Name: Shikhar Sahu

Roll No: 74

Sec: A

Semester: 5

Shift: 1

# **Explanation and Thoughts:**

I've used the **backtracking + recursion + DFS** approach for this question.

We apply depth first search first for each node to all the nodes that are connected to that node.

We keep a visited hash map. It keeps track of all the nodes that we have traversed.

We also keep a Path vector. It stores the path of the cycle.

As we go deeper into the recursion tree, we push elements to the back of the path vector and insert elements to the visited set.

As we come out of the recursion tree, we pop elements back from the path vector and also erase that element from the visited set.

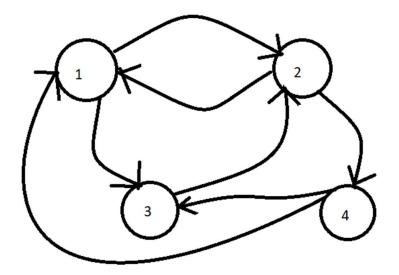
In the recursion, we check if there is possibility to return to the initial node, if it possible, then the graph is a partial cyclic graph.

If the number of elements in the partial cyclic graph is equal to the number of elements in graph + 1, then the cycle is a complete cycle.

**Now, for the discussion of test cases:** I've used 5 sample test cases explained in code.

I'll take an example test case:

For n = 4.



## Output:

Number of complete of complete cycles: 4

# complete path

$$1 \rightarrow 3 \rightarrow 2 \rightarrow 4 \rightarrow 1$$

$$2 \rightarrow 4 \rightarrow 1 \rightarrow 3 \rightarrow 2$$

$$3 \rightarrow 2 \rightarrow 4 \rightarrow 1 \rightarrow 3$$

$$4 \rightarrow 1 \rightarrow 3 \rightarrow 2 \rightarrow 4$$

Number of complete of partial cycles: 9 partial path

$$1 \rightarrow 2 \rightarrow 4 \rightarrow 1$$

$$2 \rightarrow 1 \rightarrow 3 \rightarrow 2$$

$$2 \rightarrow 4 \rightarrow 1 \rightarrow 2$$

## Code:

```
/*
@author: ShikharSahu
*/
#include <iostream>
#include <string>
```

```
#include <vector>
#include <algorithm>
#include <sstream>
#include <queue>
#include <deque>
#include <bitset>
#include <iterator>
#include <list>
#include <stack>
#include <map>
#include <set>
#include <unordered map>
#include <unordered set>
#include <functional>
#include <numeric>
#include <utility>
#include <limits>
#include <time.h>
#include <math.h>
#include <stdio.h>
#include <string.h>
#include <stdlib.h>
#include <assert.h>
typedef long long int 11;
using namespace std;
#define MOD 1e9+7;
set<vector<int>> complete, partial;
void printPath(vector<int> path){
    path.pop_back();
    for (int e : path){
        cout << e << " -> ";
    cout << path.front();</pre>
    cout << endl ;</pre>
void helper (int current, vector<int>& allConnected, vector<pair<int,vector<in</pre>
t> > >& graph, int initial, unordered_set<int>& visited, vector<int>& path){
    if (path.size()>=2){
        if( find(allConnected.begin(), allConnected.end(), initial) != allConn
ected.end() ){
            if( path.size() == graph.size() ){
                path.push_back(initial);
                complete.insert(path);
                path.pop_back();
                // printPath(path);
            // print path
```

```
path.push_back(initial);
            partial.insert(path);
            // printPath(path);
            path.pop_back();
    for(int element : allConnected){
        if(visited.count(element)==0){
            visited.insert(element);
            path.push_back(element);
            helper(element, graph[element-
1].second, graph, initial, visited, path);
            path.pop_back();
            visited.erase(element);
        }
void printMatrix(vector<vector<bool> > graph){
    int n = graph.size();
    for (int i =0; i< n; i++){
        for (int j = 0; j < n; j ++){
            cout << (int) graph[i][j] << " ";
        cout << endl;</pre>
vector<vector<bool> > getMatrix(int n){
    vector<vector<bool> > graph(n, vector<bool>(n, false));
    for (int i =0; i< n; i++){
        for (int j = 0; j < n; j ++){
            if(i!=j){
                if(rand()%3 == 0){
                    graph[i][j] = true;
            }
    return graph;
vector<pair<int, vector<int> > getList(vector<vector<bool> > mat){
    vector<pair<int, vector<int> > > graph;
    for (int i = 0 ; i < mat.size(); i++){</pre>
        vector<int> temp;
        for(int j = 0; j <mat.size(); j++){</pre>
            if(mat[i][j]){
                temp.push_back(j+1);
```

```
graph.push_back(make_pair(i+1,temp));
    return graph;
void solve(){
    // vector<pair<int, vector<int> > graph(4);
    // graph[0] = \{1,\{2,3\}\};
    // graph[1] = \{2,\{1,4\}\};
    // graph[2] = {3,{1,2}};
    // graph[3] = \{4,\{1,3\}\};
    srand(time(0));
    int size = 5 + rand() % 3;
    auto mat = getMatrix(size);
    cout << "graph is :\n";</pre>
    printMatrix(mat);
    auto graph = getList(mat);
    vector<int> path;
    unordered_set<int> visited;
    for (auto node: graph){
        visited.insert(node.first);
        path.push_back(node.first);
        helper(node.first, node.second, graph, node.first, visited, path);
        path.pop_back();
        visited.erase(node.first);
    cout << "Number of complete of complete cycles: " << complete.size() <<end</pre>
1;
    cout << "complete path\n";</pre>
    for (auto path : complete){
        printPath(path);
    cout << endl;</pre>
    set<vector<int>> perfectPartials;
    for (auto path : partial){
        if(path.size()>3){
             perfectPartials.insert(path);
    cout << "Number of complete of partial cycles: " << perfectPartials.size(</pre>
 <<endl;
    cout << "partial path\n";</pre>
```

```
for (auto path : perfectPartials){
    printPath(path);
}

int main(){
    11 T=5;
    while(T--){
        solve();
    }
}
```

# Output:

->

->

```
graph is:
0
     1
         0
              0
                   1
                        0
0
     0
                   1
         1
              0
                        0
0
     0
         0
              1
                   1
                        0
1
     1
         1
              0
                   0
                        0
1
     1
         0
              1
                   0
                        1
0
     0
                   0
              1
                        0
         1
Number of complete of complete cycles: 12
complete path
1
        2
                          5
   ->
            ->
                 3
                                  6
                                           4
                                                    1
                     ->
                             ->
                                      ->
                                               ->
1
        2
                 5
                          6
                                  3
                                                    1
                                           4
   ->
            ->
                     ->
                             ->
                                      ->
                                               ->
2
        3
                 5
                          6
                                  4
                                           1
                                                    2
   ->
            ->
                    ->
                             ->
                                      ->
                                               ->
2
        5
                 6
                          3
                                           1
                                                    2
   ->
            ->
                     ->
                             ->
                                  4
                                      ->
                                               ->
3
        4
                 1
                          2
                                  5
                                           6
                                                    3
   ->
            ->
                     ->
                             ->
                                      ->
                                               ->
3
                                           2
   ->
        5
                 6
                          4
                                  1
                                      ->
                                                    3
            ->
                     ->
                             ->
                                               ->
4
        1
                 2
                          3
                                  5
   ->
            ->
                     ->
                             ->
                                      ->
                                           6
                                               ->
                                                    4
                 2
                          5
4
        1
                                  6
                                           3
                                                    4
   ->
            ->
                     ->
                             ->
                                      ->
                                               ->
5
   ->
        6
                 3
                          4
                                  1
                                           2
                                                    5
            ->
                     ->
                             ->
                                      ->
                                               ->
5
        6
                 4
                          1
                             ->
                                  2
                                      ->
                                           3
                                                    5
   ->
            ->
                     ->
                                               ->
```

->

->

->

->

- 1 -> 2 -> 3 -> 4 -> 1
- $1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 1$
- $1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 1$
- 1 -> 2 -> 5 -> 1
- $1 \rightarrow 2 \rightarrow 5 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 5 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 1$
- 1 -> 5 -> 4 -> 1
- $1 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1$
- $2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 2$
- 2 -> 3 -> 4 -> 2
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 1 \rightarrow 2$
- 2 -> 3 -> 5 -> 2
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 4 \rightarrow 2$
- 2 -> 5 -> 6 -> 3 -> 4 -> 2
- $2 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6 \rightarrow 3$
- 3 -> 4 -> 2 -> 3

```
3 \rightarrow 4 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3
```

$$3 \rightarrow 5 \rightarrow 1 \rightarrow 2 \rightarrow 3$$

$$3 \rightarrow 5 \rightarrow 2 \rightarrow 3$$

$$3 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3$$

$$3 \rightarrow 5 \rightarrow 4 \rightarrow 2 \rightarrow 3$$

$$3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2 \rightarrow 3$$

$$3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 3$$

$$4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 4$$

$$4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 4$$

$$4 \rightarrow 1 \rightarrow 5 \rightarrow 2 \rightarrow 3 \rightarrow 4$$

$$4 \rightarrow 1 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4$$

$$4 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4$$

$$4 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4$$

$$5 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5$$

$$5 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5$$

```
5 -> 4 -> 2 -> 3 -> 5
```

$$5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5$$

$$5 \rightarrow 6 \rightarrow 4 \rightarrow 2 \rightarrow 3 \rightarrow 5$$

$$6 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6$$

$$6 \rightarrow 3 \rightarrow 4 \rightarrow 2 \rightarrow 5 \rightarrow 6$$

$$6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6$$

$$6 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6$$

$$6 \rightarrow 4 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6$$

#### graph is:

# Number of complete of complete cycles: 12

## complete path

$$1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1$$

$$2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2$$

$$2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 2$$

```
3
        4
                 1
                          2
                                   5
                                           6
                                                    3
   ->
            ->
                              ->
                                      ->
                                               ->
                     ->
3
   ->
        5
                 6
                          4
                              ->
                                   1
                                      ->
                                           2
                                               ->
                                                    3
            ->
                     ->
   ->
                 2
                          3
                              ->
                                   5
                                      ->
                                           6
                                               ->
            ->
                     ->
        1
                 2
                          5
                                   6
                                           3
   ->
            ->
                     ->
                              ->
                                      ->
                                                    5
5
        6
                 3
                                   1
                                           2
   ->
            ->
                     ->
                              ->
                                       ->
5
                                   2
                                           3
                                                    5
   ->
        6
                          1
                              ->
                                       ->
                     ->
        3
                          1
                                   2
                                           5
                                                    6
   ->
            ->
                     ->
                              ->
                                       ->
                                               ->
                 1
                          2
                              ->
                                   3
                                      ->
                                            5
                                               ->
                                                    6
   ->
            ->
                     ->
```

$$1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 1$$

$$1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 1$$

$$1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 1$$

$$1 \rightarrow 2 \rightarrow 5 \rightarrow 1$$

$$1 \rightarrow 2 \rightarrow 5 \rightarrow 4 \rightarrow 1$$

$$1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1$$

$$1 \rightarrow 5 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 1$$

$$1 \rightarrow 5 \rightarrow 4 \rightarrow 1$$

$$1 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1$$

$$1 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1$$

$$2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 2$$

$$2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 2$$

$$2 \rightarrow 3 \rightarrow 5 \rightarrow 1 \rightarrow 2$$

$$2 \rightarrow 3 \rightarrow 5 \rightarrow 2$$

$$2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2$$

$$2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 2$$

$$2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2$$

$$2 \rightarrow 5 \rightarrow 1 \rightarrow 2$$

$$2 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2$$

- $2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6 \rightarrow 3$
- 3 -> 4 -> 2 -> 3
- $3 \rightarrow 4 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3$
- $3 \rightarrow 5 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- 3 -> 5 -> 2 -> 3
- $3 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 5 \rightarrow 4 \rightarrow 2 \rightarrow 3$
- 3 -> 5 -> 4 -> 3
- 3 -> 5 -> 6 -> 3
- $3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 3$
- $4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 5 \rightarrow 2 \rightarrow 3 \rightarrow 4$
- 4 -> 1 -> 5 -> 4
- 4 -> 1 -> 5 -> 6 -> 3 -> 4
- 4 -> 1 -> 5 -> 6 -> 4
- 4 -> 2 -> 3 -> 4
- 4 -> 2 -> 3 -> 5 -> 4
- $4 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4$
- 4 -> 2 -> 5 -> 4
- $4 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4$
- 4 -> 2 -> 5 -> 6 -> 4
- 4 -> 3 -> 5 -> 4
- 4 -> 3 -> 5 -> 6 -> 4

```
5 -> 1 -> 2 -> 3 -> 5
```

$$5 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5$$

$$5 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5$$

$$5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 2 \rightarrow 5$$

$$5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5$$

$$5 \rightarrow 6 \rightarrow 4 \rightarrow 2 \rightarrow 3 \rightarrow 5$$

$$6 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6$$

$$6 \rightarrow 3 \rightarrow 4 \rightarrow 2 \rightarrow 5 \rightarrow 6$$

$$6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6$$

$$6 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6$$

$$6 \rightarrow 4 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6$$

#### graph is:

0 0 1 1 0 0

Number of complete of complete cycles: 12 complete path

- 1 -> 2 -> 3 -> 5 -> 6 -> 4 -> 1
- $1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1$
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3$
- $3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- 4 -> 1 -> 2 -> 3 -> 5 -> 6 -> 4
- $4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4$
- $5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5$
- $5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5$
- $6 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6$
- $6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6$

- 1 -> 2 -> 3 -> 4 -> 1
- $1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 1$
- $1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 2 \rightarrow 5 \rightarrow 1$
- $1 \rightarrow 2 \rightarrow 5 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 5 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 1$
- 1 -> 5 -> 4 -> 1
- $1 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1$
- $2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 2$
- 2 -> 3 -> 4 -> 2
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 1 \rightarrow 2$

- $2 \rightarrow 3 \rightarrow 5 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- 2 -> 5 -> 4 -> 2
- $2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- 2 -> 5 -> 6 -> 4 -> 2
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6 \rightarrow 3$
- 3 -> 4 -> 2 -> 3
- $3 \rightarrow 4 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3$
- $3 \rightarrow 5 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- 3 -> 5 -> 2 -> 3
- $3 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 5 \rightarrow 4 \rightarrow 2 \rightarrow 3$
- 3 -> 5 -> 4 -> 3
- $3 \rightarrow 5 \rightarrow 6 \rightarrow 3$
- $3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2 \rightarrow 3$
- 3 -> 5 -> 6 -> 4 -> 3
- 4 -> 1 -> 2 -> 3 -> 4
- 4 -> 1 -> 2 -> 3 -> 5 -> 4
- $4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 5 \rightarrow 2 \rightarrow 3 \rightarrow 4$
- 4 -> 1 -> 5 -> 4
- 4 -> 1 -> 5 -> 6 -> 3 -> 4
- 4 -> 1 -> 5 -> 6 -> 4
- 4 -> 2 -> 3 -> 4

- 4 -> 2 -> 3 -> 5 -> 4
- $4 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4$
- 4 -> 2 -> 5 -> 4
- $4 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4$
- 4 -> 2 -> 5 -> 6 -> 4
- 4 -> 3 -> 5 -> 4
- 4 -> 3 -> 5 -> 6 -> 4
- $5 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5$
- 5 -> 1 -> 2 -> 5
- $5 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5$
- 5 -> 2 -> 3 -> 5
- $5 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5$
- 5 -> 4 -> 1 -> 2 -> 5
- 5 -> 4 -> 1 -> 5
- 5 -> 4 -> 2 -> 3 -> 5
- 5 -> 4 -> 2 -> 5
- 5 -> 4 -> 3 -> 5
- 5 -> 6 -> 3 -> 4 -> 1 -> 5
- 5 -> 6 -> 3 -> 4 -> 2 -> 5
- 5 -> 6 -> 3 -> 5
- $5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5$
- 5 -> 6 -> 4 -> 1 -> 5
- $5 \rightarrow 6 \rightarrow 4 \rightarrow 2 \rightarrow 3 \rightarrow 5$
- 5 -> 6 -> 4 -> 2 -> 5
- 5 -> 6 -> 4 -> 3 -> 5
- $6 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6$
- $6 \rightarrow 3 \rightarrow 4 \rightarrow 2 \rightarrow 5 \rightarrow 6$
- 6 -> 3 -> 5 -> 6
- $6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6$
- 6 -> 4 -> 1 -> 5 -> 6
- 6 -> 4 -> 2 -> 3 -> 5 -> 6
- 6 -> 4 -> 2 -> 5 -> 6

```
->
      4
         ->
              3 -> 5 -> 6
graph is:
        0
                 0
                     1
                         0
            0
                         1
0
    0
        1
            0
                 0
                     0
0
    0
            0
                 0
                         0
        0
                     0
0
    1
        0
            0
                 0
                     0
                         1
1
    0
            1
                 0
                         0
        1
                     1
0
    0
            1
                 0
        0
                     0
                         0
```

Number of complete of complete cycles: 12 complete path

- $1 \rightarrow 5 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 5 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1$
- $2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 2$
- 2 -> 3 -> 4 -> 2
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 1 \rightarrow 2$
- 2 -> 3 -> 5 -> 2
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- 2 -> 5 -> 4 -> 2
- $2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6 \rightarrow 3$
- 3 -> 4 -> 2 -> 3
- 3 -> 4 -> 2 -> 5 -> 6 -> 3
- $3 \rightarrow 5 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- 3 -> 5 -> 2 -> 3
- $3 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 5 \rightarrow 4 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 5 \rightarrow 4 \rightarrow 3$
- 3 -> 5 -> 6 -> 3
- $3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2 \rightarrow 3$
- 3 -> 5 -> 6 -> 4 -> 3
- 4 -> 1 -> 2 -> 3 -> 4

- $4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 5 \rightarrow 2 \rightarrow 3 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 5 \rightarrow 4$
- 4 -> 1 -> 5 -> 6 -> 3 -> 4
- 4 -> 1 -> 5 -> 6 -> 4
- 4 -> 2 -> 3 -> 4
- 4 -> 2 -> 3 -> 5 -> 4
- 4 -> 2 -> 3 -> 5 -> 6 -> 4
- 4 -> 2 -> 5 -> 4
- $4 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4$
- 4 -> 2 -> 5 -> 6 -> 4
- 4 -> 3 -> 5 -> 4
- 4 -> 3 -> 5 -> 6 -> 4
- $5 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5$
- 5 -> 1 -> 2 -> 5
- 5 -> 2 -> 3 -> 4 -> 1 -> 5
- 5 -> 2 -> 3 -> 5
- 5 -> 4 -> 1 -> 2 -> 3 -> 5
- 5 -> 4 -> 1 -> 2 -> 5
- 5 -> 4 -> 1 -> 5
- 5 -> 4 -> 2 -> 3 -> 5
- 5 -> 4 -> 2 -> 5
- 5 -> 4 -> 3 -> 5
- 5 -> 6 -> 3 -> 4 -> 1 -> 5
- 5 -> 6 -> 3 -> 4 -> 2 -> 5
- 5 -> 6 -> 3 -> 5
- $5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5$
- 5 -> 6 -> 4 -> 1 -> 5
- $5 \rightarrow 6 \rightarrow 4 \rightarrow 2 \rightarrow 3 \rightarrow 5$
- 5 -> 6 -> 4 -> 2 -> 5

```
5 -> 6 -> 4 -> 3 -> 5
```

$$6 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6$$

$$6 \rightarrow 3 \rightarrow 4 \rightarrow 2 \rightarrow 5 \rightarrow 6$$

$$6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6$$

$$6 \rightarrow 4 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6$$

$$6 \rightarrow 4 \rightarrow 2 \rightarrow 5 \rightarrow 6$$

#### graph is:

## Number of complete of complete cycles: 12

## complete path

$$1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1$$

$$1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1$$

$$2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2$$

$$2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 2$$

$$3 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3$$

$$3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3$$

$$4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4$$

$$4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4$$

$$5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5$$

$$5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5$$

$$6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6$$

- $1 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 1$
- 1 -> 2 -> 3 -> 5 -> 1
- $1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 2 \rightarrow 5 \rightarrow 1$
- $1 \rightarrow 2 \rightarrow 5 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 5 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 1$
- 1 -> 5 -> 4 -> 1
- $1 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1$
- $1 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1$
- $2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 2$
- 2 -> 3 -> 4 -> 2
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 1 \rightarrow 2$
- 2 -> 3 -> 5 -> 2
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 4 \rightarrow 2$
- $2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 1 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- 2 -> 5 -> 4 -> 2
- $2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 2$
- $2 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2$
- 2 -> 5 -> 6 -> 4 -> 2
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6 \rightarrow 3$
- $3 \rightarrow 4 \rightarrow 2 \rightarrow 3$
- 3 -> 4 -> 2 -> 5 -> 6 -> 3
- $3 \rightarrow 5 \rightarrow 1 \rightarrow 2 \rightarrow 3$

- $3 \rightarrow 5 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 5 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 5 \rightarrow 4 \rightarrow 2 \rightarrow 3$
- 3 -> 5 -> 4 -> 3
- 3 -> 5 -> 6 -> 3
- $3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 2 \rightarrow 3$
- $3 \rightarrow 5 \rightarrow 6 \rightarrow 4 \rightarrow 3$
- 4 -> 1 -> 2 -> 3 -> 4
- $4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 4$
- 4 -> 1 -> 2 -> 5 -> 6 -> 4
- $4 \rightarrow 1 \rightarrow 5 \rightarrow 2 \rightarrow 3 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 5 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4$
- $4 \rightarrow 1 \rightarrow 5 \rightarrow 6 \rightarrow 4$
- 4 -> 2 -> 3 -> 4
- 4 -> 2 -> 3 -> 5 -> 4
- $4 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6 \rightarrow 4$
- 4 -> 2 -> 5 -> 4
- $4 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 3 \rightarrow 4$
- $4 \rightarrow 2 \rightarrow 5 \rightarrow 6 \rightarrow 4$
- 4 -> 3 -> 5 -> 4
- 4 -> 3 -> 5 -> 6 -> 4
- 5 -> 1 -> 2 -> 3 -> 5
- 5 -> 1 -> 2 -> 5
- $5 \rightarrow 2 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5$
- 5 -> 2 -> 3 -> 5
- $5 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 3 \rightarrow 5$
- 5 -> 4 -> 1 -> 2 -> 5
- 5 -> 4 -> 1 -> 5
- 5 -> 4 -> 2 -> 3 -> 5
- 5 -> 4 -> 2 -> 5

- 5 -> 4 -> 3 -> 5
- $5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5$
- $5 \rightarrow 6 \rightarrow 3 \rightarrow 4 \rightarrow 2 \rightarrow 5$
- 5 -> 6 -> 3 -> 5
- $5 \rightarrow 6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5$
- 5 -> 6 -> 4 -> 1 -> 5
- $5 \rightarrow 6 \rightarrow 4 \rightarrow 2 \rightarrow 3 \rightarrow 5$
- 5 -> 6 -> 4 -> 2 -> 5
- 5 -> 6 -> 4 -> 3 -> 5
- $6 \rightarrow 3 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6$
- $6 \rightarrow 3 \rightarrow 4 \rightarrow 2 \rightarrow 5 \rightarrow 6$
- 6 -> 3 -> 5 -> 6
- $6 \rightarrow 4 \rightarrow 1 \rightarrow 2 \rightarrow 5 \rightarrow 6$
- $6 \rightarrow 4 \rightarrow 1 \rightarrow 5 \rightarrow 6$
- $6 \rightarrow 4 \rightarrow 2 \rightarrow 3 \rightarrow 5 \rightarrow 6$
- $6 \rightarrow 4 \rightarrow 2 \rightarrow 5 \rightarrow 6$
- $6 \rightarrow 4 \rightarrow 3 \rightarrow 5 \rightarrow 6$