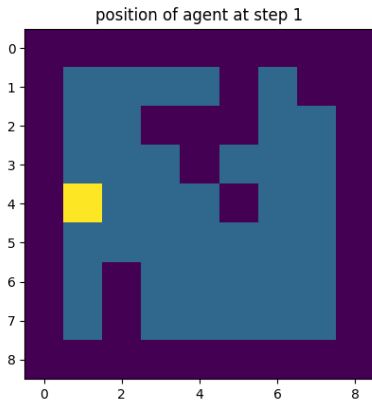


# Machine learning II, unsupervised learning and agents: reinforcement learning



- ▶ RL has many applications and is quite a hot topic.
- ▶ **Deep Reinforcement Learning** has received a lot of attention recently.

► Atari games



Figure – [Mnih et al., 2013]

## ► AlphaGo

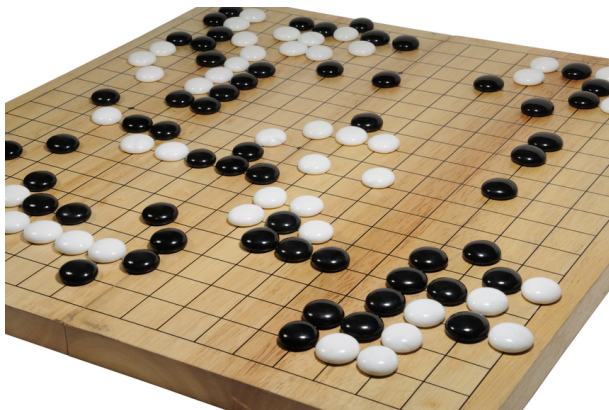


Figure – Go game, beaten by AlphaGo in 2017 [Silver et al., 2016]

- ▶ Reinforcement Learning is also being used in the community of **Computational neuroscience**.

# Overview

Presentation of Reinforcement Learning

The framework

- Supervised learning

- Reinforcement learning

Dynamic programming

Value Iteration

Policy iteration

Discussion

- Temporal Difference learning

- Additional considerations

## Supervised learning and Correction

- ▶ In **supervised learning**, the supervisor indicates the **expected answer** the agent should give.
- ▶ The feedback does not depend on the action performed by the agent (for instance the prediction from the agent)

## Supervised learning and Correction

- ▶ In **supervised learning**, the supervisor indicates the **expected answer** the agent should give.
- ▶ The feedback does not depend on the action performed by the agent (for instance the prediction from the agent)
- ▶ We say that the agent receives an **instructive feedback**.



## Supervised learning Correction

- ▶ In **supervised learning**, the supervisor indicates the **expected answer** the agent should give.
- ▶ The agent must then **correct its model** based on this answer.

## Cost sensitive learning

- ▶ In **Cost sensitive learning**, the situation is different.
- ▶ The agent receives an **evaluative feedback**. The feedback depends on the action performed by the agent.

## Cost sensitive learning

- ▶ In **Cost sensitive learning**, the situation is different.
- ▶ The agent receives an **evaluative feedback**. The feedback depends on the action performed by the agent.
- ▶ **Examples :**
  - ▶ AI playing a game and receiving "victory" or "defeat" as a feedback.
  - ▶ Child playing with an animal.

# Reinforcement learning

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# Reinforcement learning

- ▶ **Reinforcement learning** is a particular case of cost-sensitive learning.
- ▶ In reinforcement learning, the feedback is a **real number**.
- ▶ **Example** : amount of coins won after a poker turn.

# Reinforcement learning

- ▶ First, the agent does not know if a reward is good or bad *per se*.
- ▶ A reward of  $-10$  can be good or bad depending on the other rewards that are possible to obtain !

## Reinforcement learning

- ▶ First, the agent does not know if a reward is good or bad per se.
- ▶ A reward of  $-10$  could be good or bad depending on the other rewards that are possible to obtain.
- ▶ Most of the time, the objective of the agent will be to optimize the **agregation of rewards**.



## Reinforcement learning

- ▶ The agent lives in a world  $E$ , and can be in several states  $s$ .  
The agent performs **actions**  $a$  and receives rewards  $r$ .

# Reinforcement learning

- ▶ The agent lives in a world  $E$ , and can be in several states  $s$ .  
The agent performs **actions**  $a$  and receives rewards  $r$ .
- ▶ **Examples :**
  - ▶ world =  $\mathbb{R}^2$
  - ▶ state = position
  - ▶ actions = moving somewhere
  - ▶ reward = amount of food found

# Formalization

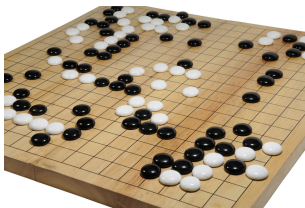
- ▶ There are many aspects of the problem that we need to formalize. Several formalizations are possible depending on the situation.

## Formalization

- ▶ There are many aspects of the problem that we need to formalize. Several formalizations are possible depending on the situation.
- ▶ We will consider **discrete spaces** :
  - ▶ the time will be discrete
  - ▶ the number of possible states will be **finite**
  - ▶ the number of possible actions will be **finite**
- ▶ Continuous spaces are also available for RL. In those cases the objects are slightly different, and the optimization procedures also differ. For an introductory course, discrete spaces are more suitable.

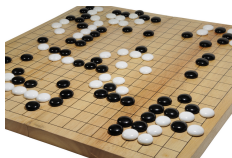
## Question

- ▶ We will consider **discrete spaces** :
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  - ▶ the number of possible states will be **finite**
  - ▶ the number of possible actions will be **finite**
- ▶ Are these hypotheses valid in the case of AlphaGo ?



## Question

- ▶ We will consider **discrete spaces** :
  - ▶ the time will be discrete
  - ▶ the number of possible states will be **finite**
  - ▶ the number of possible actions will be **finite**
- ▶ Are these hypothesis valid in the case of AlphaGo ?



- ▶ Yes! This shows that discrete spaces can still describe very complex problems.

# Formalization

- ▶ we will write :
  - ▶  $s_t$  : state at time  $t$
  - ▶  $a_t$  : action performed at time  $t$
  - ▶  $r_t$  : reward received at time  $t$
- ▶ how is the action chosen ?

## Let us continue with the formalization

- ▶ we will write :
  - ▶  $s_t$  : state at time  $t$
  - ▶  $a_t$  : action performed at time  $t$
  - ▶  $r_t$  : reward received at time  $t$
- ▶ the actions are chosen according to a **policy**  $\pi$



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- ▶ The policy  $\pi$  is a function of the current state.
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- ▶ The policy  $\pi$  is a function of the current state.
- ▶ It can be **deterministic** : the action chosen is chosen with probability 1.
- ▶ Or **stochastic** : the action performed in a given state is drawn from a **distribution**.

## Two levels of randomness

- ▶ The policy can be deterministic or stochastic.
- ▶ But the result of an action could also be stochastic! This is called a **stochastic transition function**.

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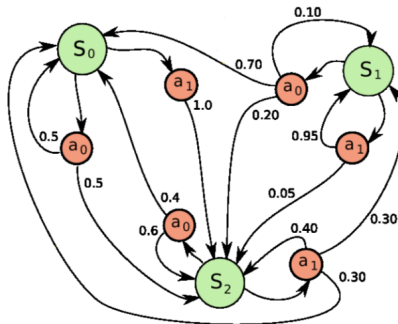


Figure – A stochastic policy with a stochastic transition function.

## Exercise 1 :

- What is the probability of staying in state  $S_0$  when performing an action from  $S_0$  ? and from  $S_1$  and  $S_2$  ?

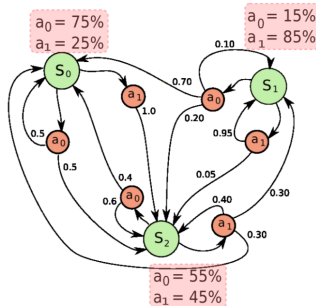


Figure – A stochastic policy with a stochastic transition function.

## Agregation of rewards

- ▶ Remember that our agent want to optimize the **agregation of the rewards**.
- ▶ There are several ways to agregate the rewards.

## Value function : episodic case

- ▶ If the *horizon* is finite (number of steps in the simulation), we can compute the *value function* of the policy  $\pi$ , (assuming the actions are always taken according to  $\pi$ )

$$V^{\pi}(s_0) = r_0 + \dots + r_N \quad (1)$$

- ▶  $s_0$  to the state and  $V$  to the *value*.

## Value function : episodic case

- ▶ If the *horizon* is finite, we can take the sum

$$V^{\pi}(s_0) = r_0 + \cdots + r_N \quad (2)$$

- ▶ We could also average a window. For instance a window of size 3 :

$$V^{\pi}(s_0) = \frac{r_0 + r_1 + r_2}{3} \quad (3)$$



## Value function : general case

- ▶ if the horizon is infinite, the **discount factor**  $\gamma \in [0, 1[$  weights the rewards  $r_k$

$$V^\pi(s_0) = \sum_{t=t_0}^{+\infty} \gamma^{t-t_0} r_t \quad (4)$$

## More considerations

- ▶ The Markov hypothesis
- ▶ Exploitation exploration compromise

## $\epsilon$ -greedy policy

A way to tackle the exploitation-exploration compromise.

- ▶ with probability  $1 - \epsilon$  : go to the best known reward (exploitation).
- ▶ with probability  $\epsilon$  : perform a random action (exploration).

# Art

"RL is a science, but dealing with the exploration-exploitation compromise is an art" (Sutton)

# Dynamic programming

- ▶ Today we will study a simple case of Reinforcement learning
- ▶ Deterministic transition function.

## World

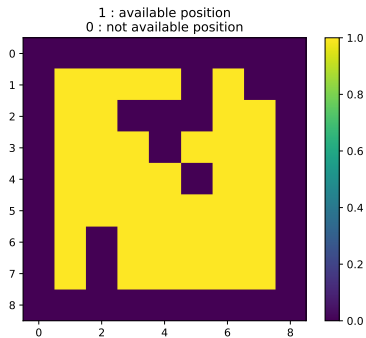


Figure – 2 dimensional world.

## Reward

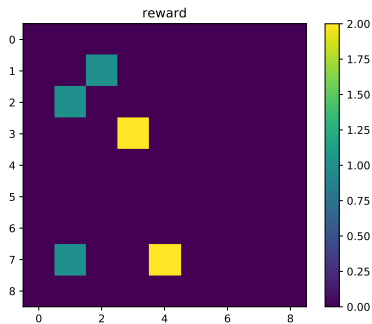


Figure – Reward function.

## 2D world

- ▶ Our agent can move in the 4 directions, one step at a time.
- ▶ We will progressively build an agent that learns to evaluate the states and then learns how to go to the best state.



## Optimal policy

We look for the value of the **optimal policy**  $\pi^*$  .

$$V^*(s_0) = \max_{(a_t)_{t \in [0, +\infty]}} \sum_{t=0}^{\infty} \gamma^t R(s_t, a_t) \quad (5)$$

In the previous equation,  $V^*$  means that we assume that we always take actions according to the policy  $\pi^*$ .

$R(s_t, a_t)$  is the reward of doing action  $a_t$  in state  $s_t$ .

## Bellman optimality equation

### Exercise 2 :

- For each state  $s_0$ ,

$$V^*(s_0) = \max_{(a_t)_{t \in [0, +\infty]}} \sum_{t=0}^{\infty} \gamma^t R(s_t, a_t) \quad (6)$$

- Can you express  $V(s_0)$  as a function of  $V(s_1)$ ?

## Bellman optimality equation

$$V^*(s_0) = r(s_0) + \max_a \left[ \gamma V^*(s_1(a)) \right] \quad (7)$$

with  $s_1(a)$  being the state reached when choosing the action  $a$  in state  $s_0$ .

This is one of the many forms of Bellman equations (see the Sutton book.)

## Value Iteration

Value iteration belongs to dynamic programming methods. They differ from RL in that a perfect model of the environment is assumed.

These methods are however building blocks for RL.

# Value Iteration

- ▶ First, the initial Value function for all the states is 0.

## Value Iteration

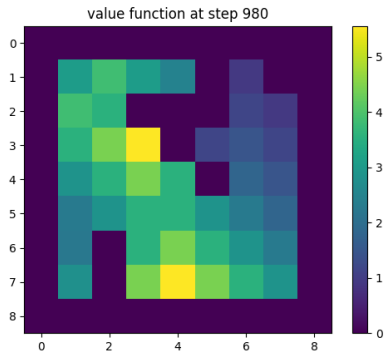
- ▶ First, the initial Value function for all the states is 0.
- ▶ Then we propagate the information about the rewards between the states, in order to **update the value function**
- ▶ We can find an optimal policy in the following way :

$$\forall s \in V(s_t) \leftarrow r(s_t) + \max_{a_t} (\gamma V(s_{t+1})) \quad (8)$$

( $s_{t+1}$  depends on  $a_t$ ).

## Value iteration

- After learning, we will obtain a value function



- ▶ `cd reinforcement_learning/`
- ▶ Use the file `create_world.py` in order to generate your own environment.
- ▶ You can also use the one that is already there if you prefer.
- ▶ We store the data about the world in `.npy` files.



### Exercise 3 :

- ▶ In `value_iteration.py`, modify the function `move_agent()` so that the agent is randomly moved at each time step.

### Exercise 4 :

- ▶ In `value_iteration.py`, modify the function `update_value_function()` in order to update the value function according to the Bellman equation, and run the algorithm until convergence of the value function.

### Exercise 5 :

- ▶ Use the file **value\_iteration\_policy** in order to design an optimal policy for our agent.

## Optimal policy

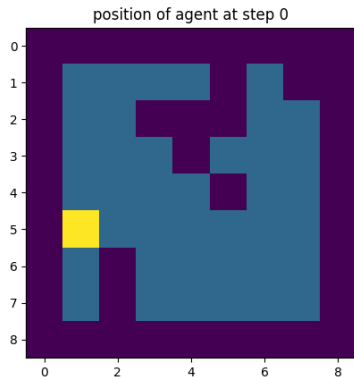


Figure – After learning the optimal policy, the agent can go to the reward.

## Optimal policy

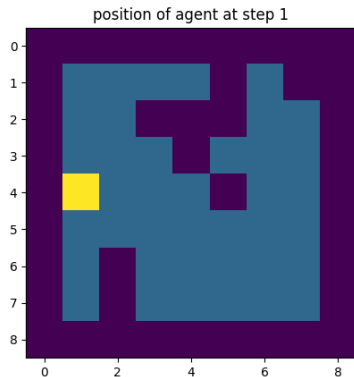


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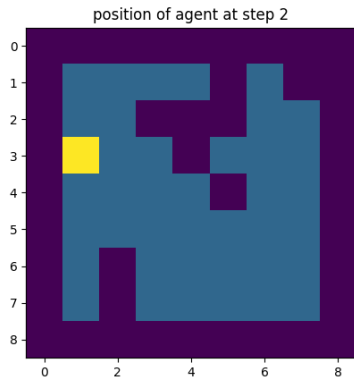


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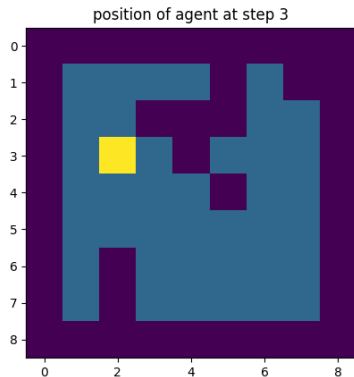


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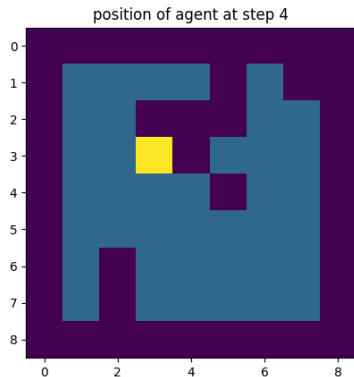


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## Optimal policy

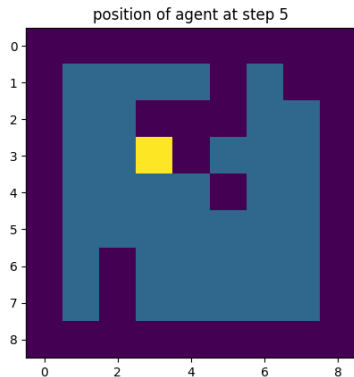


Figure – After learning, the agent can go to the reward.

## Multiple paradigms

- ▶ Reinforcement learning has many variants.
- ▶ In the ones we studied, a model of the consequence of our actions was known.
- ▶ This is not always the case.

## Temporal difference learning

- ▶ In temporal difference learning, the agent does not know a **model** of its world.
- ▶ But it can still learn the value function with the **TD updates**

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- ▶ In temporal difference learning, the agent does not know a **model** of its world.
- ▶ But it can still learn the value function with the **TD updates**

$$V(S_t) \leftarrow V(S_t) + \alpha[R_{t+1} + \gamma V(S_{t+1}) - V(S_t)] \quad (9)$$

## Monte Carlo methods

Monte Carlo methods can be used in Reinforcement Learning to estimate the expected values of some random variables (such as the expected reward in a given state).

## Actor critic methods

- ▶ Sometimes you can use **two** policies
  - ▶ the **behavior policy** provides actions and guarantees exploration
  - ▶ the **target policy** is the optimal policy learned in parallel by the agent, that would be used in exploitation mode.

## Tabular case and continuous case

- ▶ We studied **finite** (and thus discrete situations).
- ▶ However, RL can also be applied to continuous state / discrete action spaces (DQN).

## Tabular case and continuous case

- ▶ We studied **finite** (and thus discrete situations).
- ▶ However, RL can also be applied to continuous state / discrete action spaces (DQN)
- ▶ And even to continuous state / continuous action spaces (DDPG) [Bengio, 2009] .



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