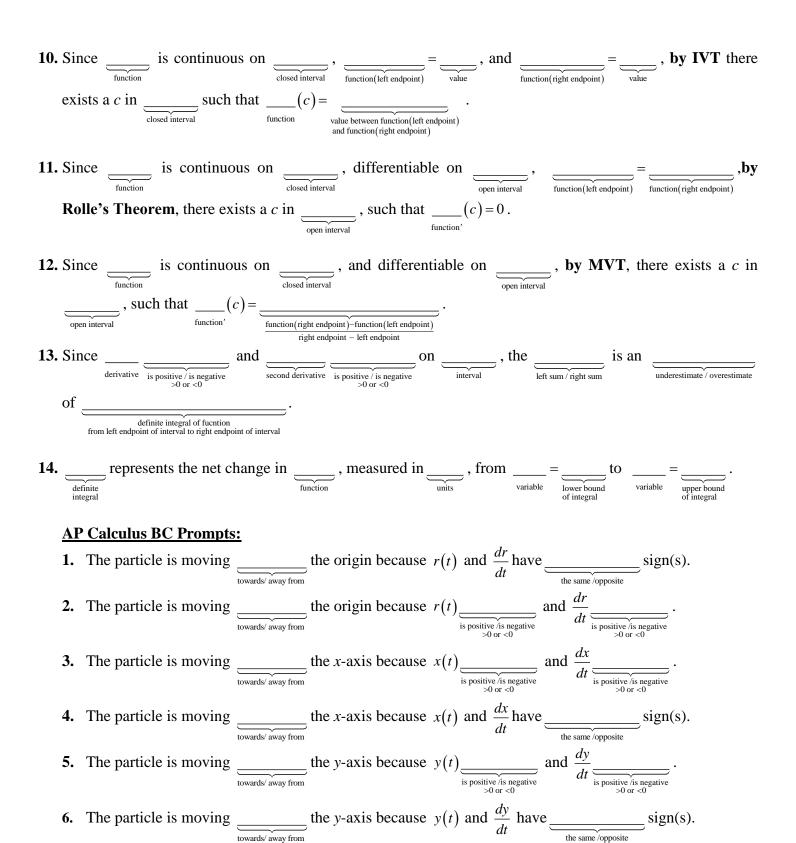
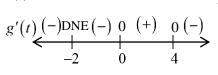
AP Calculus AB/BC Writing Prompts

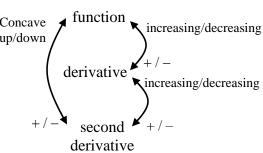
- 1. $\underbrace{\text{function}}$ is continuous at $\underbrace{\text{variable}}$ = $\underbrace{\text{value}}$ because $\underbrace{\text{lim}}_{\text{variable}}$ = $\underbrace{\text{function}}$ =
- 2. _____ is not continuous at ____ = ____ because $\begin{cases} \lim_{\text{variable}} \neq \\ \lim_{\text{variable}} \Rightarrow \\ \lim_{\text{variabl$
- $\textbf{4.} \ \ \, \underbrace{ \text{is}}_{\text{function}} \text{is} \underbrace{ \text{increasing/decreasing}}_{\text{increasing/decreasing}} \text{on} \underbrace{ \text{interval}}_{\text{interval}} \text{because} \underbrace{ \text{derivative is negative is negative}}_{\text{is positive is negative}} .$

- - (b) ____ has an inflection point at ___ = ____ because ____ changes from _____ decreasing to increasing or the control of the
- 8. The speed of the object is on increasing on interval because of the object is one of the speed of t
- 9. The speed of the object is $\underbrace{\text{increasing/decreasing}}$ at $\underbrace{\text{variable}} = \underbrace{\text{value}}$ because $\underbrace{\text{velocity funtion}}_{\text{at value}} \underbrace{\text{is positive/is negative}}_{\text{>0 or < 0}}$ and $\underbrace{\text{acceleration funtion}}_{\text{at value}}$.



1. What can you conclude about g(t) from the given sign chart? Concave f function increasing/decreasing





(+)→(−)

g(t) is continuous on $\underbrace{\hspace{1cm}}_{\text{interval}}$ and $\underbrace{\hspace{1cm}}_{\text{interval}}$ because $\underbrace{\hspace{1cm}}_{\text{function}}$ is differentiable on $\underbrace{\hspace{1cm}}_{\text{interval}}$ and $\underbrace{\hspace{1cm}}_{\text{interval}}$.

function interval interval
$$g(t)$$
 is increasing on interval because function $g(t)$ is increasing on interval $g(t)$ derivative is positive / is negative $g(t)$ is positive / is negative $g(t)$ or $g(t)$ increasing $g(t)$ interval $g(t)$

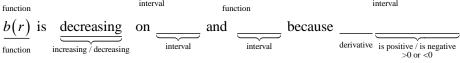
$$g(t)$$
 is decreasing on interval, and interval because derivative is positive/is negative interval.

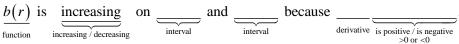
$$\underbrace{g\left(t\right)}_{\text{function}} \text{ has a relative } \underbrace{\min_{\min / \max}}_{\text{min } / \max} \text{ at } \underbrace{\underbrace{-}_{\text{variable}}}_{\text{variable}} = \underbrace{\underbrace{-}_{\text{value}}}_{\text{value}} \text{ because } \underbrace{-}_{\text{derivative}} \text{ changes sign from } \underbrace{\underbrace{-}_{\text{negative to positive } \atop \text{negative to negative to negative }}}_{\text{positive to negative to negative }} .$$

$$\frac{g(t)}{\text{function}} \text{ has a relative } \underbrace{\max_{\min / \max}} \text{ at } \underbrace{\underbrace{\max_{\text{variable}}}} = \underbrace{\underbrace{\max_{\text{value}}}} \text{ because } \underbrace{\underbrace{\max_{\text{derivative}}}} \text{ changes sign from } \underbrace{\underbrace{\max_{\text{negative to positive } (-) \to (+)}}_{\text{positive to negative to negative }}}$$

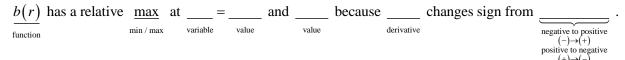
2. What can you conclude about b(r) given the graph of b'(r) below?

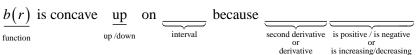
 $\underline{b(r)}$ is continuous on $\underline{\mathbb{R}}$ because $\underline{b(r)}$ is differentiable on $\underline{\mathbb{R}}$.





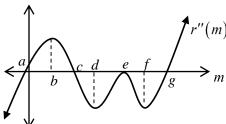






$$\frac{b(r) \text{ is concave } \underline{\text{down}}}{\text{function}} \text{ on } \underbrace{\frac{\text{down on }}{\text{up/down}}}_{\text{up/down}} \text{ on } \underbrace{\frac{\text{derivative}}{\text{interval}}}_{\text{interval}} \text{ because } \underbrace{\frac{\text{derivative}}{\text{second derivative}}}_{\text{second derivative}} \underbrace{\frac{\text{is positive/is negative}}{\text{or } \text{or } \text{$$

3. What can you conclude about r(m) or r'(m) from the graph of r''(m) below?



- r'(m) is continuous on $\underline{\mathbb{R}}$ because r'(m) is differentiable on $\underline{\mathbb{R}}$.
- $\underline{r(m)}$ is continuous on $\underline{\mathbb{R}}$ because $\underline{r(m)}$ is differentiable on $\underline{\mathbb{R}}$.
- r'(m) is increasing on and interval because derivative is positive is negative interval because
- r'(m) is decreasing on interval, and interval because derivative is positive/is negative is positive/is negative so or <0
- $\frac{r'(m)}{\text{function}} \text{ has a relative } \underline{\min} \text{ at } \underline{\underline{\quad \text{min / max} \quad \text{variable} \quad \text{value} \quad \text{value}}} = \underline{\underline{\quad \text{and} \quad \underline{\quad \text{because} \quad \text{derivative}}}} \text{ because } \underline{\underline{\quad \text{changes sign from}}} \underbrace{\underline{\quad \text{negative to positive for negative in positive to negative}}}_{\text{positive to negative}}$
- $\frac{r'(m)}{\text{function}} \text{ has a relative } \underbrace{\max_{\min / \max}}_{\text{min / max}} \text{ at } \underbrace{\underset{\text{variable}}{=}}_{\text{value}} = \underbrace{\underset{\text{derivative}}{\longrightarrow}}_{\text{derivative}} \text{ changes sign from } \underbrace{\underset{\substack{\text{negative to positive } \\ (-) \to (+) \\ \text{positive to negative}}}}_{\text{negative to negative}}.$
- r(m) is concave up on and interval and second derivative is positive/is negative solver to r(m) is concave up/down interval and interval because second derivative is positive/is negative solver to r(m) is positive/is negative solver to r(m) or r(m) is concave up/down interval.
- r(m) is concave $rac{down}{up/down}$ on $rac{down}{up/down}$, $rac{down}{up/down}$,
- $\underline{r(m)}$ has an inflection point at $\underline{} = \underline{}$, $\underline{}$, and $\underline{}$ because $\underline{\underline{}}$ changes sign function $\underline{}$ because $\underline{\underline{}}$ changes sign $\underline{}$
- **4.** A particle is moving along the x-axis so that its position at time-t seconds is given by the following graph. The graph of x(t) has points of inflection at
 - t = 5, t = 7, and t = 9.5.
 - (a) For what interval(s) of t is the particle moving to the right? Justify your answer.
 - (b) For what interval(s) of t is the particle moving to the left? Justify your answer.
 - (c) At what time(s), if any, does the particle change direction? Justify your answer.
 - (d) Identify the interval(s) of t for which the particle's speed increasing. Justify your answer.
 - (e) Identify the interval(s) of t for which particle's speed decreasing? Justify your answer.

x(t)

1. What can you conclude about g(t) from the given sign chart?

$$g'(t) \xrightarrow{(-)DNE(-)} 0 \xrightarrow{(+)} 0 \xrightarrow{(-)}$$

$$\underbrace{\frac{g\left(t\right)}{\text{function}}} \text{ is continuous on } \underbrace{\underbrace{\begin{cases} \left(-\infty,-2\right) \cup \left(-2,\infty\right)}_{\text{interval}}}_{\text{function}} \text{ because } \underbrace{\frac{g\left(t\right)}{\text{function}}}_{\text{function}} \text{ is differentiable on } \underbrace{\begin{cases} \left(-\infty,-2\right) \cup \left(-2,\infty\right)\\t<-2 \text{ and } t>-2\end{cases}}_{\text{interval}}.$$

$$\frac{g\left(t\right)}{\text{function}} \text{ is } \underbrace{\frac{\text{increasing}}{\text{increasing} / \text{decreasing}}}_{\text{increasing / decreasing}} \text{ on } \underbrace{\left\{ \begin{array}{c} \left(0,4\right) \\ 0 < t < 4 \end{array} \right\}}_{\text{interval}} \text{ because } \underbrace{\frac{g'(t)}{\text{derivative}}}_{\text{is positive / is negative}} \underbrace{\left\{ \begin{array}{c} \text{is positive} \\ > 0 \end{array} \right\}}_{\text{is positive / is negative}}$$

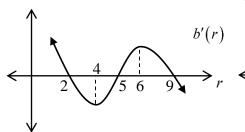
$$\frac{g(t)}{\text{function}} \text{ is } \underbrace{\frac{\text{decreasing}}{\text{increasing} / \text{decreasing}}}_{\text{increasing}} \text{ on } \underbrace{\left\{ \frac{(-\infty, -2) \cup (-2, 0) \cup (4, \infty)}{t < -2, -2 < t < 0, \text{ and } t > 4} \right\}}_{\text{interval}}_{\text{because}} \text{ because } \underbrace{\frac{g'(t)}{\text{derivative}}}_{\text{is positive} / \text{is negative}}_{\text{is positive} / \text{is negative}}.$$

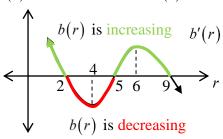
$$\frac{g(t)}{\text{function}} \text{ has a relative } \underbrace{\min_{\text{min/max}}} \text{ at } \underbrace{\frac{t}{\text{variable}}} = \underbrace{\frac{0}{\text{value}}} \text{ because } \underbrace{\frac{g'(t)}{\text{derivative}}} \text{ changes sign from } \underbrace{\underbrace{\frac{\left(-\right) \rightarrow (+)}{\left(-\right) \rightarrow (+)}}_{\text{negative to positive on equative}}} \underbrace{\frac{\left(-\right) \rightarrow (+)}{\left(-\right) \rightarrow (+)}}_{\text{positive to negative to negative}}$$

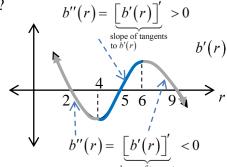
$$\frac{g\left(t\right)}{\text{function}} \text{ has a relative } \underbrace{\frac{\text{max}}{\text{min / max}}}_{\text{min / max}} \text{ at } \underbrace{\frac{t}{\text{variable}} = \underbrace{\frac{4}{\text{value}}}}_{\text{because }} \underbrace{\frac{g'\left(t\right)}{\text{derivative}}}_{\text{derivative}} \text{ changes sign from } \underbrace{\underbrace{\left\{\begin{array}{c} \text{positive to negative}}\\ \left(+\right) \rightarrow \left(-\right) \\ \end{array}\right\}}_{\text{negative to positive }}_{\substack{\left(-\right) \rightarrow \left(-\right)\\ \left(+\right) \rightarrow \left(-\right)}}_{\substack{\text{negative to negative}}}$$

 $(+)\rightarrow (-)$

2. What can you conclude about b(r) given the graph of b'(r) below?



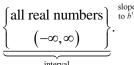




b(r) is continuous on function

$$\underbrace{\left\{ \begin{array}{c} \text{all real numbers} \\ \left(-\infty,\infty\right) \end{array} \right\}}_{}$$

because b(r) is differentiable on



b(r) is increasing function increasing / decreasing

on
$$\underbrace{\left\{ \begin{array}{c} (-\infty, 2) \cup (5, 9) \\ r < 2 \text{ and } 5 < r < 9 \end{array} \right\}}_{\text{interval}}$$

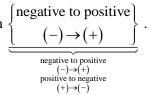
is positive / is negative

$$\frac{b(r)}{\text{function}}$$
 is $\underbrace{\text{decreasing}}_{\text{increasing}/\text{decreasing}}$ on

on
$$\underbrace{\begin{cases} (2,5) \cup (9,\infty) \\ 2 < r < 5 \text{ and } r > 9 \end{cases}}_{\text{interval}}$$

is positive / is negative >0 or <0

b(r) has a relative <u>min</u> at <u>r</u> = <u>5</u> because b'(r) changes sign from min / max variable value function derivative



function

$$\frac{\text{max}}{\text{max}}$$
 at $\frac{r}{\text{variable}} = \underbrace{2 \text{ and } 9}_{\text{value}}$

b(r) has a relative max at r = 2 and 9 because b'(r) changes sign from derivative

positive to negative negative to positive

 $(-)\rightarrow(+)$ positive to negative $(+)\rightarrow (-)$

function

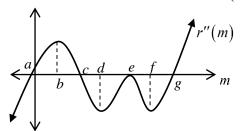
e
$$\underbrace{b''(r)}_{\text{second derivative}} \underbrace{\begin{cases} \text{is positive} \\ > 0 \end{cases}}_{\text{is positive / is negative}}$$

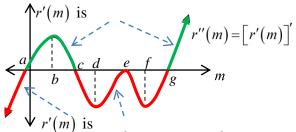
function

down on
$$\underbrace{\begin{cases} (-\infty,4) \cup (6,\infty) \\ r < 4 \text{ and } r > 6 \end{cases}}_{\text{interval}}$$

$$\frac{b''(r)}{\text{second derivative}} \underbrace{\begin{cases} \text{is negative} \\ < 0 \end{cases}}_{\text{is positive / is negative}}.$$

3. What can you conclude about r(m) or r'(m) from the graph of r''(m) below?

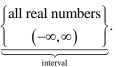




r'(m) is continuous on function

$$\underbrace{\begin{cases} \text{all real numbers}}_{\text{interval}} \right]^{-1}$$

because r'(m) is differentiable on function



r(m) is continuous on function

$$\underbrace{\begin{cases} \text{all real numbers} \\ (-\infty, \infty) \end{cases}}_{\text{interval}}$$

because r(m) is differentiable on function

$$\underbrace{\left\{\begin{array}{c} \text{all real numbers} \\ \left(-\infty,\infty\right) \end{array}\right\}}_{\text{interval}}.$$

r'(m) is increasing on function increasing / decreasing

$$1 \underbrace{\frac{\left(a,c\right) \cup \left(g,\infty\right)}{a < m < c \text{ and } m > g}}_{\text{interval}}$$

because r''(m)is positive / is negative >0 or <0

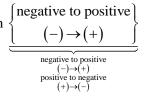
$$\underline{r'(m)} \text{ is } \underbrace{\frac{\text{decreasing}}{\text{function}}}_{\text{function}} \text{ on } \underbrace{\begin{bmatrix} (-\infty, a) \cup (c, e) \cup (e, g) \text{ or } (c, g) \\ m < a, c < m < e, \text{ and } e < m < g \\ \text{or } c < m < g \end{bmatrix}}_{\text{increasing}}$$

because r''(mis positive / is negative

function

$$\underline{\min}_{\min/\max}$$
 at $\underline{m}_{\text{variable}} = \underline{a} \text{ and } \underline{s}$

$$r'(m)$$
 has a relative min/max at $m/max = a$ and a because $m/max = a$ the derivative $min/max = a$ and a because $m/max = a$ the derivative $min/max = a$ the derivative $min/max = a$ and a because $min/max = a$ the derivative $min/max =$



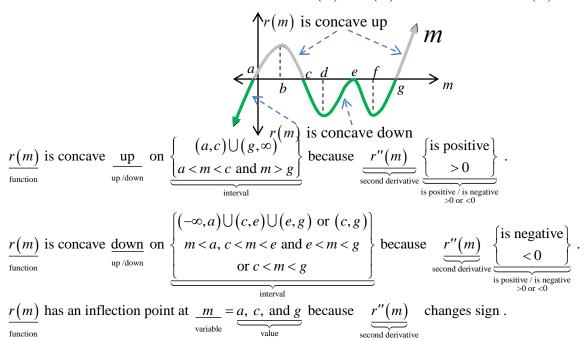
function

$$\frac{\text{max}}{\text{min / max}}$$
 at $\frac{m}{\text{variable}} = \frac{c}{\text{value}}$

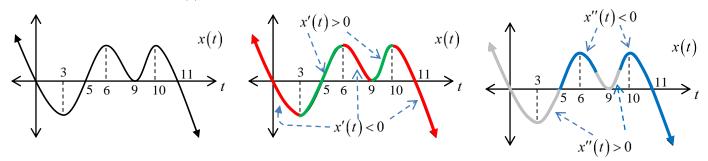
$$\frac{r'(m)}{f_{\text{unction}}}$$
 has a relative $\frac{\text{max}}{\text{min/max}}$ at $\frac{m}{\text{variable}} = \frac{c}{\text{value}}$ because $\frac{r''(m)}{\text{derivative}}$ changes sign from

positive to negative
$$(+) \rightarrow (-)$$
negative to positive
$$(-) \rightarrow (+)$$
positive to negative
$$(+) \rightarrow (-)$$

What can you conclude about the graph of r(m) or r'(m) from the graph of r''(m) below?



4. A particle is moving along the x-axis so that its position at time-t seconds is given by the following graph. The graph of x(t) has points of inflection at t = 5, t = 7, and t = 9.5.



(a) For what interval(s) of t is the particle moving to the right? Justify your answer.

The particle is moving to the right on $\begin{cases} (3,6) \cup (9,10) \\ 3 < t < 6 \text{ and } 9 < t < 10 \end{cases} \text{ because } x'(t) \text{ } \begin{cases} \text{is positive} \\ > 0 \end{cases}.$

(b) For what interval(s) of t is the particle moving to the left? Justify your answer.

The particle is moving to the left on $\begin{cases} (-\infty,3) \cup (6,9) \cup (10,\infty) \\ t < 3, \ 6 < t < 9, \ \text{and} \ t > 10 \end{cases}$ because x'(t) $\begin{cases} \text{is negative} \\ < 0 \end{cases}$.

(c) At what time(s), if any, does the particle change direction? Justify your answer.

The particle changes direction at t = 3, 6, 9, and 10 because x'(t) changes sign.

(d) Identify the interval(s) of t for which the particle's speed increasing. Justify your answer.

The particle's speed is increasing on $\begin{cases} (3,5) \cup (6,7) \cup (9,9.5) \cup (10,\infty) \\ 3 < t < 5, \ 6 < t < 7, \ 9 < t < 9.5 \text{ and } t > 10 \end{cases}$ because x'(t) and x''(t) have the same sign.

(e) Identify the interval(s) of t for which particle's speed decreasing? Justify your answer.

The particle's speed is decreasing on $\begin{cases} (-\infty,3) \cup (5,6) \cup (7,9) \cup (9.5,10) \\ t < 3, \ 5 < t < 6, \ 7 < t < 9, \ \text{and} \ 9.5 < t < 10 \end{cases}$ because x'(t) and x''(t) have opposite signs.