

Cheese Engine

A Chess Engine with NNUE Evaluation

Chess: A Zero-Sum Game

What is Zero-Sum?

One player's gain = other's loss.

White wins (+1), Black loses (-1). Total: zero.

Why Can't We Solve It?

- Legal positions: 10^{44}
- Possible games: 10^{120} (Shannon Number)

Compare: Checkers solved with 5×10^{20} positions (2007)

Perfect Information

Both players see entire board.

No hidden cards, no dice, no luck.

We need smarter ways to explore the game tree

Exploring the Game Tree

We can't explore every position, so we need:

Search Algorithm

How to traverse the tree efficiently

Evaluation Function

How to score positions we reach

Negamax

Deterministic depth-first search with pruning

MCTS

Probabilistic sampling with statistics

Negamax Search

Core Insight

In a zero-sum game:

$$\max(a, b) = -\min(-a, -b)$$

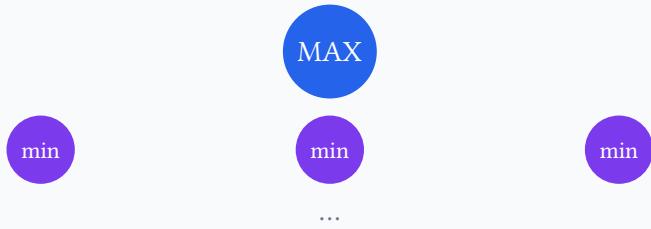
Your best move = opponent's worst outcome. Just negate scores!

Alpha-Beta Pruning

Track best scores for both players. Skip branches that can't affect result.

Reduces $O(b^d)$ to $O(b^{\frac{d}{2}})$ in best case!

Game Tree



Monte Carlo Tree Search (MCTS)

1. Select

UCT formula balances explore vs exploit

$$\text{UCT} = \frac{Q}{N} + c\sqrt{\ln \frac{N_p}{N}}$$

2. Expand

Add child node for unexplored move

3. Evaluate

Score position with eval function

4. Backprop

Update stats back to root

Pros

- Works well with neural network eval
- Naturally handles uncertainty
- Used by AlphaZero

Cons

- Slower in tactical positions
- Needs many iterations
- Memory intensive

Why Negamax for Chess is Hard

Branching factor: 35 moves/position At depth 6: $35^6 = 1.8$ billion nodes!

We need heuristics to prune effectively:

Iterative Deepening

Search depth 1, then 2, then 3... Use shallow results to order deeper search.

Move Ordering

Try best first: TT move, captures, killers, history heuristic.

Transposition Tables

Cache positions by hash. Same position via different moves? Reuse!

Quiescence Search

Don't stop in "noisy" positions. Extend for captures until quiet.

Evaluation: Simple Approaches

Material Counting

Sum piece values:

P=100 N=320 B=330 R=500 Q=900

Simple but misses positional nuance

Piece-Square Tables

Position-based bonuses:

- Knights love the center
- Rooks love open files
- King hides early, advances late

Separate midgame & endgame tables

Extra heuristics: Passed pawns (+), Doubled pawns (-), Bishop pair (+), King safety...

NNUE: Neural Networks for Chess

What Makes NNUE Special?

NNUE = Efficiently Updatable Neural Network Originally from Shogi (Yu Nasu, 2018)

Standard Neural Network

Every evaluation requires:

- Full forward pass
- All weights \times all inputs
- $789 \times \text{hidden_size}$ multiplications
- **Expensive!**

NNUE Approach

Exploit incremental changes:

- Most inputs unchanged between moves
- Update only what changed
- **Massive speedup!**

Key insight: A move only changes 2-4 pieces on the board

NNUE Architecture vs Standard MLP

Input Encoding (789 features)

768 Piece-square (12 pieces × 64 squares)

4 Castling rights

16 En passant squares

1 Side to move

The Sparsity Trick

768 features, but only 32 pieces! **95%+ are zero**

Network Structure

Input: 789 (sparse)



Hidden layers



Output: 1

(position score)

NNUE: Why CPU Beats GPU

Accumulator Technique

Maintain running sum of active features:

$$\text{acc} = \mathbf{W}[\text{piece1}] + \mathbf{W}[\text{piece2}] + \dots$$

On each move:

- Subtract: removed piece contribution
- Add: new position contribution

No full forward pass needed!

Why Not GPU?

- Batch size = 1 (single position)
- GPU excels at large batches
- Memory transfer overhead
- CPU cache faster for small ops

SIMD Acceleration

- AVX2/AVX-512 parallel ops
- 8-16 values at once
- Perfect for accumulator

Result: Millions of evaluations per second on CPU

Implementation in Cheese Engine

Search: Negamax

- Alpha-beta with PVS
- Iterative deepening (depth 1-4)
- 16M entry transposition table
- Aspiration windows

Move Ordering: TT → Captures → Killers → History

Tech Stack

Rust, chess crate, ort (ONNX Runtime), UCI protocol

Evaluation Options

1. **Material counting**
 - Simple piece sum
2. **Piece-Square Tables**
 - Phase-interpolated
3. **NNUE**
 - 789-dim neural network

Also: MCTS

Alternative search with UCT, 4000 iterations/move

Conclusion & Future Work

Chess AI = Search + Evaluation

NNUE bridges classical heuristics with neural networks,
enabling strong play without expensive hardware.

Key Takeaways

- Chess too complex to solve completely
- Smart heuristics make search tractable
- Sparse inputs enable CPU-friendly nets

Future Directions

- Deeper search with better pruning
- Time management optimization
- Train stronger NNUE models

Thank you!