



IIT Madras
ONLINE DEGREE



Polynomial

Algebra with Polynomial

Polynomials in One Variable

Description: As seen earlier, the polynomial of degree n , is represented as

$$a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0.$$

This expression can be treated as a function from $\mathbb{R} \longrightarrow \mathbb{R}$.

That is, the domain of $p(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_1 x + a_0$ is \mathbb{R} , and the range depends on the function.

Addition of Polynomials

Add the following polynomials:

1. $p(x) = x^2 + 4x + 4$, $q(x) = 10$
2. $p(x) = x^4 + 4x$, $q(x) = x^3 + 1$
3. $p(x) = x^3 + 2x^2 + x$, $q(x) = x^2 + 2x + 2$

$$p(x) = 1x^2 + 4x + 4$$

$$q(x) = 0x^2 + 0x + 10$$

$$p(x) + q(x) = x^2 + 4x + 14$$

$$p(x) = 1x^4 + 0x^3 + 0x^2 + 4x + 0$$

$$q(x) = 0x^4 + x^3 + 0x^2 + 0x + 1$$

$$p(x) + q(x) = x^4 + x^3 + 4x + 1$$

$$p(x) = 1x^3 + 2x^2 + x + 0$$

$$q(x) = 0x^3 + x^2 + 2x + 2$$

$$p(x) + q(x) = x^3 + (2+1)x^2 + (1+2)x + 2 = x^3 + 3x^2 + 3x + 2$$

Let $p(x) = \sum_{k=0}^n a_k x^k$, and $q(x) = \sum_{j=0}^m b_j x^j$. Then

$$p(x) + q(x) = \sum_{k=0}^{m \vee n} (a_k + b_k) x^k.$$

Subtraction of Polynomials

Subtract the following polynomials:

1. $p(x) = x^2 + 4x + 4$, $q(x) = 10$
2. $p(x) = x^4 + 4x$, $q(x) = x^3 + 1$
3. $p(x) = x^3 + 2x^2 + x$, $q(x) = x^2 + 2x + 2$

$$p(x) = 1x^2 + 4x + 4$$

$$-q(x) = -0x^2 - 0x - 10$$

$$p(x) - q(x) = x^2 + 4x - 6$$

$$p(x) = 1x^4 + 0x^3 + 0x^2 + 4x + 0$$

$$-q(x) = -0x^4 - x^3 - 0x^2 - 0x - 1$$

$$p(x) + q(x) = x^4 - x^3 + 4x - 1$$

$$p(x) = 1x^3 + 2x^2 + x + 0$$

$$-q(x) = -0x^3 - 1x^2 - 2x - 2$$

$$p(x) - q(x) = x^3 + (2-1)x^2 + (1-2)x - 2 = x^3 + x^2 - x - 2$$

Let $p(x) = \sum_{k=0}^n a_k x^k$, and $q(x) = \sum_{j=0}^m b_j x^j$. Then

$$p(x) - q(x) = \sum_{k=0}^{m \vee n} (a_k - b_k) x^k.$$