

# Enhancing Domain Word Embedding via Latent Semantic Imputation

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#### Outline

Word Embedding and issues.

How to fuse different data sources in word embedding?

Problem Definition.

Model and Analysis.

Empirical Study.

Conclusions.

### Word Representation Learning

# Unsupervised / Self-supervised Learning on Corpora

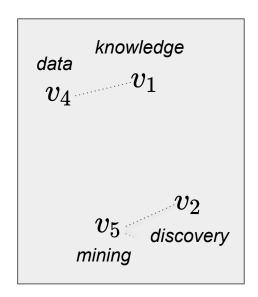


Word2Vec

Glove

FastText

**Matrix Factorization** 



#### Issues

Limited-size corpus

Low-frequency domain words

Out-of-vocabulary words

# into word embedding?

How to fuse different data sources

# Example in Chemistry and Medicine

ethanol  $v_1$ 

calcium carbonate  $-v_2$ 

potassium  $v_3$ 

.



|                      | State of mass | organic<br>? | metal<br>? |  |
|----------------------|---------------|--------------|------------|--|
| ethanol              | liquid        | 1            | 0          |  |
| calcium<br>carbonate | solid         | 0            | 0          |  |
| potassium            | solid         | 0            | 1          |  |
|                      |               |              |            |  |

**Semantic Space** 

 $\mathbb{R}^{S}$ 

**Domain Data** 

 $\mathbb{R}^D$ 

# **Example in Financial Text**

nvidia  $v_1$ 

qualcomm  $v_2$ 

google  $v_3$ 

•



|          | Return<br>of day1 | Return of day2 | <br>Return<br>of dayD |
|----------|-------------------|----------------|-----------------------|
| nvidia   | 0.23%             | -1.21%         | <br>2.49%             |
| qualcomm | 0.34%             | -0.98%         | <br>3.07%             |
| google   | -0.11%            | -0.55%         | <br>1.86%             |
|          |                   |                |                       |

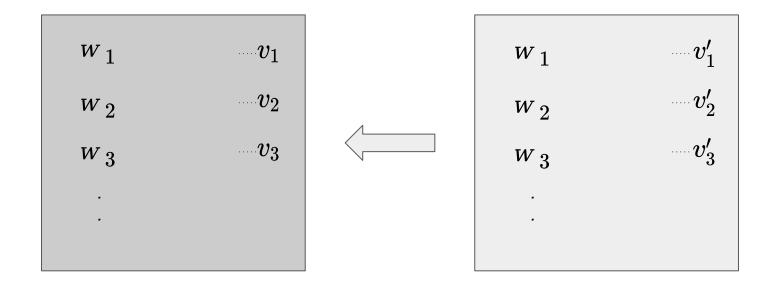
**Semantic Space** 

 $\mathbb{R}^{S}$ 

**Domain Data** 

 $\mathbb{R}^D$ 

#### **Two Semantic Spaces**



**Semantic Space A** 

 $\mathbb{R}^{A}$ 

**Semantic Space B** 

 $\mathbb{R}^{B}$ 

#### Contributions

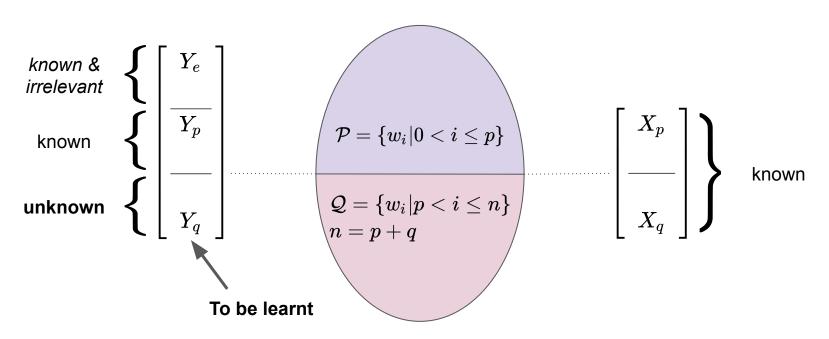
Formalize the problem of combining embeddings in different spaces.

Propose Latent Semantic Imputation to solve it.

Prove the deterministic convergence of *LSI*.

Conduct experiments to support our arguments.

#### **Problem Definition**



**Semantic Space** 

 $\mathbb{R}^{S}$ 

**Domain Data** 

 $\mathbb{R}^D$ 

#### Assumptions

The **local** geometric structures of the data points in  $\mathbb{R}^S$  and  $\mathbb{R}^D$  are the same.

ST Roweis, LK Saul. 2000 Locally Linear Embedding

$$\left[egin{array}{c} Y_p \ Y_q \end{array}
ight]$$
  $\mathcal{G}=(V,E)$   $\left[egin{array}{c} X_p \ X_q \end{array}
ight]$  To be learnt

Each data point can be represented by a linear combination of its *one-hop in-neighbors* in the graph.

#### The Model

1. Given X, build a MST-kNN Graph (0-1 Adjacency Matrix) based on Euclidean distance

2. Obtain a Weighted Adjacency Matrix

$$\|\mathbf{x}_i - \sum_j w_{ij} \mathbf{x}_j\|^2$$
 s.t.  $\sum_j w_{ij} = 1,$   $j \in \{k | (v_k, v_i) \in E\},$   $w_{ij} \geq 0$ 

$$egin{aligned} W &= egin{bmatrix} W_p \ W_q \end{bmatrix} = egin{bmatrix} W_{pp} & W_{pq} \ \hline W_{qp} & W_{qq} \end{bmatrix} \ & o egin{bmatrix} I_p & 0 \ \hline W_{qp} & W_{qq} \end{bmatrix} \end{aligned}$$

3. Power Iteration to solve Y

$$Y^{(t+1)} = WY^{(t)}$$

#### Latent Semantic Imputation guarantees Deterministic Convergence.

$$\lim_{t o\infty} \left[ egin{array}{c} Y_p^{(t)} \ Y_q^{(t)} \end{array} 
ight] = \lim_{t o\infty} W^t \left[ egin{array}{c} Y_p^{(0)} \ Y_q^{(0)} \end{array} 
ight].$$

# A High-level Proof of Convergence

W is a **Random Walk** Matrix.

$$egin{aligned} orall i, \sum_j w_{ij} &= 1 \ orall i orall j, w_{ij} &\geq 0 \end{aligned}$$

W does not have any eigenvalue of -1.

$$\forall i, -1 < \lambda_i \leq 1$$

Each dimension of Y will converge to a linear combination of W's dominant eigenvectors.

$$egin{aligned} \lim_{t o\infty} W^t ec{b} &= \lim_{t o\infty} W^t \sum_i c_i ec{v}_i \ &= \lim_{t o\infty} \sum_i c_i W^t ec{v}_i \ &= \lim_{t o\infty} \sum_i c_i \lambda_i^t ec{v}_i = \sum_k c_k ec{v}_k \end{aligned}$$

# A High-level Proof of Deterministic Convergence

$$W = \left[egin{array}{c|c} I_p & 0 \ \hline W_{qp} & W_{qq} \end{array}
ight]$$

$$W = \left[egin{array}{c|c} I_p & 0 \ \hline W_{qp} & W_{qq} \end{array}
ight] \qquad \lim_{t o\infty} Y_q^{(t)} = \lim_{t o\infty} W_{qq}^t Y_q^{(0)} + \lim_{t o\infty} [\sum_{i=0}^{t-1} W_{qq}^t] W_{qp} Y_p \ \hline W_{qq} & W_{qq} \end{array}$$

Xiaojin Zhu, Zoubin Ghahramani. 2002 Label Propagation

 $W_{qq}$  is a **Substochastic** Matrix.

$$\exists i, r_i < 1$$

In MST-kNNG, for every node in  $V_q$  there exists a path from  $V_{t}$ to it.

 $\overline{W_{qq}}$  is a **Convergent** Matrix.

$$orall i, r_i^{(t)} < 1 ~~~ \lim_{t o \infty} W_{qq}^t = 0$$

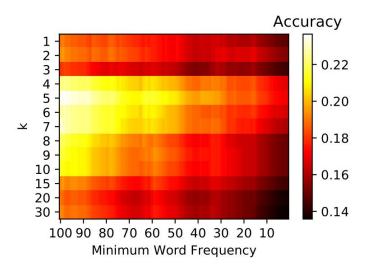
# **Empirical Study**

**Argument**: low-frequency words are associated with unreliable embedding vectors.

**Task 1**: Classification on Embedding Vectors

**Textual Data**: ~50k Wiki articles about S&P 500 companies.

(word2vec, self-trained with Tensorflow example code)



### **Empirical Study**

**Argument**: fusing a different data source can enhance word embedding.

**Task 1**: Classification on Embedding Vectors

**Domain Data**: S&P 500 company historical daily stock returns. **Pretrained embeddings**: word2vec, fastText, Glove, self-trained.

| E k          | 2     | 5     | 8     | 10    | 15    | 20    | 30    |
|--------------|-------|-------|-------|-------|-------|-------|-------|
| self         | 0.154 | 0.170 | 0.150 | 0.150 | 0.144 | 0.138 | 0.135 |
| self(hf)     | 0.180 | 0.190 | 0.172 | 0.167 | 0.157 | 0.157 | 0.157 |
| self(hf)+aff | 0.556 | 0.472 | 0.396 | 0.359 | 0.302 | 0.261 | 0.187 |
| Google       | 0.220 | 0.297 | 0.271 | 0.305 | 0.280 | 0.280 | 0.186 |
| Google+aff   | 0.838 | 0.803 | 0.784 | 0.768 | 0.725 | 0.678 | 0.626 |
| Glove        | 0.417 | 0.466 | 0.490 | 0.500 | 0.500 | 0.505 | 0.451 |
| Glove+aff    | 0.832 | 0.766 | 0.690 | 0.653 | 0.606 | 0.542 | 0.405 |
| fast         | 0.443 | 0.496 | 0.527 | 0.500 | 0.511 | 0.470 | 0.447 |
| fast+aff     | 0.811 | 0.749 | 0.713 | 0.684 | 0.641 | 0.608 | 0.595 |

#### **Empirical Study**

**Argument**: Enhanced domain word embedding can facilitate downstream LM.

**Task 2**: Language modeling (LSTM, Tensorflow example code)

**Textual Data**: ~50k financial news headlines about ~4k companies retrieved from *WRDS*.

**Domain Data**: ~4k company historical daily stock return.

Pretrained embeddings: word2vec, fastText, Glove, self-trained.

| Embedding     | Test PP | %decrease |
|---------------|---------|-----------|
| self          | 13.093  |           |
| self+Google   | 12.742  | 2.75      |
| self+fastText | 12.477  | 4.94      |
| self+Glove    | 12.646  | 3.54      |
| Google        | 12.431  | 5.33      |
| fastText      | 12.215  | 7.19      |
| Glove         | 12.218  | 7.16      |
| self+aff      | 11.883  | 10.18     |
| Google+aff    | 11.646  | 12.42     |
| fastText+aff  | 11.638  | 12.51     |
| Glove+aff     | 11.510  | 13.76     |

#### Conclusions

We can leverage different data sources to enhance word representation.

LSI is proposed to combine entity representations defined in different spaces.

LSI guarantees deterministic convergence and has few hyperparameters.

Empirical study results support our arguments.

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