# Introduction to Computational Chemistry

CH20238 / CH30239

Dr Claire L. McMullin and Dr Vera Krewald

WH 1.24

WH 1.28

## **Computational Chemistry**

- i... is not just chemistry done "using" a computer
- As computing power has advanced and there are many more "user-friendly" software packages almost anyone who fancies a go can run a calculation (even if some of them maybe shouldn't!)
- The main goal of this course is to gently introduce the different methodologies available, present their advantages and disadvantages, to identify the best methods to use depending on what the chemistry question / system is
  - ... meaning you can judge the suitability of computational studies when you come across them

## **Objectives**

- Understand the concept of an energy surface and how it relates to chemical behaviour and reactivity, and the role of computational modelling in bridging between theory and experiment
- Demonstrate basic understanding of energy minimisation, geometry optimisation, relative energies, isodesmic relations, vibrational frequencies and molecular dynamics
- Appreciate the operational working of molecular mechanics, molecular orbital (Hartree-Fock and semi-empirical) and density functional theory methods within a typical computational chemistry software package and the significance of basis sets and empirical parameters in context
- Appreciate the advantages and disadvantages of popular computational methods for different problems

## **Topics**

- Molecular mechanics and empirical force-field methods
- Potential energy surfaces, energy minimisation and geometry optimisation
- Practical application of molecular orbital and density functional methods
- Electron density, electronic charge and electrostatic potential
- Molecular vibrations, zero-point energy, free energy
- Transition structures and reactivity
- Molecular dynamics

#### **Your Next Five Weeks**

#### 10 Lectures

W19-23; every Thursday (11:15 4E 3.10) and Friday (13:15 CB 2.6)

- Molecular Mechanics (MM)
- Semi-Empirical Methods
- Periodic Boundary Conditions (PBC)
- Molecular Dynamics (MD)
- Hartree-Fock (HF)
- Density Functional Theory (DFT)
- Basis Sets and Pseudopotentials
- Computed vs. Real Life

3 Lectures (CLM)

5 Lectures (VK)

2 Lectures (CLM)

#### **Your Next Five Weeks**

#### Workshops

W22-24; either Wednesday (12:15 CB 3.1) or Friday (14:15 CB 5.1)

- W22 Multiple Choice Question Practice
- W23 Student Drop-In?
- W24 Evaluating Methods Practice

#### **Textbooks**

Level 4 of the Library "541.28" – under the Group Theory books!

Introduction to Computational Chemistry

1 (and online)

- Frank Jensen, Wiley (2017 3rd Edition, 2007 2nd Edition)
- Molecular Modeling Basics

4 (and online)

- Jan Jensen, Routledge (2010)
- Essentials of Computational Chemistry: Theories and Models

1

- Christopher Cramer, Wiley (2004 2<sup>nd</sup> Edition)
- Molecular Quantum Mechanics

4

Peter Atkins & Ronald Friedman, Oxford University Press (2010)

#### **Textbook**

Less relevant textbooks:

•	<ul> <li>Chemical Applications of Molecular Modelling</li> <li>Jonathan Goodman, RSC (1998)</li> </ul>	•
۰	Molecular Modeling of Inorganic Compounds • Peter Comba, Trevor Hambley & Bodo Martin, Wiley (2009)	•
•	Structural Methods in Molecular Inorganic Chemistry  • David Rankin, Norbert Mitzel & Carole Morrison, Wiley (2013)	•

- Advanced reading:
  - Modern Quantum Chemistry Introduction to Advanced Electronic Structure Theory
    - Attila Szabo & Neil S. Ostlund, Dover Publications Inc. (1989)

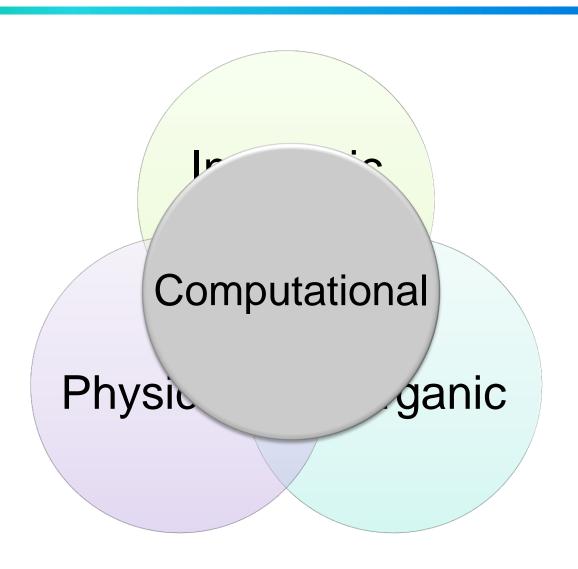
#### **Examinations**

• Exam 100 %

- Three Sections:
  - 1. Multiple Choice Questions
  - 2. "Medium"-length Questions
  - 3. Essay-like Question

As this is the first time the unit has run, we've made a mock paper for you – because there aren't any past papers!

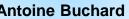
## **Research Themes at UoBath**



#### Research Themes at UoBath

- Catalyst design for renewable resources
- Metal-organic frameworks and metal-protein interactions
- Biological enzyme mechanisms
- Solid-state batteries and perovskite solar cells
- N<sub>2</sub> / H<sub>2</sub>O catalyst properties (redox, magnetic, spectroscopic)
- Organometallic reaction mechanisms; e.g. cross coupling and C-H activation
- Ion transport through solids (Li batteries)
- Structure / stability of ceramics and minerals
- Reactions in solution and enzyme active sites







**Rob Deeth** 



**Carmen Domene** 



Saiful Islam



**Vera Krewald** 



Claire McMullin



Ben Morgan

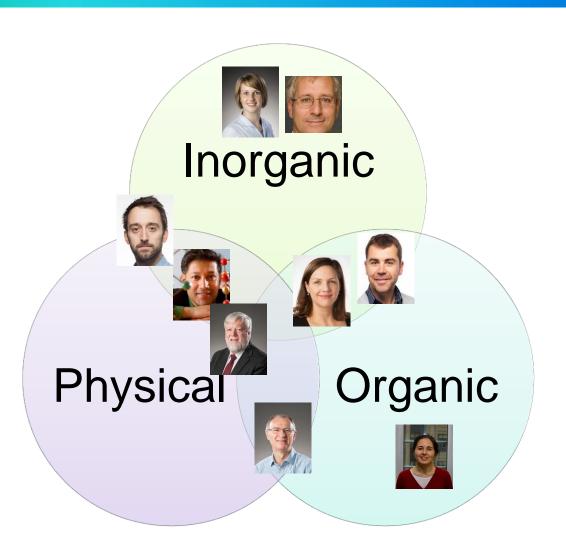


**Steve Parker** 



Ian Williams

## **Research Themes at UoBath**

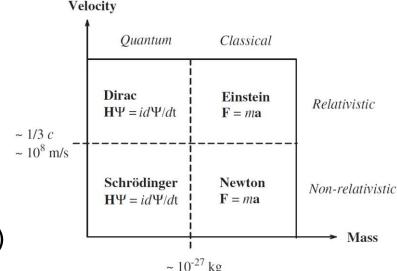


## Previously, In Quantum Mechanics...

- Prof. Steve Parker's CH20147 lectures at the end of S1
- Topics to familiarise yourself with for this course:
  - Wave-particle duality
  - Wavefunctions, operators, eigenvalues
  - Particle in a box
  - $\widehat{H}\Psi = E\Psi$
  - Zero point energy
  - Ground states and excited states
  - Variation method
  - Expectation value

## **Dynamical Equations**

- Mathematical form depends on <u>mass</u> and <u>velocity</u> of the particle(s)
- Classical mechanics is deterministic it can be integrated over time
- QM is **probabilistic** which is square of the wave function  $(\Psi^2)$
- Newton = heavy and slow
- Einstein = velocity ~ speed of light
  - increasing mass relative to rest mass

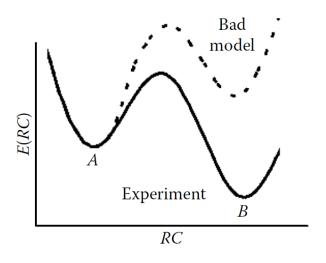


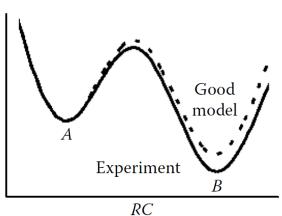
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- Borderline mass = a proton (a H nucleus)
- Electrons much lighter = only QM
- Light particles have <u>wave</u> and <u>particle</u> characteristics
- Hydrogen atoms are special sometimes they need QM corrections (e.g. tunnelling through barriers)

## **Potential Energy Surface (PES)**

- Connection between experimental data and molecular modelling
- Reactants, products, stable intermediates and transition states (TS) are found along a reaction coordinate (RC) on the PES





# **Potential Energy Surface (PES)**

- Connection between experimental data and molecular modelling
- Reactants, products, stable intermediates and transition states (TS) are found along a reaction coordinate (RC) on the PES
- Stationary points; when gradient is zero

$$\frac{dE}{dR}=\mathbf{0}$$

- Second energy derivatives identify what type of stationary point has been found:
  - $\frac{d^2E}{dR^2} > 0$ ; minima stable intermediates
  - $\frac{d^2E}{dP^2} < 0$ ; maxima TSs

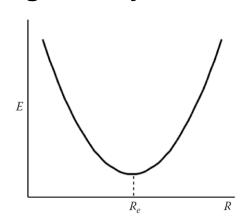
Remember: a TS has a negative (imaginary) frequency as it is a maximum

## What is an Optimisation?

- Finding the best position (x, y, z) for all atoms in the molecule / structure
- Trying to get to the bottom of the "well"
- E.g. for a quadratic PES

$$\bullet \quad E = \frac{1}{2}k(R - R_e)^2$$

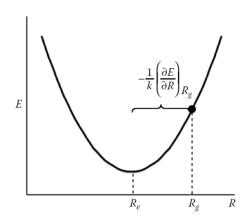
R<sub>e</sub> is the value of R at which the energy is lowest – the equilibrium geometry



Work out gradient

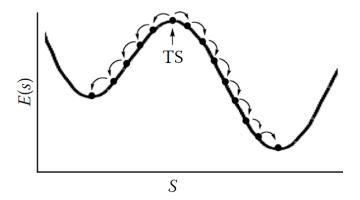
Tells you which direction the energy is *decreasing* 

Take small steps in that direction



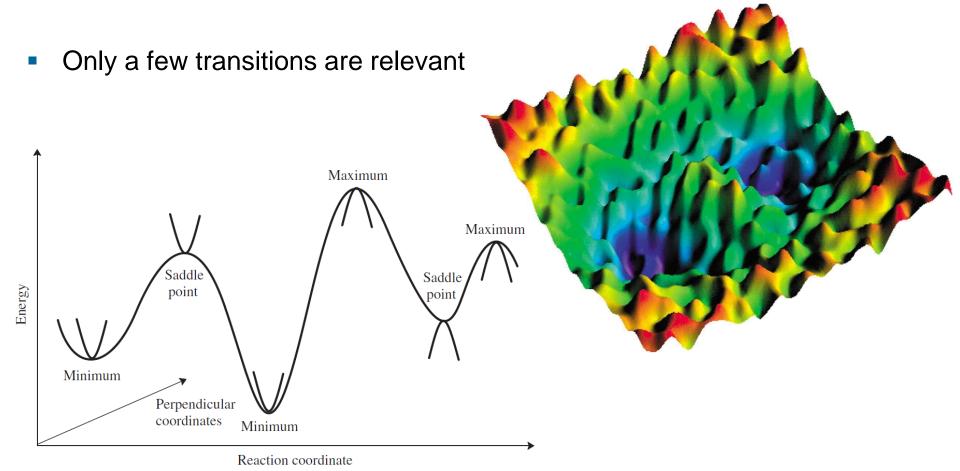
## **Minimum Energy Pathway**

- This connects a transition state with its two closest minima.
- The guess structure is the TS displaced along the imaginary frequency mode
- The resulting collection of structures is known as the intrinsic reaction coordinate (IRC)



#### **Multidimensional Surface**

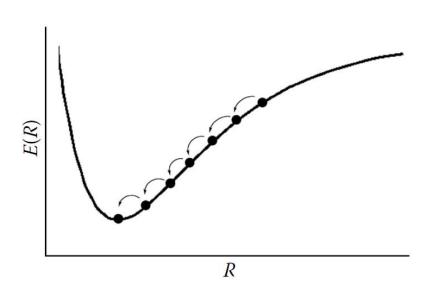
PES for a complex system is dense in saddle points

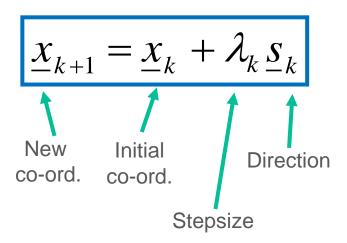


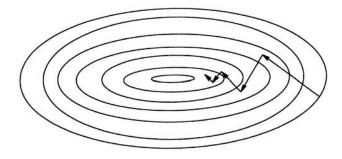
Frank Jensen, *Wiley* (2017) **Annu. Rev. Phys. Chem.**, P. G. Bolhuis *et al*, *53*, 291-318 (2002)

## **Steepest Descent**

- 1st order method
- Moves downhill to calculate forces (gradients)
- Relieves strain in built model
- Slow convergence
- Can't locate TSs





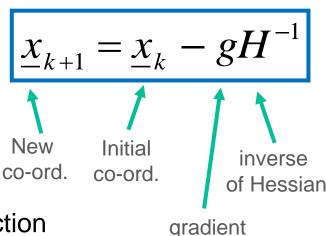


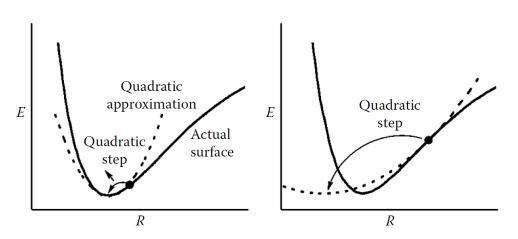
Means you are minimising the energy to find the closest minimum to the <u>starting geometry</u>

## **Quadratic / Newton-Raphson step**

- 2<sup>nd</sup> order method
- Reduces computational cost
  - One instead of many steps
  - Works out k (2<sup>nd</sup> derivative of E)
  - Uses the Hessian matrix
- Can locate TSs as Hessian provides uphill direction
- Works if the surface is quadratic
  - i.e. close to the minimum
  - but not if far away

The Hessian matrix is the 3N x 3N diagonalised square matrix of second-order partial derivatives of a function



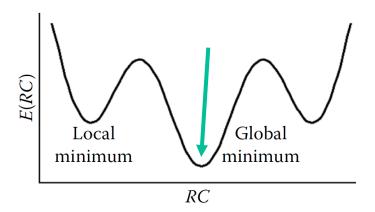


## **Geometry Optimisation**

- So we use an energy minimisation to find the optimal geometry for a structure
- Optimisations end either when the stationary point has been found (calculation has converged) or the program runs out of steps
  - Number of steps is often linked to number of atoms in the system
  - Each step explores one degree of freedom of the structure
- If the PES is flat, likely will require more steps to converge
  - "Flat" means small gradients and so a smaller stepsize
  - PES tends to be nonquadratic too so can't use Newton-Raphson

## **Global Minimum**

- Danger that optimisation may trap you in a local minimum not the global minimum
- Can try many different starting geometries
  - i.e. a conformational search
- Programs typically achieve this by changing dihedral angles of rotatable bonds



#### **Monte Carlo Method**

- A class of computational algorithms, that involve repeated random sampling to compute results (to satisfy Boltzmann distribution)
- Especially useful when trying to simulate systems with many coupled degrees of freedom; i.e. fluids, disordered materials, solids and cellular structures
- For models with significant uncertainty in the input
- Unbiased approach to conformational searching
  - A random "kick" is given to coordinates of a randomly chosen atom / molecule

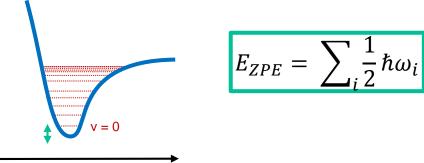
## **Monte Carlo (MC)**

- Energy comparison made between structure (E<sub>1</sub>) and random distortion (E<sub>2</sub>)
- 2. If E<sub>2</sub> < E<sub>1</sub>, then the second geometry is a better candidate for the global minimum and excepted
- 3. Process 1-2 repeated
- 4. If  $E_2 > E_1$ , then the second geometry is a worst candidate and is rejected if geometry 2 is much higher in energy
- Energy of system not fixed selected according to Boltzmann probability

$$P(x) = \frac{\exp(-U(x)/kT)}{\int \exp(-U(x)/kT)dX}$$

# **Zero-Point Energy**

- At the equilibrium structure the atoms are (hypothetically) at rest and free from the effects of vibration
- Energy difference between vibrational ground state and the equilibrium structure



- "Simply" add up the  $\frac{1}{2}\hbar\omega_i$  contribution from each vibration mode i
  - Multiple by Avogadro's number to report energies in units of kJ mol<sup>-1</sup>
- Modes that contribute the most to the ZPE correction have a higher wavenumber e.g. hydrogen bond modes – due to reduced mass term

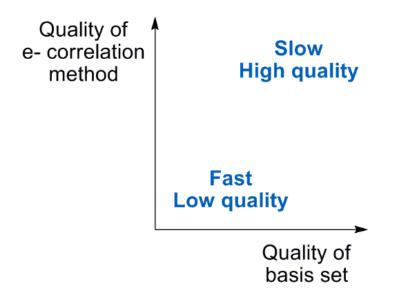
## **Z** Matrix

- Describes the geometry of a molecule not by Cartesian coordinates (x, y, z), but by the atom connectivity
  - An internal coordinate representation
- It identifies each atom in a molecule by a bond distance, bond angle and dihedral angle in relation to other atoms in the molecule
- Can allow symmetry to be enforced upon the molecule
  - Speeds up parts of the calculation
- Example: CH<sub>4</sub> (methane)

```
C 0.000000 0.000000 0.000000 C

H 0.628736 0.628736 0.628736 H 1 1.089000 H 1 1.089000 D 1 1.089
```

## **Computing Power**



The "cost" of a calculation isn't defined by how expensive the machine is that you use, but by **how long** the calculation will take to run – i.e. how many processors will be used and how long you have to wait before convergence. This is what we mean when we refer to the computational cost!

#### Computing power keeps increasing:

When I was doing my PhD (2007-2010) the biggest system I worked on had ~ 80 atoms and took 2 weeks to optimise using DFT.

Now running on the HPC in Bath (2018) I can optimise a 150 atom structure in a day!

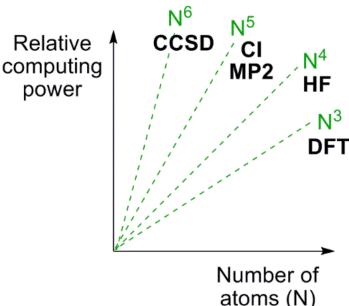
## **Increasing Computational Quality**

- Increase quality of electron correlation method increases computing cost
  - Depending on method it scales N³ (DFT), N⁴ (HF) or even higher, when N is the number of atoms in the system

 Increase quality of basis set (more functions used to describe electrons / orbitals) – increases computing cost

orbitals) – increases computing cost

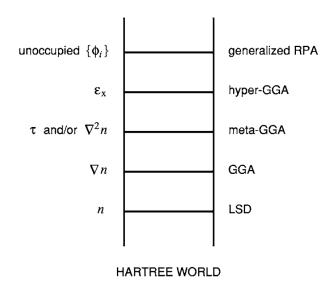
DFT = Density Functional Theory
HF = Hartree Fock
CI = Configuration Interaction
MP2 = Møller Plesset 2
CCSD = Coupled Cluster (Single Double)



#### Jacob's Ladder

- A staircase to heaven (from a dream of Jacob described in the Old Testament)
- Also refers to improvements in density functional approximations (DFT) to the exchange-correlation energy
- Accuracy increases as you go up the ladder





J. Chem. Phys. 123, 062201 (2005) DOI: 10.1063/1.1904565

#### One Method Does Not Fit All

- Different questions require different methods...
- Variables to consider:
  - The size of the system
  - Accuracy required
  - What questions you are trying to answer
  - Solid, liquid or gas?
  - Electronic, structural or dynamic?

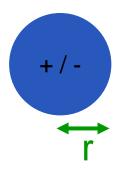
## **Programs**

- Lots of different software packages that use specific or a variety of methodologies:
  - SPARTAN
  - Gaussian / GaussView
  - Jaguar
  - ORCA
  - Turbomole
  - PCModel
  - CHARMM

# **Molecular Mechanics**

#### What is Molecular Mechanics?

- Classical Newtonian mechanics used to model molecular systems
- Potential Energy calculated using force fields
- Can model small molecules as well as large biological systems (N > 1000)
- Simplifications:
  - Atom = point charge



Bond = spring



<sup>\*\*</sup>No electrons - so can not treat a chemical reaction\*\*

#### The Forcefield

$$V(r) = \sum_{bonds} \frac{k_i}{2} (l_i - l_{i,0})^2 + \sum_{angles} \frac{k_i}{2} (\theta - \theta_i)^2 + \sum_{torsions} \frac{V_n}{2} (1 + \cos(n\omega - \gamma))$$

Total Potential Energy

**BONDS** 

**ANGLES** 

**DIHEDRAL** 

$$+\sum_{i=1}^{N}\sum_{j=1}^{N}\left(4\varepsilon_{ij}\left[\left(\frac{\sigma_{ij}}{r_{ij}}\right)^{12}-\left(\frac{\sigma_{ij}}{r_{ij}}\right)^{6}\right]\right)+\frac{q_{i}q_{j}}{4\pi\varepsilon_{0}r_{ij}}$$

**Lennard Jones potential (VdW)** 

**Electrostatic term** 

#### The Forcefield

#### **BONDING INTERACTIONS**

$$V(r) = \sum_{bonds} \frac{k_i}{2} (l_i - l_{i,0})^2 + \sum_{angles} \frac{k_i}{2} (\theta - \theta_i)^2 + \sum_{torsions} \frac{V_n}{2} (1 + \cos(n\omega - \gamma))$$

**Total Potential Energy** 

stretching bending

rotation

$$+\sum_{i=1}^{N}\sum_{j=1}^{N}\left(4\varepsilon_{ij}\left[\left(\frac{\sigma_{ij}}{r_{ij}}\right)^{12}-\left(\frac{\sigma_{ij}}{r_{ij}}\right)^{6}\right]\right)+\frac{q_{i}q_{j}}{4\pi\varepsilon_{0}r_{ij}}$$
repulsive attractive charge

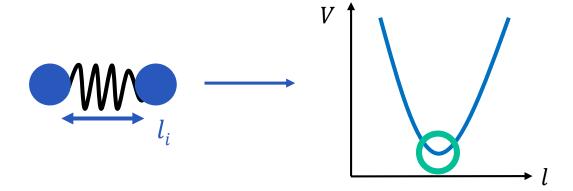
NON-BONDING INTERACTIONS

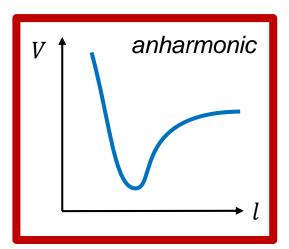
# **V**<sub>bond</sub>

- $l_i$  is bond length
- $l_{i,0}$  is equilibrium bond length
- $k_i$  is force constant
- Harmonic term

 $\sum_{bonds} \frac{k_i}{2} (l_i - l_{i,0})^2$ 

**Problem:** bonds are "springs" so does not model bond dissociation



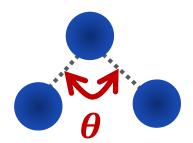


# **V**angle

- $\theta$  is bond angle
- $\theta_i$  is equilibrium bond angle

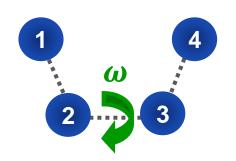
$$\sum_{angles} \frac{k_i}{2} (\theta - \theta_i)^2$$

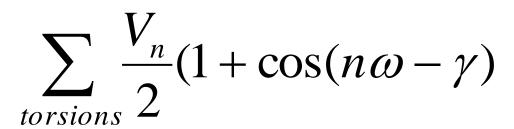
- Also a harmonic term
- Less energy needed to distort angle from equilibrium value hence force constants are smaller

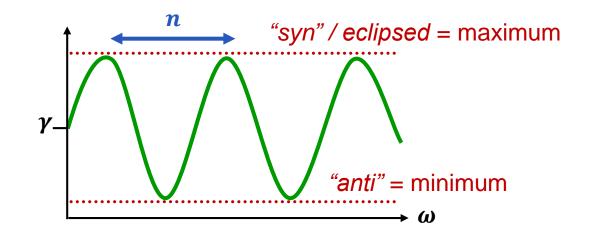


# V<sub>dihedral</sub>

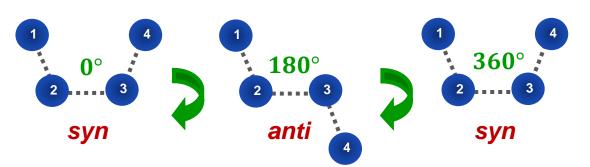
- n is the multiplicity
- $\gamma$  is the phase factor
- $\omega$  is the torsion angle







Looking down / along the 2-3 bond:



### **Improper Torsions**

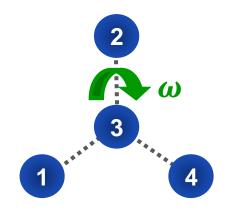
 Improper torsions use the cosine potential to restrain angle between 0°-180°

$$\sum_{improper} \frac{V_2}{2} [1 + \cos(2\omega - 180)]$$

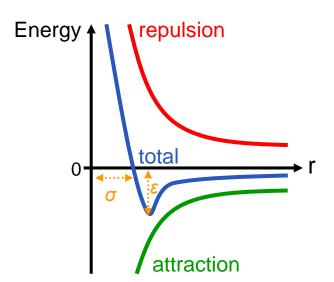
Or a harmonic function

$$\sum_{improper} \frac{k_w}{2} (\omega - \omega_0)^2$$

- Energy of out of plane functions
- Not a normal 1-2-3-4 connectivity, but 3 atoms bonded to an atom in same plane e.g. sp<sup>2</sup> centre such as carbon in carbonyl or aromatic rings
  - A "normal" torsion parameter doesn't keep planarity at 0°



# $V_{VdW}$

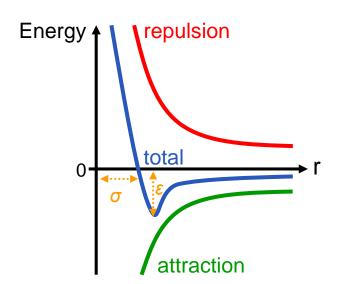


#### Lennard-Jones 12,-6 potential

$$\sum_{i=1}^{N} \sum_{j=1}^{N} \left(4arepsilon_{ij} \left[\left(rac{\sigma_{ij}}{r_{ij}}
ight)^{12} - \left(rac{\sigma_{ij}}{r_{ij}}
ight)^{6}
ight]
ight)$$

- $r_{ij}$  is distance between two atoms i and j
- $\varepsilon_{ij}$  is the well depth (of the energy minimum)
- $\sigma_{ij}$  is the collision diameter (where interaction energy = 0)

# **V**<sub>VdW</sub>



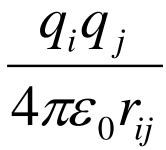
#### Lennard-Jones 12,-6 potential

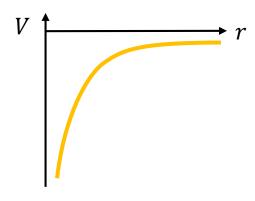
$$\sum_{i=1}^{N} \sum_{j=1}^{N} \left( 4arepsilon_{ij} \left[ \left( rac{\sigma_{ij}}{r_{ij}} 
ight)^{12} - \left( rac{\sigma_{ij}}{r_{ij}} 
ight)^{6} 
ight] 
ight)$$

- Attraction (dispersion) and short-range repulsion
- Dispersion interactions ~ 1 / r<sup>6</sup>
  - Attractive due to instantaneous dipoles from fluctuations of electronic distributions
- Repulsive interactions ~ 1 / r<sup>12</sup>
  - At very short distances molecules repel each other insignificant over large distances.
  - Pauli Principle: ↓e⁻ density between nuclei = ↑ nuclear-nuclear repulsion

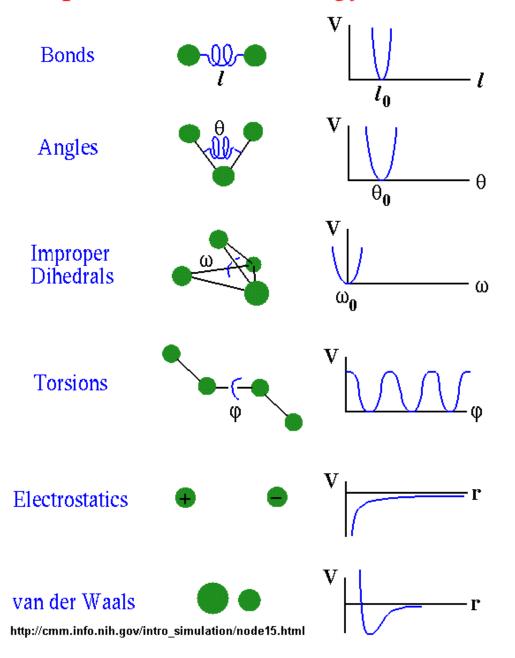
# **V**electrostatic

- $q_i$  and  $q_j$  are the charges of the atoms
- $\varepsilon_{ij}$  molecular dielectric expression accounts for attenuation of electrostatic interaction by the environment
- Coulombic potential
- Influence of polarity on energy and structure
- A linearly varying distance-dependent dielectric  $\frac{1}{r_{ij}}$  accounts for increase in environmental bulk as the separation distance between interacting atoms increases





#### **Empirical Potential Energy Function**



# The MM Forcefield is Collectively:

- Potential Functions
- Force constants
- VdW multipliers
- Other constant terms
- Equilibrium bond, angle & dihedral values
- Partial charge values
- Atomic masses and radii

Lets actually have a look at one...

```
**********************
 3
 4
         ## Force Field Definition ##
5
         ************************
 6
7
8
9
    forcefield
                          MMFF94
10
11 bondunit
                          71.9663
12 bond-cubic
                          -2.0
13 bond-quartic
                          2.333333
                                         !! (7/12) * bond-cubic^2
14 angleunit
                          0.021922
15 angle-cubic
                          -0.007
16 str-bndunit
                          2.51210
17 torsionunit
                          0.5
18 vdwtype
                          BUFFERED-14-7
19 radiusrule
                          CUBIC-MEAN
20 radiustype
                          R-MIN
21 radiussize
                          DIAMETER
22 epsrule
                          HHG
23 vdw-14-scale
                          1.0
24 chg-14-scale
                          0.75
25 dielectric
                          2.0
26
27
28
         ***********************
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30
         ## Literature References ##
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35 T. A. Halgren, "Representation of van der Waals (vdW) Interactions in
   Molecular Mechanics Force Fields: Potential Form, Combination Rules,
37
    and vdW Parameters", JACS, 114, 7827-7843 (1992)
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         ***********************
41
42
         ## Atom Type Definitions ##
43
44
         **********************
45
46
                                                   12.000
47 atom
                  С
                       "Alkvl Carbon"
                                                6
                                                                4
                                                                                              1
48
    atom
                       "Olefinic Carbon"
                                                   12,000
                                                                               3
49
             3
                  С
                       "Carbonyl Carbon"
                                                6
                                                   12.000
                                                                3
                                                                       4
                                                                                      3
                                                                                              1
    atom
50
   atom
                       "Acetylenic Carbon"
                                                    12.000
                                                                                              1
51 atom
                       "Nonpolar Hydrogen"
                                                1
                                                    1.008
                                                               1
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40		***************************************													
41		##		##											
42		## Ato	om Type	Definitions ##											
43		##		##											
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45															
46															
47	atom	1	С	"Alkyl Carbon"	6	12.000	4	4	1	1	1				
48	atom	2	С	"Olefinic Carbon"	6	12.000	3	4	2	2	1				
49	atom	3	С	"Carbonyl Carbon"	6	12.000	3	4	3	3	1				
50	atom	4	С	"Acetylenic Carbon"	6	12.000	2	4	4	4	1				
51	atom	5	H	"Nonpolar Hydrogen"	1	1.008	1	1	5	5	5				
52	atom	6	0	"Divalent Oxygen"	8	15.995	2	2	6	6	6				
53	atom	7	0	"Carbonyl Oxygen"	8	15.995	1	2	7	7	6				
54	atom	8	N	"Amine Nitrogen"	7	14.003	3	3	8	8	8				
55	atom	9	N	"Imine Nitrogen"	7	14.003	2	3	9	9	8				
56	atom	10	N	"Amide Nitrogen"	7	14.003	3	3	10	10	8				
57	atom	11	F	"Fluorine"	9	18.998	1	1	11	11	11				
58	atom	12	C1 Br	"Chlorine" "Bromine"	17 35	34.969	1	1	12	12 13	12 13				
59 60	atom	13 14	I	"Iodine"	53	78.918 126.900	1	1	13 14	14	14				
61	atom	15	S	"Sulfide -S-"	16	31.972	2	2	15	15	15				
62	atom	16	S	"Thiocarbonyl S=C"	16	31.972	1	2	16	16	15				
63	atom	17	S	"Sulfoxide Sulfur"	16	31.972	3	6	17	17	15				
64	atom	18	S	"Sulfone, Sulfate"	16	31.972	4	6	18	18	15				
65	atom	19	Si	"Silicon"	14	27.977	4	4	19	19	19				
66	atom	20	C	"Csp3 in 4-Ring"	6	12.000	4	4	20	20	1				
67	atom	21	Н	"Hydroxyl Hydrogen"	1	1.008	1	1	21	21	5				
68	atom	22	C	"Csp3 in 3-Ring"	6	12.000	4	4	22	22	1				
69	atom	23	Н	"Amine Hydrogen"	1	1.008	1	1	23	23	5				
70	atom	24	Н	"Carboxyl Hydrogen"	1	1.008	1	1	24	24	5				
71	atom	25	P	"Phosphate"	15	30.994	4	4	25	25	25				
72	atom	26	P	"Phosphine"	15	30.994	3	3	26	26	25				
73	atom	27	H	"Imine Hydrogen"	1	1.008	1	1	27	27	5				
74	atom	28	H	"Amide Hydrogen"	1	1.008	1	1	28	28	5				
75	atom	29	H	"Phenolic Hydrogen"	1	1.008	1	1	29	29	5				
76	atom	30	С	"Csp2 in 4-Ring"	6	12.000	3	4	30	2	1				
77	atom	31	H	"Water Hydrogen"	1	1.008	1	1	31	31	31				
78	atom	32	0-	"Carboxylate Oxygen"	8	15.995	1	2	32	7	6				
79	atom	33	H	"Sulfoxy Hydrogen"	1	1.008	1	1	33	21	5				
80	atom	34	N+	"Quaternary Nitrogen"	7	14.003	4	3	34	8	8				
81	atom	35	0-	"Oxide at Metal"	8	15.995	1	2	35	6	6				
82	atom	36	H	"Hydrogen on N+"	1	1.008	1	1	36	36	5				
83	atom	37	С	"Aromatic Carbon"	6	12.000	3	4	37	2	1				
84	atom	38	N	"Pyridine Nitrogen"	7	14.003	2	3	38	9	8				
85	atom	39	N	"Pyrrole Nitrogen"	7	14.003	3	3	39	10	8				
86	atom	40	N	"N-C=C or N-C=N"	7	14.003	3	3	40	10	8				
87	atom	41	C	"Carboxylate Carbon"	6	12.000	3	4	41	3	1				
88	atom	42	N	"Nitrile Nitrogen"	7	14.003	1	3	42	42	8				
89	atom	43	N	"Sulfonamide Nitrogen"	7	14.003	3	3	43	10	8				
90	atom	44	S	"Thiophene Sulfur"	16	31.972	2	2	44	16	15				

```
230
         ##
231
         ## Van der Waals Parameters ##
232
233
         *************************
234
235
236
    *13. MMFFVDW.PAR: This file supplies parameters for van der Waals interactions.
237
             Copyright (c) Merck and Co., Inc., 1994, 1995, 1996
238
239
                          All Rights Reserved
240
241
    * E94 - From empirical rule (JACS 1992, 114, 7827)
    * C94 - Adjusted in fit to HF/6-31G* dimer energies and geometries
    * X94 - Chosen in the extension of the paratererization for MMFF94
244
            by analogy to other, similar atom types or, for ions, by
            fitting to atomic radii (and sometimes to association energies
245
246
            for hydrates)
247
                              DARAD
                                        DAEPS
248
    * power
                В
                       Beta
249
      0.25
               0.2
                       12.
                              0.8
                                         0.5
250
251
              type alpha-i N-i
                                    A-i
                                          G-i
252
    *-----
253 vdwmmff
            1 1.0500 2.4900
                                   3.8900
                                         1.2820 -
254 vdwmmff
            2 1.3500
                          2.4900
                                   3.8900
                                          1.2820
255 vdwmmff
            3 1.1000 2.4900
                                         1.2820
                                   3.8900
256 vdwmmff
            4 1.3000 2.4900
                                   3.8900
                                          1.2820
257 vdwmmff
            5 0.2500 0.8000
                                   4.2000
                                          1.2090
258 vdwmmff
            6 0.7000 3.1500
                                   3.8900
                                          1.2820 A
259 vdwmmff
            7 0.6500
                          3.1500
                                   3.8900
                                          1.2820 A
            8 1.1500 2.8200
260 vdwmmff
                                   3.8900
                                          1.2820 A
261 vdwmmff
            9 0.9000 2.8200
                                   3.8900
                                          1.2820 A
             10 1.0000 2.8200
262 vdwmmff
                                   3.8900
                                           1.2820 A
263 vdwmmff
            11 0.3500 3.4800
                                   3.8900
                                           1.2820 A
264 vdwmmff
            12 2.3000 5.1000
                                   3.3200
                                           1.3450 A
265 vdwmmff
             13 3.4000
                          6.0000
                                   3.1900
                                           1.3590 A
                          6.9500
266 vdwmmff
             14 5.5000
                                   3.0800
                                           1.4040 A
267 vdwmmff
              15 3.0000 4.8000
                                   3.3200
                                          1.3450
268 vdwmmff
             16 3.9000 4.8000
                                   3.3200
                                          1.3450 A
269 vdwmmff
             17 2.7000 4.8000
                                   3.3200
                                          1.3450
270 vdwmmff
             18 2.1000
                          4.8000
                                   3.3200
                                           1.3450
271 vdwmmff
             19 4.5000
                          4.2000
                                   3.3200
                                           1.3450
272 vdwmmff
              20 1.0500 2.4900
                                   3.8900
                                           1.2820
273
    vdwmmff
              21 0.1500
                          0.8000
                                   4.2000
                                          1.2090
274 vdwmmff
              22 1.1000 2.4900
                                   3.8900
                                           1.2820
275 vdwmmff
              23 0.1500
                          0.8000
                                   4.2000
                                          1.2090
                                                   D
276 vdwmmff
             24 0.1500
                          0.8000
                                   4.2000
                                           1.2090
277
    vdwmmff
              25 1.6000 4.5000
                                   3.3200
                                           1.3450
278
    vdwmmff
              26 3.6000 4.5000
                                   3.3200
                                           1.3450
279 vdwmmff
              27 0.1500 0.8000
                                   4.2000
                                           1.2090
```

229

\*

436		########	****	********	*********		942		******							
437		##			##		943		##				##			
438		## Bond	Stret	ching Para	meters ##		944		## Angle	Bend	ing Pa	rameters	##			
439		##		_	##		945		##				##			
440		*******	****	*********	*********		946		*******	####	*****	********	##			
441							947									
442							948									
443	bond	1	1	4.2580	1.5080	C94	949	angle		1	1		109.6080	C94		
444	bond	1	2	4.5390	1.4820	C94	950	angle		1	2	0.7360	109.4450	C94		
445	bond	1	3	4.1900	1.4920	C94	951	angle		1	3	0.7770	107.5170	C94		
446	bond	1	4	4.7070	1.4590	X94	952	angle		1	4	1.0060	110.2650	E94		
447		1	5			C94	953	angle		1	5	0.6360	110.5490	C94		
	bond			4.7660	1.0930		954	angle		1	6	0.9920	108.1330	C94		
448	bond	1	6	5.0470	1.4180	C94	955	angle		1	8 9	0.7770	108.2900	C94 E94		
449	bond	1	8	5.0840	1.4510	C94	956 957	angle		1	10	1.1360 1.0500	108.1940	C94		
450	bond	1	9	4.7630	1.4580	C94		angle		1	11	1.2250	109.9600	C94		
451	bond	1	10	4.6640	1.4360	C94	958	angle		1	12	1.0560	108.5130	C94		
452	bond	1	11	6.0110	1.3600	#C94	960	angle		1	13	1.0360	106.8200	E94		
453	bond	1	12	2.9740	1.7730	C94	961	angle		1	14	0.9800	100.0200	E94		
454	bond	1	13	2.5290	1.9490	E94	962	angle		1	15	0.7430	107.3970	C94		
455	bond	1	14	1.7060	2.0900	E94	963	angle		1	17	1.0890	108.5780	E94		
456	bond	1	15	2.8930	1.8050	C94	964	angle		1	18	1.0930	109.3150	E94		
457	bond	1	17	2.8410	1.8130	X94	965	angle		1	19	0.7550	115.4360	E94		
458	bond	1	18	3.2580	1.7720	X94	966	angle		1	20	1.0210	108.6590	E94		
459	bond	1	19	2.8660	1.8300	#X94	967	angle		1	22	1.0010	110.1250	E94		
460	bond	1	20	4.6500	1.5040	C94	968	angle	<u> </u>	1	25	0.8030	112.3560	X94		
461	bond	1	22	4.2860	1.4820	E94	969	angle	1	1	26	0.8330	109.8790	E94		
462	bond	1	25	2.9800	1.8100	#X94	970	angle	1	1	34	1.1790	106.4930	C94		
463	bond	1	26	2.7900	1.8300	#X94	971	angle	1	1	37	0.7560	108.6170	C94		
464	bond	1	34	3.8440	1.4800	#C94	972	angle	1	1	39	0.9270	109.1700	C94		
465	bond	1	35	7.9150	1.3070	X94	973	angle	1	1	40	1.1300	108.6780	E94		
466	bond	1	37	4.9570	1.4860	C94	974	angle	1	1	41	0.3300	98.4220	C94		
467	bond	1	39	6.1140	1.4450	C94	975	angle	1	1	43	1.1350	108.0190	E94		
468	bond	1	40	4.9220	1.4460	C94	976	angle	1	1	45	1.1970	105.0280	E94		
469	bond	1	41	3.8300	1.5100	#C94	977	angle	1	1	54	1.1730	106.4240	E94		
470	bond	1	43	3.9710	1.4720	#C94 X94	978	angle	1	1	55	1.1500	107.6040	E94		
471						X94 X94	979	angle		1	56	1.1990	110.3710	C94		
	bond	1	45	3.8440	1.4800		980	angle		1	57	1.0120	109.9000	E94		
472	bond	1	46	3.8130	1.4820	X94	981	angle		1	58	1.1790	106.3270	E94		
473	bond	1	54	4.2670	1.4610	C94	982	angle		1	61	1.1250	109.3110	E94		
474	bond	1	55	4.6460	1.4540	C94	983	angle		1	63	1.0060	110.0580	E94		
475	bond	1	56	4.1660	1.4530	C94	984	angle		1	64	0.9880	111.0640	E94		
476	bond	1	57	4.6690	1.4610	E94	985	angle		1	67	1.2160	104.5570	E94		
477	bond	1	58	4.3290	1.4510	E94	986	angle		1	68	1.0180	107.1950	C94		
478	bond	1	61	4.8450	1.4240	X94	987	angle		1	73	1.1600	104.6580	E94		
479	bond	1	62	4.4560	1.4440	X94	988	angle		1	78	1.0120	109.8500	E94		
480	bond	1	63	4.4810	1.4710	E94	989	angle		1	80	0.9470	113.3270	E94		
481	bond	1	64	4.5180	1.4690	E94	990	angle	1	1	81	1.1080	109.8370	E94		
482	bond	1	67	4.1880	1.4590	E94										
483	bond	1	68	4.2170	1.4790	C94										
484	bond	1	72	2.9560	1.8010	X94							sti	rbnd		

2.6080

2.5470

75

486 bond

1.8390

1.8580

X94

E94

strbnd angle stretches opbend out of plane bends

3617	##	*****	****	****	*****	**					4564						
		m				##					4565	##				##	
3618 3619	##	Torsions				##					4566	##	Atomic	Partial Char	rge Parame		
3620						*********					4567	## ##					
	***	*****	****	****	*****	***********					4568	###	#######	*********	********	#######	
3621											4569						
3622 3623	torsion	1	1	1	1	0.1030 +1	0.6810 -2	0.3320	+3	C94	4570						
3624	torsion5	1	1	1	1	0.1440 +1	-0.5470 -2	1.1260	+3	C94	4571	mmffchrg	1	0.0000	0.0000	0.0000	E94
3625	torsion	1	1	1	2	-0.2950 +1	0.4380 -2	0.5840	+3	C94	4572	mmffchrg	2	-0.1350	0.0000	0.0000	E94
3626	torsion	1	1	1	3	0.0660 +1	-0.1560 -2		+3	C94	4573	mmffchrg	3	-0.0950	0.0000	0.0000	E94
3627	torsion	1	1	1	5	0.6390 +1	-0.6300 -2	0.2640	+3	C94	4574	mmffchrg	4	-0.2000	0.0000	0.0000	E94
3628	torsion	1	1	1	6	-0.6880 +1	1.7570 -2	0.4770	+3	C94	4575	mmffchrg	5	-0.0230	0.0000	0.0000	E94
3629	torsion5	1	1	1	6	0.0000 +1	0.0000 -2		+3	C94	4576	mmffchrg	6	-0.2430	0.0000	0.0000	E94
3630	torsion	1	1	1	8	-1.4200 +1	-0.0920 -2	1.1010	+3	C94	4577	mmffchrg	7	-0.6870	0.0000	0.0000	E94
3631	torsion5	1	1	1	8	0.0000 +1	-0.1580 -2	0.3230	+3	C94	4578	mmffchrg	8	-0.2530	0.0000	0.0000	E94
3632	torsion	1	1	1	11	0.5930 +1	0.6620 -2	1.1200	+3	C94	4579	mmffchrg	9	-0.3060	0.0000	0.0000	E94
3633	torsion	1	1	1	12	-0.6780 +1	0.4170 -2		+3	C94	4580	mmffchrg	10	-0.2440	0.0000	0.0000	E94
3634	torsion	1	1	1	15	-0.7140 +1	0.6980 -2	0.0000	+3	C94	4581	mmffchrg	11	-0.3170	0.0000	0.0000	E94
3635	torsion	1	1	1	34	-0.6470 +1	0.5500 -2	0.5900	+3	C94	4582	mmffchrg	12	-0.3040	0.0000	0.0000	E94
3636	torsion	2	1	1	5	0.3210 +1	-0.4110 -2	0.1440	+3	C94	4583	mmffchrg	13	-0.2380	0.0000	0.0000	E94
3637	torsion	3	1	1	3	0.4430 +1	0.0000 -2	-1.1400	+3	C94	4584	mmffchrg	14	-0.2080	0.0000	0.0000	E94
3638	torsion	3	1	1	5	-0.2560 +1	0.0580 -2	0.0000	+3	C94	4585	mmffchrg	15	-0.2360	0.0000	0.0000	E94
3639	torsion	3	1	1	6	-0.6790 +1	-0.0290 -2	0.0000	+3	C94	4586	mmffchrg	16	-0.4750	0.0000	0.0000	E94
3640	torsion	5	1	1	5	0.2840 +1	-1.3860 -2	0.3140	+3	C94	4587	mmffchrg	17	-0.1910	0.0000	0.0000	E94
3641	torsion	5	1	1	6	-0.6540 +1	1.0720 -2	0.2790	+3	C94	4588	mmffchrg	18	-0.1180	0.0000	0.0000	E94
3642	torsion	5	1	1	8	-0.7440 +1	-1.2350 -2	0.3370	+3	C94	4589	mmffchrg	19	0.0940	0.0000	0.0000	E94
3643	torsion	5	1	1	10	0.0000 +1	0.0000 -2	0.4270	+3	C94	4590	mmffchrg	20	-0.0190	0.0000	0.0000	E94
3644	torsion	5	1	1	11	0.0000 +1	0.5160 -2	0.2910	+3	C94	4591	mmffchrg	21	0.1570	0.0000	0.0000	E94
3645	torsion	5	1	1	12	0.6780 +1	-0.6020 -2	0.3980	+3	C94	4592	mmffchrq	22	-0.0950	0.0000	0.0000	E94
3646	torsion	5	1	1	15	1.1420 +1	-0.6440 -2	0.3670	+3	C94	4593	mmffchrg	23	0.1930	0.0000	0.0000	E94
3647	torsion	5	1	1	25	0.0000 +1	0.0000 -2	0.2950	+3	X94	4594	mmffchrq	24	0.2570	0.0000	0.0000	E94
3648	torsion	5	1	1	34	0.6920 +1	-0.5300 -2	0.2780	+3	C94	4595	mmffchrq	25	0.0120	0.0000	0.0000	E94
3649	torsion	5	1	1	37	0.0000 +1	0.0000 -2	0.3890	+3	C94	4596	mmffchrq	26	-0.1420	0.0000	0.0000	E94
3650	torsion	5	1	1	39	0.0000 +1	0.0000 -2	0.2780	+3	C94	4597	mmffchrq	27	0.0940	0.0000	0.0000	E94
3651	torsion	5	1	1	41	0.0000 +1	0.0000 -2	-0.1410	+3	C94	4598	mmffchrq	28	0.0580	0.0000	0.0000	E94
3652	torsion	5	1	1	56	0.0000 +1	0.0000 -2		+3	C94	4599	mmffchra	29	0.2070	0.0000	0.0000	E94
3653	torsion	5	1	1	68	0.0000 +1	0.0000 -2	0.1360	+3	C94	4600	mmffchrq	30	-0.1660	0.0000	0.0000	E94
3654	torsion	6	1	1	6	0.4080 +1	1.3970 -2	0.9610	+3	C94	4601	mmffchrq	31	0.1610	0.0000	0.0000	E94
3655	torsion5	6	1	1	6	0.3130 +1	-1.0350 -2	1.6310	+3	C94	4602	mmffchrq	32	-0.7320	0.5000	-0.5000	E94
3656	torsion	8	1	1	8	1.0550 +1	0.8340 -2	0.0000	+3	C94	4603	mmffchrq	33	0.2570	0.0000	0.0000	E94
3657	torsion	11	1	1	11	-0.3870 +1	-0.5430 -2		+3	C94	4604	mmffchrq	34	-0.4910	0.0000	1.0000	E94
3658	torsion	12	1	1	12	0.0000 +1	0.0000 -2	0.8930	+3	C94	4605	mmffchrq	35	-0.4560	0.5000	-1.0000	E94
3659	torsion	15	1	1	15	-0.1770 +1	0.0000 -2	0.0490	+3	C94	4606	mmffchrq	36	-0.0310	0.0000	0.0000	E94
3660	torsion	1	1	2	1	0.4190 +1	0.2960 -2	0.2820	+3	C94	4607	mmffchra	37	-0.1270	0.0000	0.0000	E94
3661	torsion	1	1	2	2	-0.4940 +1	0.2740 -2	-0.6300	+3	C94	4608	mmffchrq	38	-0.4370	0.0000	0.0000	E94
3662	torsion	1	1	2	5 2	0.0750 +1	0.0000 -2	0.3580	+3	C94	4609	mmffchrq	39	-0.1040	0.0000	0.0000	E94
3663	torsion	2	1	2	_	-0.2930 +1	0.1150 -2	-0.5080	+3	C94 C94	4610	mmffchra	40	-0.2640	0.0000	0.0000	E94
3664 3665	torsion	2	1	2	5 1	0.3010 +1 0.5650 +1	0.1040 -2 -0.5540 -2	0.5070	+3	C94 C94	4611	mmffchrq	41	0.0520	0.0000	0.0000	E94
		_	_	2	2		-0.5540 -2 -0.4820 -2					mmffchrg	42	-0.7570	0.0000	0.0000	E94
3666	torsion	3	1	2	2	-0.5770 +1	-0.4820 -2	-0.4270	+3	C94	4012	nuntrenrg	72	-0.7570	0.0000	0.0000	E34

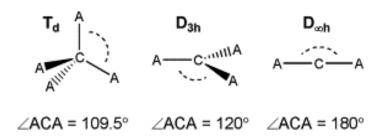
### Forcefield names

- MM2
- MM3
- MMFF94
- AMBER
- CHARMM
- TINKER
- UFF

What is the name of the MM forcefield that SPARTAN uses?

# **MM Problems for TM Complexes**

- 1. "Unique Labelling Problem"
  - How to describe the angular geometry at metal?
    - Simple for carbon 3 common geometries (tetrahedral, trigonal planar and linear with angles 109.5°, 120° and 180°)



 Common TM complex geometries have multiple reference angles for the same A-M-A triad

$$A = 90^{\circ}$$
 $A = 180^{\circ}$ 
 $A = 180^{\circ}$ 

# **MM Problems for TM Complexes**

- Can't model ligand field splitting
  - No concept of strong or weak ligands / metals
  - Or high and low spin
    - No evaluation of octahedral vs. tetrahedral vs. square planar
- 3. Doesn't capture trans effect and influence
- 4. Doesn't capture Jahn-Teller distortions
- 5. Can't describe bonding of  $\pi$ -donor and  $\pi$ -acceptor ligands

These are all **stereoelectronic** effects... The forcefield parameterisation is not molecule specific but general and so doesn't account for these electronic effects that lead to structural and thermodynamic variation.

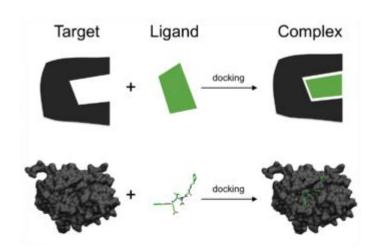
### **MM Uses**

- Energy minimisation
- Geometry optimisation
  - 1st order uses 1st derivatives of energy  $\frac{dV}{dR}$
  - $2^{\text{nd}}$  order uses  $1^{\text{st}}$  and  $2^{\text{nd}}$  order derivatives  $\frac{dV^2}{d^2R}$
- Conformation searches
- Computer Aided Design
- Molecular Dynamics calculations

# **Computer Aided Design**

Ligand = small molecule

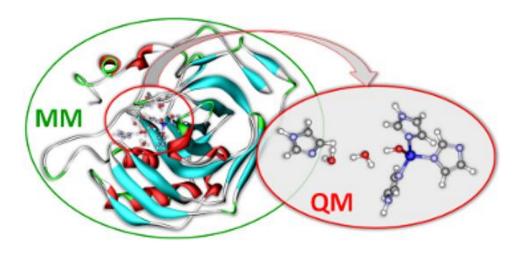
- "in silico"
- Used in drug discovery
  - Relies on knowledge of the three-dimensional structure of target and charges in the surrounding environment
  - High throughput screening
- Structure-based approach
  - Protein-Ligand docking
  - Pharmacophore
  - Ligand design



- Ligand-based approach
  - Similarity (or not) to previously known active ligands
  - Molecular descriptors
  - Quantitative structure-activity relationships

### QM/MM

- MM calculations take significantly less time than QM methods
  - But ignore electrons and orbitals
- QM/MM = combination of the two, where the reactive parts of the system are treated with QM
- Scales as N<sup>2</sup>



### QM/MM

Partition the system into two regions

Active site requires accurate QM calculation

Rest of system approximate and fast MM calculation

- Partitioning correctly is the tricky part... where should the boundary be?
  - Use "capping" replacing large groups with H atoms in QM region
- Chemistry Nobel prize in 2013 awarded to Warshel and Levitt for this topic (and also Karplus for Molecular Dynamics)

Will show examples in the final two lectures

# **Ab Initio**

### **Ab Initio**

- QM uses Schrödinger wave equation to compute the electronic structure of a molecule
- Describes the wave function in terms of the Hamiltonian operator  $(\widehat{H})$ , which contains kinetic  $(\widehat{T})$  and potential  $(\widehat{V})$  energy operators for a general N-particle system
- $\widehat{H}$  operator is equal to the energy (E) of the system

$$\widehat{H}\Psi = \left[\widehat{T} + \widehat{V}\right]\Psi = E\Psi$$

### **Molecular Hamiltonian**

 The kinetic and potential operators are then split further into five terms to give the Molecular Hamiltonian:

> Kinetic energy due to nuclei in system

Potential energy arising from Coulombic electron-nucleus attraction

Potential energy due to nuclei-nuclei repulsions

$$\widehat{H} = \widehat{T}_n + \widehat{T}_e + \widehat{V}_{en} + \widehat{V}_{ee} + \widehat{V}_{nm}$$

Kinetic energy due to each electron

Potential energy due to electron-electron repulsion

 Solving this equation is only possible for the simplest of systems as the wavefunction depends simultaneously on the coordinates of ALL the electrons and nuclei!

# **Born-Oppenheimer Approximation**

- Separates the electronic and nuclear motions of the system
- Treat the nuclei as stationary
  - Electrons move much faster than nuclei, so they appear stationary and we ignore their kinetic motion
- Means electronic structure can be calculated with the nuclear coordinates and not their momentum to give a potential energy surface
- Excludes nuclear kinetic energy term  $(\widehat{T}_n)$  gives the electronic Hamiltonian  $(\widehat{H}_{el})$ , and the electronic Schrödinger equation:

$$\widehat{H}_{el} = \widehat{T}_e + \widehat{V}_{en} + \widehat{V}_{ee} + \widehat{V}_{nm}$$

# **Hartree Fock (HF)**

- Calculates each electron in an orbital independently
- Views other electrons as a mean field neglecting electron-electron correlation
- Starting point for QM approaches

HF will be covered in more detail from lecture 4 onwards

By adding parameters to HF you are creating semi-empirical methods...

# **Semi Empirical**

# Semi Empirical (SE)

- Attempts to solve the electronic structure calculation for a many-body system
- Adds approximations based on experimental parameters
- [Ab initio methods are generated without reference to experimental data]
- For many years with HF calculations, computational chemists were limited to the study of very small (5-10 atom) molecules – due to lack of computational power
- Frustrated QM chemists derived approximate versions of HF that were faster but included empirical parameters derived from experiment to help correct the deficiencies introduced by their approximations

# Semi Empirical (SE) Part 2

- These SE methods retain a QM component and can be used to describe bond making and breaking
- Half way house between accuracy of QM methods and speed of classical simulations
- SE = approximate QM methods, as still seeking solutions to Schrödinger's equation...
  - ... but with a series parameterisation schemes (often derived from experimental data) to dramatically cut computational cost

# Semi Empirical (SE) Part 3

- Remember technique is based on parameterisation so quality of results obtained only reflects the quality of the parameterisation scheme
  - Experimentally observed data;
    - Structures
    - Ionisation energies
    - Heats of formation
- SE methods were widely popular have now been displaced by DFT
- Increase in computational power over time has also benefited SE:
  - Can now perform relatively long MD simulations at a SE level of theory

# **SE Approximations**

- Neglect all electrons except the valence electrons
- Parameters required for every element in a system but not for bond lengths and angles
- Advantages
  - Simplification to integrals so that time required to compute increases only as N<sup>3</sup>
  - Hence can study large molecules
  - Experimental results include effects of electron correlation, so some of this is implicit in the calculations
    - Also a disadvantage difficult to assess the errors and not clear how great an allowance is made

# **Hückel Approximation**

- First SE method developed
  - Was for conjugated π systems
- HMO = Hückel molecular orbital theory
- Each molecular orbital is written as a linear combination of atomic orbitals (LCAO)
- Gives rise to a set of secular equations, which have non trivial solutions
  - Set selected matrix elements to zero and parameterize non zero elements

# **Neglecting Overlaps**

- Pople and Dewar (and co-workers) made significant progress in treating general molecular systems with SE methods
- Treat valence electrons explicitly
  - The valence-electron Hamiltonian H<sub>v</sub> is:

$$H_{V} = \sum_{i=1}^{N_{V}} h_{i}^{V} + \frac{1}{2} j_{o} \sum_{i,j}^{N_{V}} \frac{1}{r_{ij}}$$

 Most primitive approach = CNDO (Complete Neglect of Differential Overlap)

# What is an Overlap?

$$\Psi = c_1 \phi_1 + c_2 \phi_2$$

$$\frac{\int \Psi^* \widehat{H} \Psi d\tau}{\int \Psi^* \Psi d\tau} = \frac{\int [c_1 \phi_A + c_2 \phi_B] \widehat{H} [c_1 \phi_A + c_2 \phi_B] d\tau}{\int [c_1 \phi_A + c_2 \phi_B]^2 d\tau}$$

$$= \frac{c_1^2 H_{AA} + 2c_1 c_2 H_{AB} + c_2^2 H_{BB}}{c_1^2 S_{AA} + 2c_1 c_2 S_{AB} + c_2^2 S_{BB}}$$
bability
$$= \frac{c_1^2 H_{AA} + 2c_1 c_2 H_{AB} + c_2^2 H_{BB}}{c_1^2 + 2c_1 c_2 S + c_2^2}$$

- H is energy, S probability
- $H_{AA}$  = **Coulomb integral**: interaction energy of  $e^-$  with its' "home" AO
- $H_{AB}$  = **Resonance integral**: interaction energy between orbital A and e<sup>-</sup> of orbital B
- S =Overlap integral:  $\int \phi_1 \phi_2 d\tau$

$$\phi_1$$
  $\phi_2$ 

$$S_{AA} = S_{BB} = 1$$
$$S_{AB} = S_{BA} = S$$

# **Differential Overlap**

- What is a differential overlap?
  - The two-electron repulsion integral
  - Number of orbitals used in calculation = N, number of two-electron repulsion integrals scales as N<sup>4</sup>, but after removing the differential overlaps scales as N<sup>2</sup>
- So, the two-electron integrals are set to zero
- Neglects all 3-centre and 4-centre two-electron integrals
- Pariser-Parr-Pople (PPP) and Complete Neglect of Differential Overlap (CNDO) methods are examples of Zero Differential Overlap (ZDO) approximations

### Intermediate Neglect of Differential Overlap (INDO)

- Intermediate neglect is not applied when A = B = C = D
  - i.e. when all four basis functions are on the same atom.
- These one-centre exchange integrals are important for explaining the splitting between electronic states that comes from the same electronic configuration, so INDO gives vastly improved results over CNDO (especially spectroscopically)
- Although CNDO and INDO give reasonable equilibrium geometries when compared to experiment, they give poor results (as do HF-SCF methods) when compared with experimental quantities such as standard enthalpies of formation
- Methods = INDO, MINDO, ZINDO, SINDO

### **Neglect of Diatomic Differential Overlap (NDDO)**

- From Pople
- Does not apply "ZDO" when A = B and C = D
  - When the basis functions for the first electron are on the same atom and the basis functions for the second electron are on the same atom
- This relies on fact that many of two-electron integrals involving basis functions centered on more than two atoms are very small – so can be neglected
- Gives dramatic computational time saving
- Methods = MNDO, AM1, PM3

### **Modified Neglect of Differential Overlap (MNDO)**

- Tends to give covalent bonds that are too short
- Activation energies too high
- Poorly predicted proton affinities
- Added in additional parameters for nuclear repulsion energy
- Was all done ad hoc, some parameters fitted against a subset of data

# **Austin Model 1 (AM1)**

- MNDO refitted simultaneously against larger set of experimental data
- Dewar developed improved MNDO called Austin model 1 (AM1) named after the University Texas at Austin where it was developed
- Applies Koopmans theorem to get better enthalpies and ionisation energies than MNDO
- But can get some very peculiar geometries for H-bonds

# Parameterisation Model 3 (PM3)

- MNDO refitted again to give Parameterization Model 3 (PM3)
- Is the third parameterisation of the MNDO method
  - version 1 = MNDO, version 2 = AM1
- Gives better bond lengths, ionisation energies and enthalpies of formation than previous two versions
- There are some cases where PM3 is worse than MNDO though
  - E.g. all sp³ nitrogens predicted to be pyramidal!
- PM3 fixed some problems with AM1 but introduced others, so on balance if one method performs very poorly for your set of molecules it is worth trying the other

# Semi Empirical in the Future

- Continues to be developed always room for improvement!
- Current methods do not use d orbitals in their basis sets so rubbish for most d metal compounds
  - Or any p elements where we know d orbitals are important
- Both MNDO and AM1 have had further iterations where attempts to extend parameterisation to include d orbitals:
  - MNDO/d and AM1/d

# **Periodic Boundary Conditions**

#### **Solids**

- An infinite three dimensional-periodic array
- Electronic energy levels are more complicated than isolated molecules
- How can we treat this computationally when we've been previously looking at discrete individual molecules?
- Have to set boundary conditions, similar in the way that crystallography identifies a unit cell, ie. an independent "block" that repeats to make up the macro structure
- Approach is called **Periodic Boundary Conditions** (PBC)

## **Reciprocal Lattice and Brillouin Zone**

- Unit cell = includes all the unique symmetry of a crystal / solid
  - The entire lattice can be built by repetition of the unit cell in three dimensions
  - A repeating "brick" of 7 potential 3D shapes
- Reciprocal lattice = Fourier transformation of the real-space lattice
- Brillouin zone = crystallographic primitive cell in reciprocal space
  - Allows us to classify how waves propagate through a material
  - Relates to allowed lattice vibrations and electronic wave functions

#### **Band Structure**

- Not isolated energy levels
- Is a continuum of <u>occupied orbitals</u> (valence band) and <u>vacant orbitals</u> (conduction band)
  - Collectively called band structure
- Energy gap between the valence and conduction bands defines whether the material is:

Insulator large band gap

Conductor no gap

Semi-conductor intermediate band gap

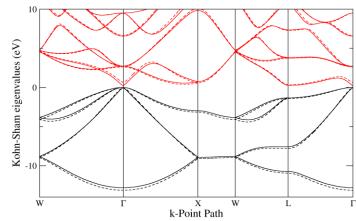
#### k Vectors and Points

- Simplify the 3D Brillouin zone by slicing it to create 2D representations
- k vectors link k points along pathways in the Brillouin zone
  - Generates 2D band structure diagrams
- x-axis is the k vector showing k point positions, y-axis represents energy

Permitted electronic levels correspond to occupied (valence) and

unoccupied (conduction) bands

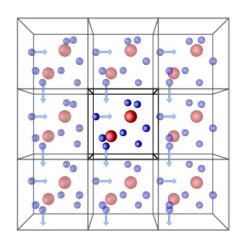
- Γ is the mid-point of the reciprocal lattice
- Band gap is shortest crossing from HOMO to LUMO



http://cmt.dur.ac.uk/sjc/thesis\_dbj/node75.html

# **Setting the Boundaries**

- A calculation on an infinite array of molecules is achieved by just treating the atoms shown in the asymmetric unit of the unit cell
  - All other molecules of the array are replicas of these parts
- Boundaries are "soft"
  - Should an atom cross one of the boundaries it will reappear at the opposite side
  - By its replica moving into the central cell to take its place...
- PBCs stop electrons falling off the end of the model



#### **Plane Waves**

- Electrons modeled as waves propagating through the model using continuous sinusoidal-type functions
  - Called plane waves
- For reciprocal lattice vectors **G**;  $\Psi(r) = \sum_{G} c_{G} \exp(iGr)$ 
  - $c_{\mathbf{G}}$  are basis set weighting coefficients
  - $\exp(i\mathbf{G}r)$  is the representation of a plane wave at any position r
- Collection of plane waves used with different wavelengths to capture the range of electrons and their kinetic energies
  - Slow valence electrons
  - Fast core electrons

#### **Cutoffs**

- The greater the range of plane waves used = better the basis set
- Quality of plane-wave basis set controlled in simulation by defining the energy cut-off
- This is the value chosen so that the lowering of the total energy by the addition of any further plane waves to the basis set is negligible
- Linear combination of plane waves effective in modeling the behaviour of valence electrons
  - Core electron density varies rapidly so require many plane waves to describe the core wavefunction – simplify by using a pseudopotential
- Delocalised basis sets model kinetic energies of valence e<sup>-</sup> and atomic pseudopotential functions to mimic effects of the core e<sup>-</sup>

## **Optimising a Solid-State Structure**

#### Lattice Dynamics

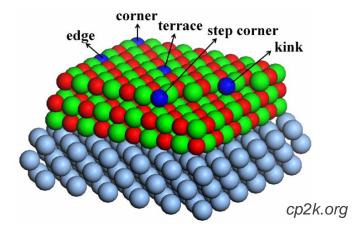
- Harmonic approximation
- Each atom of asymmetric unit is displaced by small amounts from equilibrium position
- Resulting energy points fitted to parabolas to obtain force constants k
- Combine with reduced masses → get harmonic vibrational frequencies

#### Molecular Dynamics

- Convert calculated forces on atoms to velocities and accelerations via Newton's equations of motion
- Simulation generates configurations of the molecular system connected to time
- Statistical treatment leads to time-dependent properties
- Have to manually assign vibrational modes to their symmetry species

#### **Problems with PBC**

- The Slater determinant in Fock-theory applied to plane-wave basis set is very large when approximating  $\widehat{H}$ 
  - Impedes performance of calculation
  - Currently can only use density functional theory
- MD simulation requires manual symmetry assignment to vibrational modes
- Lattice Dynamics assumes that system behaves harmonically



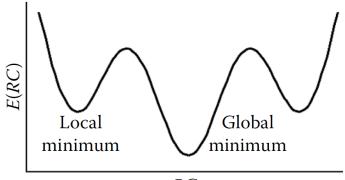
# **Molecular Dynamics**

# **Molecular Dynamics (MD)**

- Molecules are always moving even at the absolute zero of temperature
- Ideally, molecules shouldn't be treated as a collection of static conformations
- Molecular Dynamics aims to simulate movement and motion
- Conformational searches can extract information about which conformer geometries have the lowest energies
  - But would not show if they slowly interconverted
    - ... a long MD simulation would!
- Karplus won the Nobel prize in 2013 for work in this area

# **Conformational Searching**

- Conformational searching will provide a list of the global minimum and local minima
- Populations then described by a Boltzmann distribution
  - Two assumptions:
    - Conformations are in equilibrium
    - 2. Energy barriers to interconversion are high
      - If barriers are low then molecules may spend most of time converting instead of being minima!



#### **Boltzmann Distribution**

 In statistical mechanics this is a <u>probability distribution</u> that gives the probability that a system will be a certain state (*i.e.* conformation) as a function of the state's energy and the temperature of the system

$$p_{i} = \frac{e^{\frac{-\varepsilon_{i}}{kT}}}{\sum_{j=1}^{M} e^{\frac{-\varepsilon_{j}}{kT}}}$$

The denominator is known as the canonical partition function; Q (or Z)

$$p_i = \frac{1}{Q} e^{\frac{-\varepsilon_i}{kT}}$$

 $p_i$  = probability of state i

 $\varepsilon_i$  = energy of state i

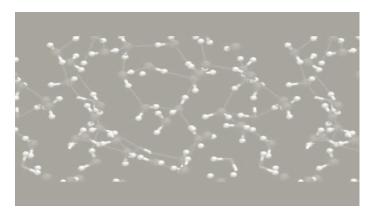
k = Boltzmann constant,

T = temperature of the system

M = number of states accessible to the system

# **Basic Algorithm**

- Divide time into discrete time steps
  - ~ 10<sup>-15</sup> seconds each
- At each step:
  - Compute the forces acting on each atom
  - Move the atoms a little bit
    - Updating the position and velocity of each atoms using Newton's laws of motion



#### **Newton's Laws of Motion**

• First law: The velocity of a body remains constant unless the body is acted upon by an external force  $\sum \pmb{F} = 0 \Rightarrow \frac{d\pmb{v}}{dt} = 0$ 

• Second law: The acceleration, a, of a body is parallel and directly proportional to the net force, F, and inversely proportional to the mass, m

$$\mathbf{F} = m\frac{d\mathbf{v}}{dt} = m\mathbf{a}$$

 Third law: The mutual forces of action and reaction between two bodies are equal, opposite and co-linear

$$\sum \boldsymbol{F}_{a,b} = \sum \boldsymbol{F}_{b,a}$$

# **Equations of Motion**

- Since velocity (v) is the derivative of position (x)
- And acceleration (a) is the derivative of velocity
- We can write the equations of motion as:

$$\frac{d\mathbf{x}}{dt} = \mathbf{v}$$

$$\frac{d\mathbf{v}}{dt} = \frac{F(\mathbf{x})}{m}$$

 For N atoms, we have 3N position coordinates and 3N velocity coordinates

$$\mathbf{x}_{i+1} = \mathbf{x}_i + \delta_t \mathbf{v}_i$$
$$\mathbf{v}_{i+1} = \mathbf{v}_i + \delta_t F(\mathbf{x}_i) / m$$

• Where  $\delta_t$  is the time step

#### **Parameters for MD**

- A starting structure
- The temperature
  - Amount of energy given to the structure depends on the temperature
  - Energy is divided between movement and potential energy
  - Equally divided between all the atoms
- The step size
  - A short time that needs to be shorter than the shortest time in which anything interesting can happen to the molecule!
- The length of the run
  - As long as possible! Depends on the information required...

Give atoms initial positions  $r^{(t=0)}$ , choose short  $\Delta t$ Get forces  $\mathbf{F} = -\nabla V(\mathbf{r}^{(i)})$  and  $\mathbf{a} = \mathbf{F}/m$ Move atoms:  $\mathbf{r}^{(i+1)} = \mathbf{r}^{(i)} + \mathbf{v}^{(i)} \Delta t + \frac{1}{2} \mathbf{a} \Delta t^2 + \dots$ Move time forward:  $t = t + \Delta t$ Repeat as long as you need

#### **Differences between MD and MC**

Property	MD	MC
Basic information needed	Gradient	Energy
Particles moved in each step	All	One
Coordinates	Cartesian	Any
Constraints	Difficult	Easy
Atomic velocities	Yes	No
Time dimension	Yes	No
Deterministic	(Yes)	No
Sampling	Physical	Non-physical
Natural ensemble	NVE	NVT

# **Constant Energy**

- Total energy of the system can change from being mainly kinetic energy (KE) to mainly potential energy (PE)
- At the bottom of a "well" / minimum there state has a high KE and low PE
- Therefore, simulation will spend most of its time in high PE states as they correspond to time when the system is moving slowly
- This is not an ideal description of molecular behaviour
  - Produces a microcanonical ensemble of states:
    - isolated system with constant energy, no energy or mass exchanged with the rest of the universe

## **Constant Temperature**

- Temperature corresponds to system's kinetic energy
- As calculation proceeds more energy is added to cool it down
  - System is in a high energy conformation
- Energy is removed from the system when it heats up
  - System is in a low energy conformation
- Produces a canonical ensemble of states:
  - system in thermal equilibrium, can only exchange heat with the outside

#### Microcanonical Ensemble

- System isolated from changes in moles (N), volume (V) and energy (E).
- Adiabatic process with no heat exchange
- Total energy is conserved exchange of potential and kinetic energy
- For every time-step, each particle's position and velocity may be integrated – giving a trajectory
- Therefore, given the initial positions and velocities, we can calculate all future (or past) positions and velocities
  - N constant number of particles
  - V constant volume
  - E constant Energy
- Temperature of system not fixed



#### **Canonical Ensemble**

- Moles (N), volume (V) and temperature (T) are conserved
- Energy of endothermic and exothermic processes is exchanged with a thermostat
- Probability distribution over microcanonical ensembles
- Energy exchanged with a large reservoir
- Total energy of system and reservoir combined remains constant, given by the Boltzmann distribution
- i.e. a heat bath
- NVT = canonical ensemble
  - N constant number of particles
  - V constant volume
  - T constant temperature



#### Isothermal-Isobaric Ensemble

- Moles (N), pressure (p) and temperature (T) are conserved
- Thermostat and barostat are needed
  - For a constant number of particles either the volume or pressure can be fixed, but not both
- Corresponds to an open flask at ambient temperature and pressure
- For the simulation of biological membranes, isotropic pressure control is not appropriate, and instead either constant membrane area (Np<sub>A</sub>T) or constant surface tension (Np<sub>V</sub>T)



#### **Grand Canonical**

- Volume (V), energy (E) and chemical potential (µ) are conserved
- A constant chemical potential (µ) is incommensurable with a constant number of particles
  - open system, can exchange both energy and mass with the outside



# **Ensembles Summary**

N	р	V	Т	E	μ	Acronym	Equilibrium	Name
X		X	X			NVT	A has minimum	Canonical (MC)
X		X		X		NVE	S has minimum	Micro-canonical (MD)
X	X		X			NpT	G has minimum	Isothermal-Isobaric
		X	X		X	VEμ	(pV) has maximum	Grand-canonical

# **Simulated Annealing**

- Makes random changes to a structure to find global minimum
- Random configuration and velocity for each atom
- Traces the movement of the molecule as the energy is slowly removed
- Works provided energy is removed infinitely slowly
  - More rapid rate of cooling will remove the certainty of success

#### **Molecules in Solution**

- A very large number of solvent molecules are required to solvate even the smallest of systems
- We want to know the solvent's effect on the solute molecule not necessarily all possible arrangements of the system
- To provide useful data we consider a sufficient number of solvent molecule arrangements (a representative sample) produced by MD simulations
- Particularly suited to studying protein conformations or other large molecules

# **Stochastic Dynamics**

- Focus interest on small part of system
  - E.g. active site of a large protein or molecule in a large amount of solvent
- A full MD simulation would take a prohibitively long time so "cheat" by constraining part of the system of lesser interest and only allowing the interesting part to move
- Difficulty is what to do an interface between moving and non-moving parts
  - Hence stochastic dynamics used to transfer energy in this situation

# **MD Summary**

- Molecules are not static but continuously move
  - Closer to reality than extracting information from a forcefield
- Investigates low lying regions of PES not just minima
- Can limit searches to accessible conformations rather than all possible conformations
- Can find entropy (S), free energy (G) as well as internal energy (U)

# **MD Challenges**

- Non-bonded interactions involve weak interactions between all particles in the system, which is normally the bottleneck in speed of MD simulations
- Get temperature-related phenomenon (rises) due to the small number of atoms that are used in MD simulations
  - E.g. when undergoing exothermic conformational changes, binding, or depositions of substrates on surfaces
  - Can cause the substrate to be vaporized in the model
- Complexity prevents it being used for simpler problems, such as conformation analysis of small molecules in vacuo

# Computed vs. Real Life

Lectures 9 and 10 Week 23