

The following table gives the values of a differentiable function  $f$ , and its derivative  $f'$  at given values of  $x$ .

$x$	$f$	$f'$
1	2	$\frac{1}{2}$
2	3	1
3	4	2
4	6	4

If  $g(x)$  is the inverse function of  $f(x)$ , then what is the value of  $g'(4)$  ?

(a) $\frac{1}{6}$	(b) $\frac{1}{4}$	(c) $\frac{1}{3}$	(d) $\frac{1}{2}$	(e) 2
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If  $f(x) = x^3 - 3x^2 + 8x + 5$  and  $g(x) = f^{-1}(x)$ , then  $g'(5) =$

(a) 8	(b) $\frac{1}{8}$	(c) 1	(d) $\frac{1}{53}$	(e) 5
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If  $g(x)$  is the inverse function of  $f(x)$ , then what is the value of  $g'(4)$  ?

$$\begin{aligned}
 g'(4) &= (f^{-1})'(4) \\
 &= \frac{1}{f'(\text{whatever makes } f(x)=4)} && f(x)=4 \text{ when } x=3 \\
 &= \frac{1}{f'(3)} \\
 &= \frac{1}{2}
 \end{aligned}$$

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$$g'(5) = (f^{-1})'(5)$$

$$= \frac{1}{f'(\text{whatever makes } f(x) = 5)}$$

$$f(x) = x^3 - 3x^2 + 8x + 5$$

$$5 = x^3 - 3x^2 + 8x + 5$$

$$0 = x^3 - 3x^2 + 8x$$

$$0 = x(x^2 - 3x + 8)$$

↓

$$x = 0$$

$$f(x) = x^3 - 3x^2 + 8x + 5$$

$$f'(x) = 3x^2 - 6x + 8$$

$$f'(0) = 8$$

$$g'(5) = (f^{-1})'(5)$$

$$= \frac{1}{f'(\text{whatever makes } f(x) = 5)}$$

$$= \frac{1}{f'(0)}$$

$$= \frac{1}{8}$$

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