



**IIT Madras**  
ONLINE DEGREE

Pseudocode: List example, correlating student performance

# Correlating marks in Maths and Physics

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*Student who perform well in Mathematics perform at least as well in Physics*

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- Count students in A list for Maths who are also in A list for Physics

- Count students in B list for Maths who are also in A list or B list for Physics

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- Assign grades in each subject

- Construct lists of students with grades A and B in both subjects — four lists

- Count students in A list for Maths who are also in A list for Physics

- Count students in B list for Maths who are also in A list or B list for Physics

- Use these counts to confirm or reject the hypothesis

# Assigning grades

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approximately at quartile boundaries
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[StudentId,Marks]
- Procedure to extract marks  
information as a list for a subject

Procedure BuildMarksList(field)

```
marksList = []  
while (Table 1 has more rows) {  
    Read the first row X in Table 1  
    marksList = marksList ++  
                        [[X.SeqNo, X.field]]  
    Move X to Table 2  
}  
return(marksList)
```

End BuildMarksList

# Assigning grades

- Assign grades {A,B,C,D} approximately at quartile boundaries
  - Top 25% get A, next 25% get B, next 25% get C, bottom 25% get D
- To calculate quartiles, extract marks as a list and sort the list
- Need to identify the students — each entry in the marks list is a pair [StudentId,Marks]
- Procedure to extract marks information as a list for a subject
- Get the marks lists for Maths and Physics

Procedure BuildMarksList(field)

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marksList = []  
while (Table 1 has more rows) {  
    Read the first row X in Table 1  
    marksList = marksList ++  
                                     [[X.SeqNo, X.field]]  
    Move X to Table 2  
}  
return(marksList)
```

End BuildMarksList

```
mathsList = BuildMarksList(Mathematics)
```

```
physicsList = BuildMarksList(Physics)
```

# Assigning grades ...

- Use insertion sort for `mathList` and `physicsList`?
  - Entries are `[id,marks]`
  - To compare `[i1,m1]` and `[i2,m2]`, only look at `m1`, `m2`



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- Extracting values at the beginning and end of a list
  - `first(l)` and `last(l)`  
`first([1,2,3,4])` is 1,  
`last([1,2,3,4])` is 4

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  - `first(l)` and `last(l)`  
`first([1,2,3,4])` is 1,  
`last([1,2,3,4])` is 4
  - The remainder of the list is given by `rest(l)` and `init(l)`, respectively  
`rest([1,2,3,4])` is `[2,3,4]`,  
`init([1,2,3,4])` is `[1,2,3]`

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- Extracting values at the beginning and end of a list
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`rest([1,2,3,4])` is `[2,3,4]`,  
`init([1,2,3,4])` is `[1,2,3]`
- Modify `SortedListInsert`

Procedure `SortedListInsert(l,x)`

```
newList = []
inserted = False

foreach z in l {
  if (not(inserted)) {
    if (last(x) < last(z)) {
      newList = newList ++ [x]
      inserted = True
    }
  }
  newList = newList ++ [z]
}

if (not(inserted)) {
  newList = newList ++ [x]
}

return(newList)
```

End `SortedListInsert`

# Assigning grades ...

- `InsertionSort` uses updated `SortedListInsert`

```
sortedMathsList =  
    InsertionSort(mathsList)  
  
sortedPhysicsList =  
    InsertionSort(physicsList)
```

# Assigning grades ...

- Assign grades to a sorted list by quartile

Procedure SimpleGradeAssignment(I)

End SimpleGradeAssignment

# Assigning grades ...

- Assign grades to a sorted list by quartile
  - `length(l)` returns number of elements in `l`
  - Compute quartile boundaries based on class size

Procedure SimpleGradeAssignment(l)

```
classSize = length(l)
q4 = classSize/4
q3 = classSize/2
q2 = 3*classSize/4
```

# Assigning grades ...

- Assign grades to a sorted list by quartile
  - `length(l)` returns number of elements in `l`
  - Compute quartile boundaries based on class size
  - Initialize list for each grade

Procedure SimpleGradeAssignment(l)

`q4 = ..., q3 = ..., q2 = ...`

`gradeA = []`

`gradeB = []`

`gradeC = []`

`gradeD = []`

# Assigning grades ...

- Assign grades to a sorted list by quartile
  - `length(l)` returns number of elements in `l`
  - Compute quartile boundaries based on class size
  - Initialize list for each grade
  - Assign grades based on the position in the list

Procedure SimpleGradeAssignment(l)

```
q4 = ..., q3 = ..., q2 = ...
gradeA = [], ..., gradeD = []

position = 0
foreach x in l {
  if (position > q2) {
    gradeA = gradeA ++ [first(x)]
  }
  if (position > q3 and position <= q2) {
    gradeB = gradeB ++ [first(x)]
  }
  if (position > q4 and position <= q3) {
    gradeC = gradeC ++ [first(x)]
  }
  if (position <= q4) {
    gradeD = gradeD ++ [first(x)]
  }
  position = position + 1
}
return([gradeA, gradeB, gradeC, gradeD])
```

End SimpleGradeAssignment



# Assigning grades ...

- Assign grades to a sorted list by quartile
  - `length(l)` returns number of elements in `l`
  - Compute quartile boundaries based on class size
  - Initialize list for each grade
  - Assign grades based on the position in the list
- `SimpleGradeAssignment` returns a list containing four lists, for the four grades

Procedure SimpleGradeAssignment(l)

```
q4 = ..., q3 = ..., q2 = ...
gradeA = [], ..., gradeD = []

position = 0
foreach x in l {
  if (position > q2) {
    gradeA = gradeA ++ [first(x)]
  }
  if (position > q3 and position <= q2) {
    gradeB = gradeB ++ [first(x)]
  }
  if (position > q4 and position <= q3) {
    gradeC = gradeC ++ [first(x)]
  }
  if (position <= q4) {
    gradeD = gradeD ++ [first(x)]
  }
  position = position + 1
}
return([gradeA, gradeB, gradeC, gradeD])
```

End SimpleGradeAssignment

# Assigning grades ...

- Assign grades corresponding to Maths and Physics marks

```
mathsGrades =  
    SimpleGradeAssignment(sortedMathsList)  
physicsGrades =  
    SimpleGradeAssignment(sortedPhysicsList)
```

# Assigning grades ...

- Assign grades corresponding to Maths and Physics marks
- Unpack the four lists into four separate lists

```
mathsGrades =  
    SimpleGradeAssignment(sortedMathsList)  
  
physicsGrades =  
    SimpleGradeAssignment(sortedPhysicsList)  
  
mathsAGrades = first(mathsGrades)  
mathsBGrades = first(rest(mathsGrades))  
mathsCGrades = last(init(mathsGrades))  
mathsDGrades = last(mathsGrades)  
  
physicsAGrades = first(physicsGrades)  
physicsBGrades = first(rest(physicsGrades))  
physicsCGrades = last(init(physicsGrades))  
physicsDGrades = last(physicsGrades)
```

# Test the hypothesis

- Check how many students with A in Maths confirm the hypothesis
  - `exitloop` prematurely terminates a `foreach` loop

```
confirm = []
reject = []
foreach x in mathsAGrades {
    found = False
    foreach y in physicsAGrades {
        if (x == y) {
            confirm = confirm ++ [x]
            found = True
            exitloop
        }
    }
    if (not(found)) {
        reject = reject ++ [x]
    }
}
```

# Test the hypothesis

- Check how many students with A in Maths confirm the hypothesis
  - `exitloop` prematurely terminates a `foreach` loop
- Check how many students with B in Maths confirm the hypothesis

```
foreach x in mathsBGrades {  
    found = False  
    foreach y in physicsAGrades {  
        if (x == y) {  
            confirm = confirm ++ [x]  
            found = True, exitloop  
        }  
    }  
    if (not(found)) {  
        foreach y in physicsBGrades {  
            if (x == y) {  
                confirm = confirm ++ [x]  
                found = True, exitloop  
            }  
        }  
    }  
    if (not(found)) {  
        reject = reject ++ [x]  
    }  
}
```

# Test the hypothesis

- Check how many students with A in Maths confirm the hypothesis
  - `exitloop` prematurely terminates a `foreach` loop
- Check how many students with B in Maths confirm the hypothesis
- Finally check `length(confirm)` against `length(confirm)+length(reject)` to decide if the hypothesis holds

```
foreach x in mathsBGrades {  
    found = False  
    foreach y in physicsAGrades {  
        if (x == y) {  
            confirm = confirm ++ [x]  
            found = True, exitloop  
        }  
    }  
    if (not(found)) {  
        foreach y in physicsBGrades {  
            if (x == y) {  
                confirm = confirm ++ [x]  
                found = True, exitloop  
            }  
        }  
    }  
    if (not(found)) {  
        reject = reject ++ [x]  
    }  
}
```

# Summary

- Sorting was used to identify quartiles for grade assignment
- Need to modify the comparison function based on the items in the list
- `length(l)` returns number of elements in `l`
- New functions to extract first and last items of a list
  - `first(l)` and `rest(l)`
  - `last(l)` and `init(l)`
- `exitloop` to abort a `foreach` loop