

**Week - 7**  
Tutorial  
**Functions**  
Mathematics for Data Science - 1

1. Draw a graph of the functions  $x, x^2, x^3$ .

2. Draw a graph of the functions  $f(x) = x^2 - 8x + 15$ .

3. Draw a graph of the functions  $f(x) = (x - 2)(x + 3)(x - 5)$ .

4. Given functions  $f(x) = \frac{x^2-8x+15}{x+3}$ ,  $g(y) = \sqrt{y^2-4}$ , then answer the following questions.
- (a) If the domain of  $f(x)$  is  $(-\infty, -m) \cup (-m, \infty)$ , then find the value of  $m$ .
  - (b) If the domain of  $g(x)$  is  $(-\infty, -n] \cup [n, \infty)$ , then find the value of  $n$ ?

5. What will be the range of  $g(x) = \sqrt{x^2 - 4}$ ?

6. Find the domain of  $h(x)$  if  $h(x) = f \circ g(x)$  where  $f(x) = \frac{x^2 - 8x + 15}{x + 3}$  and  $g(x) = \sqrt{x^2 - 4}$ .

7. Rohan (age 22) saw a birthday offer outside of a shop. The offer includes a discount of  $D(a)\%$  on the payable amount if the customer has birthday on that particular day, where  $a$  is the age of the customer and  $D(a) = (-a^2 + 50a - 600)$ . The shop also has a Sunday offer which is flat discount of ₹1500, if the initial purchased amount is more than ₹12000. Suppose Rohan has a friend (age 25) who shares the same birthday with Rohan on a particular sunday. Express the final payable amount as a function in terms of  $a$  and find the possible minimum amount needed to be paid if Rohan purchased some commodities of ₹15000 from the shop.

Assume the following :

- Any offer can be applied first.
- Rohan can use either his or his friend's birthday for the birthday offer.

8. Ramya wants to have a sum of amount in her bank account for launching her own startup company. She currently has 12 lakh in her account and the bank provides interest at the rate of  $x\%$  per annum. Assuming that the bank calculate the amount quarterly,
- find the total amount in terms of  $x$  (denoted by the function  $f(x)$ ), in her account after  $n$  years.
  - find a function  $g(y)$  to calculate the required rate based on the amount Ramya required for launching her startup company after  $n$  years.