

1. a)



b) Using N's Second:

$$F_{\text{net},y} = m a_y$$

$$n_{sc} - W_{Ec} = m a_y$$

$$n_{sc} - mg = m a_y$$

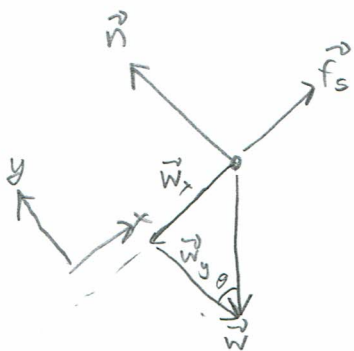
$$\text{Now, } a_y = \frac{v^2}{r}$$

Since the car is moving in a circle, accelerating towards the center,

$$\text{so } n_{sc} - mg = m \frac{v^2}{R}$$

$$\begin{aligned} \Rightarrow n_{sc} &= \frac{mv^2}{R} + mg = m \left(\frac{v^2}{R} + g \right) \\ &= 1000 \text{ kg} \left(\frac{(30 \text{ m/s})^2}{200 \text{ m}} + 9.8 \frac{\text{m}}{\text{s}^2} \right) \\ &= 14300 \text{ N} \end{aligned}$$

2. FBD for Box:



(must be this way to "hold up" the box)

$$W_x = W \sin \theta = mg \sin \theta$$

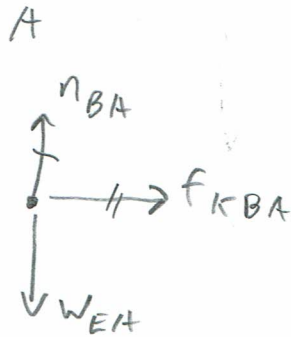
$$W_y = W \cos \theta = mg \cos \theta$$

$$F_{\text{net},x} = f_s - W_x = m a_x = 0 \quad (\text{not moving})$$

$$\begin{aligned} \text{so } f_s &= W_x = mg \sin \theta \\ &= (10 \text{ kg}) \left(9.8 \frac{\text{m}}{\text{s}^2} \right) \sin 20^\circ \\ &= 33.52 \text{ N} \end{aligned}$$

Note that since we know the box is not moving, we know the maximum friction is not exceeded. There is no guarantee $f_{s,\text{max}} = f_s$ here.

3. a)



$$b) \textcircled{1} F_{\text{net}, A, x} = f_{K, BA} = m_A a_{Ax}$$

$$\textcircled{2} F_{\text{net}, A, y} = n_{BA} - W_{EA} = m_A a_{Ay}$$

$$\textcircled{3} F_{\text{net}, B, x} = F - f_{KAB} - f_{KSB} = m_B a_{Bx}$$

$$\textcircled{4} F_{\text{net}, B, y} = n_{SB} - n_{AB} - W_{EB} = m_B a_{By}$$

c) We know a_{Ay} and a_{By} are zero (no vertical motion).

$$\text{so } \textcircled{2} n_{BA} - W_{EA} = 0 \Rightarrow n_{BA} = W_{EA} = m_A g$$

$$\text{so } f_{K, BA} = \mu_K n_{BA} = \mu_K m_A g \quad (\text{between blocks})$$

$$\text{so } \textcircled{1} f_{KBA} = \mu_K m_A g = m_A a_{Ax}$$

$$\Rightarrow a_{Ax} = \mu_K g = 0.18 \text{ m/s}^2$$

$$d) \text{ From } \textcircled{4} n_{SB} - n_{AB} - W_{EB} = 0 \quad (a_{By} = 0)$$

$$\Rightarrow n_{SB} = n_{AB} + W_{EB} = m_A g + m_B g \quad (\text{since } n_{AB} = n_{BA} = m_A g)$$

$$= (m_A + m_B) g$$

$$\text{so } f_{KSB} = \mu_K n_{SB} = 0.3 (m_A + m_B) g. \quad (f_{KAB} = f_{KBA} = \mu_K m_A g \quad \text{bet. blocks})$$

$$\text{From } \textcircled{3} F - f_{KAB} - f_{KSB} = m_B a_{Bx}$$

$$\Rightarrow a_{Bx} = \frac{F - f_{KAB} - f_{KSB}}{m_B} = \frac{F - 0.1 m_A g - 0.3 (m_A + m_B) g}{m_B}$$

$$= \frac{40 \text{ N} - 0.1 (3 \text{ kg}) (9.8 \text{ m/s}^2) - 0.3 (7 \text{ kg}) (9.8 \text{ m/s}^2)}{4 \text{ kg}}$$

$$= 4.12 \text{ m/s}^2$$