Data Mining: Data

Lecture Notes for Chapter 2

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Outline

- Attributes and Objects
- Types of Data
- Data Quality
- Similarity and Distance
- Data Preprocessing

What is Data?

- Collection of data objects and their attributes
- An attribute is a property or characteristic of an object
 - Examples: eye color of a person, temperature, etc.
 - Attribute is also known as variable, field, characteristic, dimension, or feature
- A collection of attributes describe an *object*
 - Object is also known as record, point, case, sample, entity, or instance

Attributes

'				
Tid	Refund	Marital Status	Taxable Income	Cheat
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

A More Complete View of Data

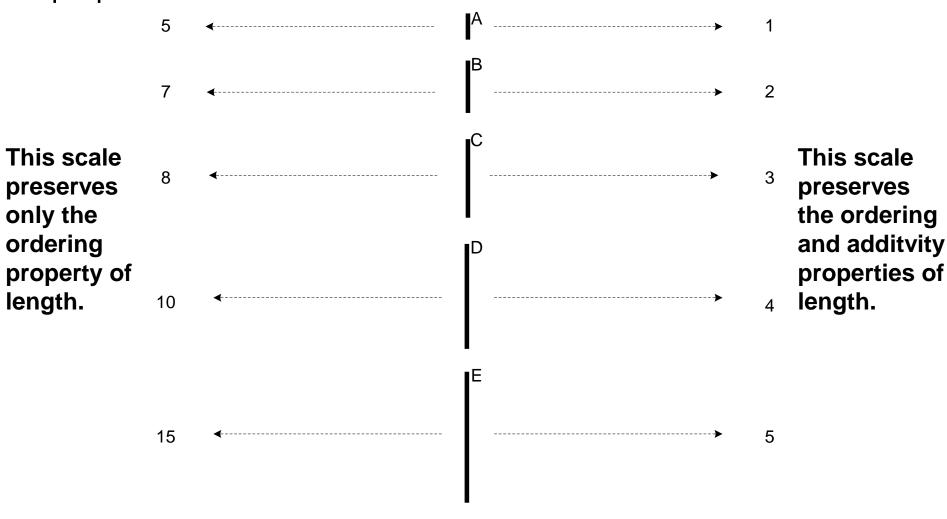
- Data may have parts
- Attributes (objects) may have relationships with other attributes (objects)
- More generally, data may have structure
- Data can be incomplete
- We will discuss this in more detail later

Attribute Values

- Attribute values are numbers or symbols assigned to an attribute for a particular object
- Distinction between attributes and attribute values
 - Same attribute can be mapped to different attribute values
 - Example: height can be measured in feet or meters
 - Different attributes can be mapped to the same set of values
 - Example: Attribute values for ID and age are integers
 - But properties of attribute values can be different

Measurement of Length

• The way you measure an attribute may not match the attributes properties.



Types of Attributes • There are different types of attributes

Nominal

Examples: ID numbers, eye color, zip codes

Ordinal

Examples: rankings (e.g., taste of potato chips on a scale from 1-10), grades, height {tall, medium, short}

Interval

Examples: calendar dates, temperatures in Celsius or Fahrenheit.

Ratio

Examples: temperature in Kelvin, length, elapsed time, counts

Properties of Attribute Values

 The type of an attribute depends on which of the following properties/operations it possesses:

- Nominal attribute: distinctness
- Ordinal attribute: distinctness & order
- Interval attribute: distinctness, order & meaningful differences
- Ratio attribute: all 4 properties/operations

Difference Between Ratio and Interval

- Is it physically meaningful to say that a temperature of 10 ° is twice that of 5° on
 - the Celsius scale?
 - the Fahrenheit scale?
 - the Kelvin scale?
- Consider measuring the height above average
 - If Bill's height is three inches above average and Bob's height is six inches above average, then would we say that Bob is twice as tall as Bill?
 - Is this situation analogous to that of temperature?

	Attribute Type	Description	Examples	Operations
Categorical Qualitative	Nominal	Nominal attribute values only distinguish. (=, ≠)	zip codes, employee ID numbers, eye color, sex: {male, female}	mode, entropy, contingency correlation, χ2 test
Cate Qua	Ordinal	Ordinal attribute values also order objects. (<, >)	hardness of minerals, {good, better, best}, grades, street numbers	median, percentiles, rank correlation, run tests, sign tests
Numeric Quantitative	Interval	For interval attributes, differences between values are meaningful. (+, -)	calendar dates, temperature in Celsius or Fahrenheit	mean, standard deviation, Pearson's correlation, t and F tests
Nu Quar	Ratio	For ratio variables, both differences and ratios are meaningful. (*, /)	temperature in Kelvin, monetary quantities, counts, age, mass, length, current	geometric mean, harmonic mean, percent variation

This categorization of attributes is due to S. S. Stevens

	Attribute Type	Transformation	Comments
cal /e	Nominal	Any permutation of values	If all employee ID numbers were reassigned, would it make any difference?
Categorical Qualitative	Ordinal	An order preserving change of values, i.e., new_value = f(old_value) where f is a monotonic function	An attribute encompassing the notion of good, better best can be represented equally well by the values {1, 2, 3} or by { 0.5, 1, 10}.
Numeric Quantitative	Interval	new_value = a * old_value + b where a and b are constants	Thus, the Fahrenheit and Celsius temperature scales differ in terms of where their zero value is and the size of a unit (degree).
_ g	Ratio	new_value = a * old_value	Length can be measured in meters or feet.

This categorization of attributes is due to S. S. Stevens

Discrete and Continuous Attributes

Discrete Attribute

- Has only a finite or countably infinite set of values
- Examples: zip codes, counts, or the set of words in a collection of documents
- Often represented as integer variables.
- Note: binary attributes are a special case of discrete attributes

Continuous Attribute

- Has real numbers as attribute values
- Examples: temperature, height, or weight.
- Practically, real values can only be measured and represented using a finite number of digits.
- Continuous attributes are typically represented as floating-point variables.

Asymmetric Attributes

- Only presence (a non-zero attribute value) is regarded as important
 - Words present in documents
 - Items present in customer transactions
- If we met a friend in the grocery store would we ever say the following?

"I see our purchases are very similar since we didn't buy most of the same things."

Asymmetric attributes typically arise from objects that are sets

Some Extensions and Critiques

- Velleman, Paul F., and Leland Wilkinson. "Nominal, ordinal, interval, and ratio typologies are misleading." The American Statistician 47, no. 1 (1993): 65-72.
- Mosteller, Frederick, and John W. Tukey. "Data analysis and regression. A second course in statistics." Addison-Wesley Series in Behavioral Science: Quantitative Methods, Reading, Mass.: Addison-Wesley, 1977.
- Chrisman, Nicholas R. "Rethinking levels of measurement for cartography." Cartography and Geographic Information Systems 25, no. 4 (1998): 231-242.

Critiques

- Incomplete
 - Asymmetric binary
 - Cyclical
 - Partially ordered

- Real data is approximate and noisy
 - This can complicate recognition of the proper attribute type
 - Treating one attribute type as another may be approximately correct

More Complicated Examples

- ID numbers
 - Nominal, ordinal?

- Number of cylinders in an automobile engine
 - Nominal, ordinal, or ratio?

Key Messages for Attribute Types

- The types of operations you choose should be "meaningful" for the type of data you have
 - Distinctness, order, meaningful intervals, and meaningful ratios are only four properties of data
 - The data type you see often numbers or strings may not capture all the properties or may suggest properties that are not present
 - Analysis may depend on these other properties of the data
 - Many statistical analyses depend only on the distribution
 - Many times what is meaningful is measured by statistical significance
 - But in the end, what is meaningful is measured by the domain

Types of data sets

- Record
 - Data Matrix
 - Document Data
 - Transaction Data
- Graph
 - World Wide Web
 - Molecular Structures
- Ordered
 - Spatial Data
 - Temporal Data
 - Sequential Data
 - Genetic Sequence Data

Important Characteristics of Data

- Dimensionality (number of attributes)
 - High dimensional data brings a number of challenges
- Sparsity
 - Only presence counts
- Resolution
 - Patterns depend on the scale
- Size
 - Type of analysis may depend on size of data

Record Data

 Data that consists of a collection of records, each of which consists of a fixed set of attributes

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1	Yes	Single	125K	No
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3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
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7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

Data Matrix

- If data objects have the same fixed set of numeric attributes, then the data objects can be thought of as points in a multidimensional space, where each dimension represents a distinct attribute
- Such a data set can be represented by an m by n matrix, where there are m rows, one for each object, and n columns, one for each attribute

Projection of x Load	Projection of y load	Distance	Load	Thickness
10.23	5.27	15.22	2.7	1.2
12.65	6.25	16.22	2.2	1.1

Document Data

- Each document becomes a 'term' vector
 - Each term is a component (attribute) of the vector
 - The value of each component is the number of times the corresponding term occurs in the document.

	team	coach	play	ball	score	game	win	lost	timeout	season
Document 1	3	0	5	0	2	6	0	2	0	2
Document 2	0	7	0	2	1	0	0	3	0	0
Document 3	0	1	0	0	1	2	2	0	3	0

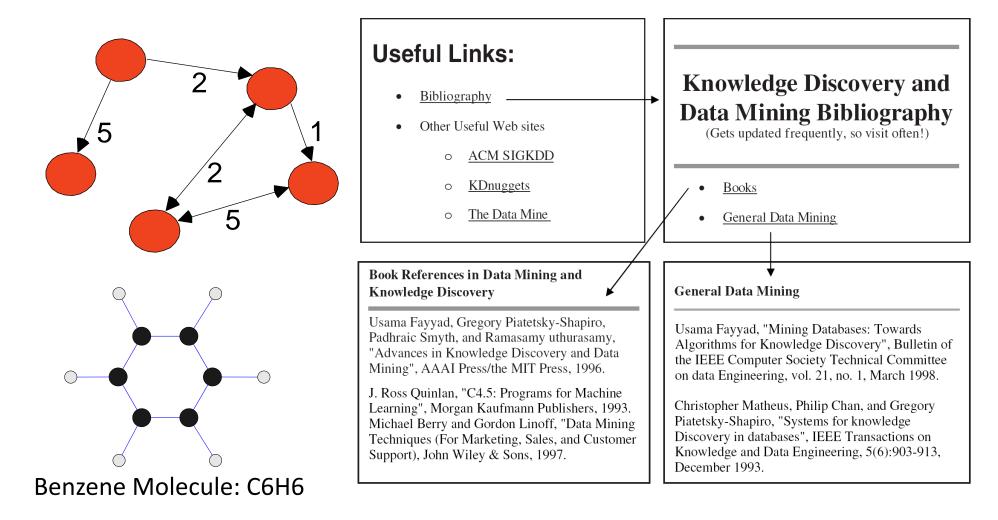
Transaction Data

- A special type of data, where
 - Each transaction involves a set of items.
 - For example, consider a grocery store. The set of products purchased by a customer during one shopping trip constitute a transaction, while the individual products that were purchased are the items.
 - Can represent transaction data as record data

TID	Items
1	Bread, Coke, Milk
2	Beer, Bread
3	Beer, Coke, Diaper, Milk
4	Beer, Bread, Diaper, Milk
5	Coke, Diaper, Milk

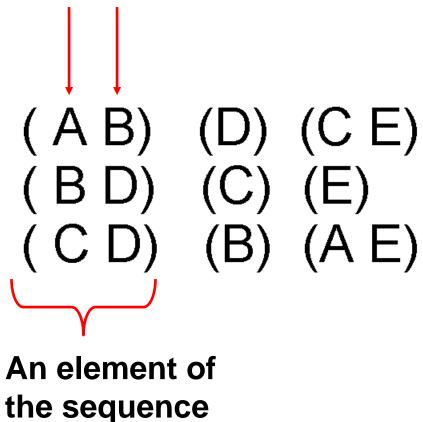
Graph Data

• Examples: Generic graph, a molecule, and webpages



Ordered Data

• Sequences of transadtems/Events



Ordered Data

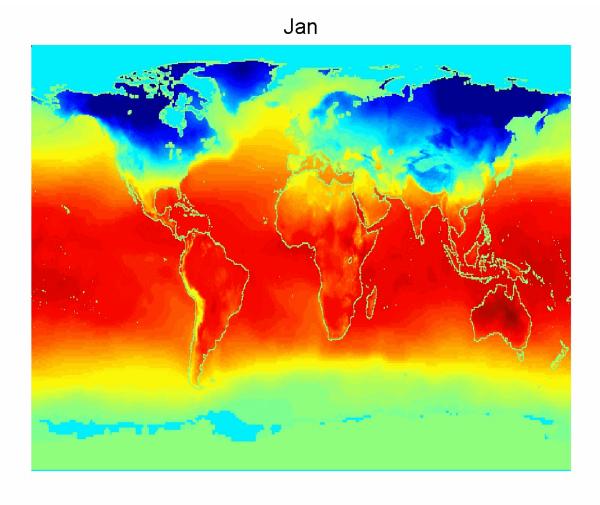
Genomic sequence data

GGTTCCGCCTTCAGCCCCGCGCC CGCAGGGCCCGCCCCGCGCGTC GAGAAGGCCCGCCTGGCGGCG GGGGGAGCCGGCCCGAGC CCAACCGAGTCCGACCAGGTGCC CCCTCTGCTCGGCCTAGACCTGA GCTCATTAGGCGGCAGCGGACAG GCCAAGTAGAACACGCGAAGCGC TGGGCTGCCTGCGACCAGGG

Ordered Data

• Spatio-Temporal Data

Average Monthly Temperature of land and ocean



Data Quality

- Poor data quality negatively affects many data processing efforts
- "The most important point is that poor data quality is an unfolding disaster.
 - Poor data quality costs the typical company at least ten percent (10%) of revenue; twenty percent (20%) is probably a better estimate."

Thomas C. Redman, DM Review, August 2004

- Data mining example: a classification model for detecting people who are loan risks is built using poor data
 - Some credit-worthy candidates are denied loans
 - More loans are given to individuals that default

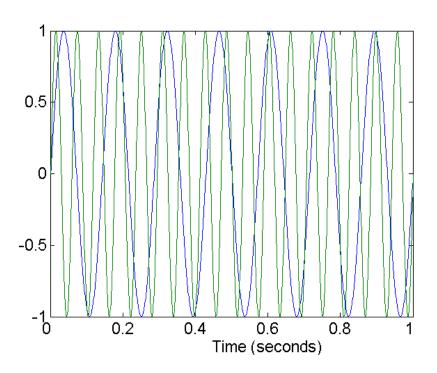
Data Quality ...

- What kinds of data quality problems?
- How can we detect problems with the data?
- What can we do about these problems?

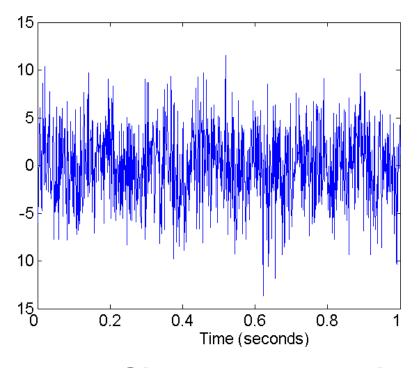
- Examples of data quality problems:
 - Noise and outliers
 - Missing values
 - Duplicate data
 - Wrong data
 - Fake data

Noise

- For objects, noise is an extraneous object
- For attributes, noise refers to modification of original values
 - Examples: distortion of a person's voice when talking on a poor phone and "snow" on television screen



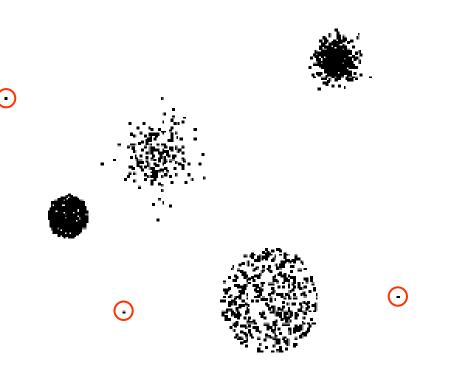
Two Sine Waves



Two Sine Waves + Noise

Outliers

- Outliers are data objects with characteristics that are considerably different than most of the other data chicate in the data cot
 - Case 1: Outliers are noise that interferes with data analysis
 - Case 2: Outliers are the goal of our analysis
 - Credit card fraud
 - Intrusion detection
- Causes?



Missing Values

- Reasons for missing values
 - Information is not collected
 (e.g., people decline to give their age and weight)
 - Attributes may not be applicable to all cases (e.g., annual income is not applicable to children)
- Handling missing values
 - Eliminate data objects or variables
 - Estimate missing values
 - Example: time series of temperature
 - Example: census results
 - Ignore the missing value during analysis

Missing Values ...

- Missing completely at random (MCAR)
 - Missingness of a value is independent of attributes
 - Fill in values based on the attribute
 - Analysis may be unbiased overall
- Missing at Random (MAR)
 - Missingness is related to other variables
 - Fill in values based other values
 - Almost always produces a bias in the analysis
- Missing Not at Random (MNAR)
 - Missingness is related to unobserved measurements
 - Informative or non-ignorable missingness
- Not possible to know the situation from the data

Duplicate Data

- Data set may include data objects that are duplicates, or almost duplicates of one another
 - Major issue when merging data from heterogeneous sources
- Examples:
 - Same person with multiple email addresses
- Data cleaning
 - Process of dealing with duplicate data issues
- When should duplicate data not be removed?

Similarity and Dissimilarity Measures

- Similarity measure
 - Numerical measure of how alike two data objects are.
 - Is higher when objects are more alike.
 - Often falls in the range [0,1]
- Dissimilarity measure
 - Numerical measure of how different two data objects are
 - Lower when objects are more alike
 - Minimum dissimilarity is often 0
 - Upper limit varies
- Proximity refers to a similarity or dissimilarity

Similarity/Dissimilarity for Simple Attributes

The following table shows the similarity and dissimilarity between two objects, *x* and *y*, with respect to a single, simple attribute.

Attribute	Dissimilarity	Similarity		
Type				
Nominal	$d = \begin{cases} 0 & \text{if } x = y \\ 1 & \text{if } x \neq y \end{cases}$	$s = \begin{cases} 1 & \text{if } x = y \\ 0 & \text{if } x \neq y \end{cases}$		
Ordinal	d = x - y /(n - 1) (values mapped to integers 0 to $n-1$, where n is the number of values)	s = 1 - d		
Interval or Ratio	d = x - y	$s = -d, s = \frac{1}{1+d}, s = e^{-d},$ $s = 1 - \frac{d - min \cdot d}{max \cdot d - min \cdot d}$		
		$s = 1 - \frac{a \cdot min_a}{max_d - min_d}$		

Euclidean Distance

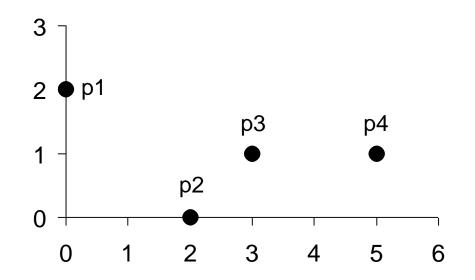
Euclidean Distance

$$d(\mathbf{x}, \mathbf{y}) = \sqrt{\sum_{k=1}^{n} (x_k - y_k)^2}$$

where n is the number of dimensions (attributes) and x_k and y_k are, respectively, the k^{th} attributes (components) or data objects \mathbf{x} and \mathbf{y} .

Standardization is necessary, if scales differ.

Euclidean Distance



point	X	y
p1	0	2
p2	2	0
р3	3	1
p4	5	1

	p1	p2	р3	p4
p1	0	2.828	3.162	5.099
p2	2.828	0	1.414	3.162
p3	3.162	1.414	0	2
p4	5.099	3.162	2	0

Distance Matrix

Minkowski Distance

Minkowski Distance is a generalization of Euclidean Distance

Where r is a parameter, n is the number of dimensions (attributes) and x_k and y_k are, respectively, the k^{th} attributes (components) or data objects x and y.

$$d(\mathbf{x}, \mathbf{y}) = \left(\sum_{k=1}^{n} |x_k - y_k|^r\right)^{1/r}$$

Minkowski Distance: Examples

- r = 1. City block (Manhattan, taxicab, L_1 norm) distance.
 - A common example of this for binary vectors is the Hamming distance, which is just the number of bits that are different between two binary vectors
- r = 2. Euclidean distance
- $r \to \infty$. "supremum" (L_{max} norm, L_{∞} norm) distance.
 - This is the maximum difference between any component of the vectors
- Do not confuse *r* with *n*, i.e., all these distances are defined for all numbers of dimensions.

Minkowski Distance

point	X	y
p1	0	2
p2	2	0
р3	3	1
p4	5	1

L1	p1	p2	р3	p4
p1	0	4	4	6
p2	4	0	2	4
р3	4	2	0	2
p4	6	4	2	0

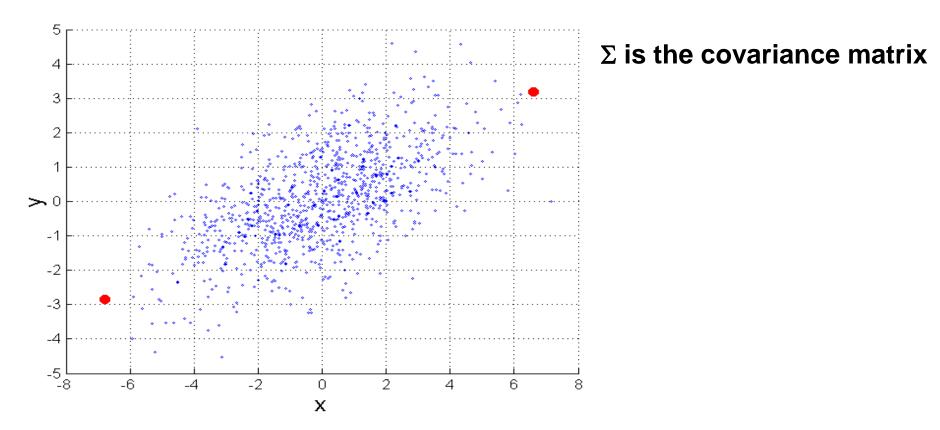
L2	p1	p2	р3	p4
p1	0	2.828	3.162	5.099
p2	2.828	0	1.414	3.162
р3	3.162	1.414	0	2
p4	5.099	3.162	2	0

L_{∞}	p1	p2	р3	p4
p1	0	2	3	5
p2	2	0	1	3
р3	3	1	0	2
p4	5	3	2	0

Distance Matrix

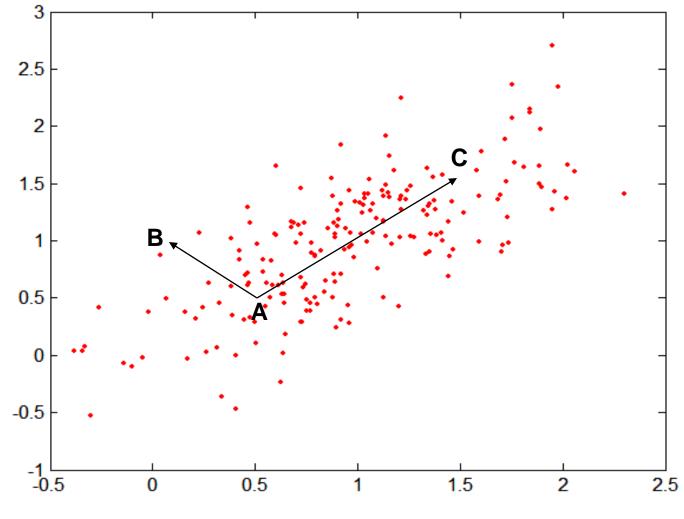
Mahalanobis Distance

mahalanobis(x, y) =
$$(x - y)^T \Sigma^{-1}(x - y)$$



For red points, the Euclidean distance is 14.7, Mahalanobis distance is 6.

Mahalanobis Distance



Covariance Matrix:

$$\Sigma = \begin{bmatrix} 0.3 & 0.2 \\ 0.2 & 0.3 \end{bmatrix}$$

A: (0.5, 0.5)

B: (0, 1)

C: (1.5, 1.5)

Mahal(A,B) = 5

Mahal(A,C) = 4

Common Properties of a Distance

- Distances, such as the Euclidean distance, have some well known properties.
 - 1. $d(\mathbf{x}, \mathbf{y}) \ge 0$ for all \mathbf{x} and \mathbf{y} and $d(\mathbf{x}, \mathbf{y}) = 0$ only if $\mathbf{x} = \mathbf{y}$. (Positive definiteness)
 - 2. $d(\mathbf{x}, \mathbf{y}) = d(\mathbf{y}, \mathbf{x})$ for all \mathbf{x} and \mathbf{y} . (Symmetry)
 - 3. $d(\mathbf{x}, \mathbf{z}) \le d(\mathbf{x}, \mathbf{y}) + d(\mathbf{y}, \mathbf{z})$ for all points \mathbf{x} , \mathbf{y} , and \mathbf{z} . (Triangle Inequality)

where $d(\mathbf{x}, \mathbf{y})$ is the distance (dissimilarity) between points (data objects), \mathbf{x} and \mathbf{y} .

A distance that satisfies these properties is a metric

Common Properties of a Similarity

- Similarities, also have some well known properties.
 - 1. $s(\mathbf{x}, \mathbf{y}) = 1$ (or maximum similarity) only if $\mathbf{x} = \mathbf{y}$.
 - 2. $s(\mathbf{x}, \mathbf{y}) = s(\mathbf{y}, \mathbf{x})$ for all \mathbf{x} and \mathbf{y} . (Symmetry)

where $s(\mathbf{x}, \mathbf{y})$ is the similarity between points (data objects), \mathbf{x} and \mathbf{y} .

Similarity Between Binary Vectors

- Common situation is that objects, x and y, have only binary attributes
- Compute similarities using the following quantities f_{01} = the number of attributes where \mathbf{x} was 0 and \mathbf{y} was 1 f_{10} = the number of attributes where \mathbf{x} was 1 and \mathbf{y} was 0 f_{00} = the number of attributes where \mathbf{x} was 0 and \mathbf{y} was 0 f_{11} = the number of attributes where \mathbf{x} was 1 and \mathbf{y} was 1
- Simple Matching and Jaccard Coefficients SMC = number of matches / number of attributes = $(f_{11} + f_{00}) / (f_{01} + f_{10} + f_{11} + f_{00})$
 - J = number of 11 matches / number of non-zero attributes = $(f_{11}) / (f_{01} + f_{10} + f_{11})$

SMC versus Jaccard: Example

$$\mathbf{x} = 10000000000$$

 $\mathbf{y} = 0000001001$

- $f_{01} = 2$ (the number of attributes where **x** was 0 and **y** was 1)
- $f_{10} = 1$ (the number of attributes where **x** was 1 and **y** was 0)
- $f_{00} = 7$ (the number of attributes where **x** was 0 and **y** was 0)
- $f_{11} = 0$ (the number of attributes where **x** was 1 and **y** was 1)

SMC =
$$(f_{11} + f_{00}) / (f_{01} + f_{10} + f_{11} + f_{00})$$

= $(0+7) / (2+1+0+7) = 0.7$

$$J = (f_{11}) / (f_{01} + f_{10} + f_{11}) = 0 / (2 + 1 + 0) = 0$$

Cosine Similarity

• If \mathbf{d}_1 and \mathbf{d}_2 are two document vectors, then

$$\cos(\mathbf{d_1}, \mathbf{d_2}) = \langle \mathbf{d_1}, \mathbf{d_2} \rangle / \|\mathbf{d_1}\| \|\mathbf{d_2}\|,$$

where $<\mathbf{d_1},\mathbf{d_2}>$ indicates inner product or vector dot product of vectors, $\mathbf{d_1}$ and $\mathbf{d_2}$ and $\parallel \mathbf{d} \parallel$ is the length of vector \mathbf{d} .

• Example:

$$d_1 = 3205000200$$

$$d_2 = 1000000102$$

$$<\mathbf{d_1}, \mathbf{d2}> = 3*1 + 2*0 + 0*0 + 5*0 + 0*0 + 0*0 + 0*0 + 2*1 + 0*0 + 0*2 = 5$$
 $|\mathbf{d_1}|| = (3*3+2*2+0*0+5*5+0*0+0*0+0*0+2*2+0*0+0*0)^{\mathbf{0.5}} = (42)^{\mathbf{0.5}} = 6.481$
 $||\mathbf{d_2}|| = (1*1+0*0+0*0+0*0+0*0+0*0+0*0+1*1+0*0+2*2)^{\mathbf{0.5}} = (6)^{\mathbf{0.5}} = 2.449$
 $\cos(\mathbf{d_1}, \mathbf{d_2}) = 0.3150$

Correlation measures the linear relationship between objects

$$corr(\mathbf{x}, \mathbf{y}) = \frac{covariance(\mathbf{x}, \mathbf{y})}{standard_deviation(\mathbf{x}) * standard_deviation(\mathbf{y})} = \frac{s_{xy}}{s_x s_y}, (2.11)$$

where we are using the following standard statistical notation and definitions

covariance(
$$\mathbf{x}, \mathbf{y}$$
) = $s_{xy} = \frac{1}{n-1} \sum_{k=1}^{n} (x_k - \overline{x})(y_k - \overline{y})$ (2.12)

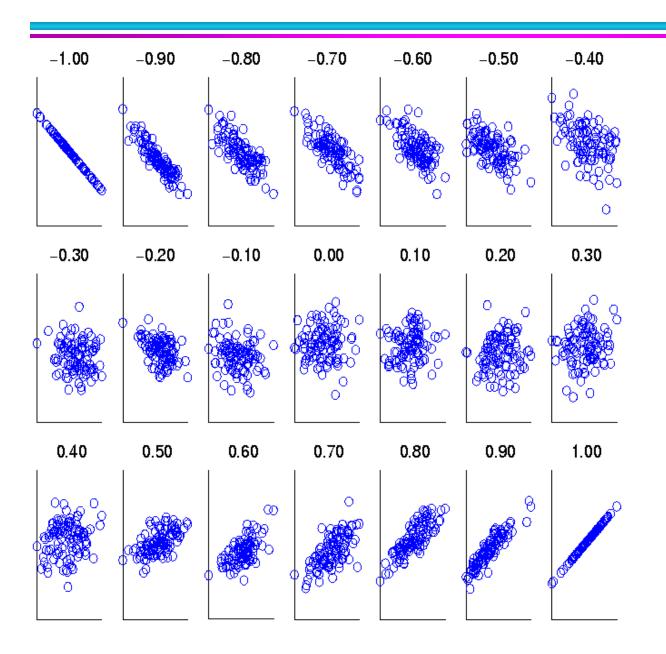
standard_deviation(
$$\mathbf{x}$$
) = $s_x = \sqrt{\frac{1}{n-1} \sum_{k=1}^{n} (x_k - \overline{x})^2}$

standard_deviation(
$$\mathbf{y}$$
) = $s_y = \sqrt{\frac{1}{n-1} \sum_{k=1}^{n} (y_k - \overline{y})^2}$

$$\overline{x} = \frac{1}{n} \sum_{k=1}^{n} x_k$$
 is the mean of \mathbf{x}

$$\overline{y} = \frac{1}{n} \sum_{k=1}^{n} y_k$$
 is the mean of \mathbf{y}

Visually Evaluating Correlation



Scatter plots showing the similarity from -1 to 1.

Drawback of Correlation

- $\mathbf{x} = (-3, -2, -1, 0, 1, 2, 3)$
- $\mathbf{y} = (9, 4, 1, 0, 1, 4, 9)$

$$y_i = x_i^2$$

- $mean(\mathbf{x}) = 0$, $mean(\mathbf{y}) = 4$
- $std(\mathbf{x}) = 2.16$, $std(\mathbf{y}) = 3.74$

•
$$corr = (-3)(5) + (-2)(0) + (-1)(-3) + (0)(-4) + (1)(-3) + (2)(0) + 3(5) / (6 * 2.16 * 3.74)$$

= 0

Comparison of Proximity Measures

- Domain of application
 - Similarity measures tend to be specific to the type of attribute and data
 - Record data, images, graphs, sequences, 3D-protein structure, etc. tend to have different measures
- However, one can talk about various properties that you would like a proximity measure to have
 - Symmetry is a common one
 - Tolerance to noise and outliers is another
 - Ability to find more types of patterns?
 - Many others possible
- The measure must be applicable to the data and produce results that agree with domain knowledge

General Approach for Combining Similarities

- Sometimes attributes are of many different types, but an overall similarity is needed.
- 1: For the k^{th} attribute, compute a similarity, $s_k(\mathbf{x}, \mathbf{y})$, in the range [0, 1].
- 2: Define an indicator variable, δ_k , for the k^{th} attribute as follows:
 - δ_k = 0 if the k^{th} attribute is an asymmetric attribute and both objects have a value of 0, or if one of the objects has a missing value for the kth attribute
 - δ_k = 1 otherwise
- 3. Compute

similarity(
$$\mathbf{x}, \mathbf{y}$$
) = $\frac{\sum_{k=1}^{n} \delta_k s_k(\mathbf{x}, \mathbf{y})}{\sum_{k=1}^{n} \delta_k}$

Using Weights to Combine Similarities

- May not want to treat all attributes the same.
 - Use non-negative weights $\,\omega_k\,$

•
$$similarity(\mathbf{x}, \mathbf{y}) = \frac{\sum_{k=1}^{n} \omega_k \delta_k s_k(\mathbf{x}, \mathbf{y})}{\sum_{k=1}^{n} \omega_k \delta_k}$$

• Can also define a weighted form of distance

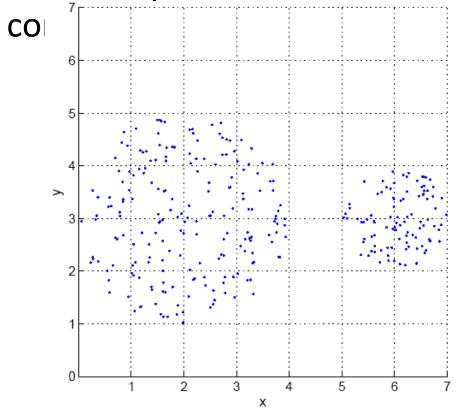
$$d(\mathbf{x}, \mathbf{y}) = \left(\sum_{k=1}^{n} w_k |x_k - y_k|^r\right)^{1/r}$$

Density

- Measures the degree to which data objects are close to each other in a specified area
- The notion of density is closely related to that of proximity
- Concept of density is typically used for clustering and anomaly detection
- Examples:
 - Euclidean density
 - Euclidean density = number of points per unit volume
 - Probability density
 - Estimate what the distribution of the data looks like
 - Graph-based density
 - Connectivity

Euclidean Density: Grid-based Approach

 Simplest approach is to divide region into a number of rectangular cells of equal volume and define density as # of points the cell



0	0	0	0	0	0	0
0	0	0	0	0	0	0
4	17	18	6	0	0	0
14	14	13	13	0	18	27
11	18	10	21	0	24	31
3	20	14	4	0	0	0
0	0	0	0	0	0	0

Euclidean Density: Center-Based

 Euclidean density is the number of points within a specified radius of the point

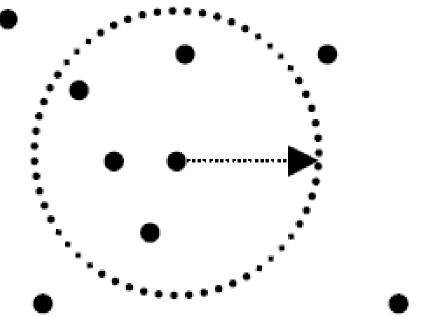


Illustration of center-based density.

Data Preprocessing

- Aggregation
- Sampling
- Dimensionality Reduction
- Feature subset selection
- Feature creation
- Discretization and Binarization
- Attribute Transformation

Discretization

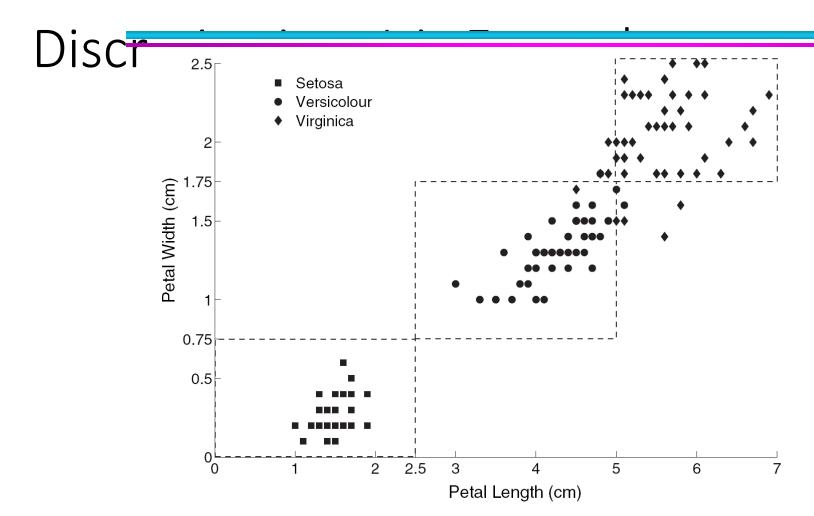
- Discretization is the process of converting a continuous attribute into an ordinal attribute
 - A potentially infinite number of values are mapped into a small number of categories
 - Discretization is commonly used in classification
 - Many classification algorithms work best if both the independent and dependent variables have only a few values
 - We give an illustration of the usefulness of discretization using the Iris data set

Iris Sample Data Set

- Iris Plant data set.
 - Can be obtained from the UCI Machine Learning Repository http://www.ics.uci.edu/~mlearn/MLRepository.html
 - From the statistician Douglas Fisher
 - Three flower types (classes):
 - Setosa
 - Versicolour
 - Virginica
 - Four (non-class) attributes
 - · Sepal width and length
 - · Petal width and length



Virginica. Robert H. Mohlenbrock. USDA NRCS. 1995. Northeast wetland flora: Field office guide to plant species. Northeast National Technical Center, Chester, PA.



Petal width low or petal length low implies Setosa.

Petal width medium or petal length medium implies Versicolour.

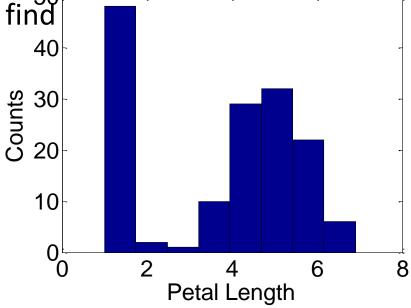
Petal width high or petal length high implies Virginica.

Discretization: iris Example ...

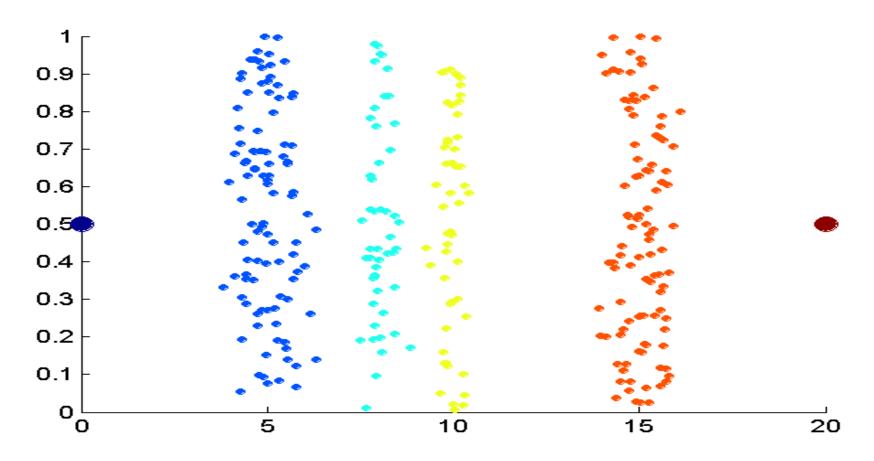
How can we tell what the best discretization is?

Unsupervised discretization: find

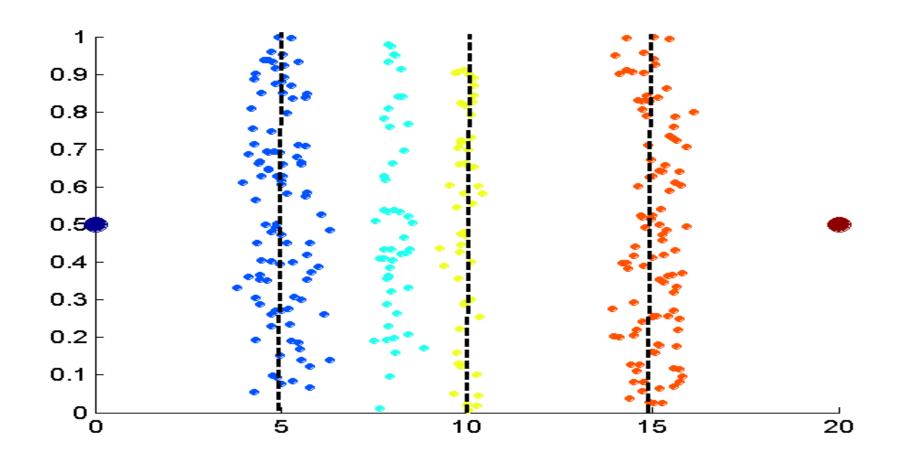
• Example: Petal Length



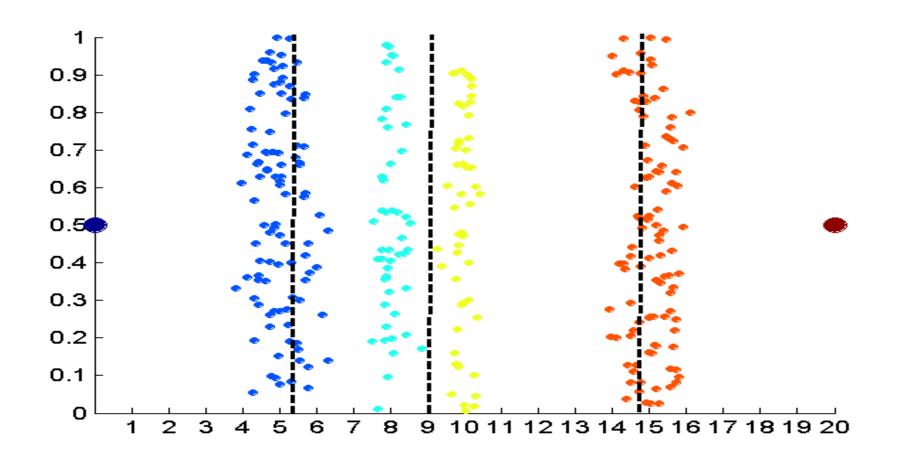
Supervised discretization: Use class labels to find breaks



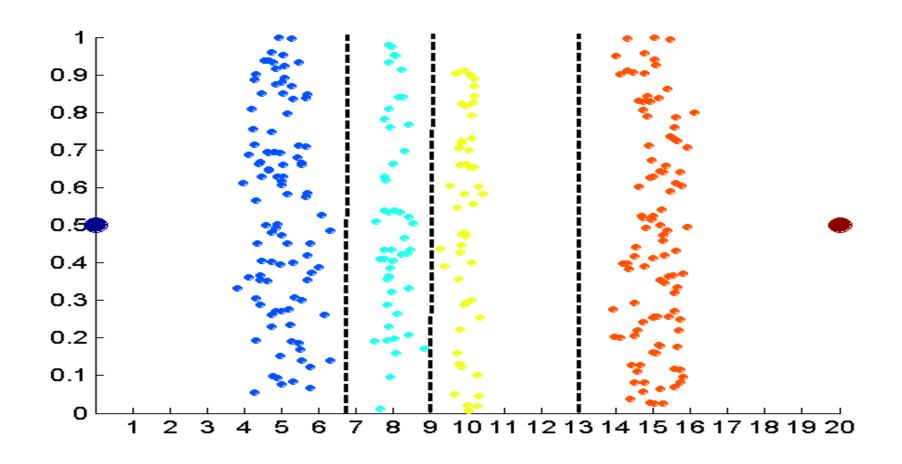
Data consists of four groups of points and two outliers. Data is onedimensional, but a random y component is added to reduce overlap.



Equal interval width approach used to obtain 4 values.



Equal frequency approach used to obtain 4 values.



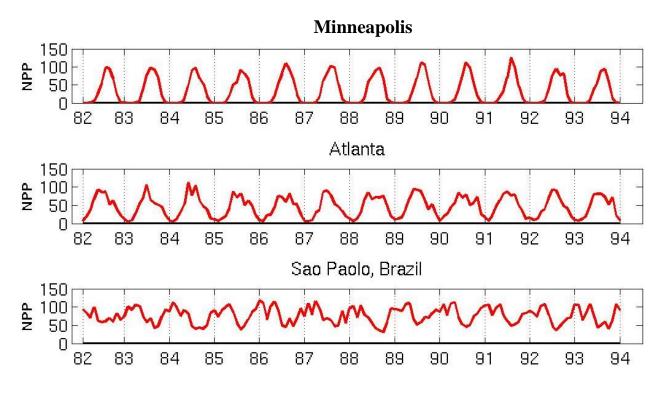
K-means approach to obtain 4 values.

Binarization

- Binarization maps a continuous or categorical attribute into one or more binary variables
- Typically used for association analysis
- Often convert a continuous attribute to a categorical attribute and then convert a categorical attribute to a set of binary attributes
 - Association analysis needs asymmetric binary attributes
 - Examples: eye color and height measured as {low, medium, high}

- Attribute Transformation
 An attribute transform is a function that maps the entire set of values of a given attribute to a new set of replacement values such that each old value can be identified with one of the new values
 - Simple functions: x^k, log(x), e^x, |x|
 - Normalization
 - Refers to various techniques to adjust to differences among attributes in terms of frequency of occurrence, mean, variance, range
 - Take out unwanted, common signal, e.g., seasonality
 - In statistics, standardization refers to subtracting off the means and dividing by the standard deviation

Example: Sample Time Series of Plant Growth

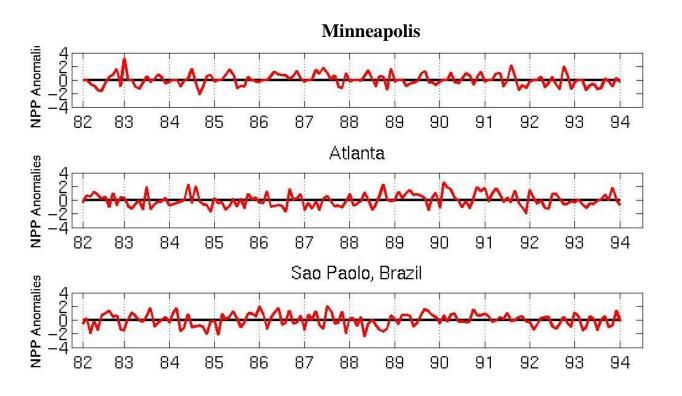


Net Primary
Production (NPP)
is a measure of
plant growth used
by ecosystem
scientists.

Correlations between time series

	Minneapolis	Atlanta	Sao Paolo
Minneapolis	1.0000	0.7591	-0.7581
Atlanta	0.7591	1.0000	-0.5739
Sao Paolo	-0.7581	-0.5739	1.0000

Seasonality Accounts for Much Correlation



Normalized using monthly Z Score:

Subtract off monthly mean and divide by monthly standard deviation

Correlations between time series

	Minneapolis	Atlanta	Sao Paolo
Minneapolis	1.0000	0.0492	0.0906
Atlanta	0.0492	1.0000	-0.0154
Sao Paolo	0.0906	-0.0154	1.0000

Aggregation

 Combining two or more attributes (or objects) into a single attribute (or object)

- Purpose
 - Data reduction
 - Reduce the number of attributes or objects
 - Change of scale
 - Cities aggregated into regions, states, countries, etc.
 - Days aggregated into weeks, months, or years
 - More "stable" data
 - Aggregated data tends to have less variability

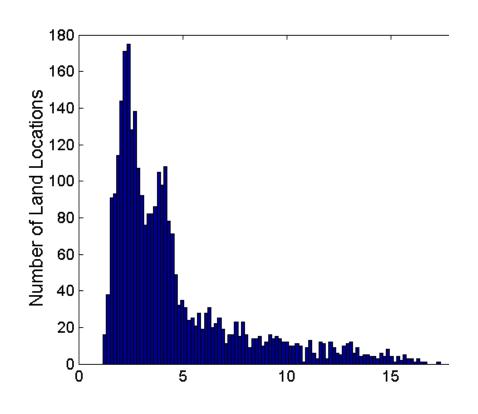
Example: Precipitation in Australia

 This example is based on precipitation in Australia from the period 1982 to 1993.

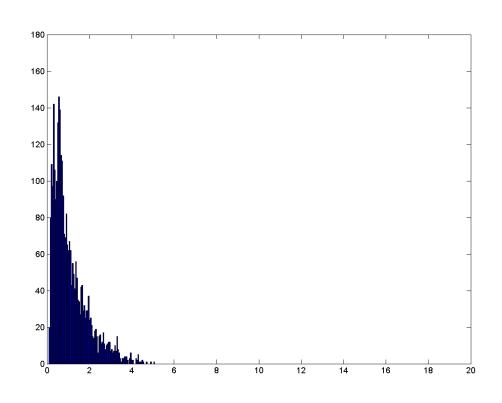
The next slide shows

- A histogram for the standard deviation of average monthly precipitation for 3,030 0.5° by 0.5° grid cells in Australia, and
- A histogram for the standard deviation of the average yearly precipitation for the same locations.
- The average yearly precipitation has less variability than the average monthly precipitation.
- All precipitation measurements (and their standard deviations) are in centimeters.

Example: Precipitation in Australia ... Variation of Precipitation in Australia



Standard Deviation of Average Monthly Precipitation



Standard Deviation of Average Yearly Precipitation

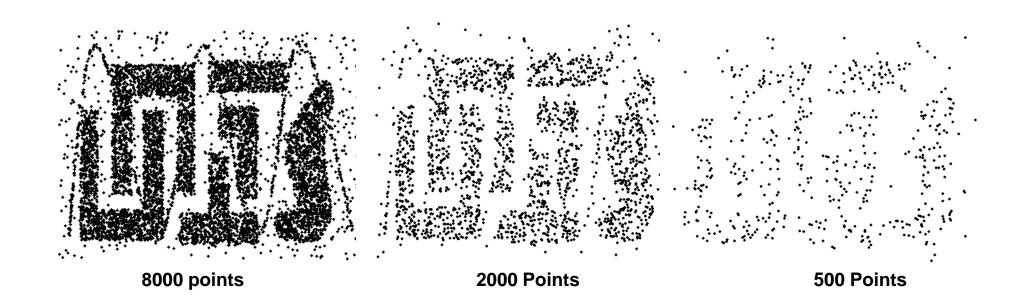
Sampling

- Sampling is the main technique employed for data reduction.
 - It is often used for both the preliminary investigation of the data and the final data analysis.
- Statisticians often sample because obtaining the entire set of data of interest is too expensive or time consuming.
- Sampling is typically used in data mining because processing the entire set of data of interest is too expensive or time consuming.

Sampling ...

- The key principle for effective sampling is the following:
 - Using a sample will work almost as well as using the entire data set, if the sample is representative
 - A sample is representative if it has approximately the same properties (of interest) as the original set of data

Sample Size

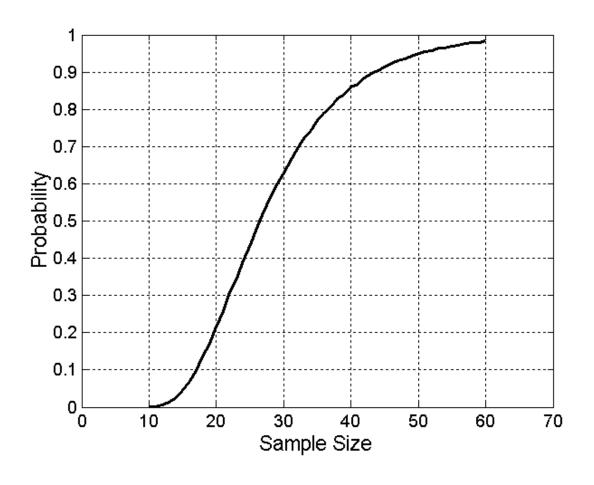


Types of Sampling mpling

- There is an equal probability of selecting any particular item
- Sampling without replacement
 - As each item is selected, it is removed from the population
- Sampling with replacement
 - Objects are not removed from the population as they are selected for the sample.
 - In sampling with replacement, the same object can be picked up more than once
- Stratified sampling
 - Split the data into several partitions; then draw random samples from each partition

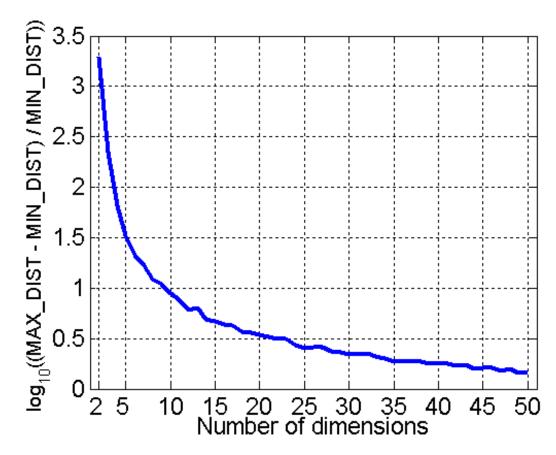
Sample Size

• What sample size is necessary to get at least one object from each of 10 equal-sized groups.



Curse of Dimensionality

- When dimensionality increases, data becomes increasingly sparse in the space that it occupies
- Definitions of density and distance between points, which are critical for clustering and outlier detection, become less meaningful



- Randomly generate 500 points
- Compute difference between max and min distance between any pair of points

Dimensionality Reduction

• Purpose:

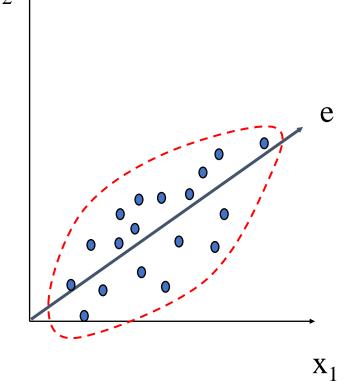
- Avoid curse of dimensionality
- Reduce amount of time and memory required by data mining algorithms
- Allow data to be more easily visualized
- May help to eliminate irrelevant features or reduce noise

Techniques

- Principal Components Analysis (PCA)
- Singular Value Decomposition
- Others: supervised and non-linear techniques

Dimensionality Reduction: PCA

• Goal is to find a projection that captures the largest amount of variation in data $_{x_{\gamma}}$ \uparrow



Dimensionality Reduction: PCA 256



Feature Subset Selection

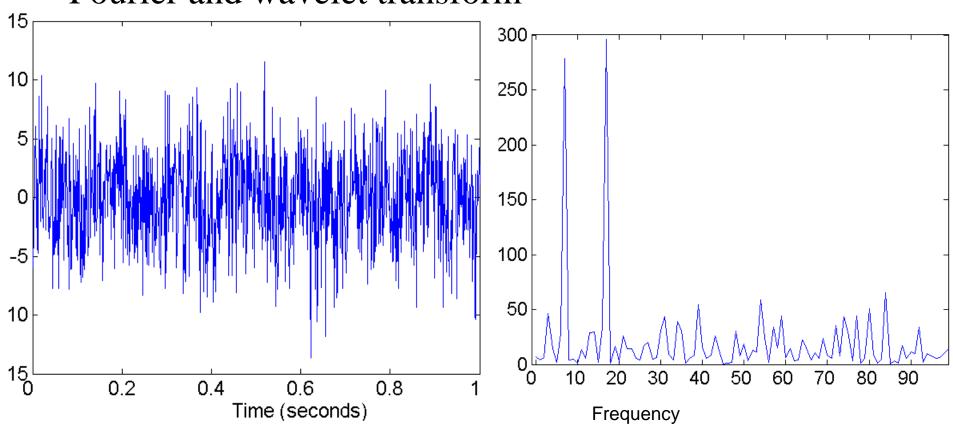
- Another way to reduce dimensionality of data
- Redundant features
 - Duplicate much or all of the information contained in one or more other attributes
 - Example: purchase price of a product and the amount of sales tax paid
- Irrelevant features
 - Contain no information that is useful for the data mining task at hand
 - Example: students' ID is often irrelevant to the task of predicting students'
 GPA
- Many techniques developed, especially for classification

Feature Creation

- Create new attributes that can capture the important information in a data set much more efficiently than the original attributes
- Three general methodologies:
 - Feature extraction
 - Example: extracting edges from images
 - Feature construction
 - Example: dividing mass by volume to get density
 - Mapping data to new space
 - Example: Fourier and wavelet analysis

Mapping Data to a New Space

Fourier and wavelet transform



Two Sine Waves + Noise

Frequency