

1. AP Calculus AB 2004 #5 (No Calculator)

- $g(0) = 3 + (3 \cdot 1)/2 = 4.5$, $g'(0) = f(0) = 1$
- There is a relative maximum at $x=3$ on the open interval $(-5,4)$ because f changes from positive to negative.
- Candidates for the absolute minimum value of g on the closed interval $[-5,4]$ are the endpoints and relative minimums. The candidates are $x=-5,-4,4$.
 $g(-5) = 1 - 1 = 0$
 $g(-4) = \int_{-3}^{-4} f(t) dt = -(2/2) = -1$
 $g(4) = \int_{-3}^0 f(t) dt + \int_0^2 f(t) dt + 0 = 4.5 + (-\pi + 4)/2$
 Therefore, the absolute minimum value of g on the closed interval is -1 .
- On the open interval $(-5,4)$, g has a point of inflection on $x=-3,1,2$

2. AP Calculus AB 2007 #4 (No Calculator)

- On the domain $(-5,5)$, f has a relative maximum at $x=-3,4$ because f' changes from positive to negative at $x=-3,4$.
- f has points of inflection at $x=-4,-1,2$ because f' changes from increasing to decreasing or vice versa at $x=-4,-1,2$.
- f is concave up and has a positive slope when f' is positive and increasing. The intervals of f that are concave up and have a positive slope are $(-5,-4)$ and $(1,2)$.
- On the interval $[-5,5]$, Candidates for the absolute minimum value are the endpoints and relative minimums. There is a relative minimum at $x=1$ because f' goes from negative to positive at $x=1$. Our candidates are $-5,1,5$.

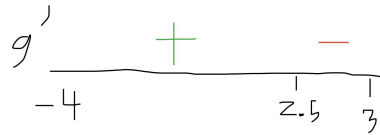
$$f(-5) = 3 + \left(\int_1^{-5} f'(x) dx \right) = (-\pi/2 + 2\pi) + 3$$

$$f(1) = 3$$

$$f(5) = 3 + \left(\int_1^5 f'(x) dx \right) = (2/2 + 4/2 - 1/2) + 3$$

3. AP Calculus AB 2011 #4 (No Calculator)

- $g(-3) = \int_0^{-3} -6 = -6 - (3^2 \pi)/4$
 $g'(x) = 2 + f(x)$
 $g'(-3) = 2 + f(-3) = 2$
- Candidates for the absolute maximum on the interval $[-4,3]$ are the endpoints and the relative maximum(s). There is a relative maximum on g



at $x=2.5$.

Because g was increasing from $(-4, 2.5)$ and decreasing from $(2.5, 3)$, $x=2.5$ is the absolute maximum of g .

- c. On the interval $(-4, 3)$, g has a point of inflection at $x=0$ because g' goes from increasing to decreasing at $x=0$.

- d. The average rate of change of f on the interval $[-4, 3]$ is

$$\frac{f(3) - f(-4)}{3 - (-4)} = -2/7.$$

MVT only works when a function is differentiable on its domain. f is not differentiable at $x=0$.