

Design and Analysis of Algorithm

Tutorial 1

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Q.1 : Asymptotic notations are languages that allows us to analyze an algorithm's running time by identifying its behaviour as the input size of algorithm.

Types :

i) Big O : It is commonly used for worst case, and gives us upper bound for the growth rate of runtime algorithm.

eg : Big O notation for linear search is $O(n)$

ii) Big Omega : It is notation used for best case complexity, it provides us with an asymptotic lower bound.

eg : Big Omega of linear search is $\Omega(1)$

iii) Theta: It is used for tight bound on the growth rate of runtime of an algorithm.

eg. Theta of linear search is $\Theta(n)$

iv) small Θ : It is used to denote the upper bound (i.e not asymptotically tight).

$$f(n) = O(g(n)) \quad \forall f(n) < C(g(n)) \quad \text{where } C > 0$$

v) small Omega: To denote lower bound that is asymptotically tight.

Q.2: for ($i = 1$ to n)

{

$$i = i * 2$$

}

Time Complexity - $O(\log n)$

Q.3: $T(n) = 3T(n-1)$

$$T(1) = 1$$

$$T(2) = 3T(2-1) = 3T$$

$$T(3) = 3T(3-1) = 9T$$

$$T(4) = 3T(4-1) = 27T$$

!

$$T(n) = 3^{n-1}T(1)$$

Time Complexity: $O(3^n)$

Q.4. $T(n) = 2(T(n-1) - 1)$

$$T(n-1) = 2T(n-2) - 1$$

$$T(n) = 4T(n-2) - 2 - 1$$

$$T(n-2) = 2T(n-3) - 1$$

$$T(n) = 8T(n-3) - 4 - 2 - 1$$

$$T(n-3) = 2T(n-4) - 1$$

$$T(n) = 16T(n-4) - 8 - 4 - 2 - 1$$

$$T(n) = 2^k \dots 2^3 - 2^2 - 2^1 - 2^0$$

Time Complexity : $O(1)$

Q.5. `int i=1, s=1;`

`while (s <= n)`

`{`

`i++;`

`s = s + i;`

`printf("#");`

`}`

s	i
---	---

1	1
---	---

3	2
---	---

6	3
---	---

10	4
----	---

Time Complexity : $O(\sqrt{n})$

Q.6. void function (int n)

{

int i, count = 0;

for (i = 1; i * i <= n; i++)

count++;

}

$i * i = n$

$i^2 = n$

$i = \sqrt{n}$

Time complexity : $O(\sqrt{n})$

Q.7. void function (int n) {

int i, j, k, count = 0

for (i = n/2; i <= n; i++)

for (j = 1; j <= n; j = j * 2)

for (k = 1; k <= n; k = k * 2)

count++;

}

Time Complexity - $O(n \log^2 n)$

Q.8. function (int n) {

int (n == 1) return;

for (i = 1 to n) {

for (j = 1 to n) {

print ("*");


```
function(n-3);  
}
```

Time Complexity : $O(n)$

```
Q.9. void function(int n)  
{  
    for(i=1 to n)  
    {  
        for(j=1; j<=n; j++)  
            printf("x");  
    }  
}
```

Time Complexity : $O(n \log n)$

Q.10. n^k is $O(C^n)$ as for example

It we take $n=2$, $k=2$, $C=2$

Then $2^2 \leq 2^2$

So, C^n is upper limit of n^k .

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