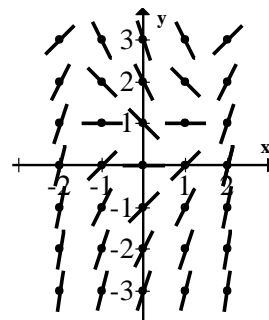


1. Which of the following differential equations matches the slope field at right?

(a)  $\frac{dy}{dx} = x + y^2$       (b)  $\frac{dy}{dx} = x - y^2$       (c)  $\frac{dy}{dx} = xy$   
 (d)  $\frac{dy}{dx} = x + y$       (e)  $\frac{dy}{dx} = x^2 - y$



2. **(Calculator Required):** A cup of coffee is heated to boiling ( $212^\circ\text{F}$ ), and taken out of a microwave and placed in a  $72^\circ\text{F}$  room at time  $t = 0$  minutes. The coffee cools at the rate of  $16e^{-0.112t}$  degrees Fahrenheit per minute. To the nearest degree, what is the temperature of the coffee at time  $t = 5$  minutes?

(a)  $105^\circ\text{F}$       (b)  $133^\circ\text{F}$       (c)  $166^\circ\text{F}$       (d)  $151^\circ\text{F}$       (e)  $203^\circ\text{F}$

3. The table below gives values of the differentiable functions  $f$  and  $g$  at  $x = -1$ . If

$$h(x) = \frac{f(x) - g(x)}{2f(x)}, \text{ then } h'(-1) =$$

$x$	$f(x)$	$g(x)$	$f'(x)$	$g'(x)$
-1	-2	4	$e$	-3

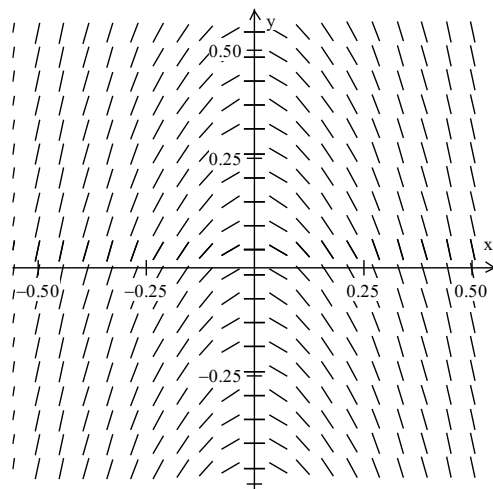
(a)  $\frac{-e-3}{4}$       (b)  $\frac{e+3}{2e}$       (c)  $\frac{e-6}{8}$       (d)  $\frac{2e-3}{4}$       (e)  $\frac{-4e-3}{4}$

4. If  $f(x)$  is an antiderivative of  $\frac{\sin^2 x}{x^2 + 2}$  such that  $f(2) = \frac{1}{2}$ , then  $f(0)$  is given by

(a)  $\int_0^2 \frac{\sin^2(x)}{x^2 + 2} dx$       (b)  $\int_2^0 \frac{\sin^2(x)}{x^2 + 2} dx$       (c)  $\frac{1}{2} + \int_2^0 \frac{\sin^2(x)}{x^2 + 2} dx$   
 (d)  $\frac{1}{2} + \int_0^2 \frac{\sin^2(x)}{x^2 + 2} dx$       (e)  $2 + \int_2^0 \frac{\sin^2(x)}{x^2 + 2} dx$

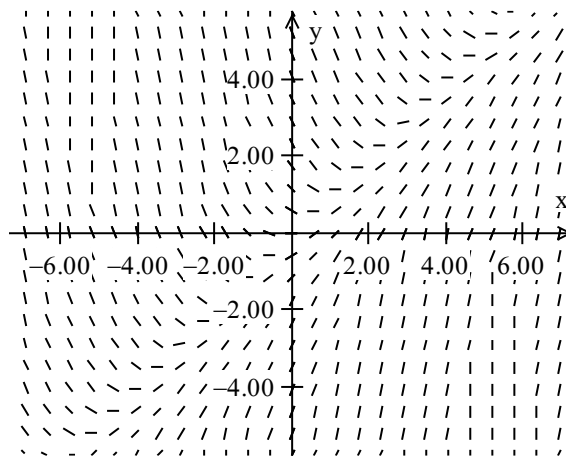
5. Shown at right is the slope field of a differential equation. Which of the following could be a solution to the differential equation?

(a)  $y = e^x$   
 (b)  $y = x^3$   
 (c)  $y = -5x^2$   
 (d)  $y = x$   
 (e)  $y = x^2$

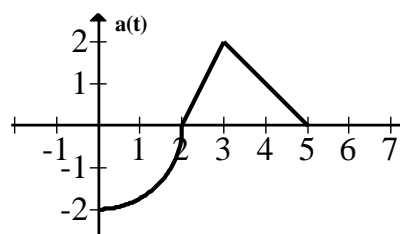


6. Which of the following differential equations is represented by the slope field at right?

- (a)  $\frac{dy}{dx} = 1 + y^2$   
 (b)  $\frac{dy}{dx} = x - y$   
 (c)  $\frac{dy}{dx} = 2x^2$   
 (d)  $\frac{dy}{dx} = 1 + x^2$   
 (e)  $\frac{dy}{dx} = 1 - y^2 + x^2$

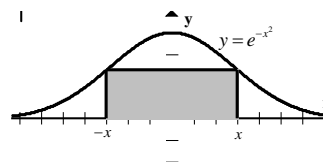


7. The graph at right shows an object's acceleration in  $\frac{\text{ft}}{\text{sec}^2}$ . It consists of a quarter circle, and two line segments. If the object was at rest at  $t = 5$  seconds, what was its initial velocity?



- (a)  $-2 \frac{\text{ft}}{\text{sec}}$       (b)  $3 - \pi \frac{\text{ft}}{\text{sec}}$       (c)  $0 \frac{\text{ft}}{\text{sec}}$       (d)  $\pi - 3 \frac{\text{ft}}{\text{sec}}$       (e)  $\pi + 3 \frac{\text{ft}}{\text{sec}}$

8. The area of the largest rectangle that can be drawn with one side along the  $x$ -axis and two vertices on the curve  $y = e^{-x^2}$  is



- (a)  $\sqrt{\frac{2}{e}}$       (b)  $\sqrt{2e}$       (c)  $\frac{2}{e}$       (d)  $\frac{1}{\sqrt{2e}}$       (e)  $\frac{2}{e^2}$

9. What is  $y$  if  $\frac{dy}{dx} = \frac{3x+2}{5y}$  and  $y = 1$  when  $x = 2$ ?

- (a)  $y = \sqrt{\frac{3x^2 + 4x - 15}{5}}$       (b)  $y = \pm \sqrt{\frac{3x^2 + 4x - 15}{5}}$       (c)  $y = \sqrt{\frac{3x^2 + 4x + 13}{5}}$   
 (d)  $y = \pm \sqrt{\frac{3x^2 + 4x}{5}}$       (e)  $y = \sqrt{\frac{3x^2 + 4x}{5}}$

10. Let  $\frac{dy}{dx} = e^{x-y}$ . Which of the following is the solution to this differential equation with the condition that  $y(0) = 1$ ?

- (a)  $y = \ln(x)$       (b)  $y = \ln(e^x + e)$       (c)  $y = x$       (d)  $y = e^x$       (e)  $y = \ln(e^x + e - 1)$