Limits at ±∞

Examples:
$$\lim_{x \to \infty} \frac{5x^{\frac{3}{2}}}{4x^{2} + 1} \sim \lim_{x \to \infty} \frac{5x^{\frac{3}{2}}}{4x^{2}} \quad \lim_{x \to \infty} \frac{3x^{3} - 1}{3 - 2x} \sim \lim_{x \to \infty} \frac{3x^{3}}{-2x} \quad \lim_{x \to \infty} \frac{-3x + 1}{\sqrt{x^{2} + x}} \sim \lim_{x \to \infty} \frac{-3x}{\sqrt{x^{2}}}$$

$$= \lim_{x \to \infty} \frac{5}{4x^{\frac{1}{2}}} \quad = \lim_{x \to \infty} \frac{-3x}{|x|}$$

$$= \lim_{x \to \infty} \frac{-3x}{-x} \text{ since } |x| = \begin{cases} x & x \ge 0 \\ -x & x < 0 \end{cases}$$

$$= \lim_{x \to \infty} (3)$$

$$= -3$$