# Machine Learning versus Economic Restrictions: Evidence from Stock Return Predictability

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Working Paper, 2021.4

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2021.7.8

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# **Backgrounds & Motivation**

- Recent work has challenged the credibility of the predictable patterns
  of a plethora of anomalies. However, anomalous return patterns
  characterize expensive-to-buy and difficult-to-arbitrage stocks.
  Notably, it is increasingly difficult to exploit anomalies in recent years
  due to increased market liquidity and arbitrage activity.
- Counter to this "anomaly challenging" strand of literature, there has been an emerging body of work that reports phenomenal investment profitability based on signals generated by ML methods. Understanding the relevant economic mechanisms is essential.
- Whether ML methods clear sensible economic restrictions in empirical finance and face the same challenges?
- ➤ Is there any economic grounds of investment decisions advocated by the seemingly opaque ML methods?

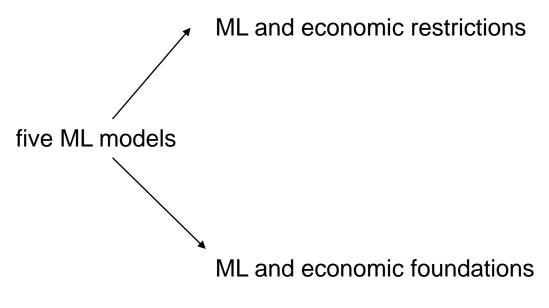
#### Research Problem

- Whether machine learning methods sensible economic restrictions in empirical finance?
  - ➤ We find that machine learning methods often fail to clear standard economic restrictions, such as VW returns and excluding microcaps or distressed firms (expensive-to-buy).
  - ➤ The trading strategy is more profitable during periods of increasing limits to arbitrage, such as high investor sentiment, high market volatility, and low market liquidity (hard-to-arbitrage).
  - ➤ Given the high turnover and transaction costs, the strategy is hard to leave alpha on the table.
- Is there any economic grounds of investment decisions advocated by the seemingly opaque machine learning methods?
  - We find DL signals identify stocks in line with most anomalybased trading strategies.

#### Contribution

- Our analysis initiates a protocol for future work to demonstrate the feasibility of trading profits, such as excluding difficult-to-arbitrage stocks and high limits-to-arbitrage market states, considering portfolio turnover and the corresponding transaction costs.
- Our paper provides evidence for the economic constraints and economic foundations of ML methods, enriches the academic and policy discussions surrounding the adoption of ML techniques in asset management, including the effectiveness and sustainability of new trading signals, the lack of transparency and economic interpretability in complex machine learning algorithms.

### **Outline**



#### cross-section: cheap to trade

- excluding microcaps
- only rated firms
- rated, exclude distressed firms time series: limits-to-arbitrage
- high volatility
- high sentiment
- low liquidity

#### turnover and transaction costs

leave alpha or not

Whether stocks with similar ML signals share same characteristics that predict future returns

# **Model Setting**

- two deep learning methods, nonlinear methods
- ➤ GKX: 32-16-8 NN3, follow Gu, Kelly, and Xiu (2020)
- ➤ CPZ: incorporate a no-arbitrage condition into multiple connected neural networks, including feed forward networks (FFNs), recurrent neural networks (RNNs) with long short-term memory (LSTM) cells, and a generative adversarial network (GAN) to estimate the SDF and its stock loadings, follow Chen, Pelger, and Zhu (2020)
- two conditional beta pricing models
- > IPCA: IPCA, follow Kelly, Pruitt, and Su (2019), linear
- ➤ CA: the conditional autoencoder, extended from Gu, Kelly, and Xiu (2021), nonlinear ML methods
- method focused on equity portfolios
- KNS: SDF and MVE portfolio, follow Kozak, Nagel, and Santosh (2020)

# **Model Setting**

Sample: all NYSE/AMEX/Nasdaq stocks

- GKX, IPCA, and CA methods: 920 predictors, 1957 to 2017
- ➤ 94 firm characteristics that have been documented as anomalies+ 74 industry dummies based on the first two digits of SIC codes + 8 monthly macroeconomic predictors + 94×8 interactions between characteristics & macroeconomic variable
- ✓ for GKX and CA: 18 (train: 1957 to 1974) + 12 (validation: 1975 to 1986)
   + 31 (test: 1987 to 2017), expanding
- ✓ for IPCA: skip the validation procedure and requires at least 120 months for the in-sample estimation, and forward rolling is performed on a monthly basis
- CPZ method: use 46 firm characteristics, 178 macroeconomic predictors, nonlinear interactions; 1967 to 2016; 20 (train: 1967 to 1986)
   + 5 (validation: 1987 to 1991) + 25 (test: 1992 to 2016), expanding

# **Model Setting**

- Data Source:
- > daily and monthly stock data obtained from the CRSP
- > quarterly / annual financial data come from the COMPUSTAT database
- Subsamples with Economic Restrictions
- excludes microcaps (stocks with a market capitalization smaller than the 20th NYSE size percentile)
- includes only rated firms (firms with data on S&P long-term issuer credit ratings)
- 3. filter downgraded firms on the universe of rated firms
- Portfolios sort using the four proposed ML signals

- the standard OLS regression methodology with all 920 predictors used in the GKX estimation to predict the one-month-ahead stock return
- portfolio sorts while combining all the signals on individual anomalies

Panel A: Returns to Investment Strategies Sorted by OLS-Predicted Returns

				mer i ii reetai	no to m. con	mem strateg	ies serieu ej	OLD I redicted	rectaring					
			E	qual-Weight	ed					Va	lue-Weighte	ed		
	Return	CAPM	FFC	FFC+PS	FF5	FF6	SY	Return	CAPM	FFC	FFC+PS	FF5	FF6	SY
Full Sample	1.215***	1.162***	1.268***	1.272***	1.521***	1.545***	1.475***	0.084	0.118	0.148	0.164	0.308	0.268	0.127
	(5.25)	(4.78)	(5.32)	(5.28)	(5.95)	(5.85)	(4.69)	(0.39)	(0.50)	(0.59)	(0.64)	(1.09)	(0.92)	(0.37)
Nonmicrocaps	0.472**	0.410*	0.368*	0.367*	0.565**	0.514**	0.409	0.013	0.060	0.118	0.128	0.237	0.223	0.074
	(2.37)	(1.84)	(1.72)	(1.66)	(2.42)	(2.19)	(1.47)	(0.07)	(0.30)	(0.58)	(0.61)	(1.04)	(0.95)	(0.25)
Credit Rating Sample	0.437*	0.361	0.503**	0.488**	0.458**	0.563**	0.632**	0.024	0.061	0.126	0.135	0.103	0.115	0.133
	(1.78)	(1.50)	(2.12)	(2.02)	(2.00)	(2.33)	(2.02)	(0.12)	(0.27)	(0.58)	(0.61)	(0.46)	(0.49)	(0.51)
Nondowngrades	0.506**	0.480**	0.542**	0.506**	0.412*	0.470**	0.550**	-0.008	0.035	0.092	0.078	0.082	0.065	0.032
	(2.39)	(2.13)	(2.41)	(2.29)	(1.96)	(2.08)	(1.97)	(-0.04)	(0.15)	(0.41)	(0.34)	(0.34)	(0.26)	(0.12)
			P	anel B: Retu	rns to Invest	ment Strateg	gies Sorted by	Individual An	omalies					
			E	qual-Weight	ed					Va	lue-Weighte	ed		
	Return	CAPM	FFC	FFC+PS	FF5	FF6	SY	Return	CAPM	FFC	FFC+PS	FF5	FF6	SY
Full Sample	0.366***	0.472***	0.342***	0.346***	0.308***	0.250***	0.221***	0.192***	0.306***	0.185***	0.189***	0.139***	0.092***	0.043
	(5.92)	(8.18)	(7.65)	(7.91)	(6.03)	(6.07)	(3.95)	(2.91)	(5.41)	(4.72)	(4.88)	(3.27)	(2.89)	(1.19)
Nonmicrocaps	0.233***	0.344***	0.214***	0.218***	0.167***	0.115***	0.079**	0.170***	0.272***	0.150***	0.151***	0.095**	0.049*	-0.003
	(3.71)	(6.11)	(5.98)	(6.21)	(4.40)	(4.60)	(2.16)	(2.74)	(4.87)	(3.97)	(4.02)	(2.57)	(1.87)	(-0.09)
Credit Rating Sample	0.302***	0.387***	0.263***	0.263***	0.244***	0.182***	0.121**	0.131**	0.215***	0.113***	0.111***	0.092**	0.045	-0.017
	(5.11)	(6.78)	(6.14)	(6.24)	(4.59)	(4.56)	(2.55)	(2.47)	(4.75)	(3.27)	(3.11)	(2.20)	(1.42)	(-0.52)
Nondowngrades	0.124***	0.197***	0.100***	0.103***	0.083**	0.039	-0.017	0.071	0.142***	0.045	0.046	0.038	-0.004	-0.071*
	(2.60)	(4.45)	(3.14)	(3.31)	(2.11)	(1.22)	(-0.44)	(1.48)	(3.28)	(1.43)	(1.44)	(0.93)	(-0.13)	(-1.93)

# Empirical Results – NN3

			Panel A:	Returns to Ir	ivestment St	rategies Sorted	d by NN3-Pred	licted Returns	3				
		Е	Equal-Weighte	èd					Va	alue-Weighted	1		
Return	CAPM	FFC	FFC+PS	FF5	FF6	SY	Return	CAPM	FFC	FFC+PS	FF5	FF6	SY
2.470***	* 2.742***	2.483***	2.497***	2.349***	2.236***	2.312***	1.556***	1.894***	1.338***	1.361***	1.206***	0.916***	0.769***
(9.03)	(9.78)	(9.02)	(9.27)	(9.35)	(8.06)	(7.91)	(4.53)	(5.64)	(5.14)	(5.31)	(4.66)	(4.08)	(3.03)
		Pane	l B: Returns t	to Investment	t Strategies ?	Sorted by NN3	3-Predicted Ret	turns (Nonmi	crocaps)				
		Ec	qual-Weighted	d					Va	lue-Weighted	i		
Return	CAPM	FFC	FFC+PS	FF5	FF6	SY	Return	CAPM	FFC	FFC+PS	FF5	FF6	SY
1.243***	1.625***	0.924***	0.940***	0.680***	0.353**	0.357	1.047***	1.389***	0.771***	0.771***	0.627**	0.312	0.179
(3.75)	(5.04)	(4.08)	(4.19)	(2.89)	(2.02)	(1.37)	(3.24)	(4.43)	(3.23)	(3.24)	(2.41)	(1.51)	(0.73)
		Pan	el A: Returns	to Investment	t Strategies S	orted by NN3	-Predicted Retu	ırns (Credit R	ating Sample)				
		J	Equal-Weight	ed					V	alue-Weighter	:d		
Return	CAPM	FFC	FFC+PS	FF5	FF6	SY	Return	CAPM	FFC	FFC+PS	FF5	FF6	SY
1.374***	1.759***	1.073***	1.083***	1.048***	0.652**	* 0.548*	1.024***	* 1.344***	* 0.746***	0.743***	0.784***	* 0.433**	0.150
(4.08)	(5.75)	(4.62)	(4.59)	(3.63)	(3.16)	(1.93)	(3.18)	(4.40)	(3.31)	(3.23)	(2.70)	(2.05)	(0.59)
		P	anel B: Return	ns to Investm	ent Strategie	s Sorted by NN	N3-Predicted Re	eturns (Nondo	owngrades)				
		F	Equal-Weighte	ed .					Va	alue-Weighted	1		
Return	CAPM	FFC	FFC+PS	FF5	FF6	SY	Return	CAPM	FFC	FFC+PS	FF5	FF6	SY
0.667**	0.997***	0.343	0.362*	0.323	-0.026	-0.205	0.723**	0.996***	0.424*	0.445**	0.517*	0.204	-0.129
(2.11)	(3.40)	(1.63)	(1.70)	(1.32)	(-0.13)	(-0.73)	(2.49)	(3.40)	(1.93)	(2.00)	(1.87)	(0.92)	(-0.52)

ML substantially improves the investment payoff compared to traditional methods. Both deliver lower payoffs in the presence of economic restrictions with a similar proportional magnitude.

### Empirical Results - CPZ

			Pan	el A: Returns	to Investmen	t Strategies Sort	ted by Risk	Loadings					
		Ec	qual-Weighted	1					Va	alue-Weighted	1		
Return	CAPM	FFC	FFC+PS	FF5	FF6	SY	Return	CAPM	FFC	FFC+PS	FF5	FF6	SY
3.446***	3.415***	3.471***	3.473***	3.465***	3.492***	3.566***	2.183***	2.056***	1.910***	1.918***	1.869***	1.867***	1.983***
(11.25)	(11.17)	(8.87)	(9.28)	(8.94)	(8.04)	(8.01)	(6.37)	(5.68)	(5.42)	(5.66)	(5.29)	(4.86)	(5.30)
			Panel B: Retu	rns to Investr	ent Strategie	es Sorted by Ris	sk Loadings	(Nonmicroca	aps)				
		!	Equal-Weight	ed					V	alue-Weighte	d		
Return	CAPM	FFC	FFC+PS	FF5	FF6	SY	Return	CAPM	FFC	FFC+PS	FF5	FF6	SY
1.586***	1.645***	1.325***	1.332***	1.306***	1.161***	1.218***	1.083***	1.083***	0.688***	0.655***	0.720***	0.548**	0.548**
(6.80)	(6.98)	(5.86)	(6.09)	(6.42)	(5.13)	(5.06)	(4.28)	(4.06)	(2.87)	(2.79)	(2.93)	(2.23)	(2.27)
		F	Panel A: Retur	ns to Investm	ent Strategies	Sorted by Risk	Loadings (C	Credit Rating	Sample)				
			Equal-Weigh	nted						Value-Weigh	ited		
Return	CAPM	FFC	FFC+PS	FF5	FF6	SY	Ref	turn CA	APM FF	FC FFC+P	S FF5	FF6	SY
1.519***	1.522***	1.337***	1.340***	1.376***	1.270***	** 1.257***	0.812	2*** 0.80	0.48	80* 0.420	0.559*	0.423	0.339
(5.74)	(5.83)	(4.36)	(4.44)	(4.89)	(3.93)	(3.77)	(2.5	83) (2.	.68) (1.7	71) (1.51)	(1.88)	(1.46)	(1.18)
			Panel B: Re	eturns to Inves	tment Strateg	gies Sorted by R	isk Loading	s (Nondowng	grades)				
		F	Equal-Weighter	:d					V	alue-Weighte	d		
Return	CAPM	FFC	FFC+PS	FF5	FF6	SY	Return	CAPM	FFC	FFC+PS	FF5	FF6	SY
1.413***	1.444***	1.131***	1.141***	1.214***	1.041***	0.994***	0.915***	0.969***	0.652**	0.597**	0.696**	0.574*	0.511
(4.85)	(5.15)	(3.78)	(3.88)	(4.53)	(3.50)	(2.88)	(2.91)	(3.01)	(2.15)	(2.00)	(2.14)	(1.82)	(1.64)

As before, machine learning-based investment payoffs deteriorate in the presence of sensible economic restrictions (60%).

## Empirical Results – IPCA & CA

Pan	el A: Value-	Weighted Re	turns to Inves	tment Strateg	gies Sorted by	IPCA-Predic	ted Returns	
	Full	Sample	Nonm	icrocaps	Credit Ra	ting Sample	Nondo	wngrades
	Return	FF6	Return	FF6	Return	FF6	Return	FF6
	0.945***	0.624***	0.901***	0.613***	0.893***	0.607***	0.733***	0.430**
	(5.62)	(3.31)	(5.57)	(3.71)	(5.08)	(3.38)	(4.08)	(2.37)
Par	nel B: Value-	Weighted Re	turns to Inves	stment Strateg	gies Sorted by	CA2-Predict	ed Returns	
	Full	Sample	Nonm	icrocaps	Credit Rat	ing Sample	Nondov	vngrades
	Return	FF6	Return	FF6	Return	FF6	Return	FF6
	1.159***	0.746***	1.105***	0.387**	0.874***	0.187	0.665**	0.048
	(4.17)	(3.01)	(4.22)	(2.03)	(2.97)	(0.79)	(2.22)	(0.20)

Collectively, ML return patterns are concentrated in stocks that are relatively difficult to value and difficult to arbitrage.

Although IPCA underperforms for the full sample, it delivers consistent risk-adjusted performance even in the presence of economic restrictions.

All ML methods substantially improve the investment payoff compared to the traditional methods with and without economic restrictions.

	Sharpe Ratio	Skewness	Excess Kurtosis	Maximum Drawdown	Return in Crisis	Turnover	全样本	子样本
Panel A: Sorted by NN3-	Predicted Retur	rns					盈亏平衡	盈亏平衡
Full Sample	0.944	0.631	5.222	0.350	4.100	0.976	交易成本	交易成本
Nonmicrocaps	0.644	0.361	7.062	0.349	3.563	0.869		
Credit Rating Sample	0.639	0.064	7.875	0.420	3.435	0.889	0.94%	0.36%
Nondowngrades	0.449	0.146	8.550	0.333	2.931	0.920		
Panel B: Sorted by Risk l	Loadings							
Full Sample	1.225	1.063	5.932	0.209	0.472	1.664		
Nonmicrocaps	0.839	0.326	1.582	0.246	0.677	1.625	1.12%	0.34%
Credit Rating Sample	0.566	0.267	1.440	0.407	-0.023	1.652	1.12/0	0.54 /6
Nondowngrades	0.602	0.344	1.675	0.447	0.903	1.678		
Panel C: Sorted by IPCA	-Predicted Retu	ırns						
Full Sample	0.967	-0.449	4.805	0.203	0.574	1.186		
Nonmicrocaps	0.978	-0.267	5.369	0.234	1.493	1.130	0.53%	0.54%
Credit Rating Sample	0.880	-0.219	4.221	0.315	0.474	1.164		
Nondowngrades	0.697	-0.069	3.158	0.349	-0.640	1.184		
Panel D: Sorted by CA2-	Predicted Retur	rns						
Full Sample	0.784	-0.077	2.418	0.202	-0.047	1.565	0.48%	0.26%
Nonmicrocaps	0.748	0.291	4.684	0.207	-0.529	1.478	0.40%	0.20%
Credit Rating Sample	0.522	-0.471	4.119	0.252	-1.796	1.542		
Nondowngrades	0.387	-0.616	4.930	0.345	-0.167	1.571		
Panel E: Market Portfoli	0							
Full Sample	0.527	-0.978	3.323	0.486	-6.954	0.089		
Nonmicrocaps	0.530	-0.959	3.222	0.485	-6.907	0.086		
Credit Rating Sample	0.543	-0.932	3.423	0.498	-6.747	0.080		
Nondowngrades	0.682	-0.856	3.311	0.408	-6.615	0.084		

- Imposing economic restrictions significantly reduces the Sharpe ratio.
- ML methods are more positively skewed than the market portfolio.
- ML methods experience comparatively smaller drawdowns, are able to mitigate downside risk and protect investors from extreme crashes.
- Accounting for reasonable transaction costs would make it difficult for most ML signals to leave alpha on the table.

Similar to CPZ, the KNS approach incorporates a no-arbitrage condition to estimate the SDF, while focus on equity portfolios that represent characteristics-based trading strategies.

train: September 1964 to December 2004

test: January 2005 to December 2017

			Cha	racteristics	of SDF-Impl	ied MVE P	ortfolios							
	CAPM	FF6	Sharpe				SDF-	Implied M	VE Portfol	io Weights				
	CAPM	611	Ratio	Mean	Std.Dev.	Min	5%	10%	25%	Median	75%	90%	95%	Max
Full Sample	3.662***	3.338***	2.318	0.083	1.338	-2.994	-2.343	-1.994	-0.912	0.341	0.964	1.687	1.895	3.182
	(6.01)	(5.90)												
Nonmicrocaps	1.543***	0.895***	0.977	0.084	0.447	-0.863	-0.666	-0.592	-0.238	0.072	0.407	0.647	0.741	1.431
	(3.88)	(2.87)												
Credit Rating Sample	1.418***	0.717*	0.898	-0.006	0.254	-0.678	-0.473	-0.382	-0.137	-0.003	0.187	0.326	0.387	0.419
	(2.97)	(1.93)												
Nondowngrades	1.308***	0.545	0.828	-0.022	0.248	-0.543	-0.448	-0.370	-0.217	0.004	0.135	0.293	0.376	0.595
	(2.92)	(1.59)												

- We analyze the out-of-sample trading profits using predictive signals generated from five machine learning methods in subsamples with economic restrictions.
- IPCA underperforms deep learning models for the full sample but does not display a material deterioration of performance in subsamples with economic restrictions. Conversely, all other ML methods are opposite.
- As machine learning-based trading strategies require relatively high portfolio turnover, investors may need to further lower their expectations of achievable performance.

#### market state variables:

- (1) investor sentiment (SENT), defined as the monthly Baker and Wurgler (2007) investor sentiment;
- (2) realized market volatility(MKTVOL), defined as the standard deviation of daily CRSP VW index returns in a month;
- (3) implied market volatility (VIX), defined as the monthly VIX index of implied volatilities of S&P 500 index options
- (4) market illiquidity (MKTILLIQ), defined as the VW average of stock-level Amihud (2002) illiquidity for all stocks in a month

	Value	-Weighted FF	6-Adjusted Re	turns of Mac	hine Learning I	Portfolios		
	SE	NT	MKT	VOL	V	IX	MKTI	ILLIQ
	Low	High	Low	High	Low	High	Low	High
Panel A: Sorted by NI	N3-Predicted	l Returns						
Full Sample	0.732***	0.879**	0.641**	1.283***	0.218	1.662***	0.736***	1.075***
	(3.00)	(2.40)	(2.34)	(3.96)	(0.95)	(4.16)	(2.70)	(3.36)
Nonmicrocaps	0.334	0.095	0.062	0.814***	-0.050	0.747**	0.222	0.461
	(1.45)	(0.29)	(0.26)	(2.87)	(-0.20)	(2.03)	(0.84)	(1.51)
Credit Rating Sample	0.389	0.274	0.095	0.896***	0.025	0.808*	0.512**	0.351
	(1.49)	(0.91)	(0.44)	(2.93)	(0.11)	(1.96)	(1.97)	(1.15)
Nondowngrades	0.355	-0.161	0.054	0.597*	-0.060	0.582	0.294	0.120
	(1.43)	(-0.50)	(0.23)	(1.70)	(-0.24)	(1.25)	(1.21)	(0.36)
Panel B: Sorted by Ris	sk Loadings							
Full Sample	1.372***	2.453***	1.352***	2.364***	0.898**	2.451***	1.150***	2.128***
	(3.83)	(3.78)	(3.64)	(4.09)	(2.30)	(3.80)	(2.73)	(4.53)
Nonmicrocaps	0.512**	0.681	0.423	0.665	0.321	0.386	0.527	0.432*
	(2.14)	(1.60)	(1.41)	(1.62)	(1.14)	(1.01)	(1.45)	(1.76)
Credit Rating Sample	0.269	0.658	0.448	0.527	0.097	0.337	0.691	0.073
	(0.84)	(1.35)	(1.12)	(1.12)	(0.31)	(0.69)	(1.63)	(0.20)
Nondowngrades	0.329	0.945*	0.453	0.699	0.031	0.651	0.847*	0.155
	(0.93)	(1.79)	(0.96)	(1.45)	(0.09)	(1.19)	(1.86)	(0.39)

	Value-Weighted FF6-Adjusted Returns of Machine Learning Portfolios									
	SE	NT	MKT	VOL	VI	X	MKTI	LLIQ		
	Low	High	Low	High	Low	High	Low	High		
Panel C: Sorted by IP	CA-Predicte	d Returns								
Full Sample	0.558**	0.667**	0.590***	0.694**	0.440**	0.763**	0.603**	0.645***		
	(2.46)	(2.03)	(3.57)	(2.56)	(2.60)	(2.23)	(2.39)	(2.78)		
Nonmicrocaps	0.606***	0.615**	0.566***	0.636**	0.478***	0.647**	0.759***	0.463**		
	(3.06)	(2.15)	(3.28)	(2.59)	(2.98)	(2.25)	(3.34)	(2.23)		
Credit Rating Sample	0.647***	0.512*	0.533***	0.653**	0.498**	0.649**	0.782***	0.447*		
	(2.82)	(1.66)	(2.97)	(2.51)	(2.56)	(2.14)	(3.18)	(1.96)		
Nondowngrades	0.535**	0.326	0.378**	0.451	0.478**	0.325	0.583**	0.292		
	(2.37)	(1.10)	(2.04)	(1.60)	(2.23)	(0.96)	(2.22)	(1.26)		
Panel D: Sorted by CA	A2-Predicted	Returns								
Full Sample	0.748***	0.617	0.634**	0.606	0.453*	0.910**	0.359	0.787**		
	(2.70)	(1.41)	(2.34)	(1.61)	(1.75)	(2.04)	(1.51)	(2.14)		
Nonmicrocaps	0.584**	0.064	0.537**	0.254	0.524**	0.122	0.292	0.275		
	(2.55)	(0.21)	(2.13)	(0.79)	(2.28)	(0.33)	(1.13)	(1.03)		
Credit Rating Sample	0.304	-0.055	0.531	-0.074	0.508*	-0.300	-0.102	0.263		
	(1.15)	(-0.15)	(1.49)	(-0.19)	(1.69)	(-0.67)	(-0.30)	(0.81)		
Nondowngrades	0.204	-0.218	0.376	-0.170	0.193	-0.248	-0.331	0.245		
	(0.73)	(-0.54)	(1.30)	(-0.45)	(0.73)	(-0.54)	(-0.89)	(0.84)		

$$\begin{split} HML_t &= \alpha_0 + \beta_1 High \, SENT_{t-1} + \beta_2 High \, MKTVOL_{t-1} + \beta_3 High \, MKTILLIQ_{t-1} \\ &+ \beta_4 M_{t-1} + c_1' F_t + c_2' F_t \times High \, SENT_{t-1} + c_3' F_t \times High \, MKTVOL_{t-1} \\ &+ c_4' F_t \times High \, MKTILLIQ_{t-1} + e_t \end{split}$$

Sorted by NN3-Predicted Return	Sorted	NN3-Pred	licted Returns
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	Model 1	Model 2	Model 3	Model 4	Model 5	Model 6
Constant	0.016	-0.453	0.865	1.252	1.491**	1.666*
	(0.03)	(-0.92)	(1.14)	(1.42)	(2.01)	(1.93)
High SENT	1.534**	1.710**	0.228	-0.005	-0.179	-0.257
	(2.43)	(2.51)	(0.58)	(-0.01)	(-0.37)	(-0.45)
High MKTVOL	0.791		0.959*		0.660	
	(1.24)		(1.93)		(1.23)	
High VIX		1.851***		1.647***		1.419**
		(2.85)		(3.28)		(2.57)
High MKTILLIQ	0.754	0.529	0.592	0.695	0.671	0.392
	(1.24)	(0.78)	(1.37)	(1.41)	(1.43)	(0.77)
DOWN			-0.691*	-0.803*	-0.311	-0.297
			(-1.71)	(-1.74)	(-0.77)	(-0.64)
TERM			-0.146	-0.194	-0.161	-0.154
			(-0.80)	(-0.95)	(-0.97)	(-0.81)
DEF			-0.245	-0.732	-0.795	-1.221*
			(-0.33)	(-0.94)	(-1.27)	(-1.78)

#### Empirical Results - Return Predictability in Recent Years

Whether ML techniques have remained meaningful in recent years?

Panel A: Valu	Panel A: Value-Weighted Returns to Investment Strategies Sorted by NN3-Predicted Returns								
	Return	CAPM	FFC	FFC+PS	FF5	FF6	SY		
Full Sample	1.568***	2.012***	1.559***	1.555***	1.096***	1.181***	0.699**		
	(3.07)	(4.63)	(5.01)	(5.20)	(3.95)	(4.32)	(2.27)		
Nonmicrocaps	1.106**	1.583***	1.128***	1.116***	0.592**	0.687***	0.276		
	(2.27)	(3.97)	(4.23)	(4.28)	(2.19)	(2.88)	(0.93)		
Credit Rating Sample	1.182**	1.635***	1.167***	1.165***	0.700**	0.803***	0.288		
	(2.37)	(4.22)	(4.14)	(4.04)	(2.36)	(3.14)	(0.87)		
Nondowngrades	0.796*	1.188***	0.747***	0.768***	0.454	0.545*	-0.037		
	(1.82)	(3.15)	(2.65)	(2.67)	(1.58)	(1.90)	(-0.11)		

 Unlike individual anomalies, ML signals continue to predict crosssectional stock returns in recent years for the full sample. On the other hand, anomalous return patterns are still confined within difficult-to-arbitrage stocks, and thus, practitioners should remain cautious in utilizing machine learning algorithms for real-time trading.

#### Empirical Results - Economic Foundations of ML

- Whether stocks with similar machine learning signals also share other characteristics that predict future returns?
- ➤ Compute the EW average of a comprehensive set of stock characteristics at the end of month for each portfolio.
- Despite their opaque nature, ML techniques successfully identify mispriced stocks with solid economic foundations

Stock Characteristics	Sort	ed by NN3	-Predicted Ret	urns
Stock Characteristics	Low	High	HML	t-stat
Log (Price)	2.092	1.386	-0.706***	(-14.63)
Log (Size)	5.483	3.613	-1.870***	(-25.33)
Book-to-Market	0.780	1.391	0.612***	(10.62)
Log (Illiquidity)	1.220	3.791	2.571***	(22.70)
Beta	1.330	1.068	-0.263***	(-6.87)
1M Return	0.027	-0.012	-0.039***	(-10.22)
12M Momentum	-0.124	0.185	0.309***	(15.64)
ldioVol	0.076	0.084	0.008***	(4.19)
Absolute Accruals	0.103	0.107	0.003	(1.08)
Log (Age)	2.171	2.463	0.292***	(9.93)
Assets Growth	0.586	0.014	-0.572***	(-11.76)
ΔShares Outstanding	0.389	0.070	-0.319***	(-10.92)
Corporate Investment	-0.107	0.022	0.129***	(9.03)
Dividend-to-Price	0.012	0.009	-0.003***	(-3.61)
Gross Profitability	0.329	0.354	0.025	(1.57)
Leverage	1.308	1.832	0.524***	(4.18)
ROA	-0.024	-0.011	0.013***	(5.41)
ROE	-0.045	-0.017	0.028***	(5.87)
%Rated	0.236	0.093	-0.142***	(-13.48)
Credit Rating	11.350	12.047	0.697**	(2.44)
Analyst Coverage	4.142	1.432	-2.710***	(-14.99)
Analyst Dispersion	0.049	0.057	0.008	(0.68)
SUE	-0.019	-0.009	0.010***	(3.17)

#### Conclusion

- ML techniques face the usual challenge of cross-sectional return predictability. In particular, the anomalous return patterns concentrate in difficult-to-value and difficult-to-arbitrage stocks.
- The trading strategy is more profitable during periods of high market volatility and low market liquidity.
- ML signals also involve remarkably high turnover.
- Beyond economic restrictions, ML-based trading strategies nonetheless display smaller downside risk, yield considerable profit in the long positions, and remain viable in the post-2001 period and the crisis period.
- Black-box-like machine learning methods generate economically interpretable trading strategies.