

3-6

$$2. \frac{1}{x} (x \cdot \ln x - x) = \frac{x}{x} + \ln x - 1 \\ = \ln x$$

$$3. \frac{2}{x} \sin(\ln x) = \cos(\ln x) \cdot \frac{1}{x}$$

$$4. \ln(\sin^2 x) = \frac{1}{\sin^2 x} \cdot 2(\sin^2 x) \cdot \cos x$$

$$5. \ln\left(\frac{1}{x}\right) = \ln(x^{-1}) = \frac{1}{x^{-1}} \cdot -x^{-2} \cdot 1$$

$$6. \frac{1}{\ln x} = (\ln x)^{-1} = -1(\ln x)^{-2} \cdot \frac{1}{x}$$

$$7. \log_{10}(x^3 + 1) = \frac{1}{\ln 10 \cdot (x^3 + 1)}$$

$$8. \log_5(xe^x) = \frac{1}{\ln 5 \cdot (xe^x)} \cdot (xe^x + e^x)$$

$$9. \sin x \cdot \ln(5x) = \frac{1}{5x} \cdot \sin x + \cos x \ln(5x)$$

$$10. \frac{v^3}{1 + \ln v} \quad \frac{1 + \ln v - \frac{1}{v} \cdot v}{(1 + \ln v)^2} = \frac{\ln v}{(1 + \ln v)^2}$$

$$11. \ln(x\sqrt{x^2-1}) = \frac{1}{(x\sqrt{x^2-1})} \cdot \left(\frac{1}{2\sqrt{x^2-1}} \cdot x + \sqrt{x^2-1} \right)$$

$$12. \ln(x + \sqrt{x^2-1}) = \frac{1}{x + \sqrt{x^2-1}} \cdot \left(1 + \left(\frac{1}{2\sqrt{x^2-1}} \cdot 2x \right) \right)$$

$$13. \ln\left(\frac{(2y+1)^5}{\sqrt{y^2+1}}\right) = \frac{\sqrt{y^2+1}}{(2y+1)^5} \cdot 5(2y+1) \cdot \left(\frac{1}{2\sqrt{y^2+1}} \cdot 2 \cdot (2y+1) \right)$$

$$15. \ln(\ln(s)) = \frac{1}{\ln s} \cdot \frac{1}{s}$$

Ex. 39

$$(x^2+2)^2 (x^4+4)^4 = y$$

$$\ln(y) = \ln((x^2+2)^2 \cdot (x^4+4)^4)$$

$$\ln(y) = 2 \ln(x^2+2) + 4 \ln(x^4+4)$$

$$\begin{aligned} \frac{1}{y} &= 2 \cdot \frac{1}{x^2+2} \cdot 2 + 4 \cdot \frac{1}{x^4+4} \cdot 4x^3 \\ &= \left(\frac{4}{x^2+2} + \frac{16x^3}{x^4+4} \right) y \end{aligned}$$

$$41. \ln y = \ln((x-1)/(x^4+1))$$

$$\ln y = \frac{1}{2} \cdot (\ln(x-1) - \ln(x^4+1))$$

$$\frac{d}{dy} \frac{1}{y} = \frac{1}{2} \left(\frac{1}{x-1} - \frac{1}{x^4+1} \cdot 4x^3 \right)$$

$$= \frac{1}{2} \left(\frac{1}{x-1} - \frac{4x^3}{x^4+1} \right)$$

43,

$$y = x^x \Rightarrow \ln y = x \ln x$$

$$\frac{1}{y} = \frac{1}{x} \cdot x + \ln x$$

$$= (1 + \ln x) y$$

45,

$$y = x^{\sin x} \Rightarrow \ln y = \sin x \cdot \ln x$$

$$\frac{1}{y} = \frac{1}{x} \cdot \sin x + \cos x \ln x$$

$$= \left(\frac{\sin x}{x} + \cos x \ln x \right) y$$