Statistics for Data Science -1

Lecture 8.2: Random Variable: Application

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Learning objectives

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3. Probability mass function, graph, and examples.
4. Cumulative distribution function, graphs, and examples.
5. Expectation and variance of a random variable.

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  - $P\{X = 2\} = P(A \cap B) = 0.05 \times 0.1 = 0.005$

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Definition

When outcomes for random event are numerical, but cannot be counted and are infinitely divisible, we have continuous random variables.

Section summary

- What is a random variable.
- Probability of a random variable.
- Defined discrete and continuous random variable.