f(x) is increasing if and only if
f(x) is decreasing if and only if
f(x) is concave up if and only if $f''(x)$
f(x) is concave down if and only if $f''(x)$
f(x) is concave down if and only if $f'(x)$
f(x) is concave up if and only if $f'(x)$
f(x) has an inflection point at $x = c$ if and only if $f''(x)$
f(x) has an inflection point at $x = c$ if and only if $f'(x)$
First Derivative Test:
f(x) has a relative minimum if and only if $f'(x)$
f(x) has a relative maximum if and only if $f'(x)$
Second Derivative Test:
f(x) has a relative minimum at $x = c$ because $f'(c) = $ and $f''(c)$
f(x) has a relative maximum at $x = c$ because $f'(c) = $ and $f''(c)$