

The optimal lambda in Lasso regression: 0.02982835

```
cat("The optimal lambda in Ridge regression: ", fit.cv.ridge$lambda.min)
```

The optimal lambda in Ridge regression: 0.03677378

Problem 1.b (2 points)

Create a data table that for each value of 'lambda.min' and 'lambda.1se' for each model fitted in problem 1.a reports: * the corresponding AUC, * the corresponding model size. Use 3 significant digits for floating point values and comment on these results. Hint: The AUC values are stored in the field called 'cvm'.

Solution:

We construct a data frame to display the value of λ in each model and corresponding AUC and model size, using 3 significant digits on floating point values. (The index attribute of regression stores the indices of both lambda_min and lambda_1se.)

From the results, we draw the following conclusions:

- 1. Both Lasso regression and Ridge regression using lambda_min have higher AUC scores than corresponding models using lambda_1se. This is reasonable as lambda_min maximises the AUC.
- 2. Using same kind of penalty parameters, Lasso regression has smaller values for both λ and AUC than Ridge regression. In terms of AUC, we may consider that Ridge regression with lambda_min preforms best out of 4 models.
- 3. The model sizes of Lasso regression models, 8 and 6, are significantly smaller than the model sizes of Ridge regression models, which keep constant at 30. This is because for Ridge regression, all predictors become very soon non-zero, while for Lasso regression this happens in a staggered way.

```
# now we create the required data table
rep.dt <- data.table(model = c("Lasso(lambda.min)", "Lasso(lambda.1se)",
                               "Ridge(lambda.min)", "Ridge(lambda.1se)"),
                     lambda = c(signif(fit.cv.lasso$lambda.min, 3),
                                signif(fit.cv.lasso$lambda.1se, 3),
                                signif(fit.cv.ridge$lambda.min, 3),
                                signif(fit.cv.ridge$lambda.1se, 3)),
                     AUC = c(signif(fit.cv.lasso$cvm[fit.cv.lasso$index[1]], 3),
                             signif(fit.cv.lasso$cvm[fit.cv.lasso$index[2]], 3),
                             signif(fit.cv.ridge$cvm[fit.cv.ridge$index[1]], 3),
                             signif(fit.cv.ridge$cvm[fit.cv.ridge$index[2]], 3)),
                     modelsize = c(fit.cv.lasso$nzero[fit.cv.lasso$index[1]],
                                   fit.cv.lasso$nzero[fit.cv.lasso$index[2]],
                                   fit.cv.ridge$nzero[fit.cv.ridge$index[1]],
                                   fit.cv.ridge$nzero[fit.cv.ridge$index[2]]))
rep.dt
```

```
## model lambda AUC modelsize
## 1: Lasso(lambda.min) 0.0298 0.981 8
## 2: Lasso(lambda.1se) 0.0572 0.976 6
## 3: Ridge(lambda.min) 0.0368 0.983 30
## 4: Ridge(lambda.1se) 2.0100 0.977 30
```

Problem 1.c (7 points)

Perform both backward (we'll later refer to this as model B) and forward (model S) stepwise selection on the same training set derived in problem 1.a. Report the variables selected and their standardized regression coefficients in decreasing order of the absolute value of their standardized regression coefficient. Discuss the results and how the different variables entering or leaving the model influenced the final result.

Solution:

To perform backward and forward stepwise selection, we pre-define a full model including all 30 biomarkers and a null model with only intercept term.

We use stepAIC() function to perform both backward and forward stepwise selection and use lm.beta() function in lm.beta package to get the standardized regression coefficients of selected variables. Note that since the number of variables is large, we set trace option in stepAIC to 'FALSE' and hide the selection steps to save space.

Finally, for each model, we report the selected variables with their standardized coefficients in decreasing order of the absolute values of the standardized regression coefficients.

We can observe that besides the intercepts, most variables selected in both backward and forward stepwise method are same, though their regression coefficients are different. This suggests that these biomarkers do have significant effects on the outcome of interest, the type of the tumour. Specifically, these biomarkers are: texture.worst, radius.stderr, smoothness.worst, radius, concavity.worst, area.worst, compactness.worst, perimeter, radius.worst and texture.stderr.

We consider the performance of a stepwise selection model based on its AIC. Generally, the lower AIC, the better performance of the model. We discuss the influence of entering or leaving variables on the model result in terms of AIC:

- 1. For backward stepwise selection, we start with the full model including all variables, together with an initial AIC. We select and drop insignificant variables and the AIC reduces until it reaches the minimum. Note that dropping variables after AIC meets the minimum will increase AIC in backward stepwise method.
- 2. For forward stepwise selection, on the contrary, we start with a null model with intercept only. Significant variables enter the model and improve model performance by reducing AIC until we reach the optimal AIC. After that, adding redundant variables increases the AIC of the model.

std.coef.B <- lm.beta(model.B)\$standardized.coefficients</pre>

```
# order the coefficients in decreasing order of their absolute values
std.coef.B <- std.coef.B[order(abs(std.coef.B), decreasing = TRUE)]
cat("selected variables in model.B: \n")</pre>
```

selected variables in model.B:

std.coef.B

```
##
          radius.worst
                                area.worst
                                                      perimeter
                                                                    concavity.worst
##
             53.047377
                                -40.610055
                                                     -18.500646
                                                                           8.472730
##
         concavepoints
                                    radius
                                                 radius.stderr
                                                                      texture.worst
##
              8.398555
                                  7.378246
                                                      7.371562
                                                                           5.605099
##
     compactness.worst concavepoints.worst
                                                 texture.stderr
                                                                   smoothness.worst
##
             -5.320776
                                 -3.831640
                                                      -3.722656
                                                                           2.008449
##
           (Intercept)
##
              0.000000
```

```
# selected variables with standardized regression coefficients in model.S
# get the standardized coefficients
std.coef.S <- lm.beta(model.S)$standardized.coefficients
# order the coefficients in decreasing order of their absolute values
std.coef.S <- std.coef.S[order(abs(std.coef.S), decreasing = TRUE)]
cat("selected variables in model.S: \n")</pre>
```

selected variables in model.S:

std.coef.S

##	area.worst	radius.worst	perimeter.worst	perimeter
##	-44.347062	39.117707	16.396414	-13.329464
##	radius.stderr	compactness.worst	radius	concavity
##	10.235291	-5.930017	5.544839	5.364296
##	texture.worst	perimeter.stderr	concavity.worst	texture.stderr
##	4.932050	-4.761290	4.299930	-3.028769
##	smoothness.worst	area.stderr	(Intercept)	
##	2.661371	2.278462	0.000000	

Problem 1.d (3 points)

Compare the goodness of fit of model B and model S in an appropriate way.

Solution:

Here we consider using AIC as an appropriate criterion to compare the goodness-of-fit to the training data of two models. As mentioned before, in general, model with lower AIC value has better performance. Thus, according to the following result, we consider the backward stepwise selection, i.e. model.B, performs better than the forward stepwise method.

```
data.frame(model.B = model.B$aic, model.S = model.S$aic, row.names = "AIC")
## model.B model.S
## AIC 99.47075 105.2948
```

Problem 1.e (2 points)

Compute the training AUC for model B and model S.

Solution:

To compute the training AUC for two stepwise models, we first obtain the predictive values of training set using model.B and model.S. With predictive values, we use roc() function from pROC package to calculate AUC of training set for model.B and model.S. From the result, we can find that the AUC scores for both models are quite high and backward stepwise selection performs slightly better than forward stepwise method, which is consistent with the conclusion from previous question.

```
# predict values on training set
pred.B <- predict(model.B, newdata = train.wdbc, type = "response")</pre>
pred.S <- predict(model.S, newdata = train.wdbc, type = "response")</pre>
# auc
auc.B <- roc(train.y.mat ~ pred.B)$auc</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
auc.S <- roc(train.y.mat ~ pred.S)$auc</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
data.frame(model = c("model.B", "model.S"), AUC = c(auc.B, auc.S))
##
       model
                    AUC
## 1 model.B 0.9936376
## 2 model.S 0.9929396
```

Problem 1.f (6 points)

Use the four models to predict the outcome for the observations in the test set (use the lambda at 1 standard error for the penalised models). Plot the ROC curves of these models (on the sameplot, using different colours) and report their test AUCs. Compare the training AUCs obtained in problems 1.b and 1.e with the test AUCs and discuss the fit of the different models.

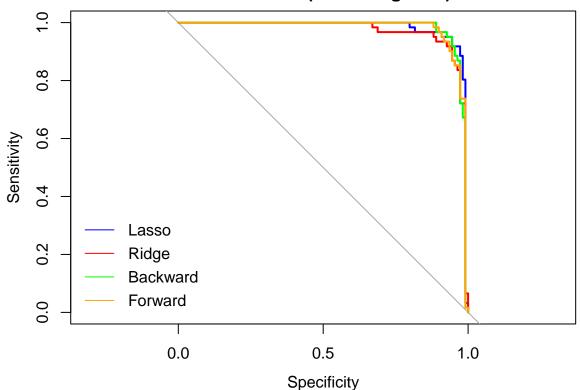
Solution:

Similar with 1.e, to get the testing AUC of each model, we need to calculate the predictive values of testing set for each model. After that, again, we use roc() function to plot the testing ROC curves of each model in the same graph. Moreover, we report the testing AUC for each model.

According to the results, Lasso regression has higher testing AUC than its training AUC, while the other 3 models has higher training AUCs than their testing AUCs. Moreover, basically stepwise models performs better on training set, while penalised models have better performances on testing model. Note that we may not consider the problem of over-fitting for penalised models as the idea of regularization reduces over-fitting. However, we possibly consider over-fitting happens to stepwise models.

```
# predict values of testing set
pred.lasso.test <- predict(fit.cv.lasso, newx = test.x.mat,</pre>
                      s = fit.cv.lasso$lambda.1se, type = "response")
pred.ridge.test <- predict(fit.cv.ridge, newx = test.x.mat,</pre>
                      s = fit.cv.ridge$lambda.1se, type = "response")
pred.B.test <- predict(model.B, newdata = test.x, type = "response")</pre>
pred.S.test <- predict(model.S, newdata = test.x, type = "response")</pre>
# plot ROC curves of four models
roc.lasso <- roc(test.y.mat, pred.lasso.test,</pre>
                 plot = TRUE, col = "blue", xlim = c(0, 1),
                 main = "ROC curves (on testing data)")
## Setting levels: control = 0, case = 1
## Warning in roc.default(test.y.mat, pred.lasso.test, plot = TRUE, col = "blue", :
## Deprecated use a matrix as predictor. Unexpected results may be produced, please
## pass a numeric vector.
## Setting direction: controls < cases
roc.ridge <- roc(test.y.mat, pred.ridge.test,</pre>
                 plot = TRUE, col = "red", add = TRUE, xlim = c(0, 1))
## Setting levels: control = 0, case = 1
## Warning in roc.default(test.y.mat, pred.ridge.test, plot = TRUE, col = "red", :
## Deprecated use a matrix as predictor. Unexpected results may be produced, please
## pass a numeric vector.
## Setting direction: controls < cases
```

ROC curves (on testing data)



##		train.AUC	test.AUC
##	Lasso	0.976	0.981
##	Ridge	0.977	0.971
##	${\tt Backward}$	0.994	0.980
##	Forward	0.993	0.979

Problem 2 (40 points)

File GDM.raw.txt (available from the accompanying zip folder on Learn) contains 176 SNPs to be studied for association with incidence of gestational diabetes (a form of diabetes that is specific to pregnant women). SNP names are given in the form "rs1234_X" where "rs1234" is the official identifier (rsID), and "X" (one of A, C, G, T) is the reference allele.

Problem 2.a (3 points)

read data into R

Read file GDM.raw.txt into a data table named gdm.dt. Impute missing values in gdm.dt according to SNP-wise median allele count.

Solution:

By looking inside the dataset, we observe that only SNP columns contains missing values. We define a function impute.to.median() to impute the missing values of each SNP column with its median. After imputation, we count the number of missing terms and the result of 0 indicates there is no missing values in the imputed dataset.

check if there is missing values after imputation

[1] 0

sum(is.na(gdm.dt.imputed))

Problem 2.b (8 points)

Write function univ.glm.test <- function(x, y, order = FALSE) where x is a data table of SNPs, y is a binary outcome vector, and order is a boolean. The function should fit a logistic regression model for each SNP in x, and return a data table containing SNP names, regression coefficients, odds ratios, standard errors and p-values. If order is set to TRUE, the output data table should be ordered by increasing p-value.

Solution:

```
univ.glm.test <- function(x, y, order = FALSE){
  # initialize lists for output
  coef <- NULL
  OR <- NULL
  se <- NULL
  p.value <- NULL
  \# get the names of columns in x
  x.cols <- colnames(x)</pre>
  \# logistic regression for each SNP in x
  for (i in 1:length(x.cols)){
    logreg <- glm(y ~ x[[i]], family = "binomial")</pre>
    reg.sum <- summary(logreg)</pre>
    name[i] <- x.cols[i]</pre>
    coef[i] <- reg.sum$coefficients[2, 1]</pre>
    OR[i] <- exp(coef[i])</pre>
    se[i] <- reg.sum$coefficients[2, 2]</pre>
    p.value[i] <- reg.sum$coefficients[2, 4]</pre>
  }
  # create a data table including the values
  dt <- data.table(name, coef, OR, se, p.value)
  \# if order = TRUE \dots
  if (order == TRUE){
    return(setorder(dt, p.value))
  }
  else{
    return(dt)
}
```

Problem 2.c (5 points)

Using function univ.glm.test(), run an association study for all the SNPs in gdm.dt against having gestational diabetes (column "pheno"). For the SNP that is most strongly associated to increased risk of gestational diabetes and the one with most significant protective effect, report the summary statistics from the GWAS as well as the 95% and 99% confidence intervals on the odds ratio.

Solution:

With pre-defined function univ.glm.test(), we run logistic regression over each SNP in gdm.dt (imputed) separately and obtained the result data table, rep. To ensure the consistence of the order of SNPs between rep and original dataset, we set the order option to "FALSE" as default.

As required, we find the SNP with the smallest regression p-value, i.e. $rs12243326_A$, which is considered to be mostly strongly associated to increased risk of gestational diabetes. Besides statistics in rep, we also report its 95% and 99% confidence intervals.

In addition, we report statistics including 95% and 99% confidence intervals for the SNP with most significant protective effect on gestational diabetes, i.e. $rs11575839_C$, which has the most negative regression coefficient.

```
# apply pre-defined function to the imputed dataset
rep \leftarrow univ.glm.test(x = gdm.dt.imputed[, -c(1, 2, 3)],
                     y = gdm.dt.imputed$pheno)
head(rep, 5)
##
                          coef
                                     OR
             name
                                                     p.value
## 1: rs7513574_T 0.002157494 1.002160 0.1051372 0.9836280
## 2: rs1627238_A 0.114637864 1.121467 0.1138224 0.3138559
## 3: rs1171278_C 0.121409445 1.129087 0.1138073 0.2860628
## 4: rs1137100_A 0.060104751 1.061948 0.1104238 0.5862285
## 5: rs2568958 A 0.149379896 1.161114 0.1233800 0.2259989
#The SNP mostly strongly associated to increased risk of gestational diabetes is:
SNP.msa <- rep[which.min(rep$p.value)]</pre>
print(SNP.msa)
##
                                    OR
                                                       p.value
              name
                         coef
## 1: rs12243326_A 0.6454198 1.906787 0.1583787 4.598104e-05
# The 95% and 99% confidence intervals of corresponding odds ratio are:
CI.95.msa \leftarrow exp(SNP.msa$coef + qnorm(0.975) * SNP.msa$se * c(-1, 1))
CI.99.msa \leftarrow exp(SNP.msa$coef + qnorm(0.995) * SNP.msa$se * c(-1, 1))
data.frame(lower = c(round(CI.95.msa[1], 3), round(CI.99.msa[1], 3)),
           upper = c(round(CI.95.msa[2], 3), round(CI.99.msa[2], 3)),
           row.names = c("95\", "99\"))
##
       lower upper
## 95% 1.398 2.601
## 99% 1.268 2.867
```

```
{\it \#The~SNP~with~most~significant~protective~effect~is:}
SNP.msp <- rep[which.min(rep$coef)]</pre>
print(SNP.msp)
##
                                      OR
              name
                         coef
                                                se p.value
## 1: rs11575839_C -0.6022542 0.5475759 0.3758156 0.1090394
# The 95% and 99% confidence intervals of corresponding odds ratio are:
CI.95.msp \leftarrow exp(SNP.msp$coef + qnorm(0.975) * SNP.msp$se * c(-1, 1))
CI.99.msp <- exp(SNP.msp$coef + qnorm(0.995) * SNP.msp$se * c(-1, 1))
data.frame(lower = c(round(CI.95.msp[1], 3), round(CI.99.msp[1], 3)),
           upper = c(round(CI.95.msp[2], 3), round(CI.99.msp[2], 3)),
           row.names = c("95\%", "99\%"))
##
       lower upper
## 95% 0.262 1.144
## 99% 0.208 1.442
```

Problem 2.d (4points)

Merge your GWAS results with the table of gene names provided in file GDM.annot.txt (available from the accompanying zip folder on Learn). For SNPs that have p-value $< 10^{-4}$ (hit SNPs) report SNP name, effect allele, chromosome number and corresponding gene name. Separately, report for each 'hit SNP' take names of the genes that are within a 1Mb window from the SNP position on the chromosome. Note: That's genes that fall within +/-1,000,000 positions using the 'pos' column in the dataset.

Solution:

##

gene

Since SNP names in rep, i.e. name terms, consist of the official identifiers of SNPs and the reference alleles, we need to split name into snp and allele. Then we merge two dataset by mutual column snp. After merging, we report the SNP name, effect allele, chromosome number and corresponding gene name of 'hit SNPs', rs12243326 and rs2237897, whose p-values < 1e - 4.

Moreover, for each 'hit SNP', we report the gene names that are within a 1Mb window from the SNP position on the chromosome.

```
# read dataset into R
gdm.annot.dt <- data.table(read.table("assignment2/GDM.annot.txt",</pre>
                                       sep = "\t", header = TRUE))
# merge previous results with gene names in gdm.annot.dt
# before merging, split 'name' in res to SNP names and effect allele
rep$snp <- sapply(rep$name, function(x) strsplit(x, split = "_")[[1]][1])</pre>
rep$allele <- sapply(rep$name, function(x) strsplit(x, split = "_")[[1]][2])</pre>
# now merge the datasets by 'snp'
rep.merged <- merge(rep, gdm.annot.dt, by = "snp")
# find the hit SNPs and report
idx.hit.SNP <- which(rep.merged$p.value < 1e-4)
rep.hit.SNP = rep.merged[idx.hit.SNP, ]
rep.hit.SNP[, .(snp, allele, chrom, gene)]
##
             snp allele chrom
                                 gene
                            10 TCF7L2
## 1: rs12243326
                      Α
## 2: rs2237897
                      Т
                            11 KCNQ1
# 1Mb window for 1st SNP in hit.SNP
unique(rep.merged[abs(rep.merged$pos - rep.hit.SNP$pos[1]) <= 10^6</pre>
                  & rep.merged$pos != rep.hit.SNP$pos[1], "gene"])
##
        gene
## 1: TCF7L2
# 1Mb window for 2nd SNP in hit.SNP
unique(rep.merged[abs(rep.merged$pos - rep.hit.SNP$pos[2]) <= 10^6</pre>
                  & rep.merged$pos != rep.hit.SNP$pos[2], "gene"])
```

1: TH ## 2: KCNQ1 ## 3: CACNA2D4 ## 4: SMG6

Problem 2.e (8 points)

Build a weighted genetic risk score that includes all SNPs with p-value $< 10^{-4}$, a score with all SNPs with p-value $< 10^{-3}$, and a score that only includes SNPs on the FTO gene (hint: ensure that the ordering of SNPs is respected). Add the three scores as columns to the gdm.dt data table. Fit the three scores in separate logistic regression models to test their association with gestational diabetes, and for each report odds ratio, 95% confidence interval and p-value.

Solution:

Generally, we construct a weighted genetic risk score for SNPs by their regression coefficients, so that both direction and contribution of the effect to final score for a SNP are considered.

Once we obtain the scores, we add them as new columns into dataset and apply logistic regression to them in separate. We report the odds ratio, 95% confidence interval and p-value of each score.

Looking the results, from the p-values, we consider the risk scores for both SNPs with p-values < 1e-4 and SNPs with p-values < 1e-3 have significant associations with gestational diabetes as p-values for two scores are relatively low. However, for SNPs on the FTO genes, the corresponding score has a p-value > 0.05, implying an insignificant contribution to the gestational diabetes.

```
# subset of SNPs with p-value < 1e-4
gdm.hit.SNP <- gdm.dt.imputed[, .SD, .SDcols = rep.hit.SNP$name]

# subset of SNPs with p-value < 1e-3
idx.p3.SNP <- which(rep.merged$p.value < 1e-3)
rep.p3.SNP <- rep.merged[idx.p3.SNP, ]
gdm.p3.SNP <- gdm.dt.imputed[, .SD, .SDcols = rep.p3.SNP$name]

# subset of SNPs on the FTO gene
idx.FTO.SNP <- which(rep.merged$gene == 'FTO')
rep.FTO.SNP <- rep.merged[idx.FTO.SNP, ]
gdm.FTO.SNP <- gdm.dt.imputed[, .SD, .SDcols = rep.FTO.SNP$name]

# weighted genetic risk score for each group of SNPs
score.hit.SNP <- as.matrix(gdm.hit.SNP) %*% rep.hit.SNP$coef
score.p3.SNP <- as.matrix(gdm.p3.SNP) %*% rep.p3.SNP$coef
score.FTO.SNP <- as.matrix(gdm.FTO.SNP) %*% rep.FTO.SNP$coef</pre>
```

add weighted scores to the original data table

gdm.dt.imputed\$score.hit <- score.hit.SNP
gdm.dt.imputed\$score.p3 <- score.p3.SNP</pre>

summary(logreg.FTO)\$coefficients[2, 1])),

```
## Waiting for profiling to be done...
## I name OR CI.lower CI.upper p.value
## 1 score.hit 2.729432 1.9243530 3.911052 2.759214e-08
## 2 socre.p3 1.451854 1.2814405 1.651126 7.813912e-09
## 3 score.FTO 1.413857 0.8191201 2.452615 2.151883e-01
```

Problem 2.f (4 points)

File GDM.test.txt (available from the accompanying zip folder on Learn) contains genotypes of another 40 pregnant women with and without gestational diabetes (assume that the reference allele is the same one that was specified in file GDM.raw.txt). Read the file into variable gdm.test. For the set of patients in gdm.test, compute the three genetic risk scores as defined in problem 2.e using the same set of SNPs and corresponding weights. Add the three scores as columns to gdm.test (hint: use the same columnnames as before).

Solution:

As required, we use the same set of SNPs and corresponding weights to construct score columns in gdm.test.

```
# read data into R
gdm.test <- fread("assignment2/GDM.test.txt")

# subset of each group
gdm.test.hit.SNP <- gdm.test[, .SD, .SDcols = rep.hit.SNP$snp]
gdm.test.p3.SNP <- gdm.test[, .SD, .SDcols = rep.p3.SNP$snp]
gdm.test.FTO.SNP <- gdm.test[, .SD, .SDcols = rep.FTO.SNP$snp]

# compute the score of each group
score.test.hit.SNP <- as.matrix(gdm.test.hit.SNP) %*% rep.hit.SNP$coef
score.test.p3.SNP <- as.matrix(gdm.test.p3.SNP) %*% rep.p3.SNP$coef
score.test.FTO.SNP <- as.matrix(gdm.test.FTO.SNP) %*% rep.FTO.SNP$coef

# add scores to gdm.test
gdm.test$score.hit <- score.test.hit.SNP
gdm.test$score.hit <- score.test.p3.SNP
gdm.test$score.FTO <- score.test.FTO.SNP</pre>
```

```
## score.hit score.p3 score.FT0
## 1: -0.2334714 -1.0420490 0.0000000
## 2: -0.8788912 -1.6874688 0.4740752
## 3: 0.0000000 0.0000000 0.0000000
## 4: -0.4394456 -0.4394456 0.4740752
## 5: 0.0000000 0.0000000 0.0000000
```

Problem 2.g (4 points)

Use the logistic regression models fitted in problem 2.e to predict the outcome of patients in gdm.test. Compute the test log-likelihood for the predicted probabilities from the three genetic risk score models.

Solution:

We use pre-fitted logistic regression models of each score to predict the outcomes of patients in gdm.test.

Problem 2.h (4points)

File GDM.study2.txt (available from the accompanying zip folder on Learn) contains the summary statistics from a different study on the same set of SNPs. Perform a meta-analysis with the results obtained in problem 2.c (hint: remember that the effect alleles should correspond) and produce a summary of the meta-analysis results for the set of SNPs with meta-analysis p-value $< 10^{-4}$ sorted by increasing p-value.

Solutions:

To preform the meta-analysis, we need to harmonize two datasets. Thus, we take out a subset of rep which only contains columns in gdm.study2, i.e. snp, allele, coef and se. Moreover, we rename some columns with the corresponding column names in gdm.study2. After that, we also ensure SNPs in two datasets correspond and order them by SNP and effect allele as SNP and effect allele are what matter in the meta-analysis.

We start with finding which SNPs have both alleles matching, and which would match if the alleles were flipped. The following result indicates that in this case, there are two SNPs whose alleles do not match even after swapping them. This could be caused by a gene-typing or imputation error, or because of some other discrepancy in the GWAS pipelines adopted by the different studies. As a result, these two SNPs cannot be meta-analysed, and we drop them from both datasets.

The effect sizes of the SNPs which we identified to have alleles flipped need to have their direction of effect swapped in one of the studies before entering the meta-analysis. Here, without loss of generality, we swap the sign for gdm.study2.

Now, with data pre-processing ready, we perform a fixed effect meta-analysis by using inverse variance weighting. According to the weights, we may consider that in general results from 2.c are more powered.

Moreover, we derive the meta-analysis effect size which is a weighted sum of effect sizes from two studies, based on weights obtained before. Finally, we compute the p-values for the meta-analysis and construct a meta-analysis summary for SNP terms with meta-analysis p-value < 1e - 4, increasingly ordered by p-values.

```
# read data into R
gdm.study2 <- fread("assignment2/GDM.study2.txt")

# make the variable names in rep consistent with gdm.study2
rep.meta <- rep[, .(snp, allele, coef, se)]
setnames(rep.meta, c("allele", "coef"), c("effect_allele", "beta"))

# ensure the SNPs in two datasets correspond
rep.meta <- rep.meta[snp %in% gdm.study2$snp]
gdm.study2 <- gdm.study2[snp %in% rep.meta$snp]

# order two datasets by SNP and effect allele
rep.meta <- rep.meta[order(snp, effect_allele)]
gdm.study2 <- gdm.study2[order(snp, effect_allele)]
stopifnot(all.equal(rep.meta$snp, gdm.study2$snp))</pre>
```

```
# SNPs with alleles matching or flipped alleles matching
both.ok <- rep.meta$effect_allele == gdm.study2$effect.allele
flipped <- rep.meta$effect_allele == gdm.study2$other.allele
table(both.ok, flipped)</pre>
```

```
## flipped
## both.ok FALSE TRUE
```

```
##
     FALSE
                    27
##
     TRUF.
             147
# drop SNPs with non-matching alleles
idx.nomatching <- which(both.ok == FALSE & flipped == FALSE)</pre>
rep.meta <- rep.meta[-idx.nomatching, ]</pre>
gdm.study2 <- gdm.study2[-idx.nomatching, ]</pre>
# update both.ok and flipped
both.ok <- both.ok[-idx.nomatching]</pre>
flipped <- flipped[-idx.nomatching]</pre>
table(both.ok, flipped)
          flipped
## both.ok FALSE TRUE
     FALSE 0
##
     TRUE
             147
                    Λ
# swap signs of betas of SNPs with alleles matching after flipped in qdm.study2
beta1 <- rep.meta$beta
beta2 <- gdm.study2$beta
beta2[flipped] <- -beta2[flipped]</pre>
# perform a fixed effect meta-analysis
weight.rep.meta <- 1 / rep.meta$se^2</pre>
weight.gdm.study2 <- 1 / gdm.study2$se^2</pre>
head(weight.rep.meta)
## [1] 95.95663 48.35218 51.12222 80.72417 32.39329 80.53452
head(weight.gdm.study2)
## [1] 9.141470 6.919489 7.069651 10.430712 3.328963 9.751846
# computation of meta-analysis effect size
beta.meta <- (weight.rep.meta*beta1+weight.gdm.study2*beta2)/</pre>
  (weight.rep.meta+weight.gdm.study2)
se.meta <- sqrt(1/(weight.rep.meta+weight.gdm.study2))</pre>
# p-values of meta-analysis
p.value.meta <- 2 * pnorm(abs(beta.meta/se.meta), lower.tail = FALSE)</pre>
# SNPs with meta-analysis p-values < 1e-4
idx.p4.meta <- which(p.value.meta < 1e-4)</pre>
# report the meta-analysis result for SNPs with meta-analysis p-values < 1e-4
summary.p4.meta <- data.table(snp = rep.meta[idx.p4.meta, ]$snp,</pre>
                               # weight.rep.meta = weight.rep.meta[idx.p4.meta],
                               # weight.gdm.study2 = weight.gdm.study2[idx.p4.meta],
                               beta.meta = beta.meta[idx.p4.meta],
                               se.meta = se.meta[idx.p4.meta],
```

```
p.value.meta = p.value.meta[idx.p4.meta])
summary.p4.meta <- summary.p4.meta[order(p.value.meta)]
summary.p4.meta</pre>
```

Problem 3 (33 points)

File nki.csv (available from the accompanying zip folder on Learn) contains data for 144 breast cancer patients. The dataset contains a binary outcome variable ("Event", indicating the insurgence of further complications after operation), covariates describing the tumour and the age of the patient, and gene expressions for 70 genes found to be prognostic of survival.

Problem 3.a (6 points)

Compute the matrix of correlations between the gene expression variables, and display it so that a block structure is highlighted. Discuss what you observe. Write some code to identify the unique pairs of (distinct) variables that have correlation coefficient greater than 0.80 in absolute value and report their correlation coefficients.

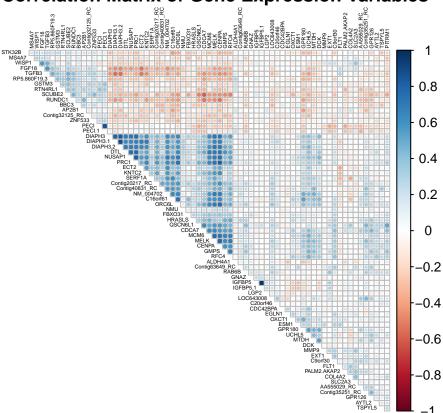
Solution:

To compute the correlations between the gene expression variables, we first obtained a subset which only contains the gene expression variables and then computed the correlation matrix using cor() function. Moreover, we visualized the strength of correlation between the gene variables by creating a correlation plot.

Since the number of gene expression variables is large (70 columns), we improved the default plot by using options including order and type.

```
# read data into R
nki <- read.csv("assignment2/nki.csv", header = TRUE)</pre>
```





Looking at the correlation plot above, we can see that there are strong correlations between variables with similar names, such as "IGFBP5" and "IGFBP5.1". It is plausible to think that variables with similar names contains similar information and have similar effect on the outcome variable. Generally, high correlation between variables indicates high strength of linear association. On the other hand, we may also consider the existence of multicollinearity among variables with relatively high correlations.

In particular, we found the unique pairs of distinct variables with correlation coefficients greater than 0.80 in absolute value and reported them in the following data frame. As we expected, high correlations appeared in variables with similar names as well as two other pairs corresponding to "PRC1".

corr.08

##		pair	correlation
##	1	DIAPH3.1, DIAPH3	0.8031368
##	2	DIAPH3.2, DIAPH3	0.8338591
##	3	DIAPH3.2, DIAPH3.1	0.8868741
##	4	PECI.1, PECI	0.8697836
##	5	IGFBP5.1, IGFBP5	0.9775030
##	6	PRC1, NUSAP1	0.8298356
##	7	CENPA, PRC1	0.8175424

Problem 3.b (8 points)

Run PCA (only over the columns containing gene expressions), in order to derive a patient-wise summary of all gene expressions (dimensionality reduction). Decide which components to keep and justify your decision. Test if those principal components are associated with the outcome in unadjusted logistic regression models and in models adjusted for age, estrogen receptor and grade. Justify the difference in results between unadjusted and adjusted models.

Solution:

Using prcomp() function, we applied PCA on the subset of gene expression variables and derived a patientwise summary of all gene expression.

```
# run PCA
pca.patients <- prcomp(gene.expression, center = TRUE, scale = TRUE)
summary(pca.patients)</pre>
```

```
## Importance of components:
##
                             PC1
                                      PC2
                                              PC3
                                                      PC4
                                                              PC5
                                                                      PC6
                                                                               PC7
## Standard deviation
                          4.1171 2.30541 2.02437 1.78597 1.73982 1.68091 1.42309
## Proportion of Variance 0.2422 0.07593 0.05854 0.04557 0.04324 0.04036 0.02893
  Cumulative Proportion 0.2422 0.31808 0.37662 0.42219 0.46543 0.50580 0.53473
                                                     PC11
                                                             PC12
##
                              PC8
                                      PC9
                                             PC10
                                                                     PC13
                                                                              PC14
## Standard deviation
                          1.36441 1.29119 1.2715 1.24741 1.18388 1.15101 1.13883
## Proportion of Variance 0.02659 0.02382 0.0231 0.02223 0.02002 0.01893 0.01853
## Cumulative Proportion
                          0.56132 0.58514 0.6082 0.63046 0.65049 0.66941 0.68794
##
                             PC15
                                      PC16
                                              PC17
                                                      PC18
                                                              PC19
                                                                      PC20
                                                                               PC21
## Standard deviation
                          1.09473 1.07016 1.04187 1.00234 0.99086 0.94095 0.93322
## Proportion of Variance 0.01712 0.01636 0.01551 0.01435 0.01403 0.01265 0.01244
  Cumulative Proportion 0.70506 0.72142 0.73693 0.75128 0.76531 0.77796 0.79040
##
                             PC22
                                      PC23
                                              PC24
                                                      PC25
                                                              PC26
                                                                      PC27
##
                                                                               PC28
                          0.90727 0.89675 0.88859 0.86019 0.84462 0.82782 0.82368
## Standard deviation
## Proportion of Variance 0.01176 0.01149 0.01128 0.01057 0.01019 0.00979 0.00969
## Cumulative Proportion
                          0.80216 0.81364 0.82492 0.83549 0.84569 0.85548 0.86517
##
                             PC29
                                      PC30
                                              PC31
                                                      PC32
                                                              PC33
                                                                      PC34
## Standard deviation
                          0.78694 0.75594 0.73942 0.70569 0.69414 0.67129 0.6639
## Proportion of Variance 0.00885 0.00816 0.00781 0.00711 0.00688 0.00644 0.0063
  Cumulative Proportion
                          0.87401 0.88218 0.88999 0.89710 0.90399 0.91042 0.9167
##
                             PC36
                                      PC37
                                              PC38
                                                      PC39
                                                              PC40
                                                                      PC41
                                                                               PC42
## Standard deviation
                          0.63815 0.61964 0.59947 0.58447 0.57195 0.55097 0.53820
## Proportion of Variance 0.00582 0.00549 0.00513 0.00488 0.00467 0.00434 0.00414
## Cumulative Proportion
                          0.92254 0.92802 0.93316 0.93804 0.94271 0.94705 0.95118
##
                             PC43
                                      PC44
                                              PC45
                                                      PC46
                                                              PC47
                                                                      PC48
                                                                               PC49
## Standard deviation
                          0.52029 0.51211 0.49533 0.48712 0.47079 0.44565 0.41879
## Proportion of Variance 0.00387 0.00375 0.00351 0.00339 0.00317 0.00284 0.00251
##
   Cumulative Proportion
                          0.95505 0.95880 0.96230 0.96569 0.96886 0.97170 0.97420
##
                             PC50
                                      PC51
                                             PC52
                                                     PC53
                                                             PC54
                                                                     PC55
                                                                              PC56
## Standard deviation
                          0.40556 0.39328 0.3925 0.38502 0.36669 0.36205 0.33734
## Proportion of Variance 0.00235 0.00221 0.0022 0.00212 0.00192 0.00187 0.00163
## Cumulative Proportion
                          0.97655 0.97876 0.9810 0.98308 0.98500 0.98687 0.98850
##
                             PC57
                                      PC58
                                              PC59
                                                      PC60
                                                              PC61
                                                                      PC62
                                                                               PC63
## Standard deviation
                          0.32150 0.30744 0.28898 0.28186 0.27274 0.25622 0.24118
## Proportion of Variance 0.00148 0.00135 0.00119 0.00113 0.00106 0.00094 0.00083
```

```
## Cumulative Proportion 0.98998 0.99133 0.99252 0.99365 0.99472 0.99565 0.99649 

## PC64 PC65 PC66 PC67 PC68 PC69 PC70 

## Standard deviation 0.23024 0.21442 0.19886 0.19371 0.17927 0.1677 0.09833 

## Proportion of Variance 0.00076 0.00066 0.00056 0.00054 0.00046 0.0004 0.00014 

## Cumulative Proportion 0.99724 0.99790 0.99846 0.99900 0.99946 0.9999 1.00000
```

The amount of variability explained by the components can be computed bearing in mind that the square root of the eigenvalues is stored in vector sdev of the PCA object. The variance explained by the principal components can be visualized through a scree plot.

```
# the proportion explained by the first 3 PCs
perc.expl <- pca.patients$sdev^2 / sum(pca.patients$sdev^2)
sum(perc.expl[1:3])

## [1] 0.3766231

# scree plot
screeplot(pca.patients, main = "Scree plot")</pre>
```

Scree plot

```
# subset of the first 3 PCs
pca.components <- pca.patients$x[, 1:3]

# logistic regressions on each PC without adjustment on other variables
fit.pc1 <- glm(nki$Event ~ pca.components[, 1],</pre>
```

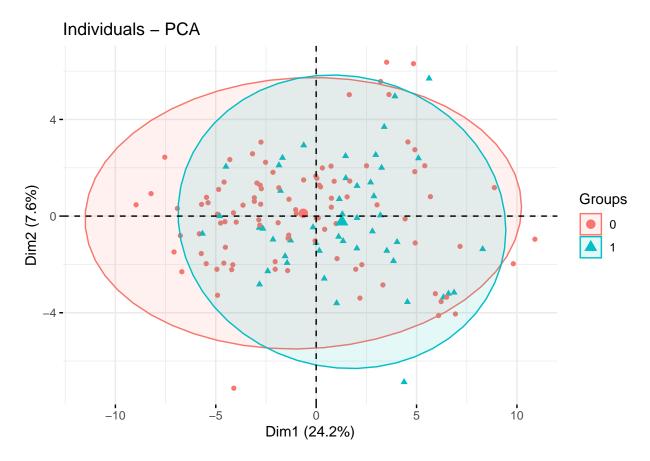
```
family = "binomial"(link = "logit"))
fit.pc2 <- glm(nki$Event ~ pca.components[, 2],</pre>
               family = "binomial"(link = "logit"))
fit.pc3 <- glm(nki$Event ~ pca.components[, 3],</pre>
               family = "binomial"(link = "logit"))
# logistic regression on each PC with adjustments
fit.pc1.adj <- glm(nki$Event ~ pca.components[, 1]</pre>
                   + nki$EstrogenReceptor + nki$Grade + nki$Age,
                   family = "binomial"(link = "logit"))
fit.pc2.adj <- glm(nki$Event ~ pca.components[, 2]</pre>
                   + nki$EstrogenReceptor + nki$Grade + nki$Age,
                   family = "binomial"(link = "logit"))
fit.pc3.adj <- glm(nki$Event ~ pca.components[, 3]</pre>
                   + nki$EstrogenReceptor + nki$Grade + nki$Age,
                   family = "binomial"(link = "logit"))
# regression coefficients and p-values in unadjusted and adjusted models
# principal component 1
data.frame(coef = c(fit.pc1$coefficients[2], fit.pc1.adj$coefficients[2]),
           p.value = c(summary(fit.pc1)$coefficients[2, 4],
                       summary(fit.pc1.adj)$coefficients[2, 4]),
           row.names = c("unadjusted", "adjuested"))
##
                    coef
                             p.value
## unadjusted 0.11768352 0.009425039
## adjuested 0.07215917 0.272381200
# principal component 2
data.frame(coef = c(fit.pc2$coefficients[2], fit.pc2.adj$coefficients[2]),
           p.value = c(summary(fit.pc2)$coefficients[2, 4],
                       summary(fit.pc2.adj)$coefficients[2, 4]),
           row.names = c("unadjusted", "adjuested"))
##
                             p.value
                      coef
## unadjusted -0.067166804 0.3885231
## adjuested
               0.005164421 0.9550636
# principal component 3
data.frame(coef = c(fit.pc3$coefficients[2], fit.pc3.adj$coefficients[2]),
           p.value = c(summary(fit.pc3)$coefficients[2, 4],
                       summary(fit.pc3.adj)$coefficients[2, 4]),
           row.names = c("unadjusted", "adjuested"))
##
                   coef
                           p.value
## unadjusted 0.2435485 0.00863000
## adjuested 0.2183706 0.02454557
```

```
fit.pca.adj <- glm(nki$Event ~ pca.components[, 1] + pca.components[, 2]</pre>
                   + pca.components[, 3] + nki$EstrogenReceptor
                   + nki$Grade + nki$Age, family = "binomial"(link = "logit"))
summary(fit.pca.adj)
##
## Call:
  glm(formula = nki$Event ~ pca.components[, 1] + pca.components[,
       2] + pca.components[, 3] + nki$EstrogenReceptor + nki$Grade +
       nki$Age, family = binomial(link = "logit"))
##
##
## Deviance Residuals:
      Min
                 10
                     Median
                                   30
                                           Max
## -1.8178 -0.8782 -0.5907
                               1.1119
                                        2.1029
##
## Coefficients:
##
                                Estimate Std. Error z value Pr(>|z|)
## (Intercept)
                                 2.24591
                                            1.69668
                                                      1.324
                                                              0.1856
## pca.components[, 1]
                                 0.09426
                                            0.07333
                                                      1.285
                                                              0.1986
## pca.components[, 2]
                                            0.10305 -0.448
                                -0.04621
                                                              0.6539
## pca.components[, 3]
                                 0.22688
                                            0.09899
                                                      2.292
                                                              0.0219 *
## nki$EstrogenReceptorPositive 0.09780
                                            0.69101
                                                      0.142
                                                              0.8875
## nki$GradePoorly diff
                                                      0.312
                                 0.15228
                                            0.48885
                                                              0.7554
## nki$GradeWell diff
                                -0.63836
                                            0.55341 -1.153
                                                              0.2487
                                -0.06788
                                            0.03632 -1.869
## nki$Age
                                                              0.0616 .
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 183.32 on 143 degrees of freedom
## Residual deviance: 162.25 on 136 degrees of freedom
## AIC: 178.25
##
## Number of Fisher Scoring iterations: 4
```

Problem 3.c (8 points)

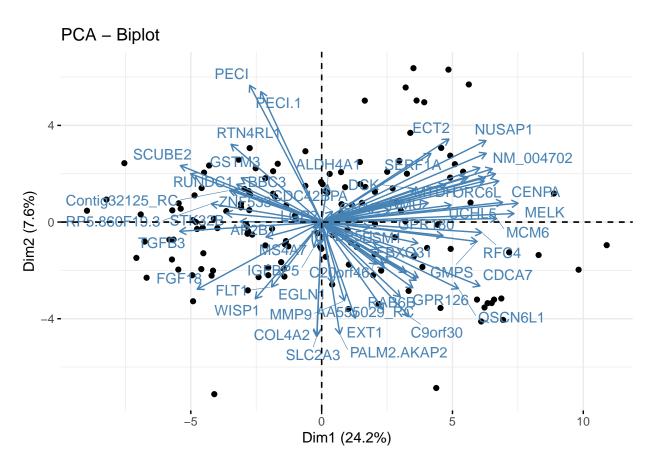
Use plots to compare with the correlation structure observed in problem 2.a and to examine how well the dataset may explain your outcome. Discuss your findings and suggest any further steps if needed.

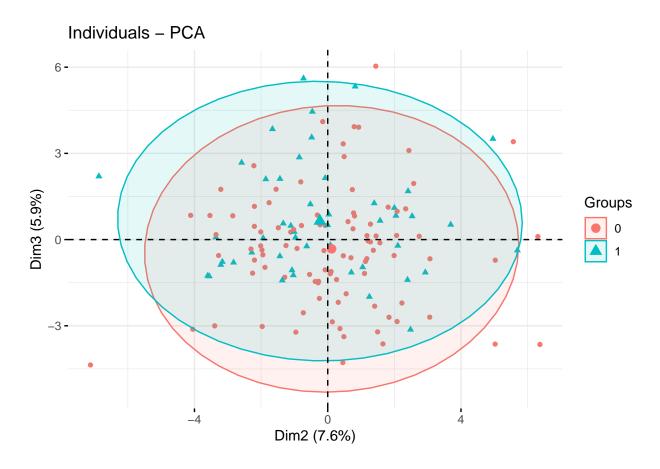
Solutions:



```
fviz_pca_biplot(pca.patients, geom = 'point', repel = TRUE)
```

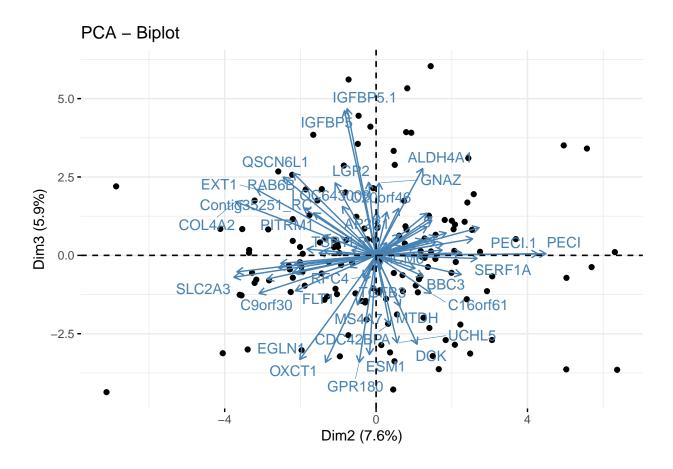
 $\mbox{\tt \#\#}$ Warning: ggrepel: 17 unlabeled data points (too many overlaps). Consider $\mbox{\tt \#\#}$ increasing max.overlaps





fviz_pca_biplot(pca.patients, geom = 'point', axes = c(2, 3), repel = TRUE)

 $\mbox{\tt \#\#}$ Warning: ggrepel: 35 unlabeled data points (too many overlaps). Consider $\mbox{\tt \#\#}$ increasing max.overlaps



Problem 3.d (11 points)

Based on the models we examined in the labs, fit an appropriate model with the aim to provide the most accurate prognosis you can for patients. Discuss and justify your decisions.

Solution:

```
# helper function in Lab4
prepare.glmnet <- function(data, formula=~ .) {</pre>
                 ## create the design matrix to deal correctly with factor variables,
                 ## without losing rows containing NAs
                 old.opts <- options(na.action='na.pass')</pre>
                 x <- model.matrix(formula, data)</pre>
                 options(old.opts)
                 ## remove the intercept column, as glmnet will add one by default
                 x <- x[, -match("(Intercept)", colnames(x))]</pre>
                 return(x)
}
# define x and y
x.mat <- prepare.glmnet(nki, ~ . - Event)</pre>
y.mat <- nki$Event
# create training and testing sets
set.seed(984065)
train.idx <- createDataPartition(y = nki$Event, p = 0.7)$Resample1</pre>
train.x.mat <- x.mat[train.idx, ]</pre>
test.x.mat <- x.mat[-train.idx, ]</pre>
train.y.mat <- y.mat[train.idx]</pre>
test.y.mat <- y.mat[-train.idx]</pre>
# Lasso regressions using CV
fit.cv.Lasso <- cv.glmnet(train.x.mat, train.y.mat,</pre>
                            family = "binomial", type.measure = "auc")
fit.cv.Lasso.gene <- cv.glmnet(train.x.mat[, -c(1:6)], train.y.mat,</pre>
                                 family = "binomial", type.measure = "auc")
# AUCs with best lambda
Lasso.auc <- fit.cv.Lasso$cvm[fit.cv.Lasso$index[1]]</pre>
Lasso.gene.auc <- fit.cv.Lasso.gene$cvm[fit.cv.Lasso.gene$index[1]]
# Ridge regression using CV
fit.cv.Ridge <- cv.glmnet(train.x.mat, train.y.mat, alpha = 0,</pre>
                            family = "binomial", type.measure = "auc")
fit.cv.Ridge.gene <- cv.glmnet(train.x.mat[, -c(1:6)], train.y.mat, alpha = 0,</pre>
                                 family = "binomial", type.measure = "auc")
# AUCs with best lambda
Ridge.auc <- fit.cv.Ridge$cvm[fit.cv.Ridge$index[1]]</pre>
Ridge.gene.auc <- fit.cv.Ridge.gene$cvm[fit.cv.Ridge.gene$index[1]]</pre>
```

```
# AUCs of Lasso and Ridge regressions on testing set
pred.Lasso.test <- predict(fit.cv.Lasso, newx = test.x.mat,</pre>
                           s = fit.cv.Lasso$lambda.min, type = "response")
pred.Lasso.gene.test <- predict(fit.cv.Lasso.gene, newx = test.x.mat[, -c(1:6)],</pre>
                                s = fit.cv.Lasso$lambda.min, type = "response")
pred.Ridge.test <- predict(fit.cv.Ridge, newx = test.x.mat,</pre>
                           s = fit.cv.Ridge$lambda.min, type = "response")
pred.Ridge.gene.test <- predict(fit.cv.Ridge.gene, newx = test.x.mat[, -c(1:6)],</pre>
                                s = fit.cv.Ridge$lambda.min, type = "response")
Lasso.test.auc <- roc(test.y.mat ~ pred.Lasso.test)$auc
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
Lasso.gene.test.auc <- roc(test.y.mat ~ pred.Lasso.gene.test)$auc
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
Ridge.test.auc <- roc(test.y.mat ~ pred.Ridge.test)$auc</pre>
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
Ridge.test.gene.auc <- roc(test.y.mat ~ pred.Ridge.gene.test)$auc
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases
data.frame(train.AUC = c(Lasso.auc, Lasso.gene.auc, Ridge.auc, Ridge.gene.auc),
           modelsize = c(fit.cv.Lasso$nzero[fit.cv.Lasso$index[1]],
                         fit.cv.Lasso.gene$nzero[fit.cv.Lasso.gene$index[1]],
                         fit.cv.Ridge$nzero[fit.cv.Ridge$index[1]],
                         fit.cv.Ridge.gene$nzero[fit.cv.Ridge.gene$index[1]]),
           test.AUC = c(Lasso.test.auc, Lasso.gene.test.auc,
                        Ridge.test.auc, Ridge.test.gene.auc),
           row.names = c("Lasso", "Lasso (gene only)",
                         "Ridge", "Ridge (gene only)"))
##
                     train.AUC modelsize test.AUC
## Lasso
                     0.6835691
                                 6 0.7846154
## Lasso (gene only) 0.7349914
                                     37 0.7384615
                                     76 0.8897436
## Ridge
                     0.6784418
## Ridge (gene only) 0.7029742
                                    70 0.8179487
```