

6G Upper Midband Technology- Near-field Communication

EEEE.789

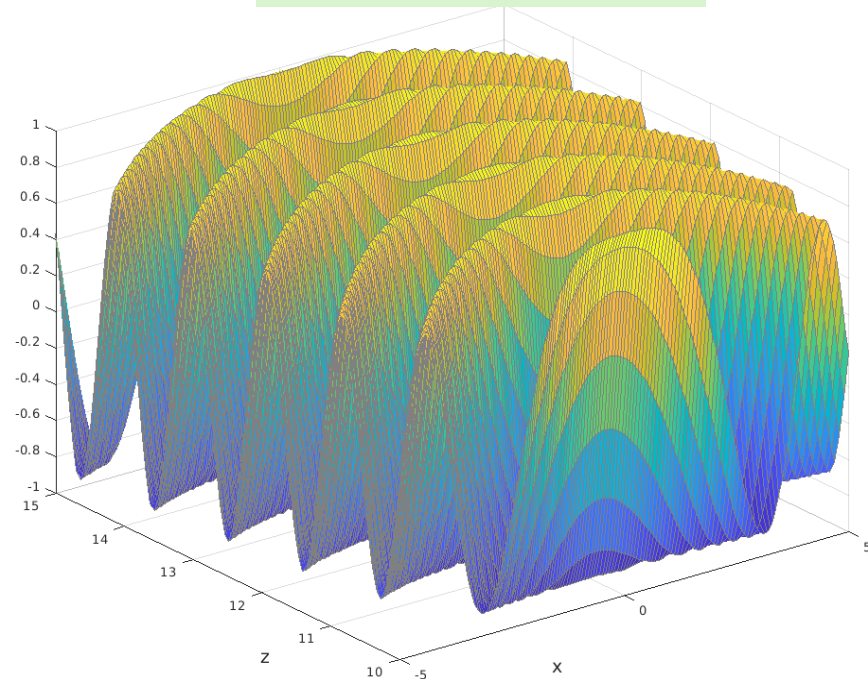
Shima Mashhadi

Jan 2025

Nearfield of the Antenna Array

- Fresnel region is characterized by the fact that the amplitude variations can be neglected, but not the phase variations.

Curved wavefront

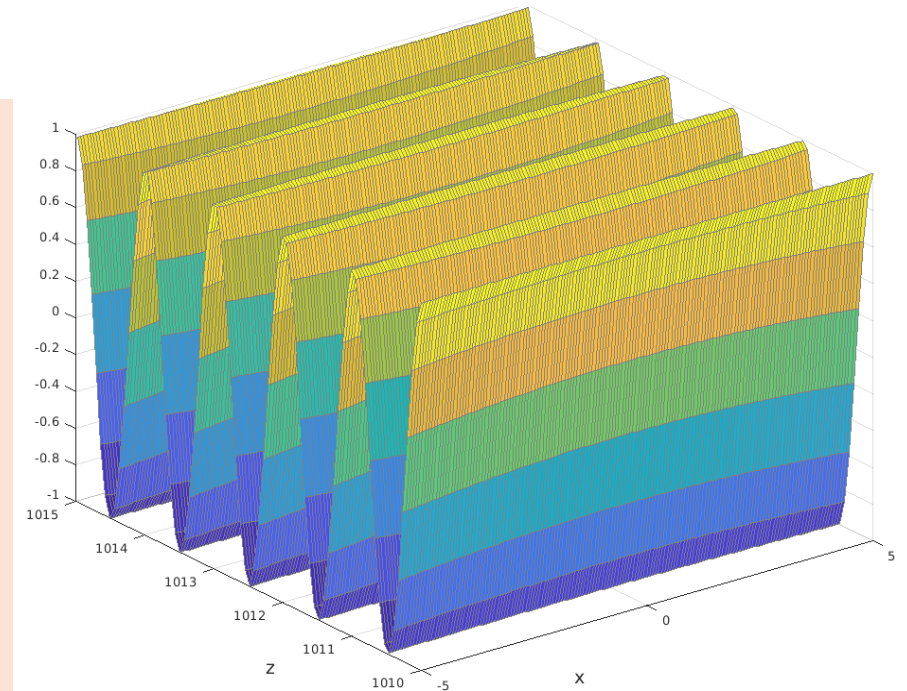


$$d_B < r < d_F$$

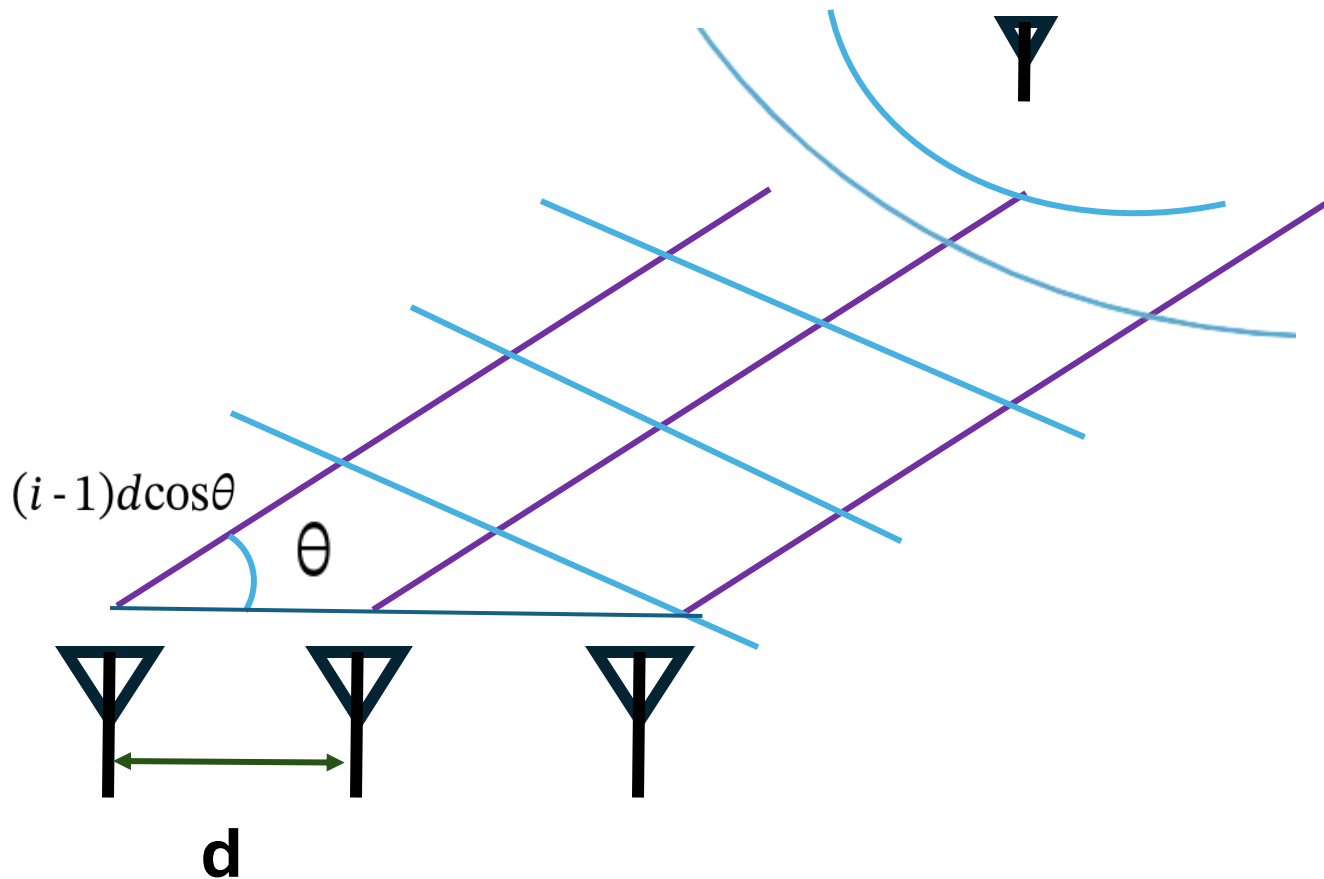
Example : Fraunhofer distance

0.5×0.5, 3 GHz = 10 m
1×1 m, 15 GHz = 200m
1×1 m, 30 GHz = 400 m

Planar wavefront



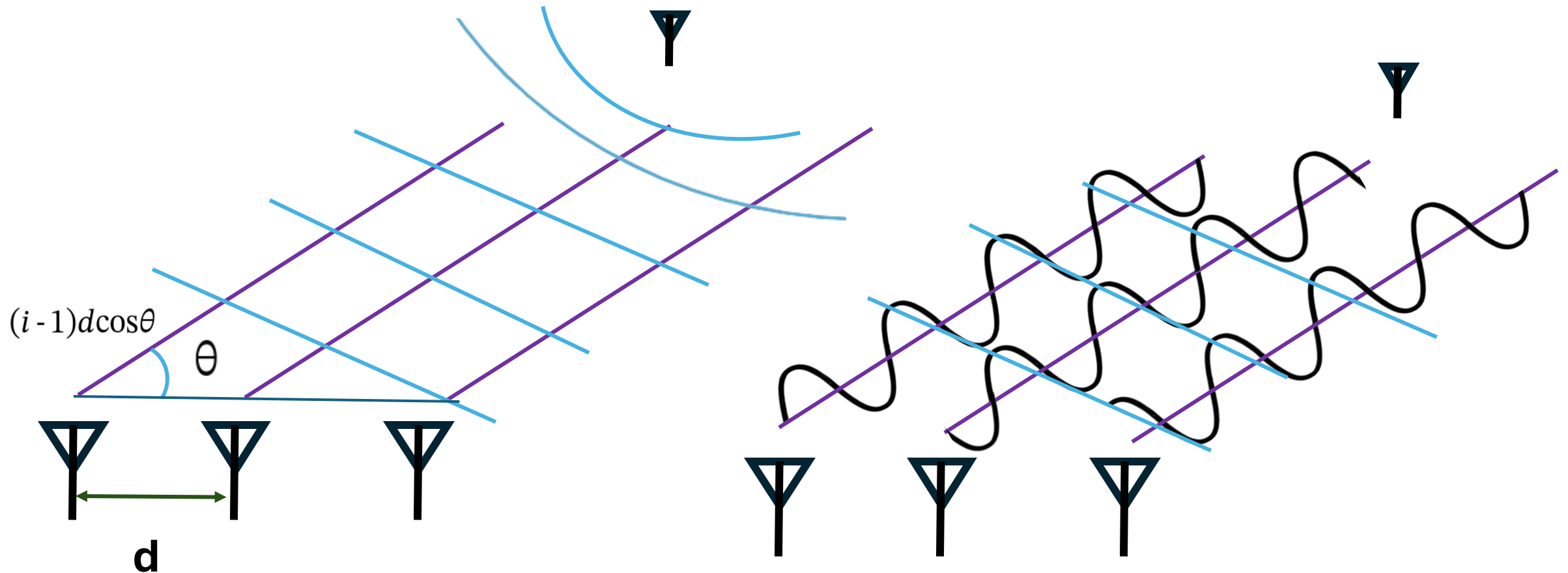
What is Beamforming ?



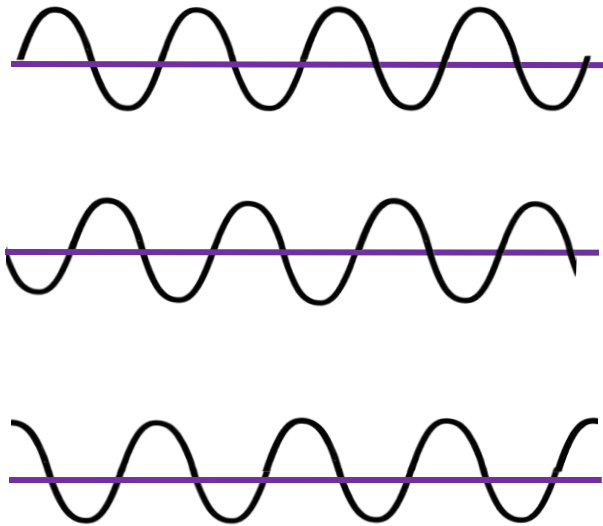
- Considering a simple SIMO
- Transmitter in the far-field

$$h_i = \frac{\lambda\sqrt{G}}{4\pi r} e^{-\left(j\frac{2\pi}{\lambda}(r - (i-1)d\cos\theta)\right)}$$

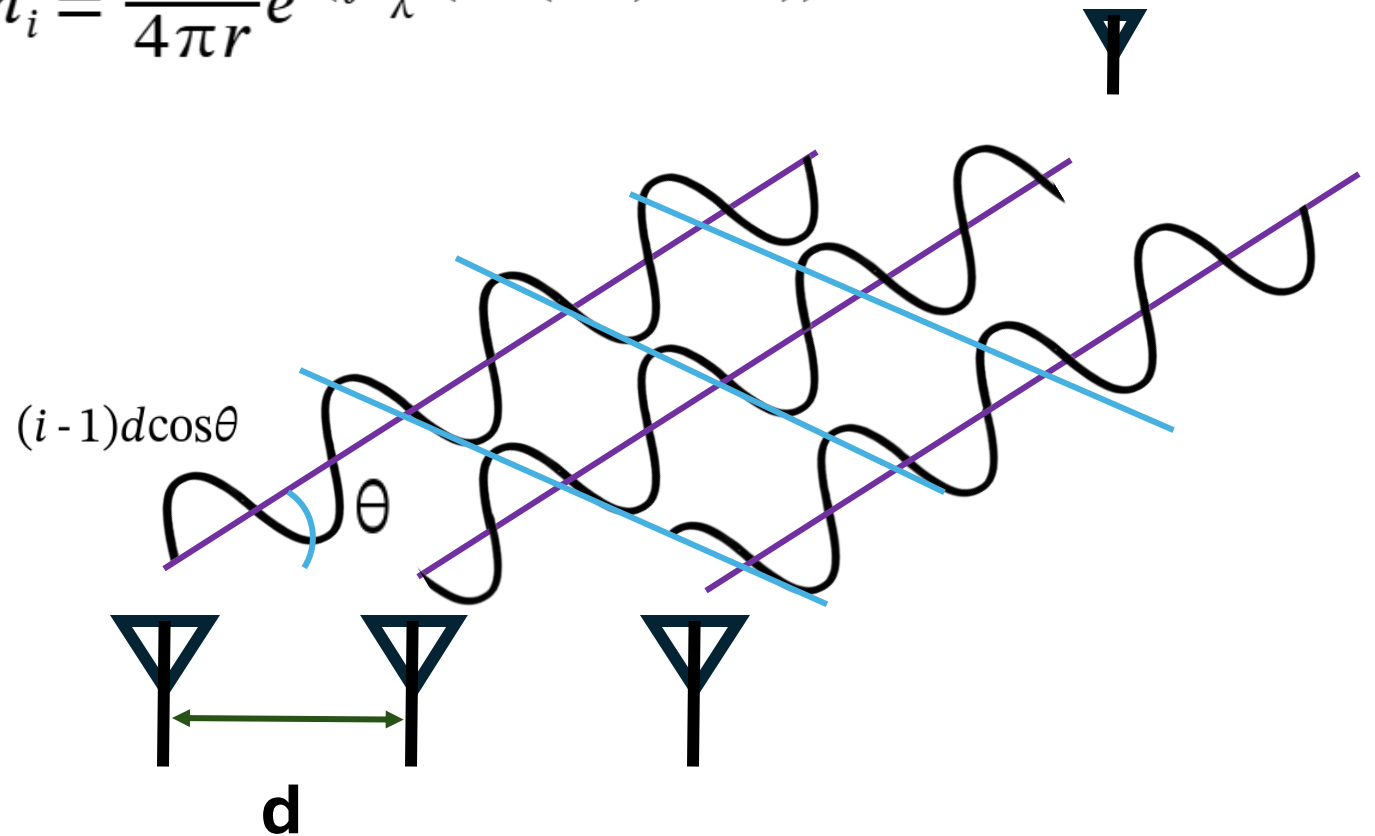
What is Beam Forming ?



What is Beam Forming ?

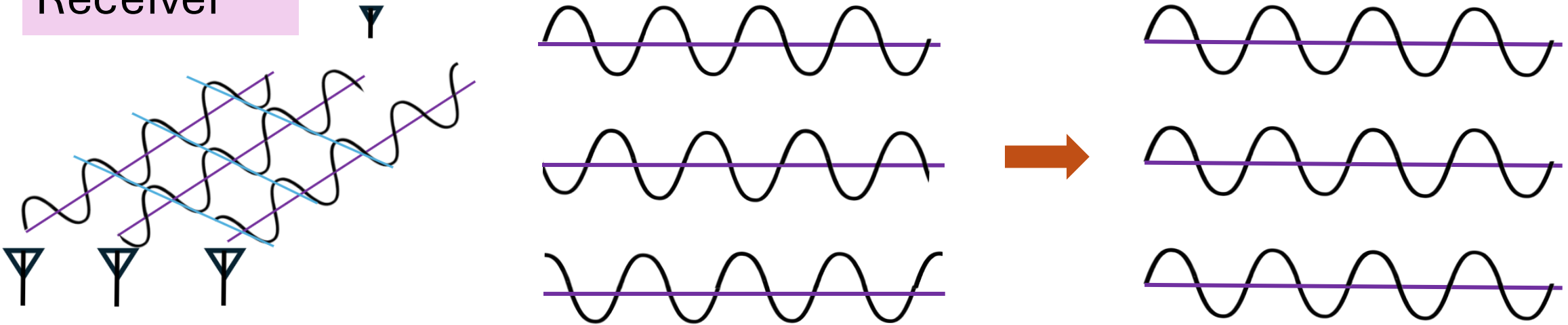


$$h_i = \frac{\lambda\sqrt{G}}{4\pi r} e^{-\left(j\frac{2\pi}{\lambda}(r + (i-1)d\cos\theta)\right)}$$



What is Beam Forming ?

Receiver



$$h_i = \frac{\lambda \sqrt{G}}{4\pi r} e^{-j \frac{2\pi}{\lambda} (r + (i-1)d \cos \theta)} \times e^{j \frac{2\pi}{\lambda} (i-1)d \cos \theta} \quad r = \sum_{i=1}^N h_i e^{j \varphi_i} s + w$$

The received signal become M times larger

Achievable in LOS

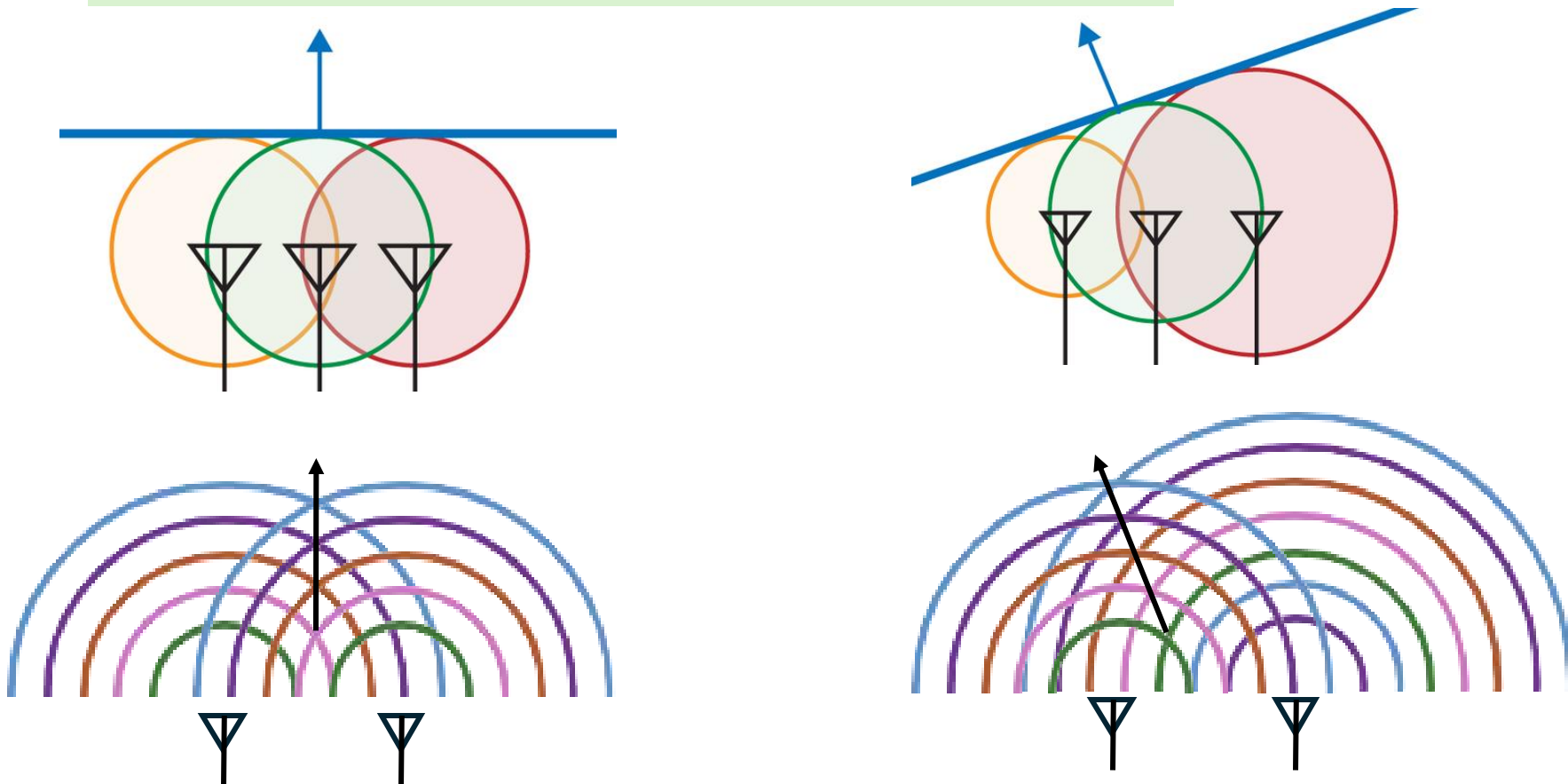
What is Beam Forming ?

Transmitter

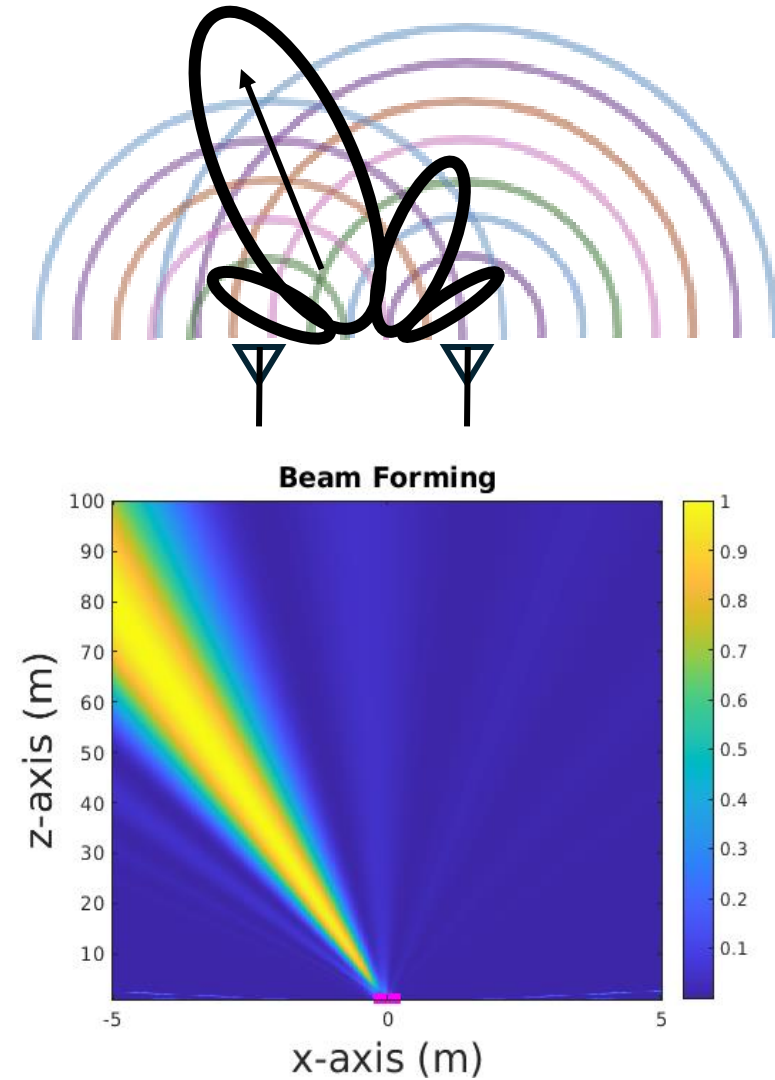
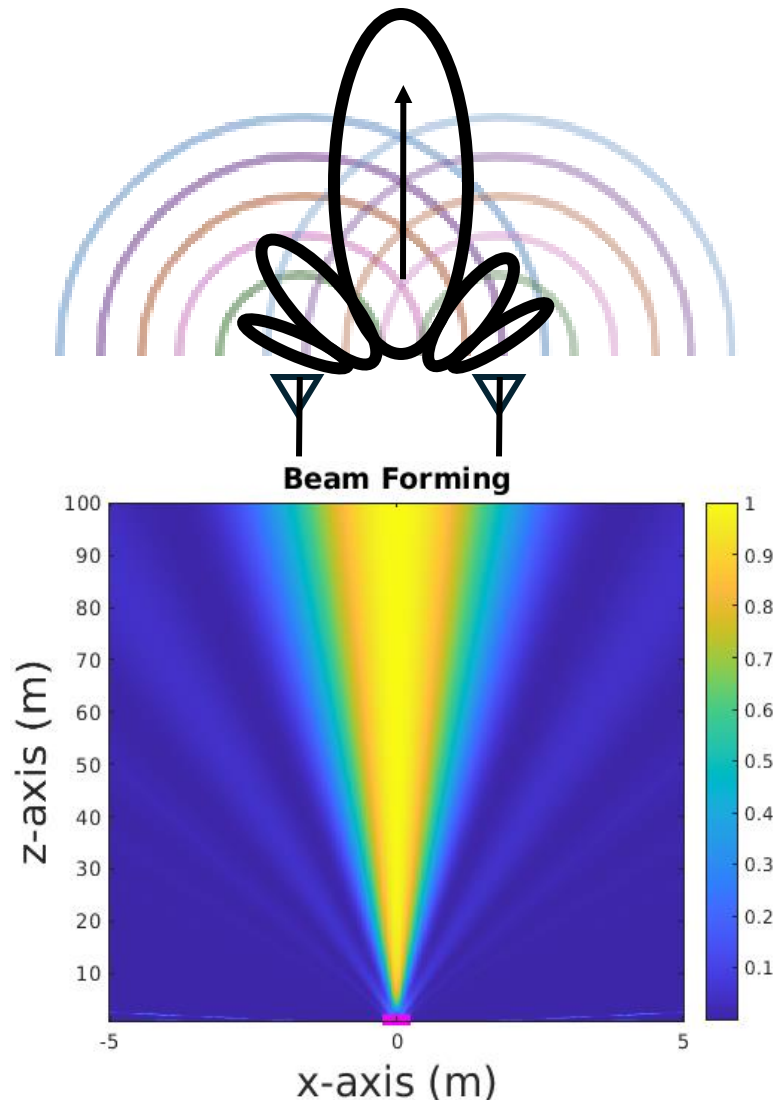
Antennas transmit the signal with the **phase-shift**

Send the radio energy preferentially in one direction

<https://www.oreilly.com/library/view/80211ac-a-survival/9781449357702/ch04.html>

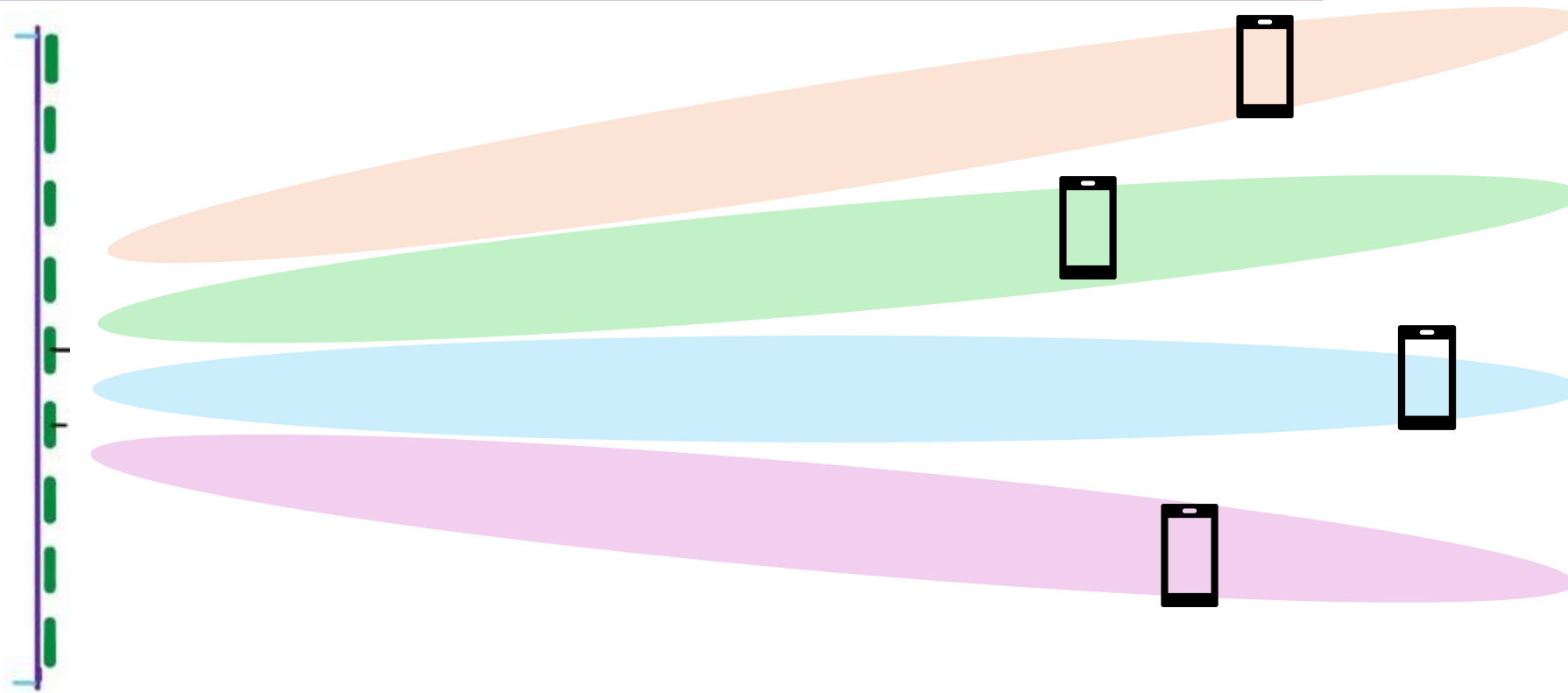


What is Beam Forming ?



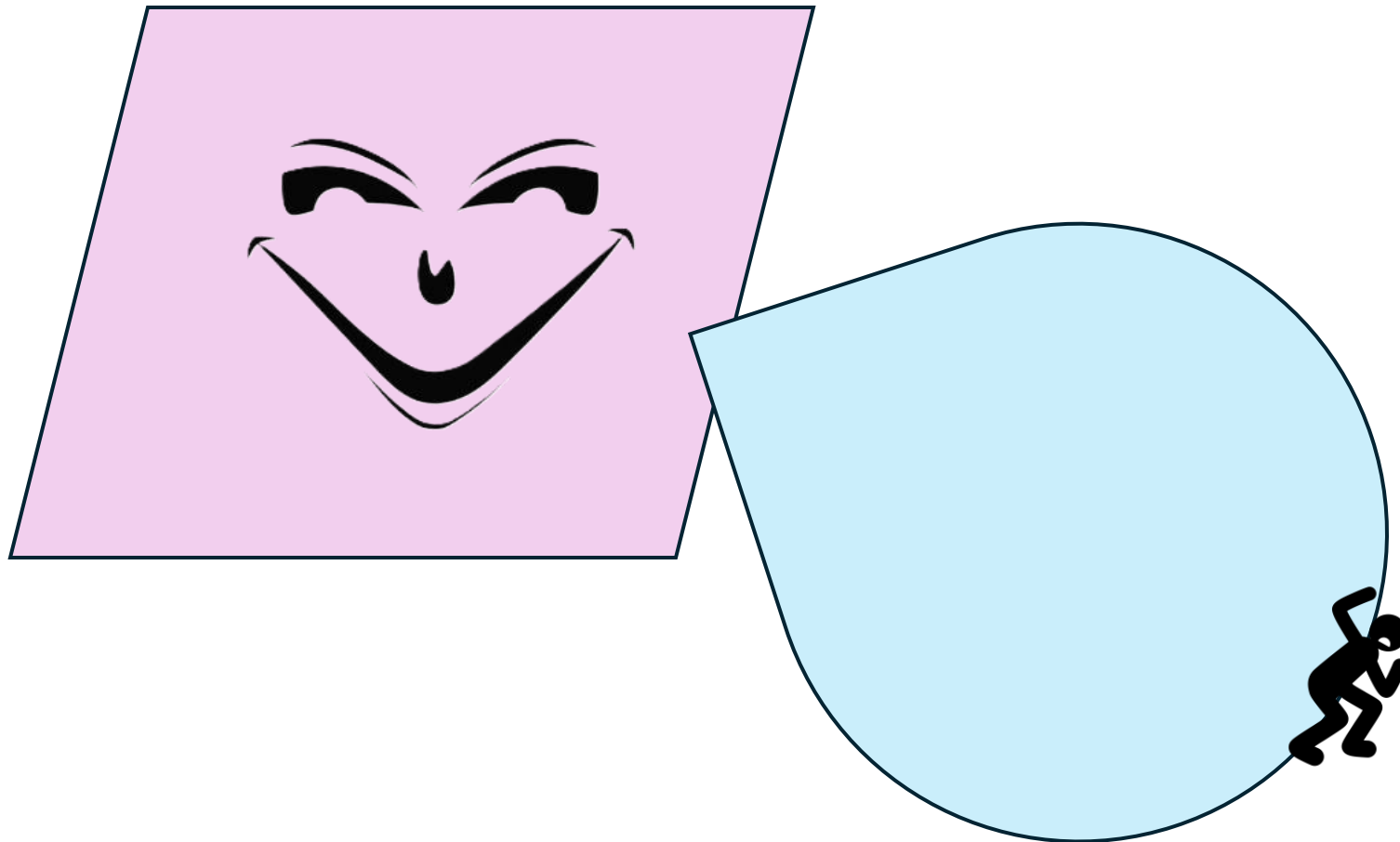
What is Beam Forming ?

What is the best thing we can do in the far-field?



Multi-user MIMO (MU-MIMO)

Beampattern in the Near-Field

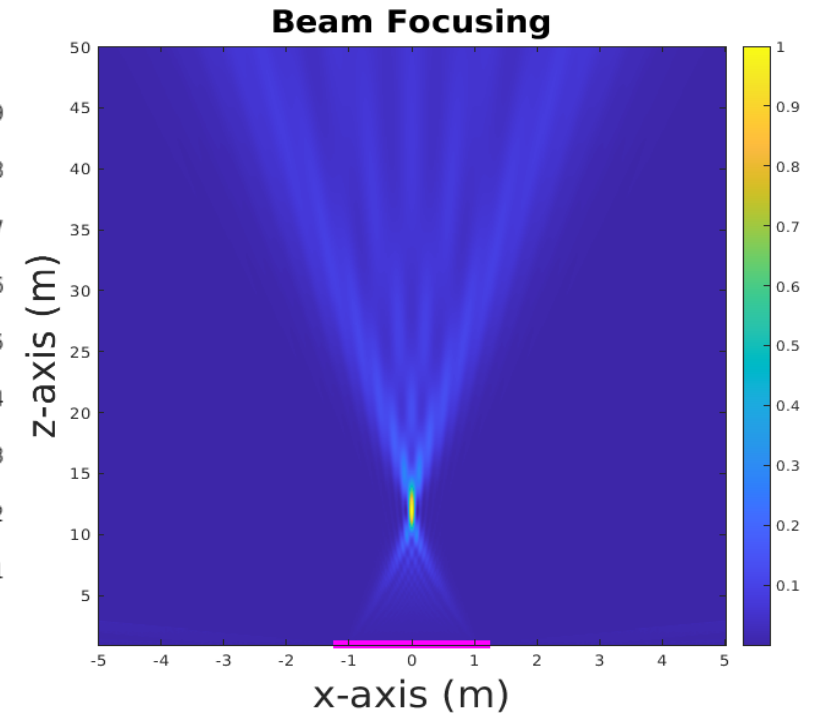
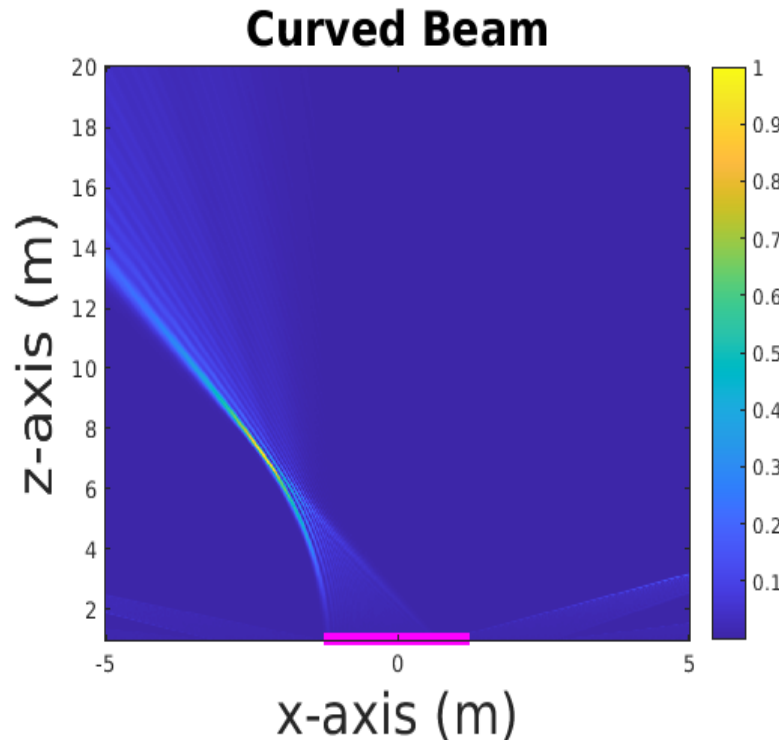
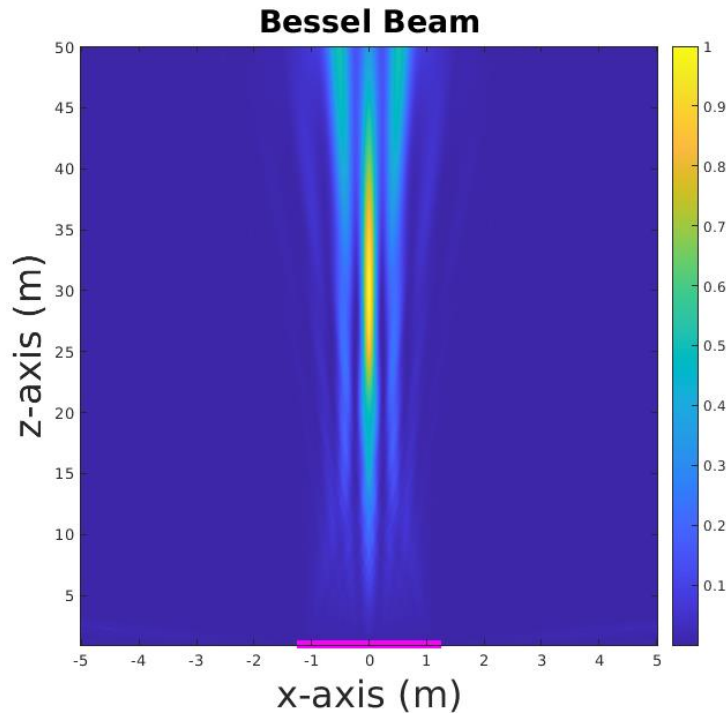


How about the shape of the beam in the Near-field?

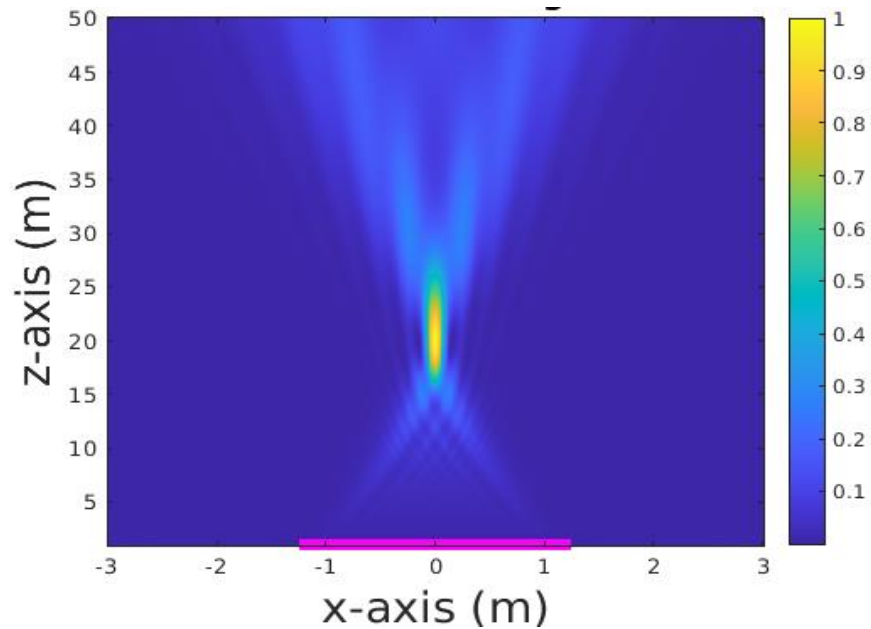
Near-field Beampatterns

- What happens if the user is located in the Fresnel region?

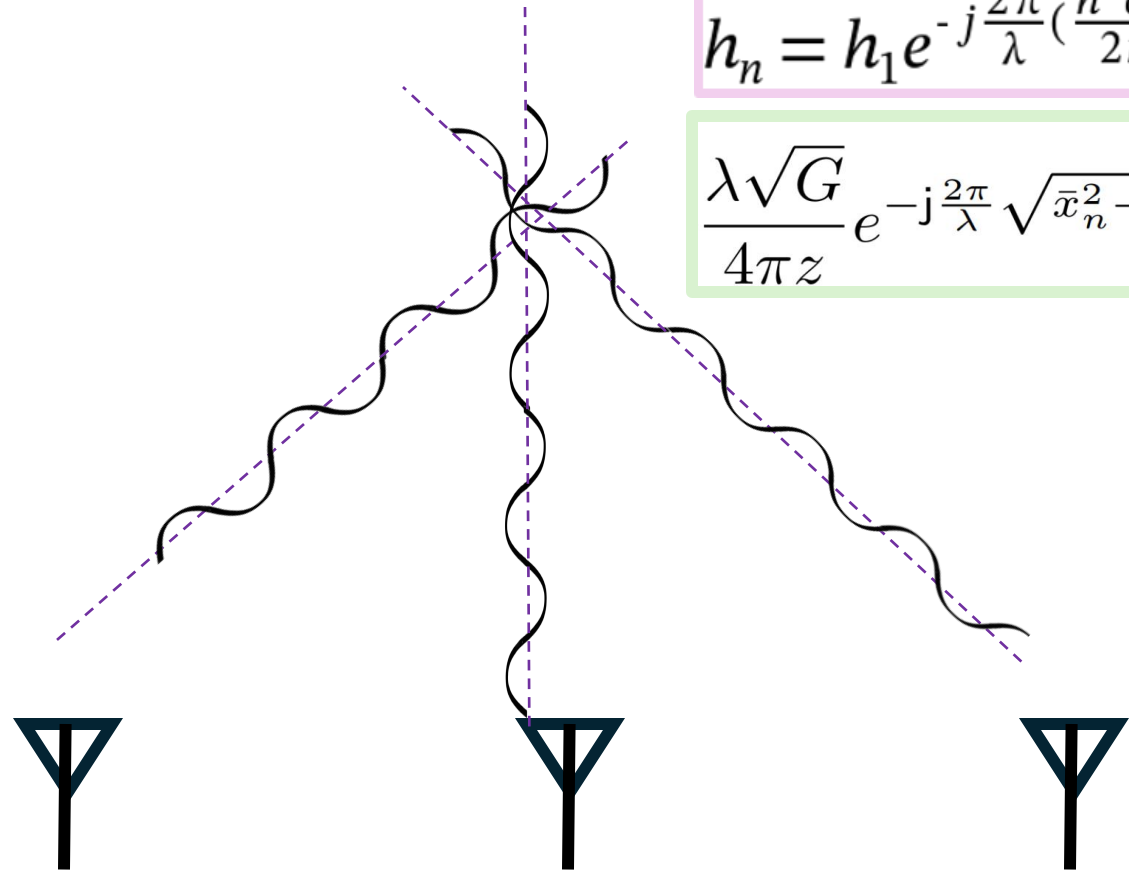
$$d_B < r < d_F$$



Beam Focusing



$M = 250$
 $F = 20 \text{ m}$



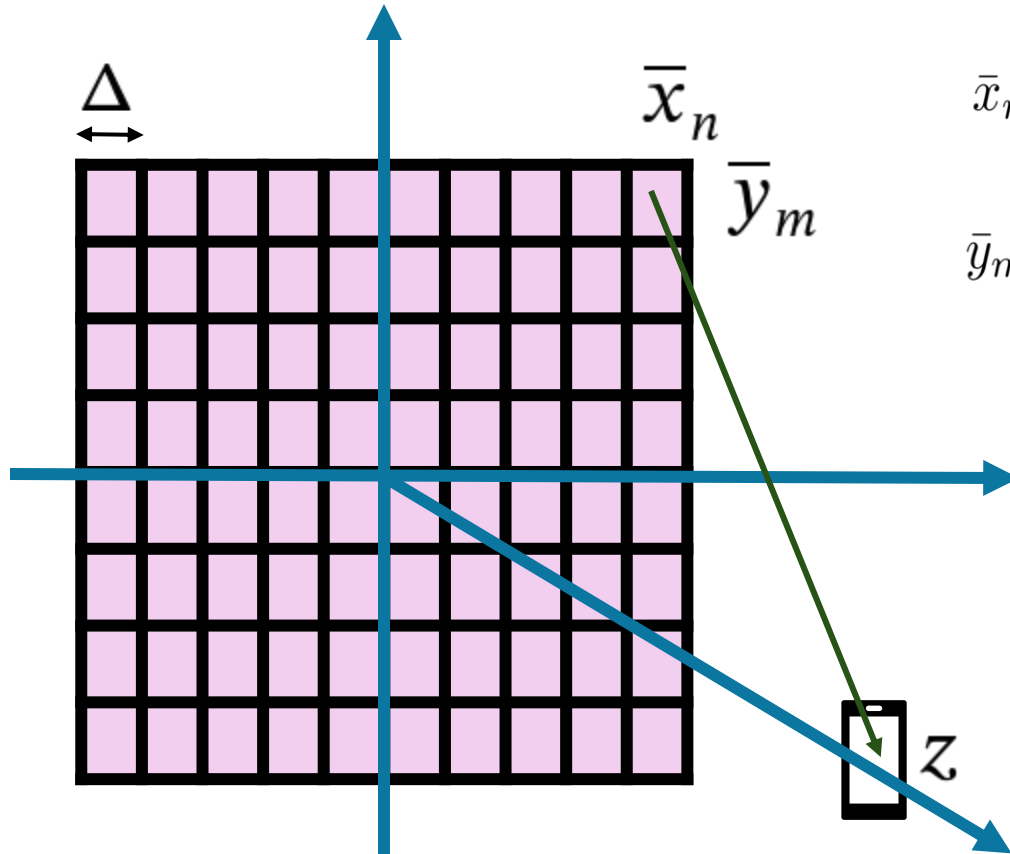
$$h_n = h_1 e^{-j \frac{2\pi}{\lambda} \left(\frac{n^2 d^2}{2r} - n d \cos \theta \right)}$$

$$\frac{\lambda \sqrt{G}}{4\pi z} e^{-j \frac{2\pi}{\lambda} \sqrt{\bar{x}_n^2 + \bar{y}_m^2 + z^2}}$$

The gain is the same in the Far-Field and Near-Field

Beam Focusing in the Near-Field

- A uniform squared array with \mathbf{M} antenna $N = \sqrt{M}$



$$\bar{x}_n = \left(n - \frac{N+1}{2} \right) \Delta,$$

$$\bar{y}_m = \left(m - \frac{N+1}{2} \right) \Delta.$$

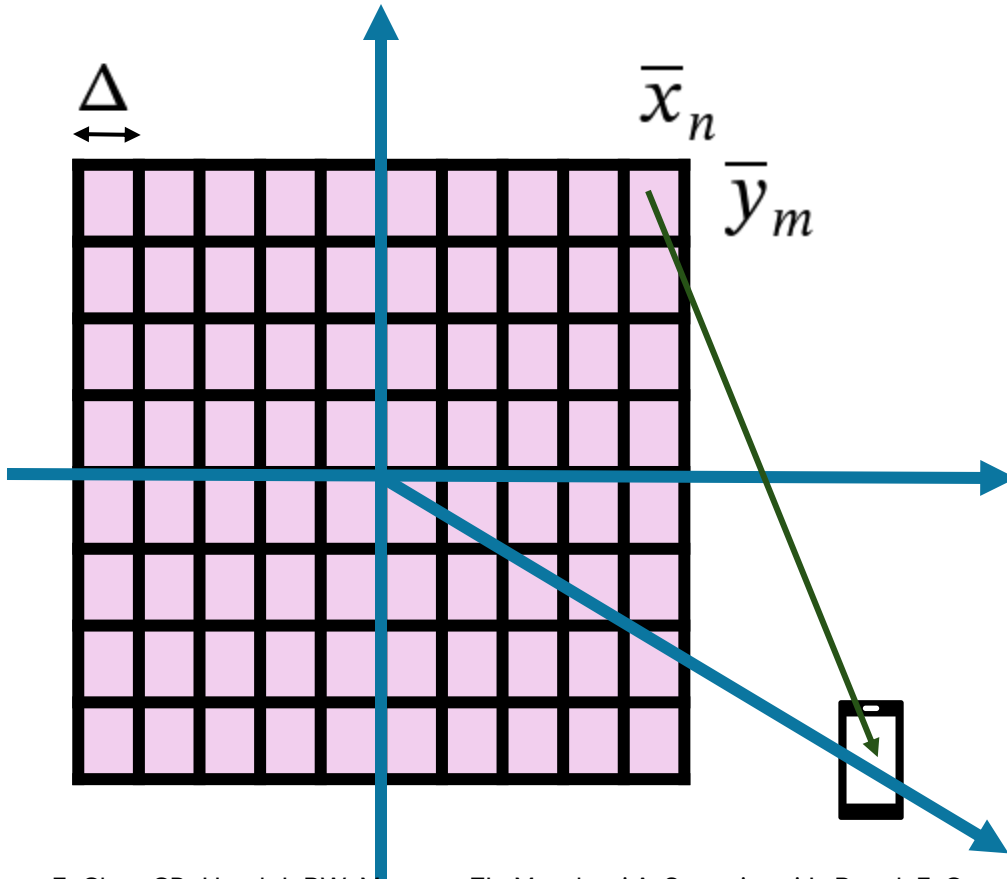
$$h_{n,m} = \frac{\lambda \sqrt{G}}{4\pi z} e^{-j \frac{2\pi}{\lambda} \sqrt{\bar{x}_n^2 + \bar{y}_m^2 + z^2}}$$

$$\approx \frac{\lambda \sqrt{G}}{4\pi z} e^{-j \frac{2\pi}{\lambda} \left(z + \frac{\bar{x}_n^2}{2z} + \frac{\bar{y}_m^2}{2z} \right)},$$

- Taylor approximation

Beam Focusing in the Near-field

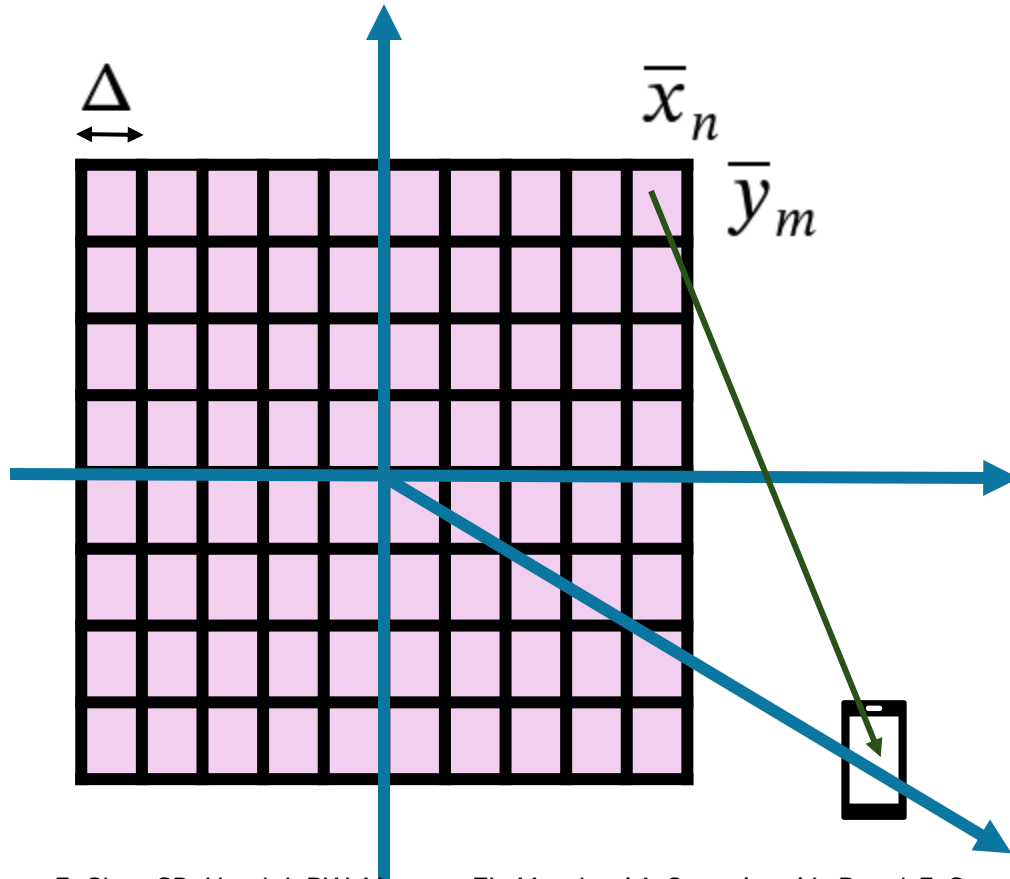
- A uniform squared array with **M** antenna



$$r = \sum_{n=1}^N \sum_{m=1}^N h_{n,m} \frac{e^{j\psi_{n,m}}}{\sqrt{M}} s + w_{n,m},$$

Beam Focusing in the Near-field

- A uniform squared array with **M** antenna



$$r = \sum_{n=1}^N \sum_{m=1}^N h_{n,m} \frac{e^{j\psi_{n,m}}}{\sqrt{M}} s + w_{n,m},$$

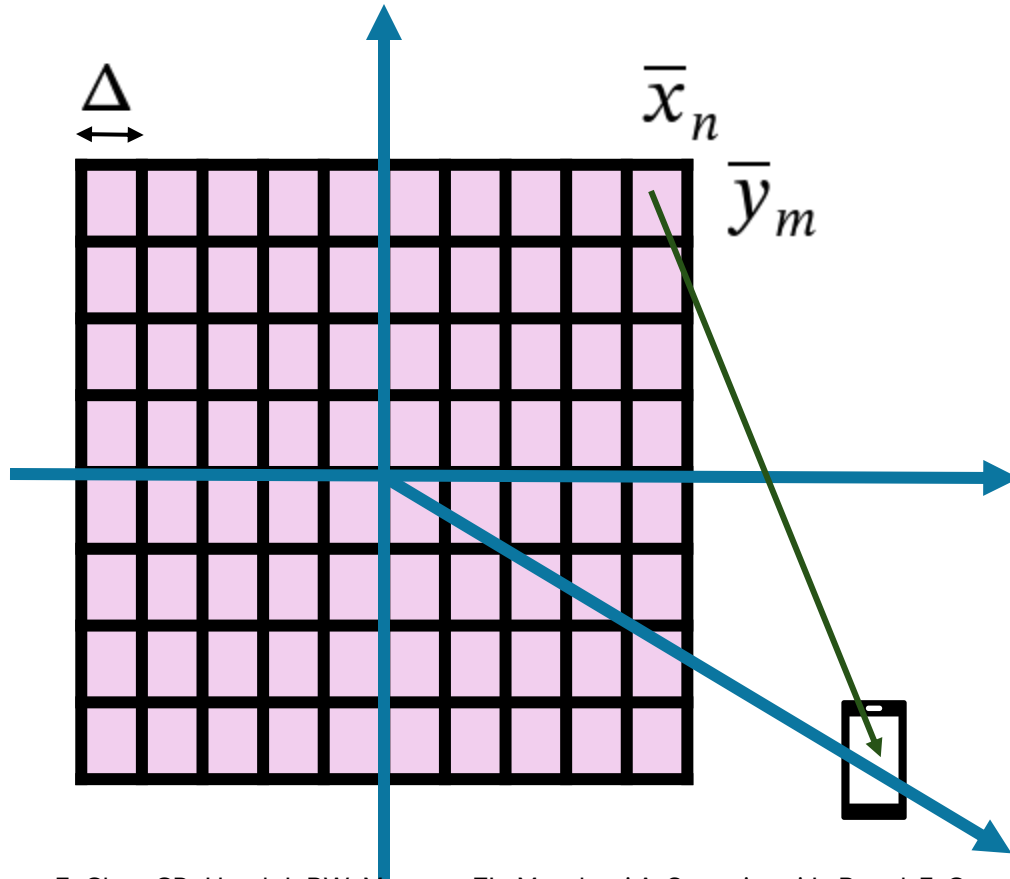
$$\text{SNR} = \frac{p}{\sigma^2} \left| \sum_{n=1}^N \sum_{m=1}^N h_{n,m} \frac{e^{j\psi_{n,m}}}{\sqrt{M}} \right|^2$$

Array Gain

$$= \frac{p}{\sigma^2} \frac{\lambda^2 G}{(4\pi z)^2} \frac{1}{M} \underbrace{\left| \sum_{n=1}^N \sum_{m=1}^N e^{-j\frac{2\pi}{\lambda} \sqrt{\bar{x}_n^2 + \bar{y}_m^2 + z^2}} e^{j\psi_{n,m}} \right|^2}_{=AG},$$

Beam Focusing in the Near-field

- A uniform squared array with **M** antenna

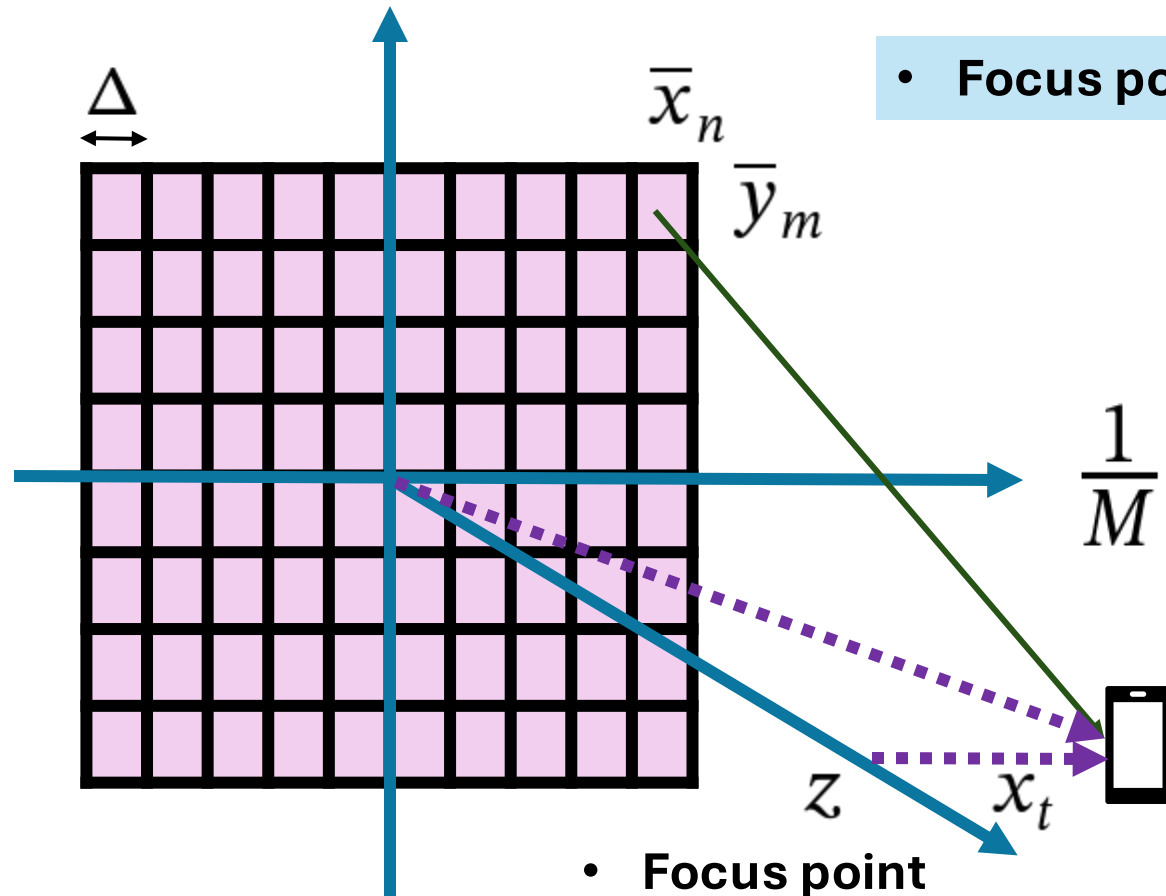


$$\text{SNR} = \frac{p}{\sigma^2} \left| \sum_{n=1}^N \sum_{m=1}^N h_{n,m} \frac{e^{j\psi_{n,m}}}{\sqrt{M}} \right|^2 \quad \text{Array Gain}$$

$$= \frac{p}{\sigma^2} \frac{\lambda^2 G}{(4\pi z)^2} \frac{1}{M} \underbrace{\left| \sum_{n=1}^N \sum_{m=1}^N e^{-j\frac{2\pi}{\lambda} \sqrt{\bar{x}_n^2 + \bar{y}_m^2 + z^2}} e^{j\psi_{n,m}} \right|^2}_{=\text{AG}},$$

$$\psi_{n,m} = \frac{2\pi}{\lambda} \sqrt{\bar{x}_n^2 + \bar{y}_m^2 + z^2}$$

Beamwidth in the nearfield



- Focus point

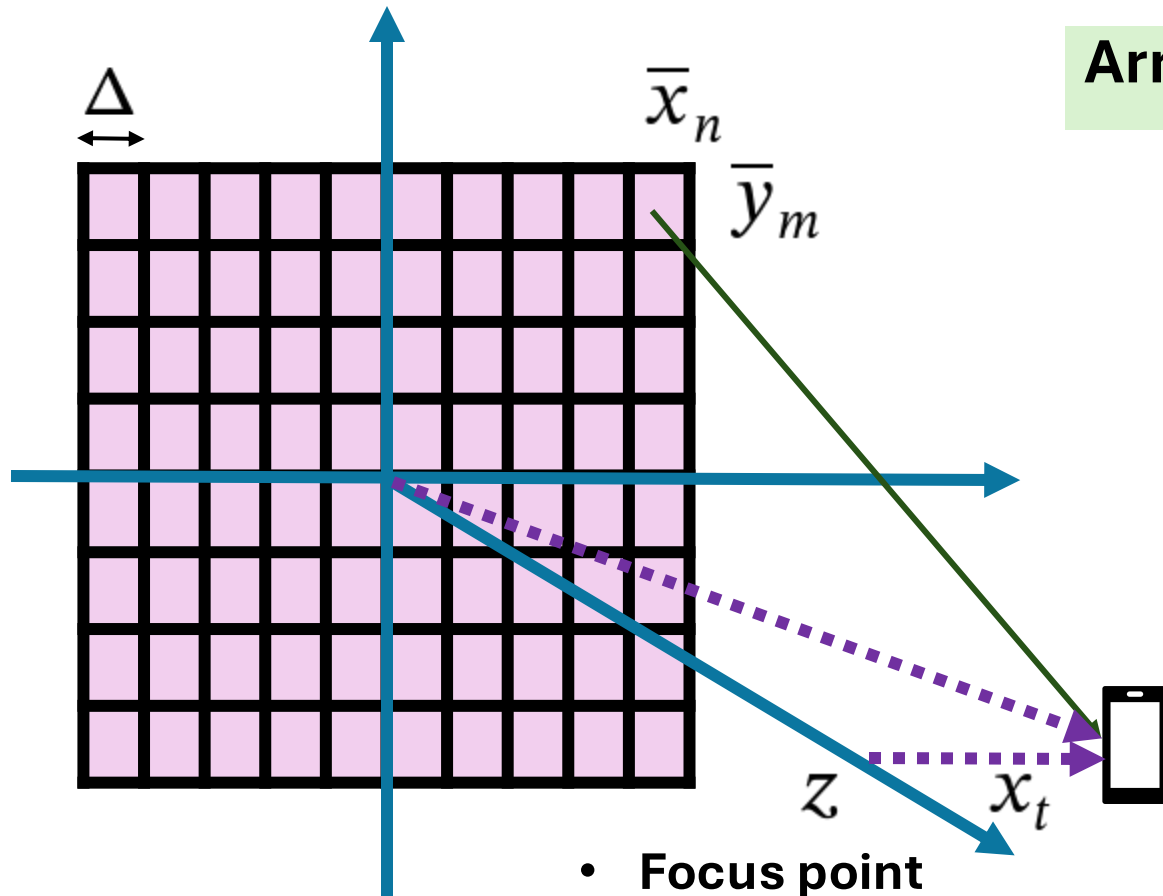
$$\psi_{n,m} = \frac{2\pi}{\lambda} \sqrt{\bar{x}_n^2 + \bar{y}_m^2 + z^2}$$

Array Gain

$$\frac{1}{M} \left| \sum_{n=1}^N \sum_{m=1}^N e^{-j \frac{2\pi}{\lambda} \sqrt{(\bar{x}_n - x_t)^2 + \bar{y}_m^2 + z^2}} e^{j \frac{2\pi}{\lambda} \sqrt{\bar{x}_n^2 + \bar{y}_m^2 + z^2}} \right|^2$$

- Focus point

Beamwidth in the nearfield



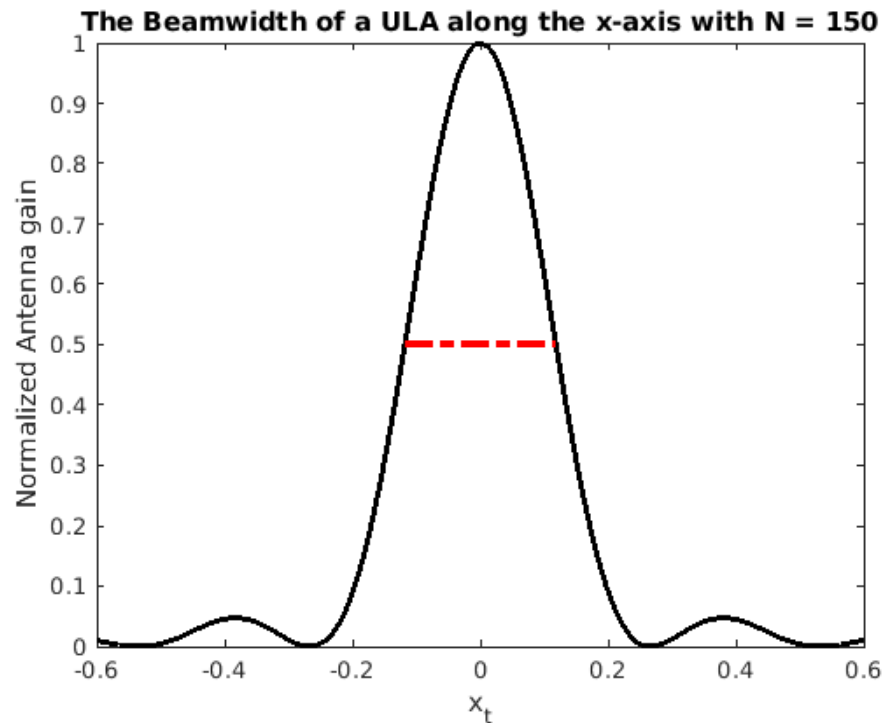
Array Gain

$$M \operatorname{sinc}^2\left(\frac{1}{\lambda} N \Delta \frac{x_t}{z}\right)$$

$$\operatorname{sinc}^2(0.443) \approx 0.5,$$

$$BW_{3dB} \approx \frac{0.886 \lambda F}{N \Delta}$$

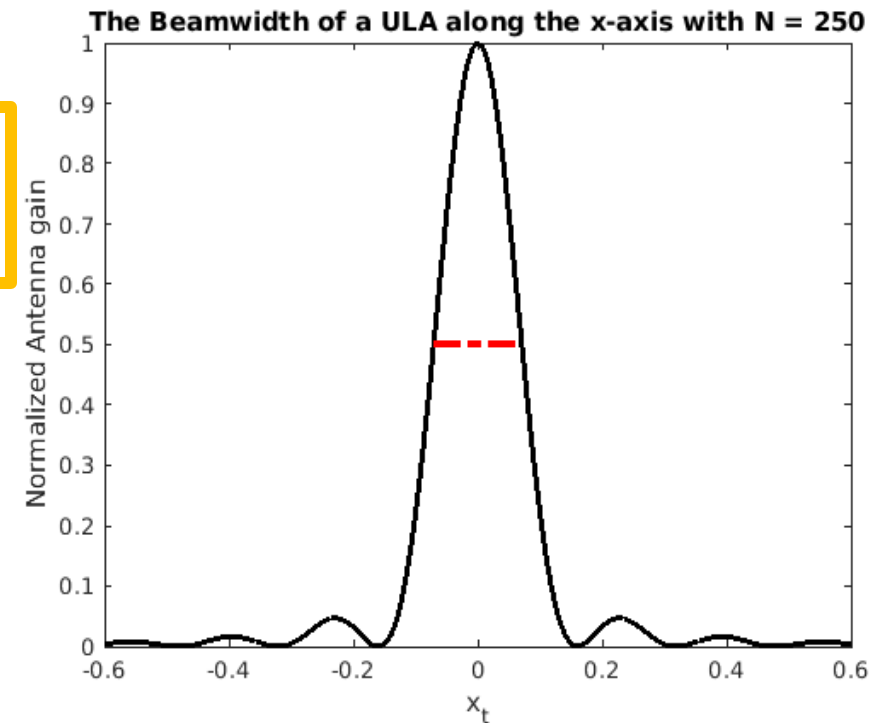
Beamwidth in the Near-field



M = 150
F = 20 m
BW3dB = 0.236 m

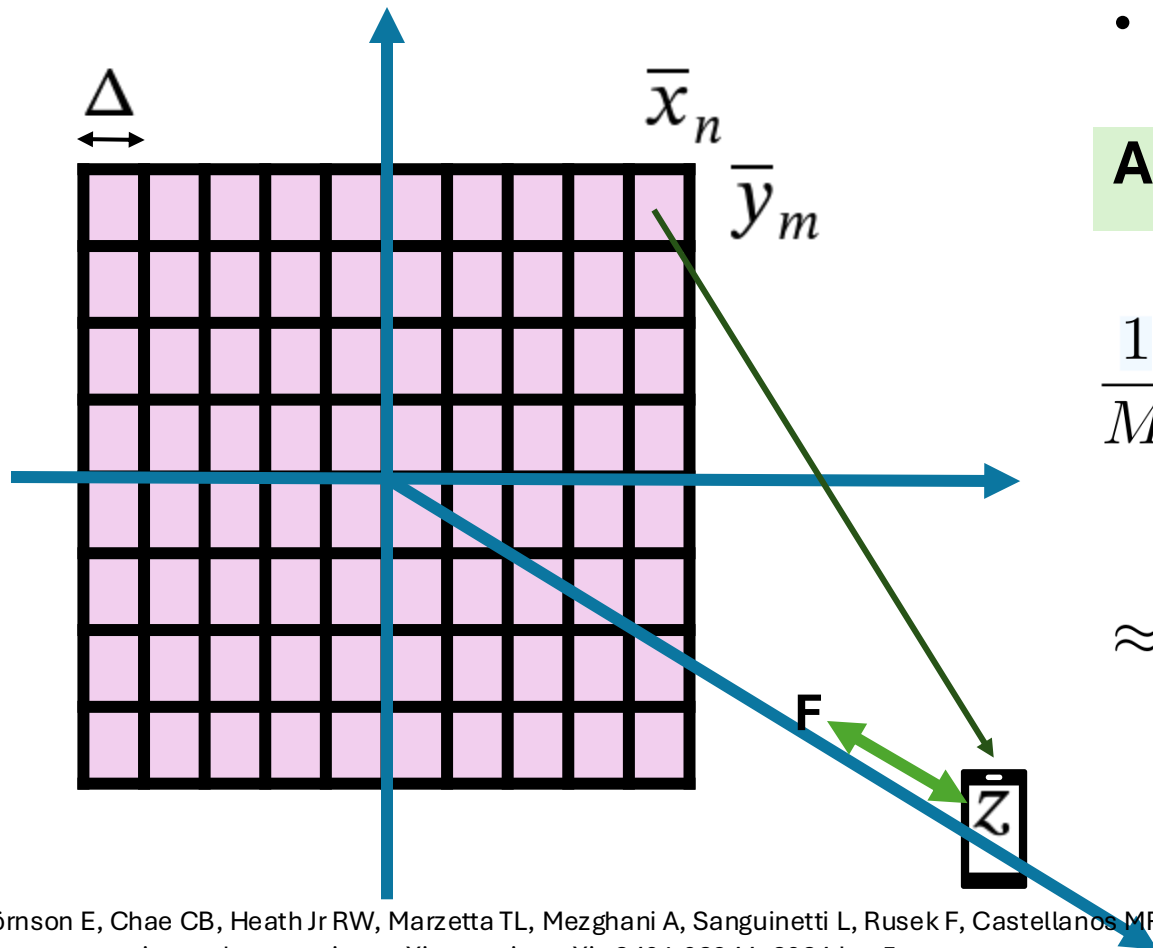
$$M \operatorname{sinc}^2\left(\frac{1}{\lambda} N \Delta \frac{x_t}{z}\right)$$

$$BW_{3dB} \approx \frac{0.886 \lambda F}{N \Delta}$$



M = 250
F = 20 m
BW3dB = 0.141 m

Beamdepth in the Near-field



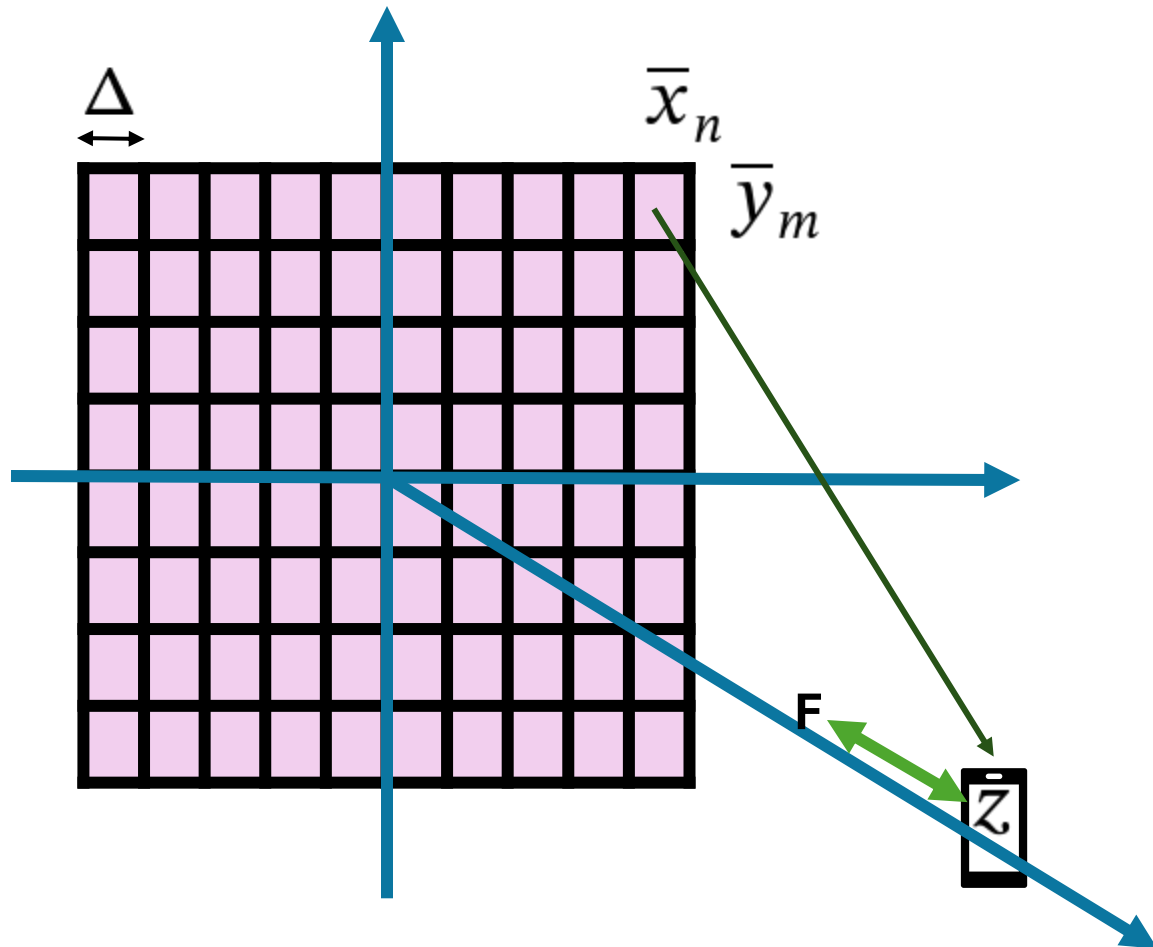
- Focus point $(0, 0, F)$ $F \neq z$

Array Gain

$$\frac{1}{M} \left| \sum_{n=1}^N \sum_{m=1}^N e^{-j \frac{2\pi}{\lambda} \sqrt{\bar{x}_n^2 + \bar{y}_m^2 + z^2}} e^{j \frac{2\pi}{\lambda} \sqrt{\bar{x}_n^2 + \bar{y}_m^2 + F^2}} \right|^2$$

$$\approx \frac{1}{M} \left| \sum_{n=1}^N \sum_{m=1}^N e^{-j \frac{2\pi}{\lambda} \left(z + \frac{\bar{x}_n^2}{2z} + \frac{\bar{y}_m^2}{2z} \right)} e^{j \frac{2\pi}{\lambda} \left(F + \frac{\bar{x}_n^2}{2F} + \frac{\bar{y}_m^2}{2F} \right)} \right|^2$$

Beamdepth in the Near-field

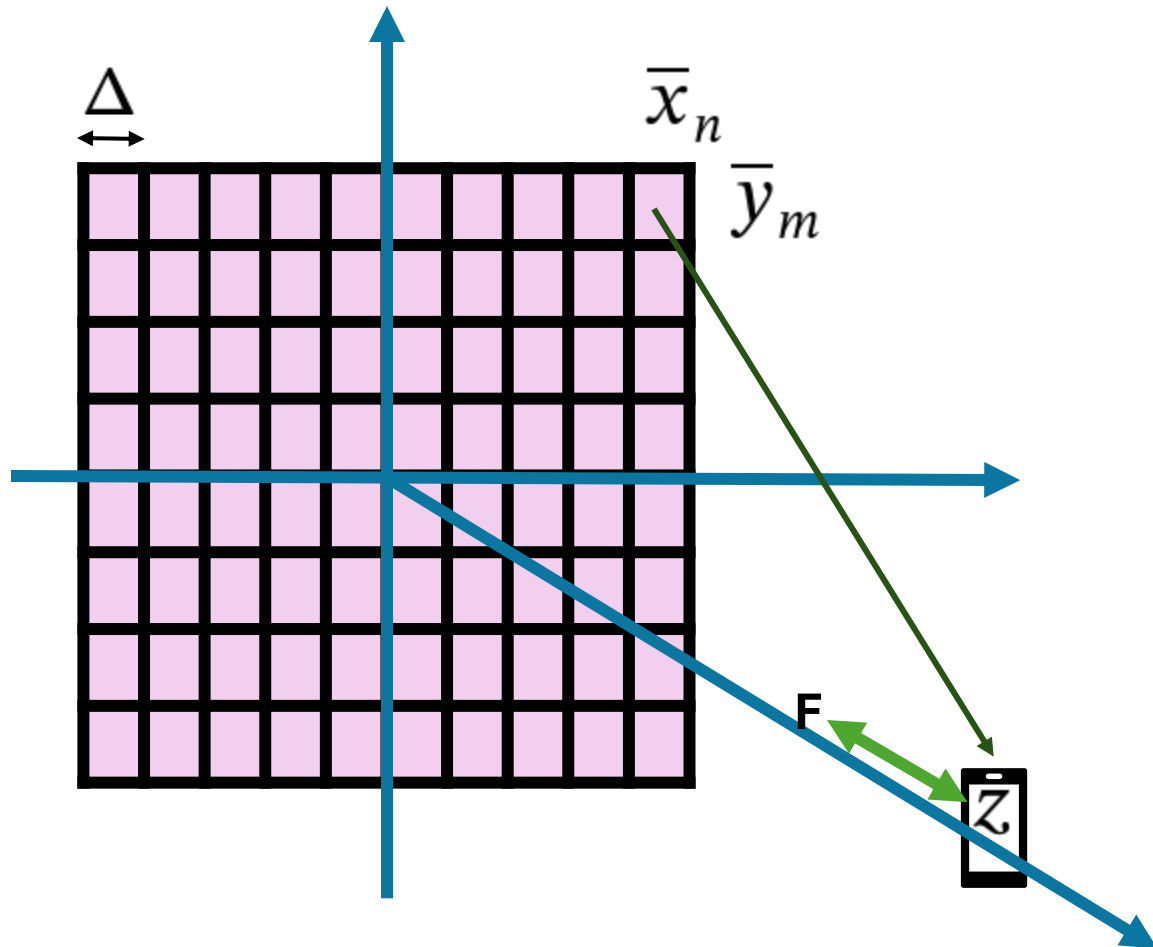


$$z_{\text{eff}} = \left| \frac{1}{F} - \frac{1}{z} \right|^{-1} = \frac{Fz}{|F - z|}$$

Array Gain

$$\begin{aligned} &\approx \frac{1}{M} \left| \sum_{n=1}^N \sum_{m=1}^N e^{-j \frac{2\pi}{\lambda} \left(z + \frac{\bar{x}_n^2}{2z} + \frac{\bar{y}_m^2}{2z} \right)} e^{j \frac{2\pi}{\lambda} \left(F + \frac{\bar{x}_n^2}{2F} + \frac{\bar{y}_m^2}{2F} \right)} \right|^2 \\ &\approx \frac{1}{M} \left| \int_{-N/2}^{N/2} e^{j \frac{\pi}{\lambda} \frac{n^2 \Delta^2}{z_{\text{eff}}}} dn \int_{-N/2}^{N/2} e^{j \frac{\pi}{\lambda} \frac{m^2 \Delta^2}{z_{\text{eff}}}} dm \right|^2 \\ &= M \left(\frac{8z_{\text{eff}}}{d_F} \right)^2 \left(C^2 \left(\sqrt{\frac{d_F}{8z_{\text{eff}}}} \right) + S^2 \left(\sqrt{\frac{d_F}{8z_{\text{eff}}}} \right) \right)^2 \end{aligned}$$

Beamdepth in the Near-field



$$= M \left(\frac{8z_{\text{eff}}}{d_F} \right)^2 \left(C^2 \left(\sqrt{\frac{d_F}{8z_{\text{eff}}}} \right) + S^2 \left(\sqrt{\frac{d_F}{8z_{\text{eff}}}} \right) \right)^2$$

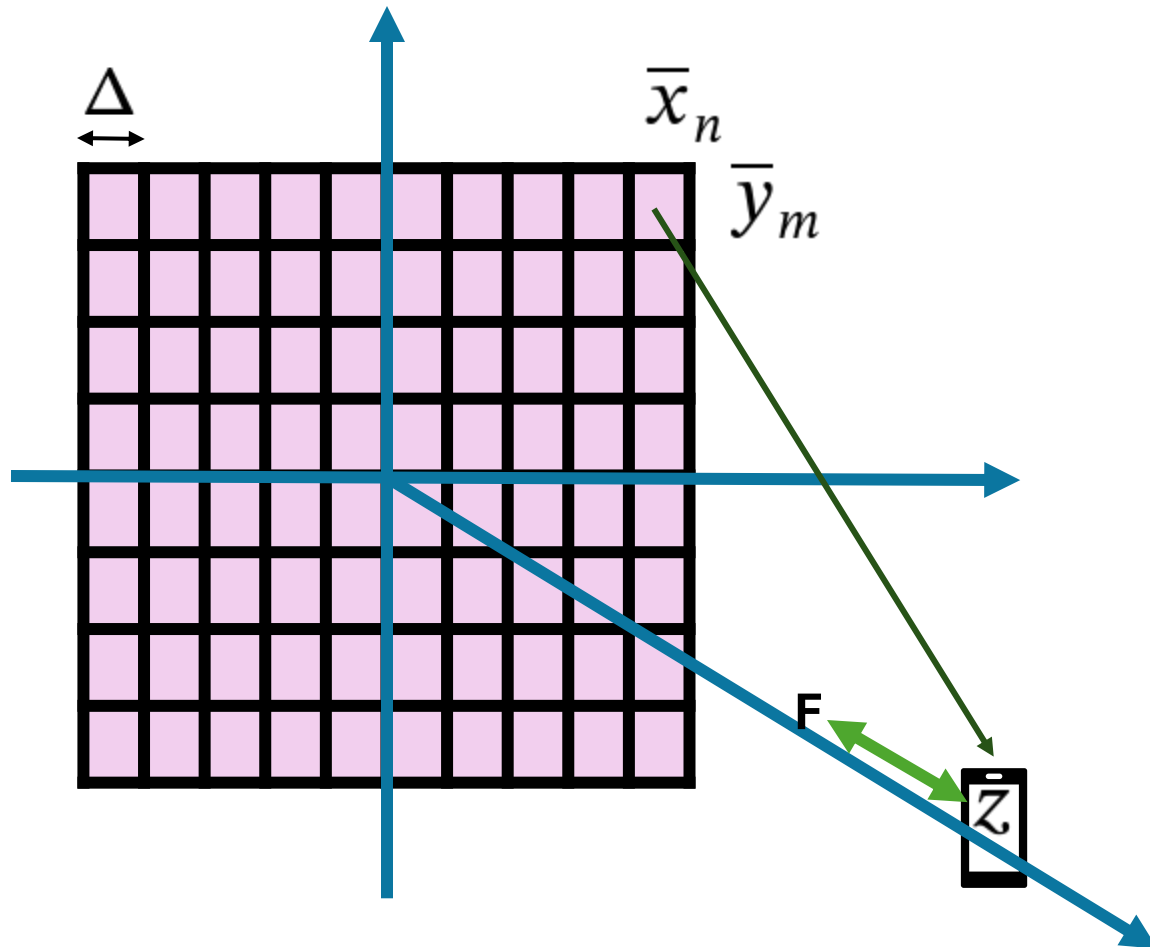
$$d_F = \frac{4N^2 \Delta^2}{\lambda}$$

Fresnel integrals

$$C(x) = \int_0^x \cos\left(\frac{\pi t^2}{2}\right) dt$$

$$S(x) = \int_0^x \sin\left(\frac{\pi t^2}{2}\right) dt$$

Beamdepth in the Near-field



$$= M \left(\frac{8z_{\text{eff}}}{d_F} \right)^2 \left(C^2 \left(\sqrt{\frac{d_F}{8z_{\text{eff}}}} \right) + S^2 \left(\sqrt{\frac{d_F}{8z_{\text{eff}}}} \right) \right)^2$$

$$\frac{(C^2(\sqrt{x}) + S^2(\sqrt{x}))^2}{x^2}$$

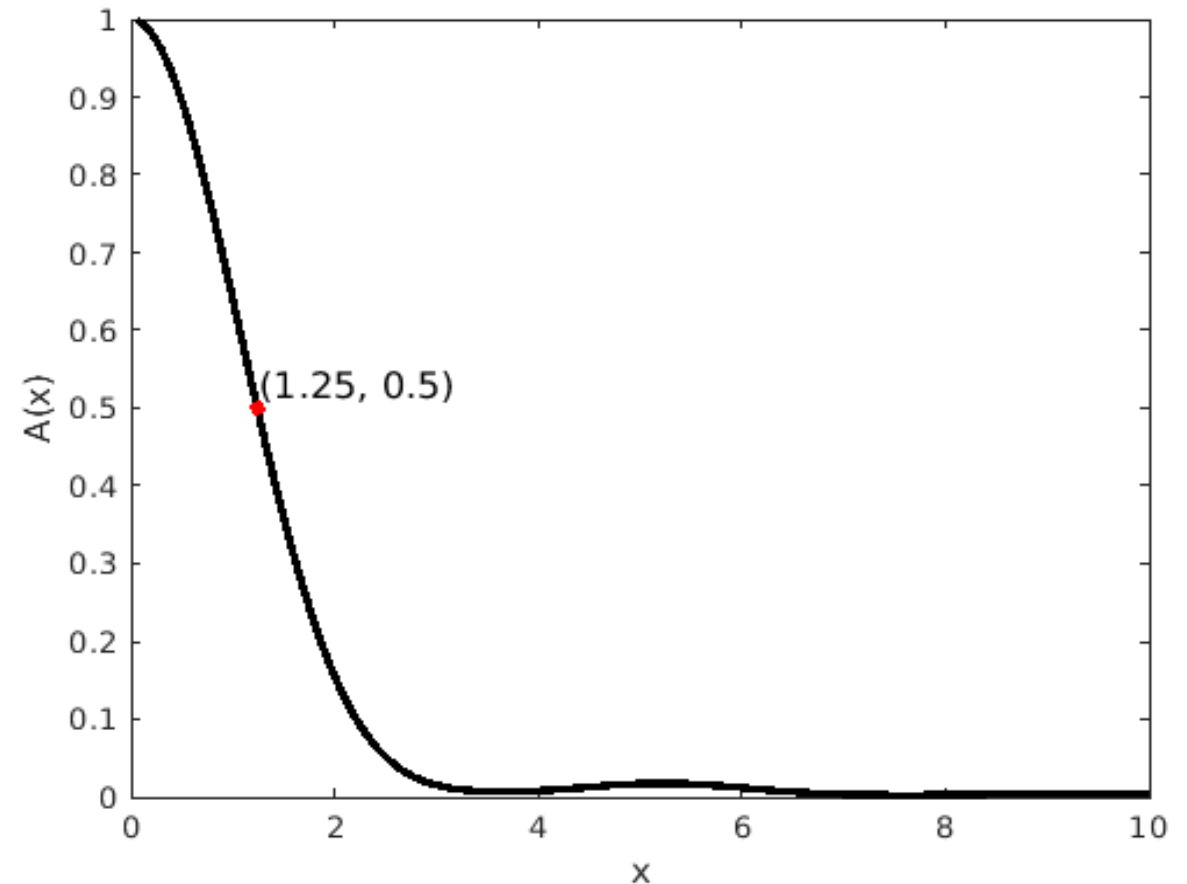
$$x = \frac{d_F}{8z_{eff}}$$

Beamdepth in the Near-field

$$A(x) = \frac{(C^2(\sqrt{x}) + S^2(\sqrt{x}))^2}{x^2} \quad \rightarrow$$

Decreasing function for $x = [0, 2]$

$$A(0) = 1, A(1.25) = 0.5$$



Beamdepth in the Near-field

$$A(x) = \frac{(C^2(\sqrt{x}) + S^2(\sqrt{x}))^2}{x^2} \quad \longrightarrow \quad \text{Decreasing function for } x = [0, 2]$$

$$A(0) = 1, A(1.25) = 0.5$$

$$1.25 = \frac{d_F}{8z_{\text{eff}}} = \frac{d_F |F - z|}{8Fz} \quad \rightarrow \quad z = \frac{d_F F}{d_F \pm 10F}$$

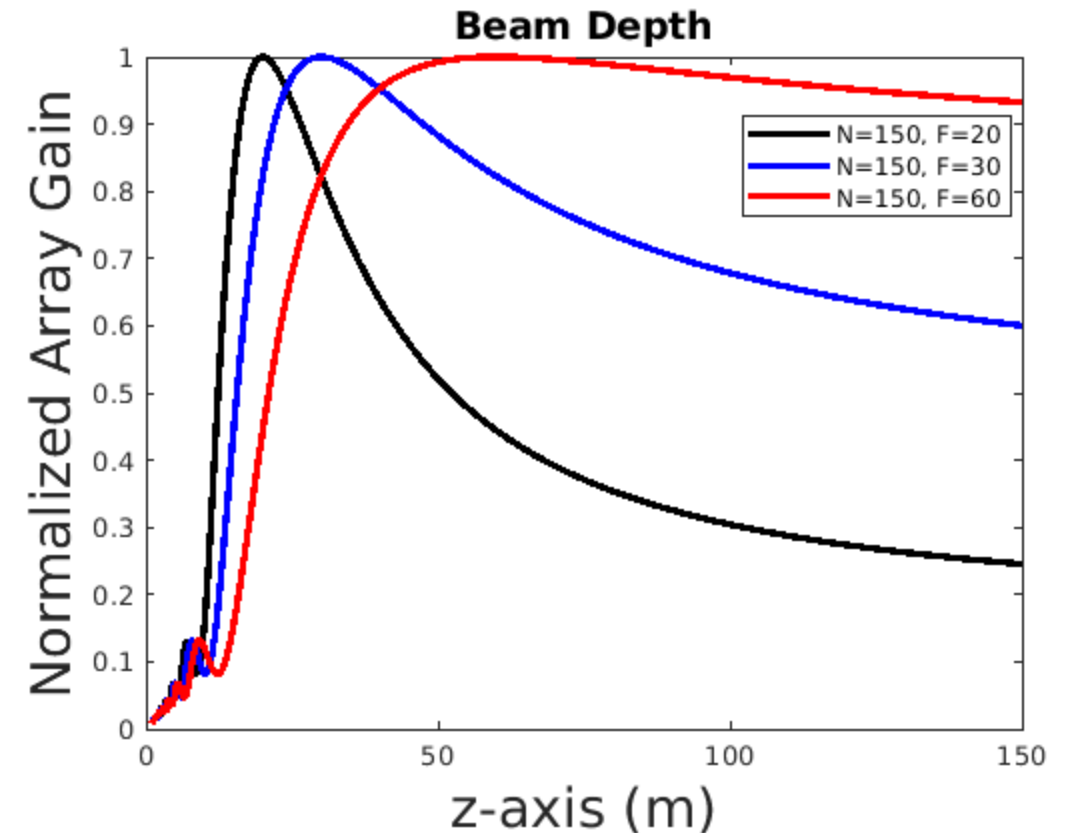
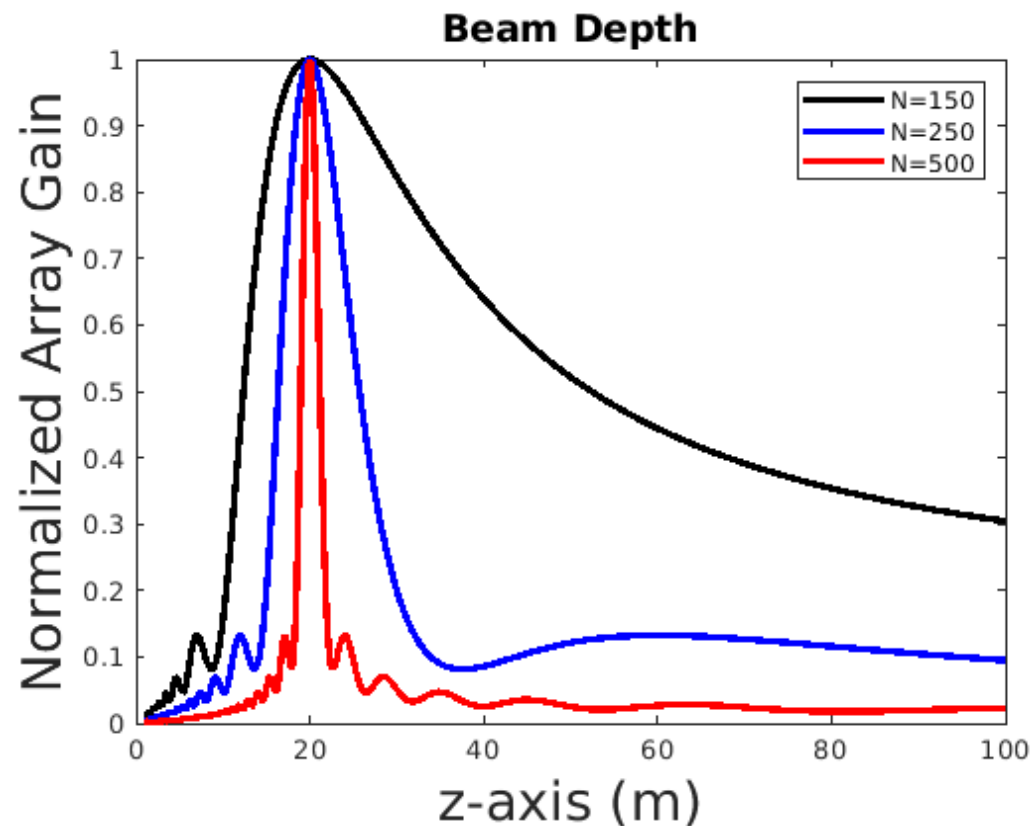
$$\text{BD}_{3\text{ dB}} = \frac{d_F F}{d_F - 10F} - \frac{d_F F}{d_F + 10F} = \frac{20d_F F^2}{d_F^2 - 100F^2}$$

$$F < \frac{d_F}{10}$$

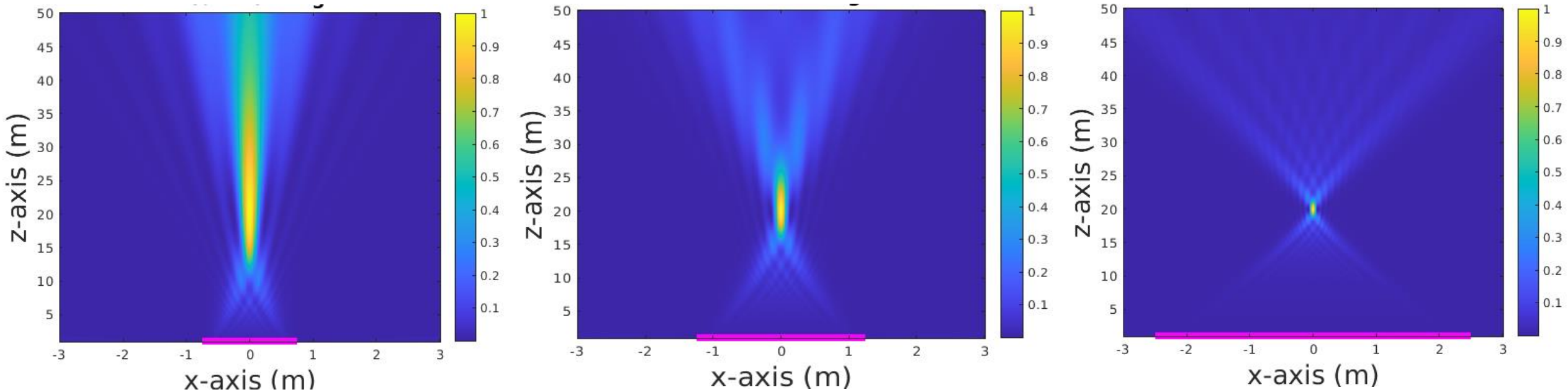
$$d_B < r < d_F$$

Beamdepth in the Near-field

$$\text{BD}_{3\text{ dB}} = \frac{d_F F}{d_F - 10F} - \frac{d_F F}{d_F + 10F} = \frac{20d_F F^2}{d_F^2 - 100F^2}.$$



Beamdepth in the Near-field

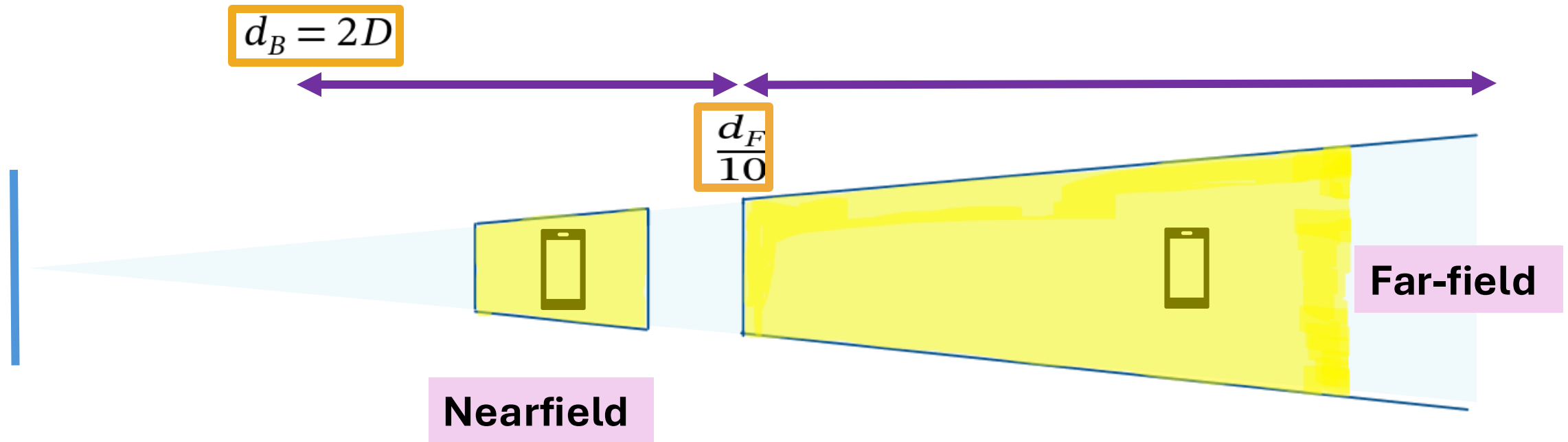


$M = 150$
 $F = 20$ m
 $BW = 0.236$ m
 $BD = 39.72$ m

$M = 250$
 $F = 20$ m
 $BW = 0.141$ m
 $BD = 9.26$ m

$M = 500$
 $F = 20$ m
 $BW = 0.0708$ m
 $BD = 3.226$ m

Nearfield spatial multiplexing

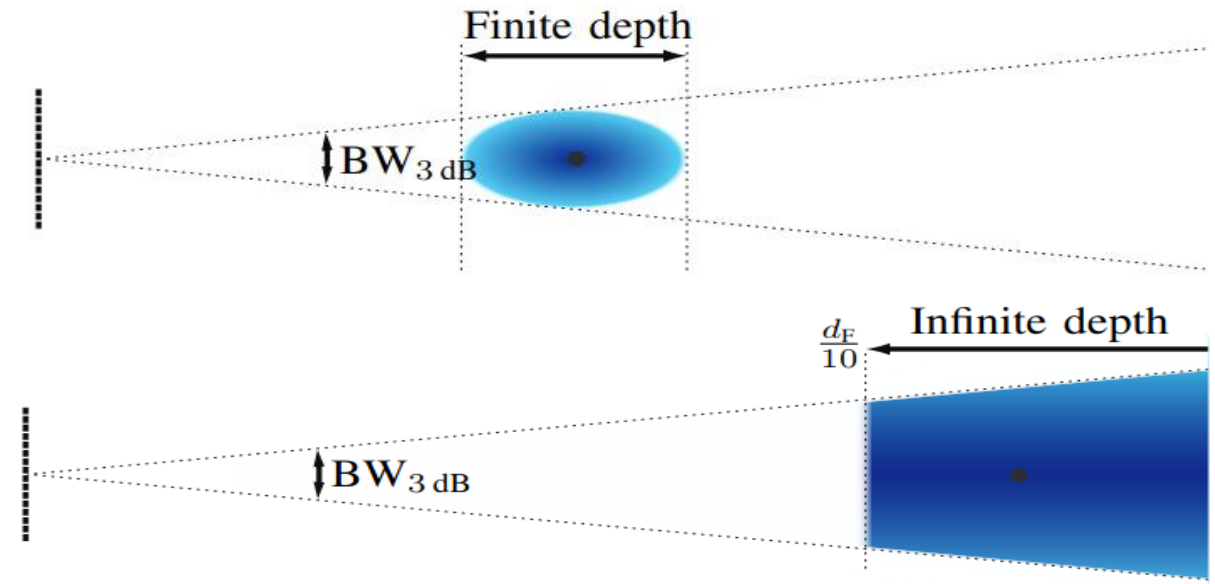
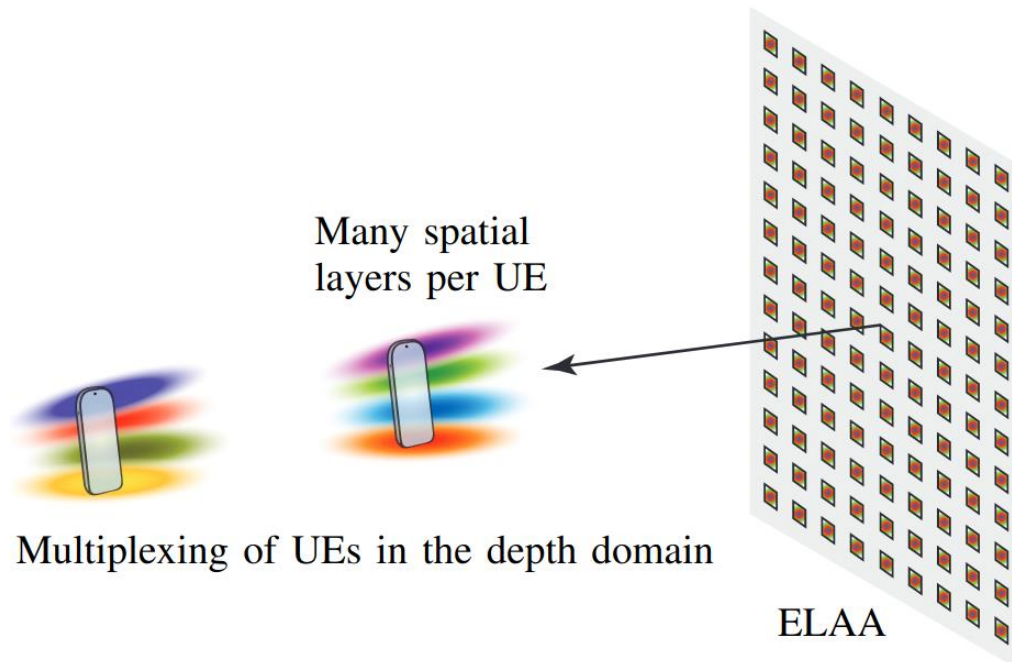


$$d_F = \frac{4N^2\Delta^2}{\lambda}$$

- **Impact of the wavelength**
- Fixed array size: $d_F \propto \lambda^{-1}$
- Fixed number of elements: $d_F \propto \lambda$

Nearfield spatial multiplexing

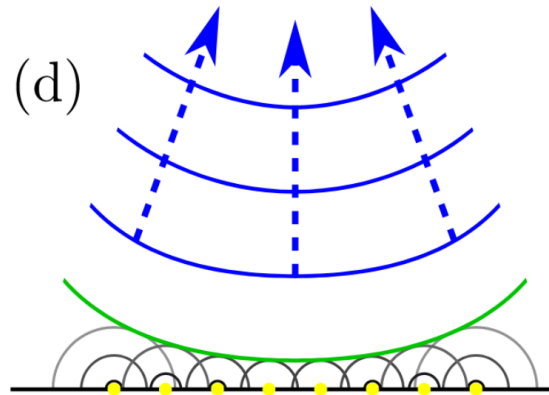
- Smaller focus area in **Nearfield**, both in **depth and width**.
- Reduce interference between concurrent signal transmission.
- Massive spatial multiplexing



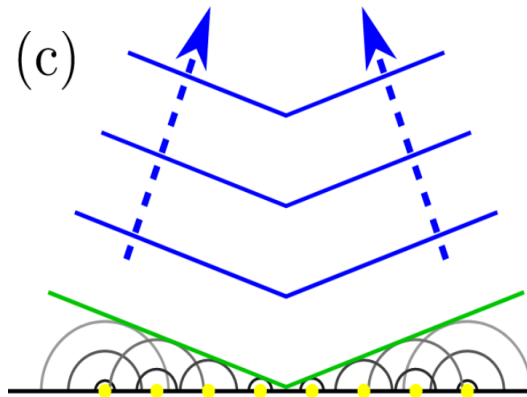
Bessel Beam

A long column of constructive interference can be seen along the z-axis.

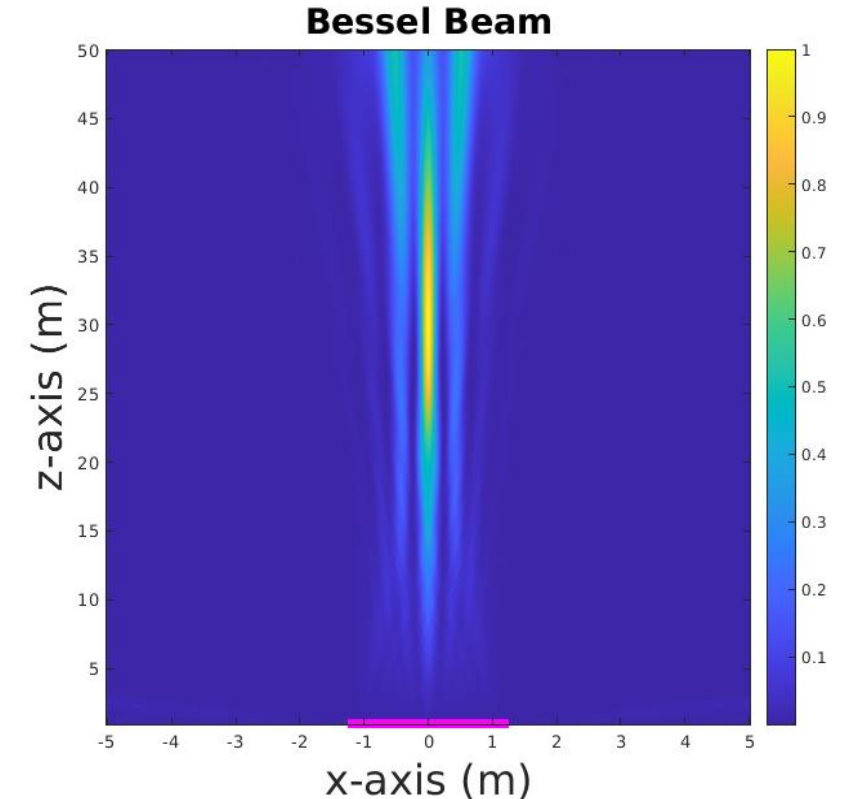
As the wave propagates, the beam profile remains invariant.



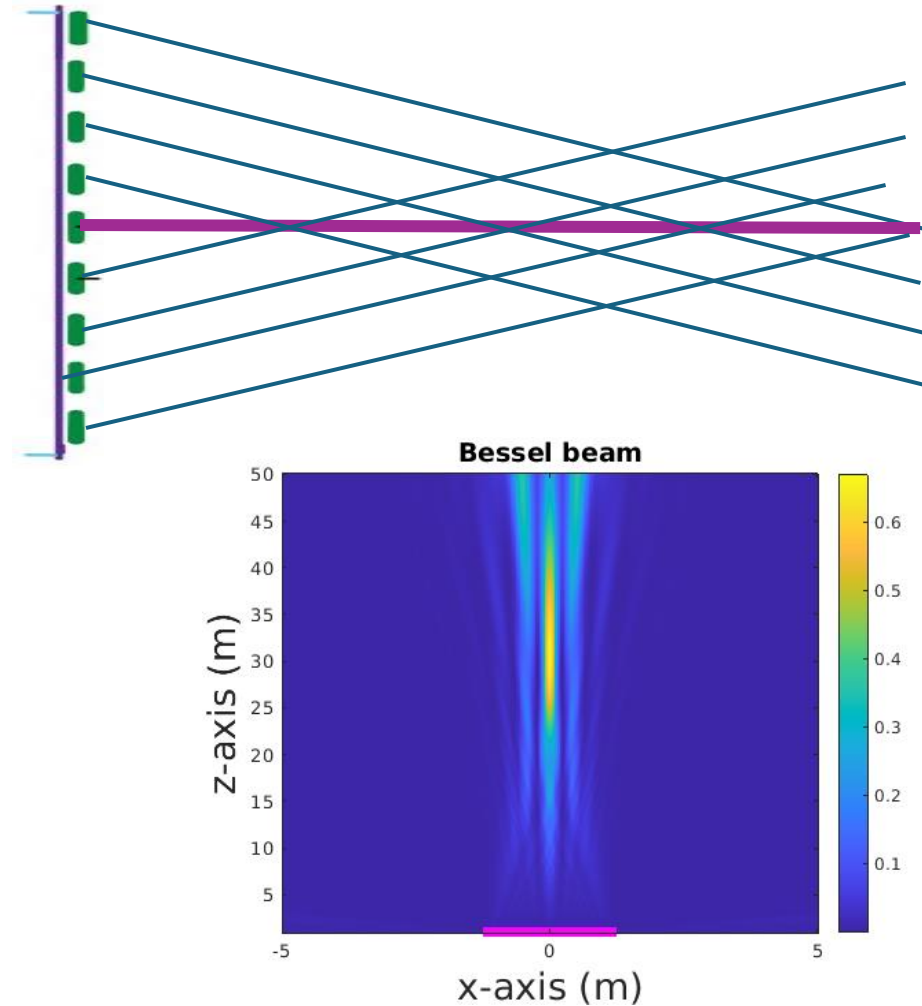
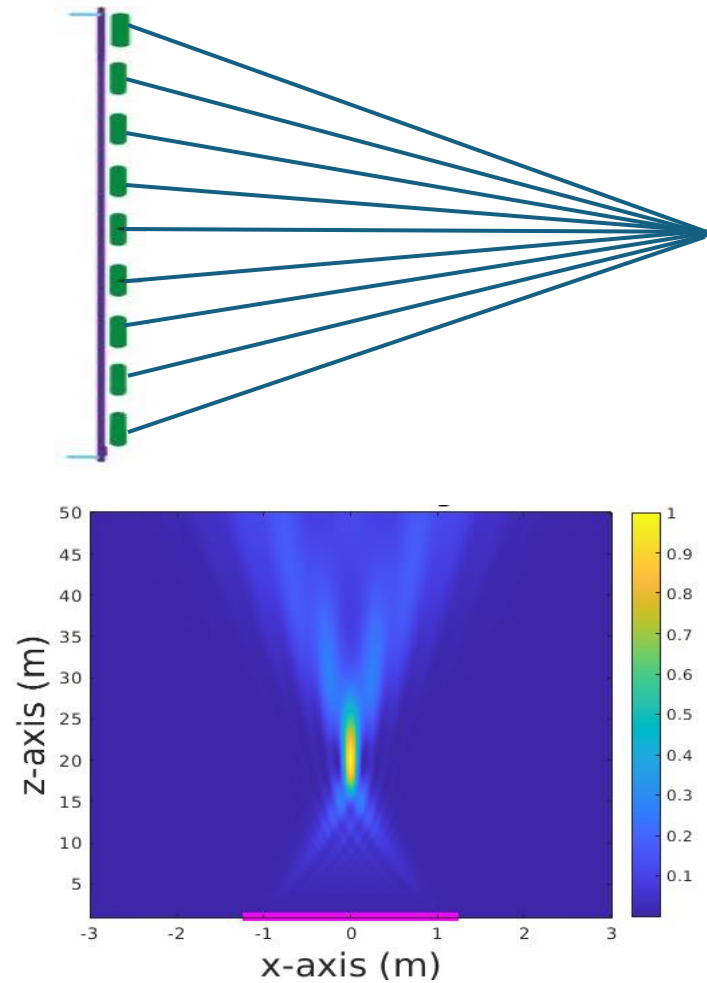
$$\varphi_{n,m} = \frac{2\pi}{\lambda} \sqrt{\bar{x}_n^2 + \bar{y}_m^2 + z^2}$$



$$\varphi_{n,m} = \frac{2\pi}{\lambda} (\sqrt{\bar{x}_n^2 + \bar{y}_m^2}) \cos\theta$$

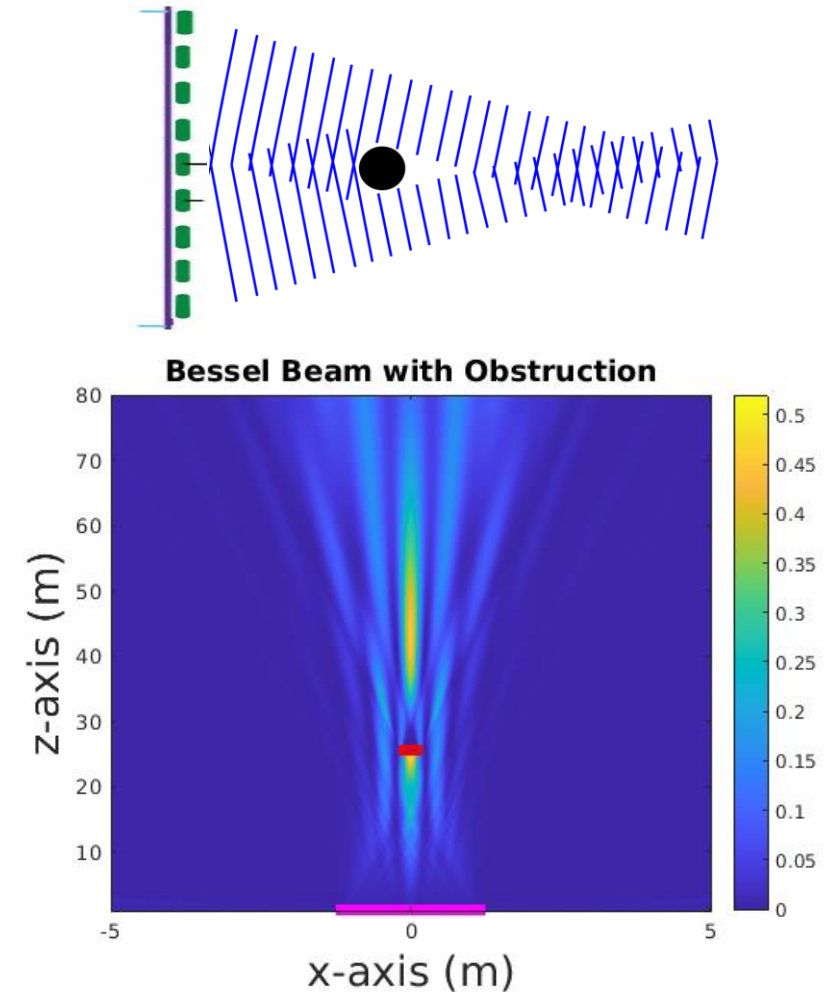
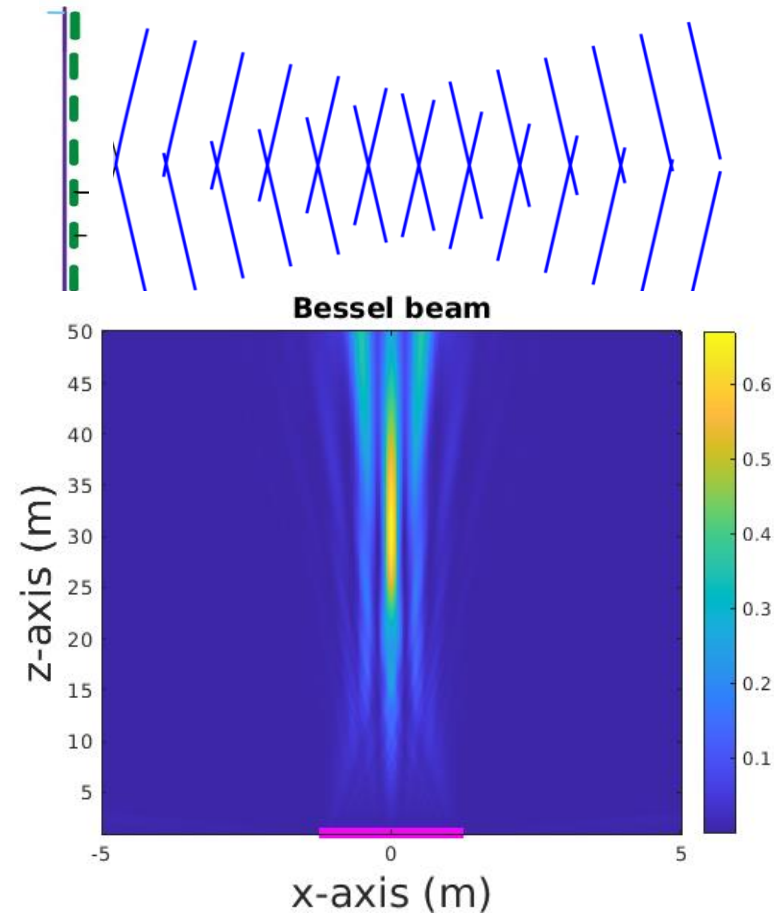


Bessel Beam



Bessel Beam

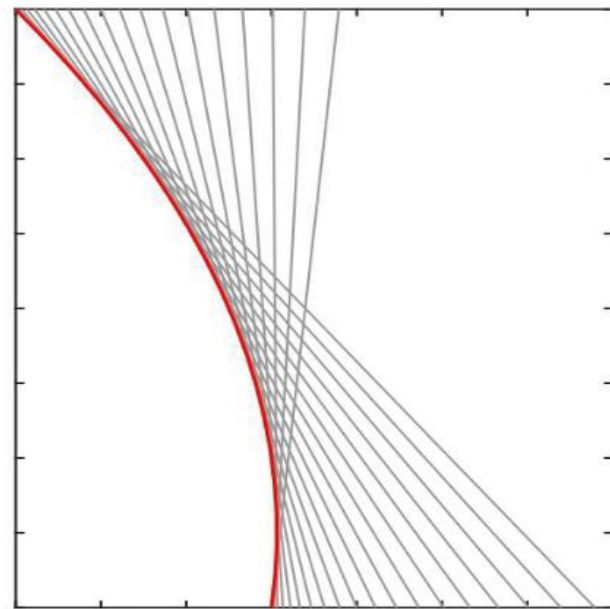
Bessel beams are **self-healing**.



Curved Beam

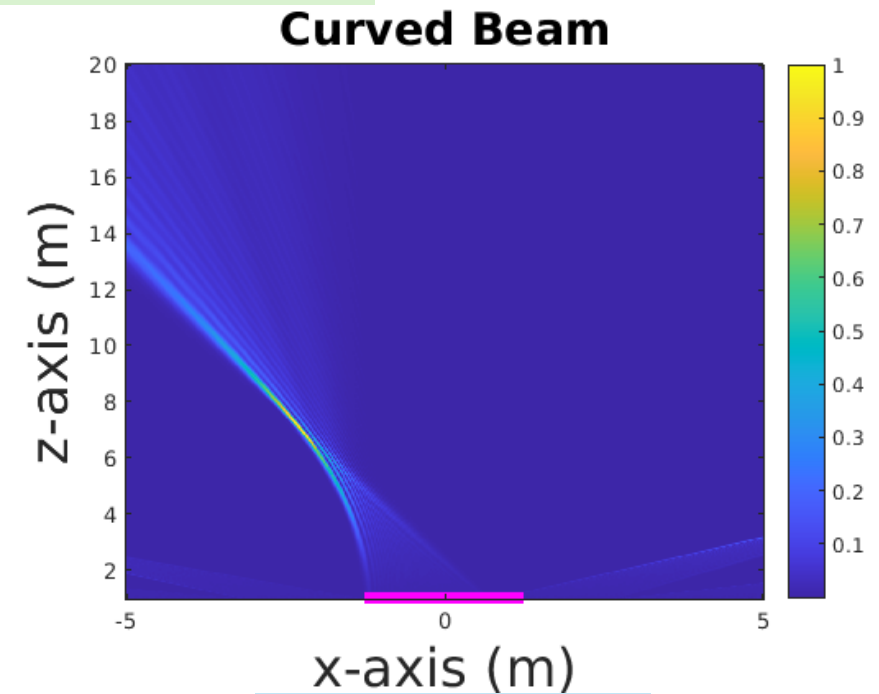
Follow arbitrary curved trajectories

Solve challenges associated to blockage.



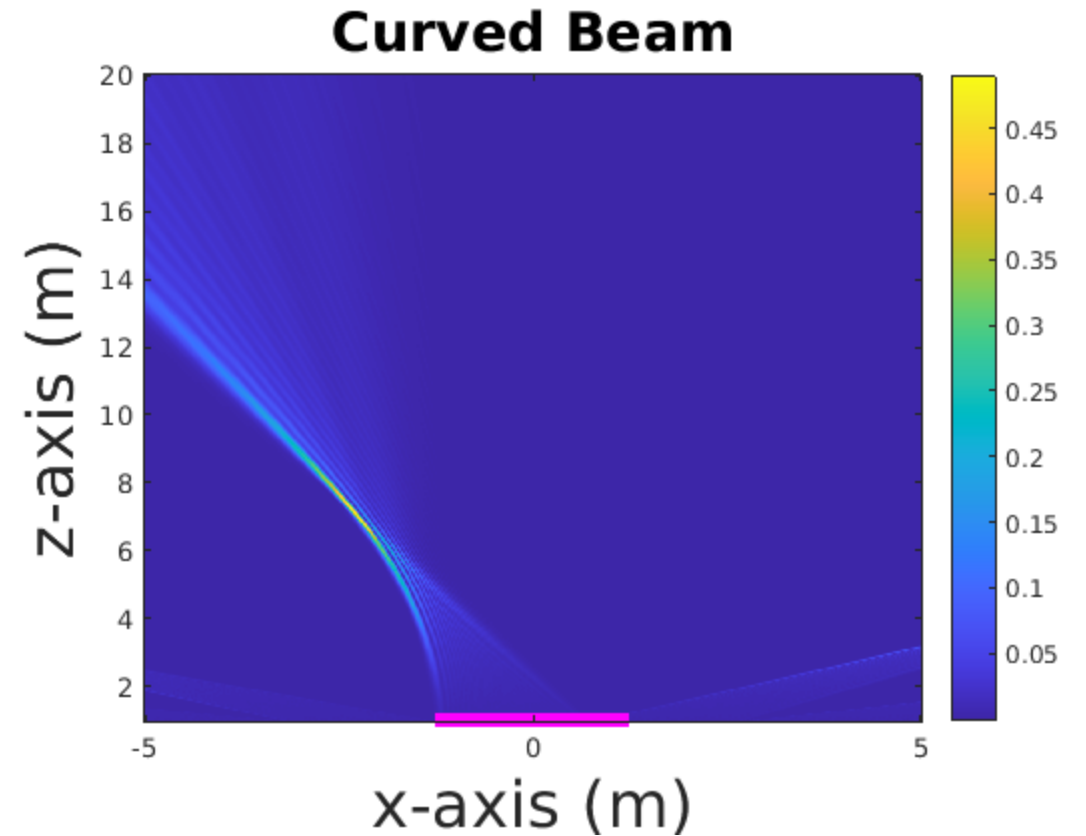
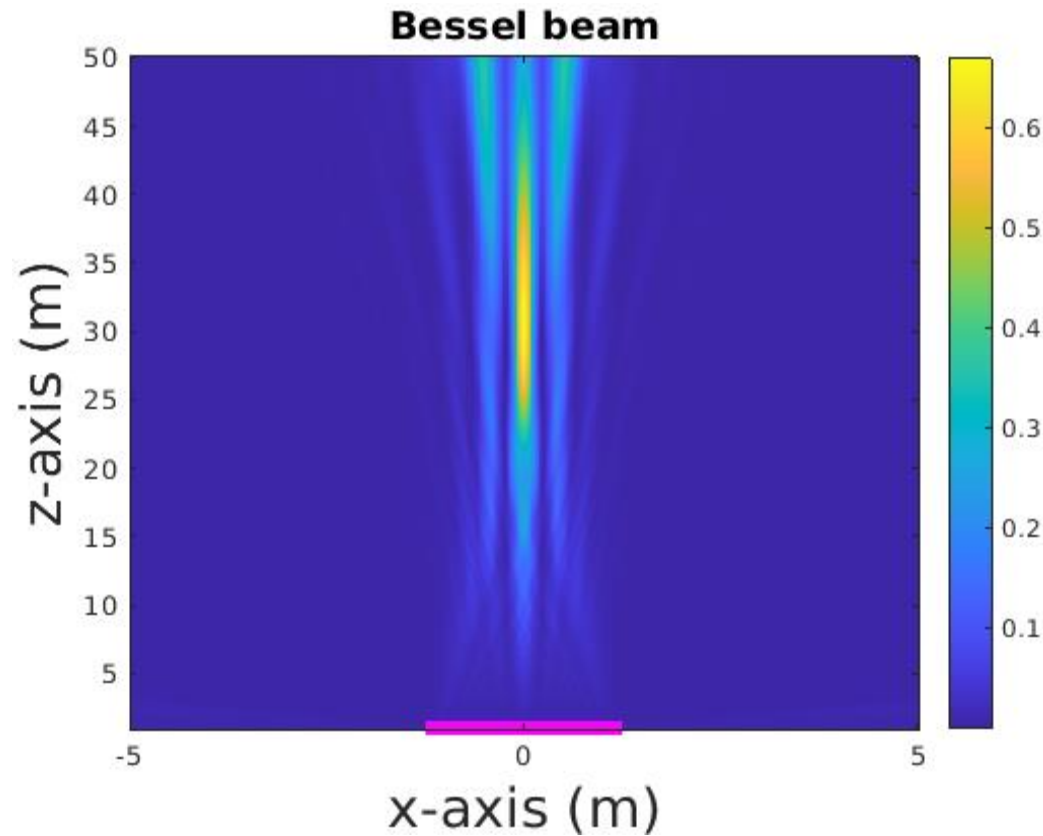
$$g(z) = -0.0125(z-1)^2 + .0025$$

Trajectory



Result Beam

Bessel and Curved Beam



Will Near-Field Effects Appear in 6G?

Example :

$$F < \frac{d_F}{10}$$

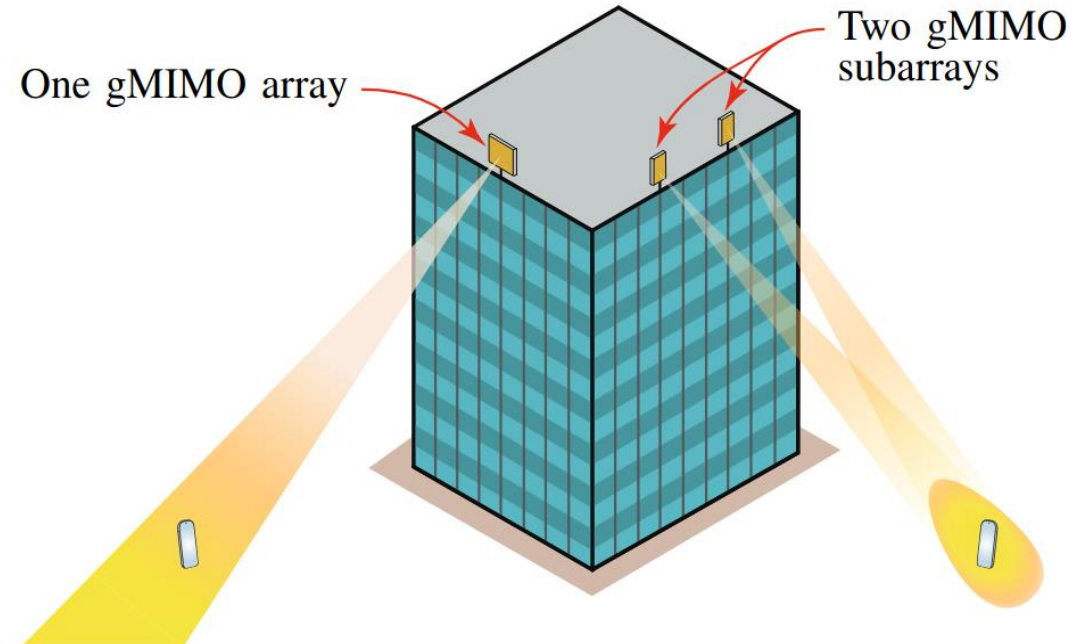
0.5×0.5, 3 GHz = 1 m

1×1 m, 15 GHz = 20m

1×1 m, 30 GHz = 40 m



We need extremely large antenna array or very high frequency



Mini Matlab Project

