If we want to eliminate the lost update problem and also not execute the transactions in strict modem, we can use a list or a hash-map to store the before images. On the basis of ACA, the before image of a variable is only updated when a transaction which writes to this variable is committed.

If we have transactions T1 and T2 with the following history

initial before images: x = 1, y = 0

T1 T2 before image

w1(x, 2); x = 1, y = 0

w2(x, 8);

w2(y, 9);

c2; x = 8, y = 9

w1(y, 3);

a1 x = 8, y = 9

Thus, when T1 aborts, x and y are recovered using the before images, T2’s updates are not lost. Also, T2 is permitted to overwrite the uncommitted data by T1, thus this execution is not in strict mode.

2a.

h0(x) = x mod 4, h1(x) = x mod 8

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Bucket # | 0 | 1 (B\_split) | 2 | 3 | 4 (B\_last) |
|  | 4 |  | 2 | 3 |  |
|  |  |  | 6 | 7 |  |
|  |  |  | 14 |  |  |

Overflow: 18

h0(x) = x mod 4, h1(x) = x mod 8

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| Bucket # | 0 | 1 | 2 (B\_split) | 3 | 4 | 5 (B\_last) |
|  | 4 | 9 | 2 | 3 |  |  |
|  |  |  | 6 | 7 |  |  |
|  |  |  | 14 | 19 |  |  |

Overflow: 18 11

2b.

table after splits under no overflow buckets:

**s = 4, h0(x) = x mod 4, h1(x) = x mod 8**

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Bucket # | 0 | 1 (B\_split) | 2 | 3 | 4 (B\_last) |
|  |  |  | 2 | 3 | 4 |
|  |  |  | 6 | 7 |  |
|  |  |  | 14 |  |  |

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| Bucket # | 0 | 1 | 2 (B\_split) | 3 | 4 | 5 (B\_last) |
|  |  |  | 2 | 3 | 4 |  |
|  |  |  | 6 | 7 |  |  |
|  |  |  | 14 |  |  |  |

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| Bucket # | 0 | 1 | 2 | 3 (B\_split) | 4 | 5 | 6 (B\_last) |
|  |  |  | 2 | 3 | 4 |  | 6 |
|  |  |  | 18 | 7 |  |  | 14 |
|  |  |  |  |  |  |  |  |

**s = 8, h0(x) = x mod 8, h1(x) = x mod 16**

|  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- |
| Bucket # | 0 (B\_split) | 1 | 2 | 3 | 4 | 5 | 6 | 7 (B\_last) |
|  |  | 9 | 2 | 3 | 4 |  | 6 | 7 |
|  |  |  | 18 | 19 |  |  | 14 |  |
|  |  |  |  | 11 |  |  |  |  |

In terms of **insertion** with no collisions, linear bucket with overflow buckets has an amortized efficiency of O(1). This is the same with linear hashing without overflow bucket, since no duplicate hash values occur and the split pointer is not moved.

During insertions with collisions, if the overflow bucket is far ahead from the split point, overflow bucket will delay the split, thus insertion is still O(1). A few split operations will trigger the freeing of an overflow bucket, causing an O(k) operation of rehashing where k is the size of the overflow bucket.

If not using overflow buckets, many insertions might cause an O(S) split time, where S is the hash key value. Split time is O(S) since the filled bucket has to constantly wait for the split pointer to reach its index, especially when multiples of a value are inserted over and over. Thus, the amortized insertion efficiency with overflow buckets is definitely superior to the that without overflow buckets.

While **Searching,** linear hashing without overflow bucket has a superior runtime since every queried data is guaranteed to be one of the records in some bucket. If we consider the number of records as a constant number, then this operation is O(1). Linear hashing with overflow buckets on the other hand, might cause a probing operation through the overflow buckets list. This might result in a linear runtime on average if significant data are stored in overflow buckets.

delete with/without compaction

The **split frequency** of linear hashing without overflow buckets is higher than linear hashing with buckets. If without overflow buckets, split pointer will have to keep moving until it reaches the index where the collision happens. If overflow buckets are used, then it is guaranteed that only one split operation will be performed upon a collision. Thus, more splits happen for linear hashing without overflow buckets than with overflow buckets.

The i**nternal fragmentation** of linear hashing without overflow buckets is more than with overflow buckets. As discussed in previous paragraphs, some collisions cause the split pointer to move to their indices. During this process, the split pointer skips over a lot of buckets, leading to a long expansion of the bucket list which has many empty buckets. If overflow buckets are used, only one split will happen per collision so not too many empty buckets will be created.

The **number of pointers** in linear hashing without overflow buckets is less than that with overflow buckets since overflow buckets of each bucket is a linked-list of buckets. Every newly overflow bucket will increase the number of pointer by 1.

3.

1