Alpha Go Everywhere: Machine Learning and International Stock Returns

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Background & Motivation

- Machine learning is widely adopted in recent empirical asset pricing literatures. This is partly motivated by the long list of characteristics that seem to predict returns.
- Machine learning can improve the explanatory power over traditional linear models, but complex algorithms are difficult to interpret economically and prone to overfitting.
- Most studies conduct their analyses on only one market—the U.S, in this paper, we apply machine learning methods to predict international stock returns.

Question: Whether machine learning can capture market-specific return-characteristic relationships internationally?

- Overall, the evidence is mixed.
- While neural network (NN) models work well internationally, regression trees (RTs) show signs of overfitting in some occasions.

Research contents

- Predicting U.S. stock returns with 12 predictors
- Predicting international stock returns with the U.S.estimated models.
- Predicting international stock returns with marketspecific models.
- Pooling all stocks to illustrate models' predictability.
- Robustness tests & Discussion

Input: U.S. data
Output: U.S. stock return

Input: U.S. data

Output: international stock return

Input: market-specific data

Output: international stock return

Input: whole market data
Output: international stock return

Robustness tests & Discussion

Purpose is to compare the performance of our models with those in GKX, who input more than 900 features.

Applying the U.S.-estimated model to each of the 33 markets individually.

- 1. Results
- 2. In-Sample and Out-of-Sample R2
- 3. Return-Characteristics Relationships

Use three different international asset pricing models to examine whether the machine learning models capture something beyond the commonly known factors

Related researches

- Gu, Shihao, Bryan T Kelly, and Dacheng Xiu, 2020, Empirical asset pricing via machine learning, Review of Financial Studies.
- Freyberger, Neuhierl, and Weber (2020) propose an adaptive group LASSO procedure to select characteristics.
- Feng, Giglio, and Xiu (2020) develop a regularized two-pass cross-sectional regression approach and show that only a small number of factors remain significant over time.
- Bianchi, Büchner, and Tamoni (2020) show that NN and RTs improve the predictions of U.S. Treasury bond returns over linear techniques.
- Karolyi and Stulz (2003) and Lewis (2011) show that International stocks can be priced locally or globally.

Contribution

- Our paper belongs to the burgeoning literature that predicts asset returns with machine learning.
- Although machine learning is powerful, our paper argues that overfitting can be a problem and we should exercise caution when applying it to different markets
- While using local factors and characteristics is important, our results suggest that the relationships between returns and characteristics seem to vary across countries.
- Our NN models provide a way to price stock returns locally with more characteristics and in a larger set of markets.

1) Linear Models

In this paper, we use these linear models: OLS-3, OLS-3 with Huber loss, OLS, OLS with Huber loss, LASSO, RIDGE, and ENET.

- "-3" means: size, momentum, and book-to-market ratio.
- Penalty function: $\|\boldsymbol{\theta}\|_p = (\sum_{i=1}^n |\theta_i|^p)^{1/p}$.
- Huber loss:

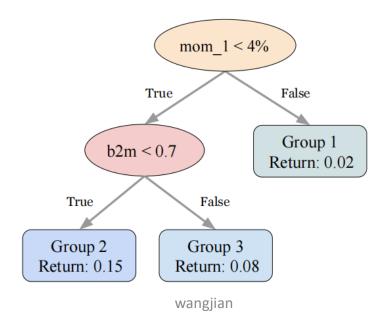
Huber Loss =
$$\begin{cases} v_{i,t}^2, & \text{if } |v_{i,t}| \le \xi \\ 2\xi |v_{i,t}| - \xi^2, & \text{if } |v_{i,t}| > \xi \end{cases}$$

	Loss Function	Penalty Function
OLS	MSE	None
$_{\mathrm{OLS+H}}$	Huber Loss	None
LASSO	MSE	$\lambda_1 * \ \boldsymbol{\theta}\ _1$
RIDGE	MSE	$\lambda_2 * \ \boldsymbol{\theta}\ _2$
ENET	MSE	$\lambda_1 * \ \boldsymbol{\theta}\ _1 + \lambda_2 * \ \boldsymbol{\theta}\ _2$
RF	MSE	None
GBRT+H	Huber Loss	None
NN1-NN5	MSE	$\lambda_1 * \ \boldsymbol{\theta}\ _1$

2) Regression Trees and Ensemble Learning

 For example, this regression tree, with a depth of two, the function can be formally written as:

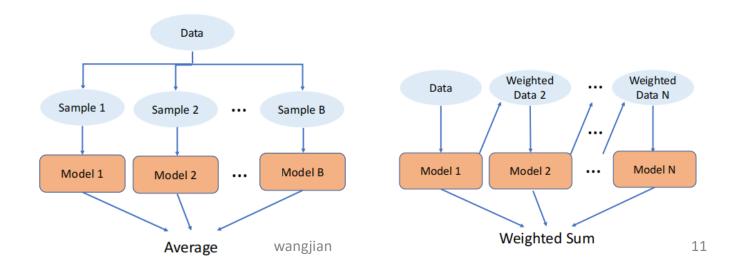
$$f = 0.15 \times \mathbf{1}_{\{mom_1 < 4\%\}} \mathbf{1}_{\{b2m < 0.7\}} + 0.08 \times \mathbf{1}_{\{mom_1 < 4\%\}} \mathbf{1}_{\{b2m \ge 0.7\}} + 0.02 \times \mathbf{1}_{\{mom_1 \ge 4\%\}}$$



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2) Regression Trees and Ensemble Learning

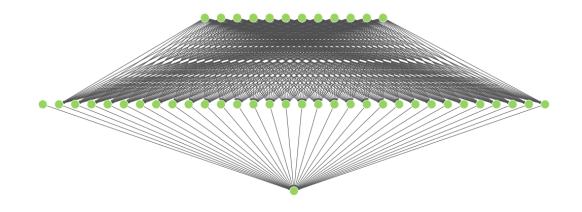
- A tree model is prone to overfit because it gives much freedom to fit the data compared with linear models.



3) Neural Network (NN)

- In this paper, we mainly explore the most widely used "vanilla" neural network.
- Figure provides a schematic of a one-layer neural network (NN1)
 used in our paper, where green circles denote the input features,
 hidden units, and output variables, from top to bottom.
- Activation function:

$$ReLU(x) = \begin{cases} 0, & \text{if } x < 0 \\ x, & \text{otherwise} \end{cases}$$



Data sources

- DataStream: Stock returns, trading volume, market capitalization, and industry information.
- Factset: Accounting ratios (book-to-market and sales-to price)
- For the U.S. and China, we use the data with CRSP and CSMAR respectively

Detail:

- We winsorize raw returns at the top and bottom 2.5% in each exchange.
- We download data for as many countries as possible and require each market to have at least 100 stocks with valid observations of return and the 12 characteristics for at least 3 years.

Acronym	Definition	in the 10 predictors
mom_1	1-month reversal	Yes
logsize	Log market capitalization	Yes
mom_12	12-month momentum	Yes
mom_6	6-month momentum	Yes
${\rm chmom_6}$	Change in mom_6	Yes
\max ret	Maximum daily return	Yes
$indmom_a_12$	Industry 12-month equal-weighted momentum	Yes
retvol	Return volatility (standard deviation) of daily return	Yes
logdolvol	Log Dollar trading volume	No
sp	Sales to price	Yes
turn	Share turnover	No
b2m	Book to market	Yes

- I. Post-estimation Evaluation
- 1) Out-of-sample R2

$$R_{oos}^2 = 1 - \frac{\sum_{(i,t) \in \text{Test}} (r_{i,t} - \hat{r}_{i,t})^2}{\sum_{(i,t) \in \text{Test}} r_{i,t}^2}$$

- Since the distribution of portfolio returns is sensitive to the dependence among stock returns, a good stock-level prediction model does not necessarily produce accurate portfolio-level forecasts.
- Portfolio R2oos: 1) sort stocks into deciles based on the prediction of models; 2) Within each decile, consider both equal weight and value weight by stocks' market capitalization, and rebalance the portfolio every month.

I. Post-estimation Evaluation

2) Sharpe Ratio

- We calculate the Sharpe ratio of long-short portfolio returns.
- The key difference between R2 and Sharpe ratios is that the calculation of the former involves predicted returns while the latter only uses the rank of predicted returns.
- 3) Relative Importance of Predictors.
- Sum of the Squares of the partial Derivatives(SSD)
- For the contribution of the j^{th} input variable, where x_k means the k^{th} observation. And than we normalize all variables' SSD to sum of one.

$$SSD_{j} = \sum_{k} \left(\left. \frac{\partial \hat{f}}{\partial x_{j}} \right|_{x=x^{k}} \right)^{2}$$

II. Predicting U.S. Stock Returns with 12 Predictors

		OLS-3	OLS-3+H	OLS	OLS+H	LASSO	RIDGE	ENET	RF	GBRT+H	NN1	NN2	NN3	NN4	NN5
R_{oos}^2	GKX		0.16		-3.46			0.11	0.33	0.34	0.33	0.39	0.40	0.39	0.36
	CJZ	0.29	0.25	0.42	0.25	0.45	0.42	0.45	0.83	0.64	0.75	0.81	0.79	0.73	0.71
Sharpe Ratio (EW)	GKX		0.83					1.33	1.48	1.73	2.13	2.33	2.36	2.45	2.15
	CJZ	0.81	0.68	1.55	1.57	1.44	1.55	1.53	2.29	2.20	2.56	2.69	2.60	2.44	2.59
Sharpe Ratio (VW)	GKX		0.61					0.39	0.98	0.81	1.17	1.16	1.20	1.35	1.15
	CJZ	0.40	0.44	0.33	0.54	0.30	0.33	0.39	1.03	0.49	0.94	1.07	1.06	1.00	1.39

- Overall, with the 12 stock characteristics, our machine learning models appear to have similar return predictability to models in GKX using more than 900 inputs.
- To examine the extent to which noisy signals can harm the performance of machine learning models, we run a simulation exercise.

4			$\overline{}$		$\overline{}$	$\overline{}$		$\overline{}$			$\overline{}$	$\overline{}$	$\overline{}$	$\overline{}$	
No. of simulated features		0			10			100			500			900	
	OLS	NN1	NN5	OLS	NN1	NN5	OLS	NN1	NN5	OLS	NN1	NN5	OLS	NN1	NN5
R_{oos}^2	0.42	0.75	0.71	0.42	0.77	0.64	0.41	0.69	0.67	0.37	0.67	0.55	0.32	0.59	0.51
Sharpe Ratio (EW)	1.55	2.56	2.59	1.56	2.61	2.33	1.55	2.40	2.05	1.53	2.02	1.87	1.42	1.91	1.81
Sharpe Ratio (VW)	0.33	0.94	1.39	0.30	0.85	1.06	0.36	0.61	1.01	0.25	0.59	0.77	0.26	0.63	0.61
Portfolio R_{oos}^2 (EW)	3.41	4.85	4.55	3.40	4.64	4.10	3.35	4.10	4.33	3.00	4.15	3.88	2.56	3.70	3.55
Portfolio R_{oos}^2 (VW)	0.97	3.03	2.95	0.88	3.00	2.79	0.83	2.57	2.99	0.10	2.88	2.63	-0.74	2.14	2.50

III. Predicting International Stock Returns with the U.S.-Estimated

Models

- First, in most of the markets, machine learning-based models outperform traditional models (i.e., OLS-3 and OLS) or the passive market portfolio.
- Second, models taking into account nonlinear and complex interaction effects (i.e., RTs and NN models) outperform linear machine learning models (LASSO and RIDGE)

	Sha	arpe Ratio (EW)	Sha	rpe Ratio (VW	")		R_{oos}^2	
	Tree-Linear	NN-Linear	NN-Tree	Tree-Linear	NN-Linear	NN-Tree	Tree-Linear	NN-Linear	NN-Tree
difference	0.47	0.69	0.22	0.22	0.52	0.29	-0.08	0.16	0.24
# of +	30	29	25	26	31	27	16	20	26
${\rm fraction}\ {\rm of}\ +$	0.91	0.88	0.76	0.79	0.94	0.82	0.48	0.61	0.79

					1	Equal-V	Veighted										1	Value-V	Veighted					
	Market	OLS-3	OLS	LASSO	RIDGE	RF	GBRT+	HNN1	NN2	NN3	NN4	NN5	Market	OLS-3	OLS	LASSO	RIDGE	RF	GBRT+	HNN1	NN2	NN3	NN4	NN5
USA	0.58	0.81	1.55	1.44	1.55	2.29	2.20	2.56	2.69	2.60	2.44	2.59	0.53	0.40	0.33	0.30	0.33	1.03	0.49	0.94	1.07	1.06	1.00	1.39
Japan	0.85	0.42	0.60	0.54	0.60	1.19	1.18	1.76	1.77	1.62	1.38	1.60	0.46	0.06	0.24	0.31	0.24	0.49	0.79	0.61	0.65	0.33	0.50	0.67
China	0.51	1.43	1.06	1.30	1.06	1.90	1.74	1.80	1.96	1.76	1.88	2.18	0.37	0.90	0.61	0.89	0.61	1.12	1.20	1.12	1.23	1.23	1.28	1.44
India	0.70	0.87	0.68	0.45	0.68	1.93	1.45	1.89	1.91	1.94	1.84	1.99	0.54	0.48	-0.12	-0.30	-0.12	0.12	0.40	-0.24	0.16	0.40	0.13	0.53
Korea	0.59	1.11	1.16	1.05	1.16	1.77	1.57	2.45	2.48	2.13	1.88	1.91	0.32	0.13	0.34	0.40	0.34	1.01	0.79	1.07	1.04	0.92	0.70	0.68
Hong_Kong	0.42	0.67	0.63	0.54	0.63	1.94	1.43	2.00	1.94	2.24	1.98	1.97	0.32	0.11	0.04	-0.06	0.03	0.41	0.05	1.01	0.60	0.80	0.57	0.73
France	0.74	1.06	1.77	2.03	1.78	2.61	2.22	2.57	2.81	2.78	2.61	2.71	0.47	0.77	0.48	0.47	0.48	0.47	0.54	0.82	1.22	0.83	0.76	1.20
Taiwan	0.44	0.31	-0.12	-0.19	-0.12	0.42	0.50	1.39	1.45	1.41	1.32	1.48	0.40	-0.17	-0.45	-0.48	-0.45	-0.13	-0.03	0.48	0.57	0.33	0.44	0.60
Australia	0.65	1.04	2.43	2.02	2.43	4.19	3.83	4.10	4.22	4.45	4.36	4.24	0.53	0.66	0.31	-0.44	0.30	0.72	0.60	1.50	1.67	1.56	1.75	2.01
${\bf United_Kingdom}$	0.42	0.37	0.43	0.15	0.42	1.36	1.25	1.32	1.46	1.24	1.29	1.19	0.54	0.46	0.11	-0.34	0.12	0.71	0.30	0.35	0.77	0.52	0.77	0.30
Thailand	0.74	0.73	0.36	0.09	0.37	0.96	0.63	1.07	1.32	1.26	1.39	1.23	0.41	0.51	-0.22	-0.51	-0.22	0.18	0.08	0.45	0.58	0.54	0.72	0.64
Singapore	0.23	0.68	2.16	2.33	2.17	2.53	2.75	3.36	3.32	3.25	3.00	3.48	0.27	0.06	0.21	0.22	0.22	0.79	0.75	1.48	1.64	1.38	1.56	2.01
South_Africa	1.10	1.53	1.72	1.58	1.72	1.79	1.39	1.41	1.56	1.57	1.56	1.49	0.67	0.53	0.72	0.33	0.72	0.90	0.62	0.61	0.93	0.86	0.84	0.90
Sweden	0.54	0.69	1.12	1.12	1.08	1.71	1.49	1.72	1.81	1.74	1.96	1.81	0.37	0.55	0.09	0.32	0.07	0.97	0.70	0.48	0.65	0.58	0.84	0.65
Poland	0.29	0.88	0.63	0.60	0.63	1.67	1.47	1.97	1.95	1.97	1.84	1.68	0.33	0.33	-0.16	-0.13	-0.16	0.79	0.57	0.33	0.94	0.86	0.91	0.64
Turkey	0.82	0.16	0.06	-0.06	0.07	0.51	0.36	0.79	0.75	0.63	0.59	0.52	0.67	-0.10	-0.03	-0.01	-0.03	0.18	0.12	0.43	0.59	0.45	0.38	0.58
Italy	0.04	0.38	0.10	0.10	0.10	0.98	0.90	0.85	0.79	0.77	0.63	0.64	0.08	0.37	0.02	0.06	0.04	0.70	0.40	0.58	0.65	0.57	0.41	0.47
Vietnam	0.74	0.85	1.54	1.51	1.54	2.33	2.15	3.01	2.62	2.45	2.71	2.63	0.59	0.09	0.25	-0.13	0.25	0.66	0.27	1.09	1.17	1.03	1.07	0.99
Switzerland	0.53	0.75	0.53	0.31	0.53	0.90	0.76	0.80	0.82	1.07	0.89	1.04	0.28	0.79	0.35	0.25	0.34	0.68	0.60	0.42	0.38	0.65	0.63	0.77
Israel	0.49	1.00	0.95	0.92	0.95	1.03	0.93	1.07	1.21	1.12	1.09	1.14	0.00	0.92	0.30	0.04	0.30	0.75	0.50	0.90	1.14	0.91	1.03	1.21
Indonesia	0.98	0.67	0.08	-0.23	0.09	0.49	0.09	0.32	0.25	0.26	0.28	0.15	0.93	0.54	0.29	0.13	0.32	0.75	0.43	0.73	0.54	0.65	0.52	0.44
Greece	0.34	0.46	2.00	2.08	2.00	2.48	2.59	2.79	2.76	2.73	2.77	2.60	-0.02	-0.15	0.19	0.59	0.19	0.71	0.68	1.18	0.81	0.85	0.49	1.12
Philippines	1.12	0.75	1.20	1.26	1.20	1.64	1.39	1.50	1.40	1.55	1.52	1.64	0.88	0.07	0.41	0.30	0.40	0.57	0.46	0.81	0.95	1.08	0.74	1.14
Denmark	0.54	0.33	0.84	0.87	0.84	1.44	1.45	1.42	1.60	1.70	1.39	1.38	0.76	0.51	0.04	0.08	0.04	0.77	0.41	0.47	0.68	0.97	0.63	0.81
Finland	0.52	0.84	0.81	0.56	0.81	1.08	1.15	0.74	0.84	0.95	0.86	1.14	0.12	0.40	0.02	0.08	0.02	0.46	0.18	0.24	0.29	0.69	0.36	0.65
Sri_Lanka	0.96	0.27	1.28	2.14	1.29	2.16	2.29	1.88	1.78	1.65	1.78	2.03	1.04	-0.14	0.54	0.70	0.54	1.46	1.43	1.33	0.97	1.12	0.74	1.67
Norway	0.05	0.41	0.37	0.28	0.38	0.96	0.72	1.12	1.06	1.12	1.10	1.21	0.25	0.32	-0.13	-0.09	-0.12	0.54	0.50	0.54	0.37	0.70	0.72	0.31
Saudi_Arabia	0.26	0.25	-0.05	0.26	-0.07	1.20	0.72	0.68	0.81	0.64	0.61	0.41	0.36	0.06	0.08	0.24	0.06	0.70	0.46	0.48	0.26	0.20	0.27	0.10
Jordan	0.38	0.37	-0.10	-0.22	-0.10	0.97	0.57	1.41	1.26	1.32	1.09	1.18	-0.04	-0.33	-0.24	0.00	-0.24	0.77	0.29	0.55	0.65	1.02	0.41	0.63
Chile	0.85	0.86	0.21	-0.25	0.23	0.46	0.30	0.04	0.29	0.23	0.40	0.30	0.65	0.52	0.21	-0.06	0.21	0.38	0.15	0.24	0.36	0.33	0.62	0.39
Belgium	0.59	0.46	0.07	-0.07	0.07	0.67	0.75	0.70	0.64	0.78	0.59	0.55	0.41	0.54	-0.29	-0.50	-0.29	0.13	-0.12	0.30	0.11	0.51	0.02	0.24
Kuwait	0.29	0.50	0.70	0.74	0.71	1.15	1.19	1.58	1.62	1.53	1.71	1.48	0.21	0.41	0.37	0.07	0.37	0.73	0.93	0.95	1.04	1.10	1.31	0.97
Spain	0.33	0.48	0.24	-0.32	0.25	0.43	0.36	0.07	0.43	0.40	0.54	0.43	0.37	0.44	0.29	-0.15	0.30	0.47	0.75	0.07	0.74	0.61	0.68	0.31
Russia	1.22	0.28	0.77	0.74	0.76	0.73	0.79	0.78	0.67	0.72	0.94	0.74	0.90	0.23	0.26	0.38	0.26	0.66	0.57	0.56	0.70	0.54	0.65	0.47

IV. Predicting International Stock Returns with Market-Specific

Models

1)results

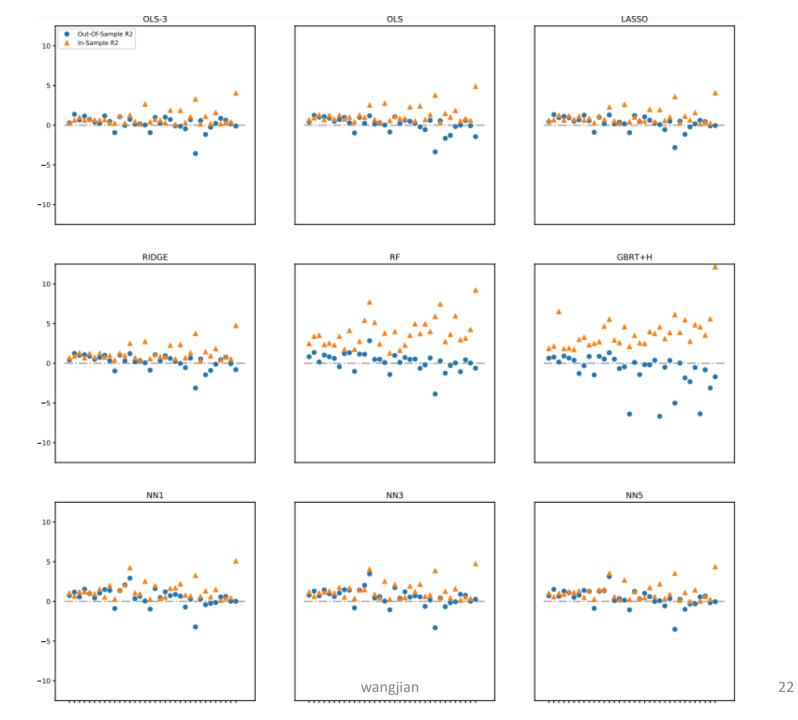
- The result is similar to what we find with U.S.-estimated models, NN models exhibit the strongest return predictability in most of the markets.
- However, different from the U.S.-estimated models, marketspecific tree models seem to underperform linear models.

		Sha	rpe Ratio (EW)	Sha	arpe Ratio (VW)		R_{oos}^2	
		Tree-Linear	NN-Linear	NN-Tree	Tree-Linear	NN-Linear	NN-Tree	Tree-Linear	NN-Linear	NN-Tree
	difference	-0.14	0.59	0.73	-0.26	0.38	0.63	-0.16	0.33	0.48
All markets	# of +	12	27	31	8	27	29	9	25	29
	fraction of $+$	0.36	0.82	0.94	0.24	0.82	0.88	0.27	0.76	0.88
	difference	0.04	0.81	0.78	-0.18	0.45	0.62	0.05	0.46	0.41
Top half	# of +	10	14	14	4	13	15	7	13	15
	fraction of $+$	0.62	0.88	0.88	0.25	0.81	0.94	0.44	0.81	0.94
	difference	-0.3	0.38	0.68	-0.33	0.31	0.64	-0.35	0.2	0.54
Bottom half	# of +	2	13	17	4	14	14	2	12	14
	fraction of $+$	0.12	0.76	1	0.24	0.82	0.82	0.12	0.71	0.82

2) In-Sample and Out-of-Sample R2

Based on the
results of 33
markets, it is true
that tree models
can achieve a
high in-sample
R2 in almost all
markets, but the
high R2 does not
survive out of the
sample.

		<i>2)</i> 111	-Sam	pic an	u O	11-01-	Samp				
	OLS-3	OLS	LASSO	RIDGE	RF	GBRT+	H NN1	NN2	NN3	NN4	NN5
USA	0.29	0.42	0.45	0.42	0.83	0.64	0.75	0.81	0.79	0.73	0.71
	(0.32)	(0.67)	(0.56)	(0.67)	(2.47)	(1.85)	(1.05)	(1.02)	(1.14)	(1.15)	(1.03)
Japan	1.38	1.25	1.34	1.25	1.37	0.79	1.17	1.31	1.30	1.26	1.51
	(0.64)	(0.92)	(0.67)	(0.92)	(3.38)	(2.14)	(0.66)	(0.63)	(0.62)	(0.60)	(0.57)
China	0.67	1.02	0.95	1.02	0.16	0.15	0.56	0.65	0.70	0.78	0.65
	(0.99)	(1.30)	(1.25)	(1.30)	(3.52)	(6.51)	(1.21)	(1.11)	(1.06)	(1.03)	(1.03)
India	1.14	1.08	1.11	1.08	1.04	0.92	1.54	1.60	1.44	1.44	1.30
	(0.61)	(0.68)	(0.64)	(0.68)	(2.34)	(1.83)	(1.21)	(1.31)	(1.15)	(1.07)	(0.89)
Korea	0.71	0.89	0.94	0.90	0.82	0.66	0.98	0.94	0.97	1.08	1.09
	(0.76)	(1.23)	(1.18)	(1.23)	(2.53)	(1.91)	(1.09)	(1.10)	(1.31)	(1.28)	(1.19)
Hong_Kong	0.42	0.50	0.51	0.50	0.62	0.39	0.43	0.63	0.62	0.86	0.52
	(0.64)	(0.75)	(0.70)	(0.75)	(2.29)	(1.71)	(0.93)	(0.90)	(1.03)	(1.13)	(1.13)
France	0.24	0.72	0.68	0.73	-0.44	-1.29	1.05	0.91	1.06	1.13	0.78
	(0.63)	(1.26)	(1.12)	(1.26)	(3.37)	(3.00)	(1.53)	(1.61)	(1.74)	(1.63)	(1.31)
Taiwan	1.17	0.98	1.26	1.01	1.22	-0.30	1.49	1.33	1.47	1.50	1.39
	(0.67)	(0.77)	(0.61)	(0.76)	(1.73)	(3.26)	(0.53)	(0.51)	(0.53)	(0.52)	(0.50)
Australia	0.48	0.30	0.57	0.32	1.33	0.86	1.38	1.40	1.43	1.35	1.26
	(0.33)	(1.00)	(0.85)	(0.99)	(4.13)	(2.30)	(1.98)	(1.59)	(1.68)	(1.81)	(1.32)
United_Kingdom	-0.93	-0.98	-0.89	-0.96	-1.02	-1.46	-0.89	-1.00	-0.81	-0.66	-0.88
	(0.24)	(0.42)	(0.26)	(0.40)	(1.75)	(2.50)	(0.27)	(0.23)	(0.37)	(0.32)	(0.26)
Thailand	1.05	1.00	1.00	1.05	1.16	0.87	1.36	1.23	1.42	1.41	1.28
	(1.15)	(1.26)	(1.12)	(1.25)	(2.74)	(2.70)	(1.43)	(1.20)	(1.41)	(1.49)	(1.42)
Singapore	-0.03	0.25	0.19	0.31	1.15	0.54	2.09	1.94	2.03	2.09	1.36
	(0.26)	(0.98)	(0.70)	(0.97)	(5.40)	(4.66)	(2.07)	(1.55)	(1.47)	(1.88)	(1.48)
South_Africa	0.73	1.18	1.29	1.21	2.84	1.33	2.93	3.11	3.47	3.56	3.13
	(1.25)	(2.52)	(2.27)	(2.50)	(7.69)	(5.54)	(4.22)	(3.67)	(4.04)	(4.10)	(3.52)
Sweden	0.12	0.15	0.17	0.18	0.49	0.52	0.36	0.36	0.43	0.36	0.10
	(0.46)	(0.70)	(0.52)	(0.69)	(5.13)	(2.90)	(1.05)	(1.14)	(0.90)	(0.87)	(0.57)
Poland	0.16	0.30	0.38	0.33	0.50	-0.67	0.64	0.59	0.60	0.35	0.35
	(0.14)	(0.40)	(0.24)	(0.39)	(2.41)	(2.60)	(0.92)	(0.63)	(0.44)	(0.23)	(0.18)
Turkey	0.03	0.03	0.17	0.07	0.10	-0.44	0.05	0.16	0.04	0.07	0.16
	(2.64)	(2.74)	(2.60)	(2.74)	(3.78)	(4.59)	(2.53)	(2.56)	(2.54)	(2.65)	(2.67)
Italy	-0.94	-0.86	w -ang jia	n -0.86	-1.41	-6.39	-0.97	-1.11	-1.06	-1.04 2	1 -1.06
	(0.42)	(0.57)	(0.43)	(0.56)	(1.27)	(2.11)	(0.26)	(0.16)	(0.24)	(0.24)	(0.24)



IV. Predicting International Stock Returns with Market-Specific Models

3) Return-Characteristics Relationships: Common or Market-Specific?

- On the one hand, there are common similarities in the returncharacteristic relationship across international equity markets.
 - size (logsize); turnover rate (turn); volume (logdolvol)
- On the other hand, some market-specific features show up.
 - (mom_1)

USA	0.019	0.17	0.034	0.047	0.015	0.018	0.07	0.32	0.12	0.03	0.022	0.14
Japan	0.02	0.1	0.037	0.062	0.074	0.12	0.099	0.14	0.19	0.064	0.042	0.05
China	0.066	0.041	0.049	0.049	0.024	0.03	0.045	0.11	0.32	0.11	0.034	0.13
India	0.062	0.14	0.042	0.061	0.06	0.076	0.092	0.2	0.086	0.077	0.039	0.067
Korea	0.075	0.093	0.049	0.077	0.05	0.072	0.068	0.2	0.051	0.03	0.094	0.14
Hong_Kong	0.069	0.13	0.026	0.054	0.04	0.053	0.043	0.25	0.054	0.036	0.065	0.18
France	0.092	0.073	0.078	0.08	0.063	0.082	0.11	0.1	0.074	0.074	0.092	0.079
Taiwan	0.11	0.071	0.18	0.083	0.08	0.044	0.084	0.11	0.013	0.037	0.11	0.083
Australia	0.081	0.083	0.074	0.081	0.085	0.078	0.087	0.081	0.095	0.095	0.072	0.088
d_Kingdom	0.054	0.045	0.13	0.095	0.039	0.082	0.057	0.11	0.18	0.039	0.026	0.14
Thailand	0.11	0.096	0.079	0.047	0.048	0.073	0.067	0.097	0.11	0.069	0.041	0.16
Singapore	0.027	0.33	0.044	0.092	0.027	0.018	0.032	0.11	0.038	0.029	0.13	0.12
iouth_Africa	0.088	0.074	0.078	0.086	0.083	0.094	0.096		0.088	0.079	0.061	0.083
Sweden	0.091	0.074	0.077	0.084	0.084	0.088	0.085	0.085	0.091	0.081	0.078	0.082
Poland	0.07	0.077	0.084	0.096	0.083	0.086	0.089	0.08	0.093	0.069	0.088	0.085
in	dmom_a_1	2 mom_1	mom_6	mom_12	chmom_6	MAXRET	retvol	logsize	turn	sp	b2m	logdolvol

0.30

0.24

0.18

0.12

0.06

IV. Predicting International Stock Returns with Market-Specific Models

3) Return-Characteristics Relationships: Common or Market-Specific?

- On the one hand, there are common similarities in the returncharacteristic relationship across international equity markets. On the other hand, some market-specific features show up.
- Whether market-specific models perform better than their U.S.estimated counterparts

		OLS-3	OLS	LASSO	RIDGE	RF	GBRT+H	NN1	NN2	NN3	NN4	NN5
	difference	0.399	0.733	0.710	0.731	0.328	0.247	0.899	0.928	0.968	0.725	0.777
Sharpe Ratio (EW)	# of +	25	29	30	27	22	22	26	27	26	25	27
	fraction of +	0.758	0.879	0.909	0.818	0.667	0.667	0.788	0.818	0.788	0.758	0.818
	difference	0.185	0.368	0.389	0.423	0.357	0.151	0.354	0.497	0.505	0.455	0.506
Sharpe Ratio (VW)	# of +	18	22	25	22	24	17	24	25	25	26	26
	fraction of +	0.545	0.667	0.758	0.667	0.727	0.515	0.727	0.758	0.758	0.788	0.788
	difference	0.093	0.592	0.080	0.578	1.391	3.277	0.345	0.334	0.385	0.454	0.638
R_{oos}^2	# of +	15	20	18	21	24	19	20	19	19	19	17
	fraction of +	0.455	0.606	0.545	0.636	0.727	0.576	0.606	0.576	0.576	0.576	0.515

IV. Pooling All Stocks

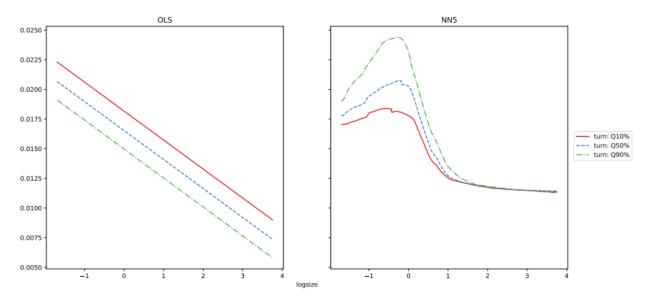
- In the top panel, it shows that NN models perform the best.
- Given the larger pool of stocks and the important role of price trend predictors in machine learning models, it is not surprising that the outperformance is achieved with relatively higher portfolio turnover rate.

	Market	OLS-3	OLS	LASSO	RIDGE	RF	GBRT+H	NN1	NN2	NN3	NN4	NN5
Sharpe Ratio (EW)	0.71	1.23	2.06	2.00	2.06	3.21	3.05	3.39	3.36	3.43	3.31	3.51
Sharpe Ratio (VW)	0.51	0.54	0.53	0.40	0.52	1.21	0.62	1.08	1.22	1.39	1.57	1.32
R_{oos}^2		0.47	0.46	0.53	0.47	0.52	0.66	0.84	0.74	0.78	0.77	0.72
Portfolio R_{oos}^2 (EW)		4.50	5.04	5.11	5.04	6.34	5.75	6.83	6.60	6.73	6.62	6.05
Portfolio R_{oos}^2 (VW)		3.27	1.06	1.32	1.05	3.09	0.12	3.12	2.66	3.62	3.38	2.88
					Drawdowns	and Turn	over (Equally	Weighted)				
Max DD (%)	51.68	28.23	16.80	21.47	16.80	26.33	21.53	13.12	7.07	13.47	11.17	10.61
Max 1M Loss (%)	29.02	17.55	14.45	15.14	14.45	16.70	16.18	13.12	7.07	13.47	11.17	10.61
Turnover (%)		49.53	156.83	172.35	156.91	155.41	159.66	149.03	147.37	146.99	148.48	147.31
					Drawdown	ns and Turr	nover (Value V	Veighted)				
Max DD (%)	52.29	40.47	45.79	45.25	45.37	32.49	34.07	42.05	31.79	33.89	25.02	31.55
Max 1M Loss (%)	22.84	21.57	14.57	20.37	14.57	19.99	18.31	18.42	19.50	17.97	14.38	16.70
Turnover (%)		46.60	140.12	169.97	140.30	174.59	172.90	150.71	157.71	158.16	161.18	161.28

	Market	OLS-3	OLS	LASSO	RIDGE	RF	GBRT+H	NN1	NN2	NN3	NN4	NN5
	Risk-adjusted Performance using FF5 + Mom model, 1992-2017 (Equally Weighted)											
Mean Return		1.58	2.56	2.51	2.56	3.52	3.44	4.00	3.89	3.99	3.82	3.85
α		1.45	2.67	2.67	2.67	3.25	3.27	3.91	3.86	3.91	3.82	3.81
t(lpha)		5.03	8.49	8.36	8.50	12.24	12.27	13.96	13.87	13.90	13.62	13.87
R^2		10.73	7.47	7.99	7.51	9.37	9.06	9.82	7.97	9.00	9.18	7.62
Information Ratio		0.35	0.60	0.59	0.60	0.86	0.86	0.98	0.97	0.98	0.96	0.97
	Risk-adjusted Performance using HKK model, 1981-2010 (Equally Weighted)											
Mean Return		1.70	3.25	3.21	3.26	4.08	3.96	4.51	4.55	4.60	4.44	4.44
α		1.42	3.34	3.32	3.34	4.08	3.94	4.50	4.53	4.58	4.45	4.46
t(lpha)		4.66	10.35	10.22	10.31	15.22	14.34	16.04	16.12	16.22	15.85	16.82
R^2		4.03	1.91	2.07	1.85	2.75	1.85	3.48	2.45	3.03	2.57	2.16
Information Ratio		0.29	0.65	0.64	0.65	0.95	0.90	1.01	1.01	1.02	0.99	1.06
	Risk-adjusted Performance using KW model, 1990-2010 (Equally Weighted)											
Mean Return		1.82	3.2	3.18	3.21	4.16	4.06	4.62	4.68	4.68	4.52	4.48
α		1.71	3.47	3.47	3.48	4.22	4.17	4.74	4.82	4.78	4.65	4.62
$t(\alpha)$		4.89	9.27	9.19	9.26	13.32	12.91	14.58	14.72	14.47	14.19	14.86
R^2		7.20	6.72	6.41	6.79	3.51	4.50	6.77	5.15	5.10	5.28	4.20
Information Ratio		0.34	0.65	0.64	0.65	0.93	0.90	1.02	1.03	1.01	0.99	1.04

The R2 of the factor models is low, typically below 10%, particularly for NN, suggesting that the factors can only explain a small fraction of the returns of the NN-based strategies.

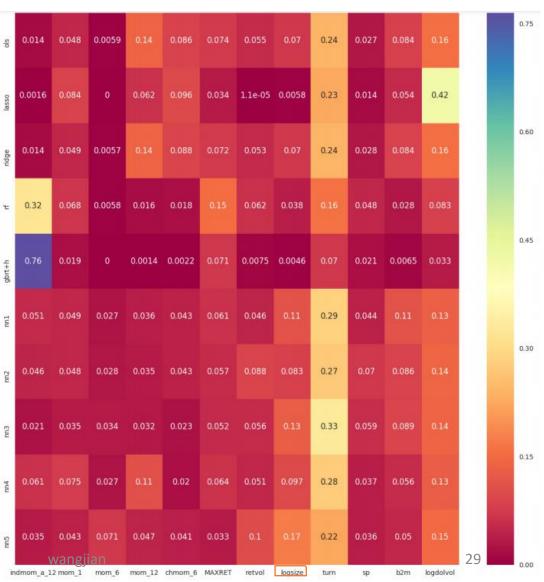
V. Discussion



 Liu, Stambaugh, and Yuan (2019) drop the smallest 30% of firms in constructing the size factor in China, pointing out that the value of these firms incorporates the possibility of reverse mergers. (in which small public firms will be acquired by private firms to circumvent IPO constraints and go public)

V. Discussion

 We also see that the variable importance of size in Figure is higher for NN5 than OLS, suggesting that NN5 can make better use of the size information to rank the returns of small stocks.



4. Conclusion

- In the U.S. market, even with only 12 characteristics, the predictive power and profitability of complex machine learning models are comparable to those documented in previous studies using hundreds of variables.
- Training our models using U.S. data and applying them on international stocks concludes that neural network (NN) outperforms linear models, possibly because of the nonlinear and complex interactions among the predictors.
- There are signs that regression trees overfit the in-sample data and underperform linear models, especially in countries where there are few observations.
- We take the first step to study the size effect in China, which is different from the U.S. and the rest of the world.