Statistics for Data Science -1

Lecture 6.5: Probability- Application of addition rule

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Learning objectives

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Application of addition rule

Example: Shopping for shirts and pants

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- Hence, $P(S \cup P)^c = 1 - 0.4 = 0.6$

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Section summary

1. Addition rule of probability.