

Choose the axis at the left so that F_L creates no torque

$$\tau_{\text{net}} = \underbrace{(2\text{m} \cdot F_r)}_{\text{CCW}} - \underbrace{(0.5\text{m} \cdot M_g)}_{\text{CW, so negative}} - \underbrace{(1\text{m} \cdot m_g)}_{\text{CW, so negative}} = 0 \quad \text{Static equilibrium}$$

$$\Rightarrow F_r = \frac{0.5\text{m} \cdot M_g + 1\text{m} \cdot m_g}{2\text{m}} = 17.15\text{N}$$

And now $F_{\text{net},y} = F_L + F_r - M_g - m_g$

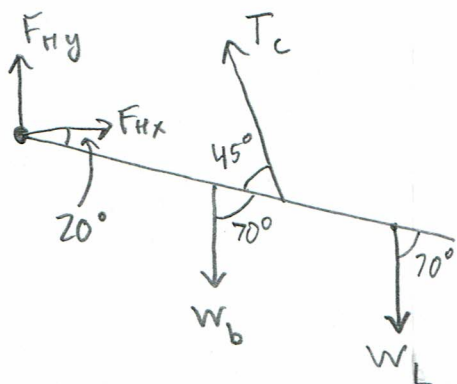
$$\Rightarrow F_L = M_g + m_g - F_r = 31.85\text{N}$$

It makes sense, given that the "extra" mass M is to the left, that $F_L > F_r$.

By choosing our axis at the location of F_L , we got a torque equation with only one unknown. This is a helpful strategy.

Practice Problems solutions,

1. Take our system to be the bridge plus sir lost-a-lot
a) Take the pivot at the hinge as shown.



$$\tau_c = r_c T_c \sin \theta_c \quad \text{where } r_c = 5 \text{ m}, \theta_c = 45^\circ$$

$$\tau_b = r_b W_b \sin \theta_b = r_b m_b g \sin \theta_b$$

$$\text{where } r_b = 4.0 \text{ m (cm of bridge)}$$

$$\theta_b = 70^\circ, m_b = 2000 \text{ kg}$$

$$\tau_L = r_L W_L \sin \theta_L = r_L m_L g \sin \theta_L$$

$$\text{where } r_L = 8 \text{ m} - 1 \text{ m} = 7 \text{ m}$$

$$m_L = 1000 \text{ kg} \quad \theta_L = 70^\circ$$

The 70° angles are the complement of the 20° angle.

Equilibrium requires $\tau_{\text{net}} = 0 = \tau_c - \tau_b - \tau_L$

$$\Rightarrow 0 = r_c T_c \sin \theta_c - r_b m_b g \sin \theta_b - r_L m_L g \sin \theta_L$$

$$\Rightarrow T_c = \frac{r_b m_b g \sin \theta_b + r_L m_L g \sin \theta_L}{r_c \sin \theta_c} = \frac{(4 \text{ m})(2000 \text{ kg})(9.8 \text{ m/s}^2) + (7 \text{ m})(1000 \text{ kg})(9.8 \text{ m/s}^2)}{(5 \text{ m}) \sin 45^\circ}$$

$$= \frac{4 \text{ m} \cdot 2000 \text{ kg} \cdot 9.8 \text{ m/s}^2 \cdot \sin 70^\circ + 7 \text{ m} \cdot 1000 \text{ kg} \cdot 9.8 \text{ m/s}^2 \cdot \sin 70^\circ}{5 \text{ m} \cdot \sin 45^\circ}$$

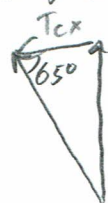
$$= 39070 \text{ N.}$$

- b) Now $F_{\text{net}, y} = 0$ and $F_{\text{net}, x} = 0$ because this is static equilib.

We have to find the components of T_c . This is a tad tricky - what direction is T_c ?

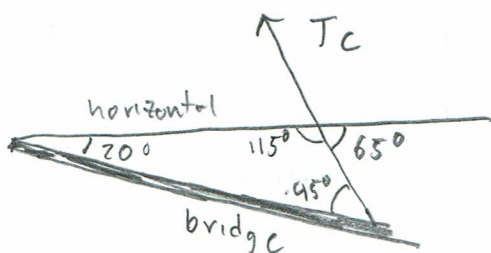
Some geometry shows that T_c is at an angle of 65° from the horizontal.

so



$$T_{cy} = T_c \sin 65^\circ = 35409 \text{ N}$$

$$T_{cx} = T_c \cos 65^\circ = 16512 \text{ N}$$



1b, continued.

$$\text{So } F_{\text{net}, x} = F_{Hx} - T_{cx} = 0$$

$$\Rightarrow F_{Hx} = T_{cx} = 16512 \text{ N}$$

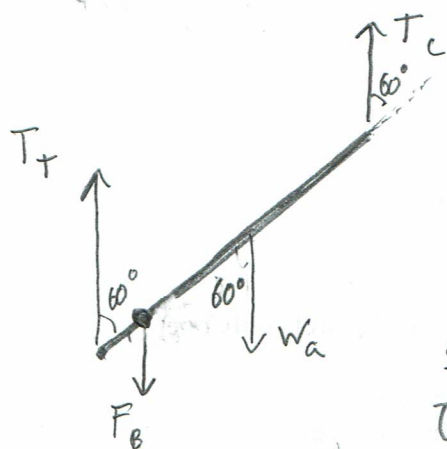
$$F_{\text{net}, y} = F_{Hy} + T_{cy} - W_b - W_L$$

$$\Rightarrow F_{Hy} = W_b + W_L - T_{cy} = m_b g + m_L g - T_{cy}$$

$$F_{Hy} = -6009 \text{ N}$$

The negative here indicates we guessed wrong about the direction of F_{Hy} . In fact, it is downwards with a force of 6009 N.

2. Consider the arm to be the system, and the point where the bones touch the pivot,



$$\tau_c = r_c T_c \sin \theta_c, \text{ and } r_c = 0.35 \text{ m}, T_c = m_w g$$

$$\text{and } \theta_c = 60^\circ$$

$$\tau_T = r_T T_T \sin \theta_T, \text{ and } r_T = 0.025 \text{ m}, \theta_T = 60^\circ$$

$$\tau_a = r_a W_a \sin \theta_a, \text{ and } r_a = 0.15 \text{ m}, \theta_a = 60^\circ$$

$$\text{and } W_a = m_a g$$

Since it's equilibrium

$$\tau_{\text{net}} = 0 = \tau_c - \tau_a - \tau_T$$

not = this is CW, so negative

The 60° angles complement the 30° angle.

$$\Rightarrow 0 = r_c T_c \sin \theta_c - r_a W_a \sin \theta_a - r_T T_T \sin \theta_T$$

$$\Rightarrow T_T = \frac{r_c m_w g \sin 60^\circ - r_a m_a g \sin 60^\circ}{r_T \sin 60^\circ}$$

$$T_T = \frac{(0.35 \text{ m})(15 \text{ kg})(9.8 \text{ m/s}^2) - (0.15 \text{ m})(2.0 \text{ kg})(9.8 \text{ m/s}^2)}{0.025 \text{ m}}$$

$$= 1940.4 \text{ N.} \quad \text{A big force!}$$



to find the force from the bone ~~one~~ downwards,
recall that

$F_{\text{net},y} = 0$ in equilibrium and so

$$F_{\text{net},y} = T_c + T_T - F_B - W_a = 0$$

$$\Rightarrow F_B = T_c + T_T - W_a = 0$$

$$= (15 \text{ kg})g + 1940.4 \text{ N} - (2 \text{ kg})(g)$$

$$= \cancel{2066} \text{ N} \quad \text{also a big force!}$$

$$2067$$
