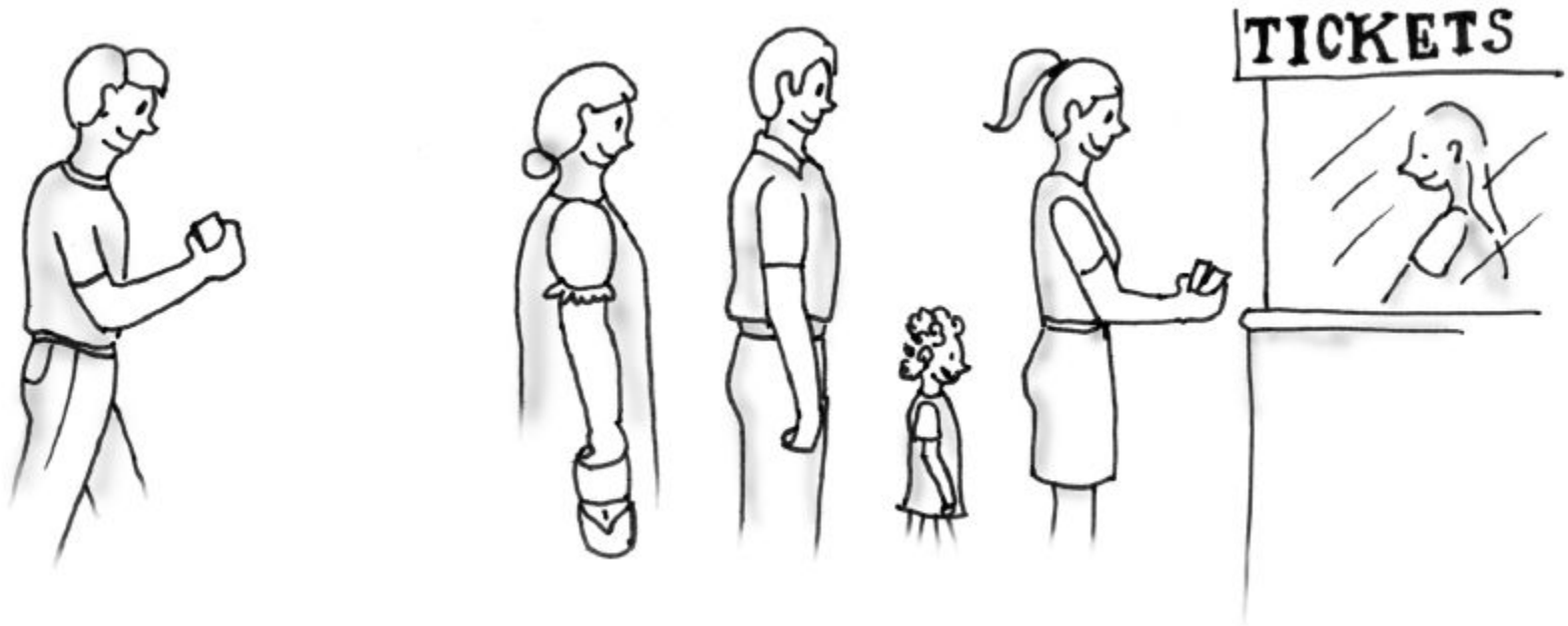


Data Structure (Queue) CSE-207

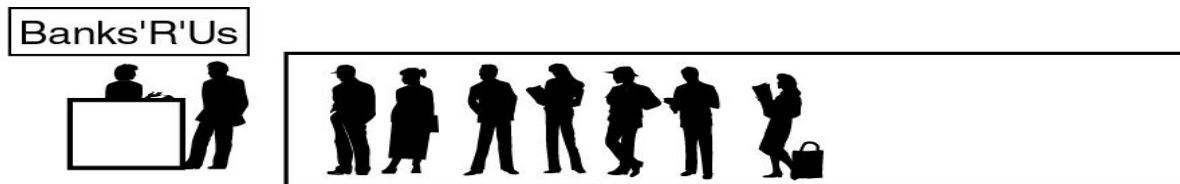
Simulating a Waiting Line



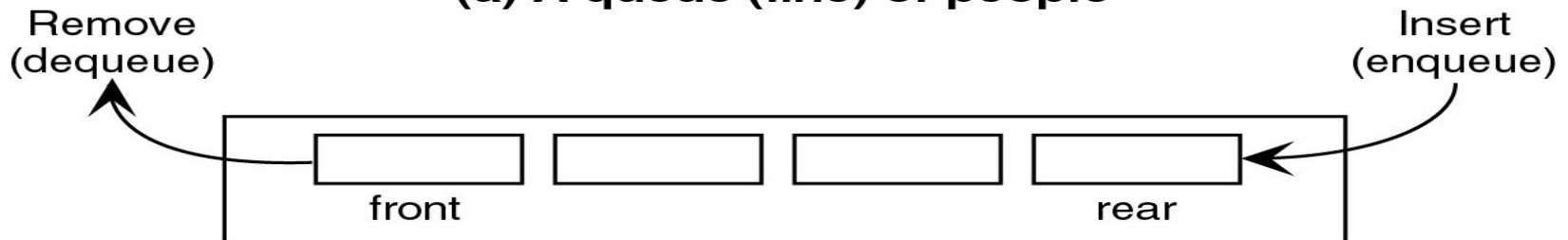
A line, or queue, of people

Queue

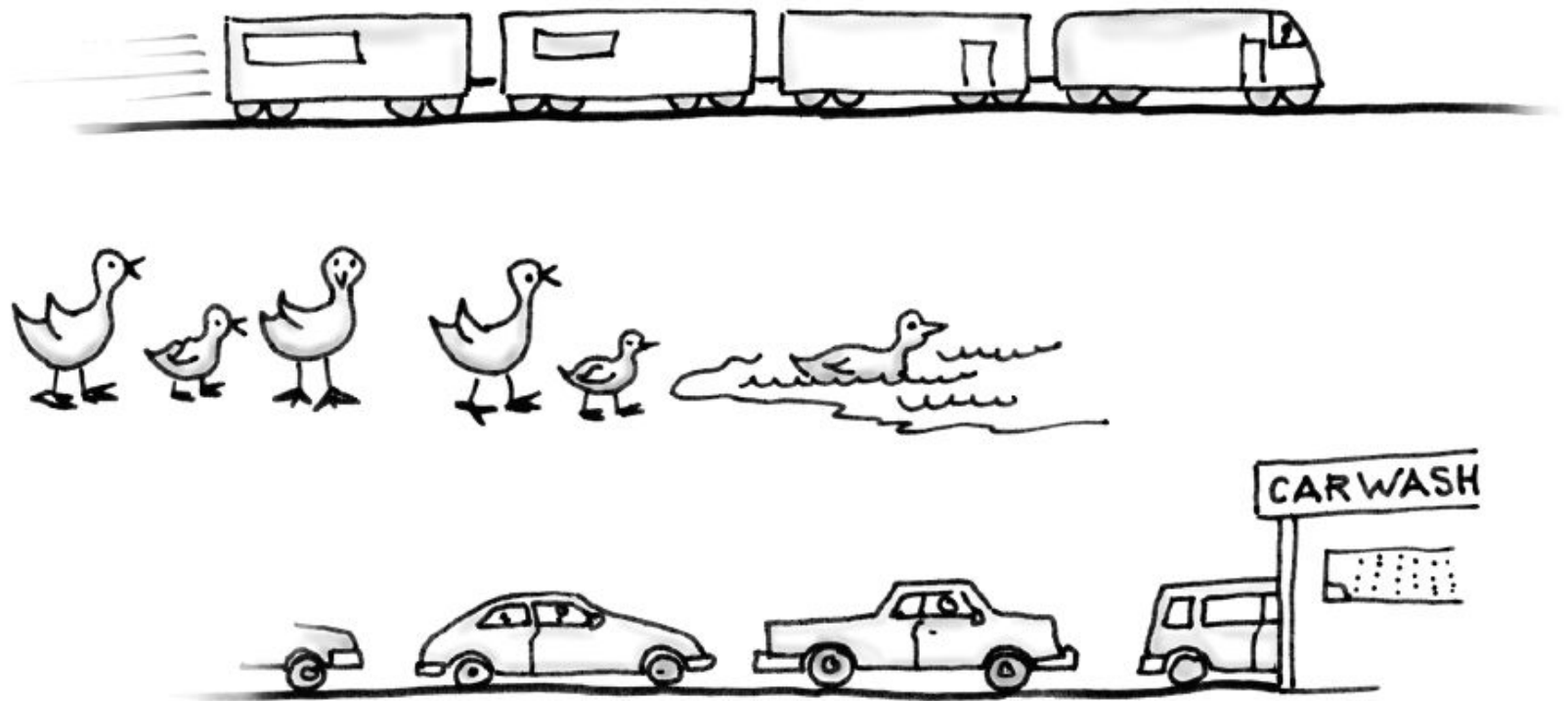
- It is a **linear data structure** consisting of list of items.
- In queue, data elements are added at one end, called the **rear** and removed from another end, called the **front** of the list.



(a) A queue (line) of people



(b) A computer queue



Some everyday queues

(a)

Jim

(b)

Jim

Jess

(c)

Jim

Jess

Jill

(d)

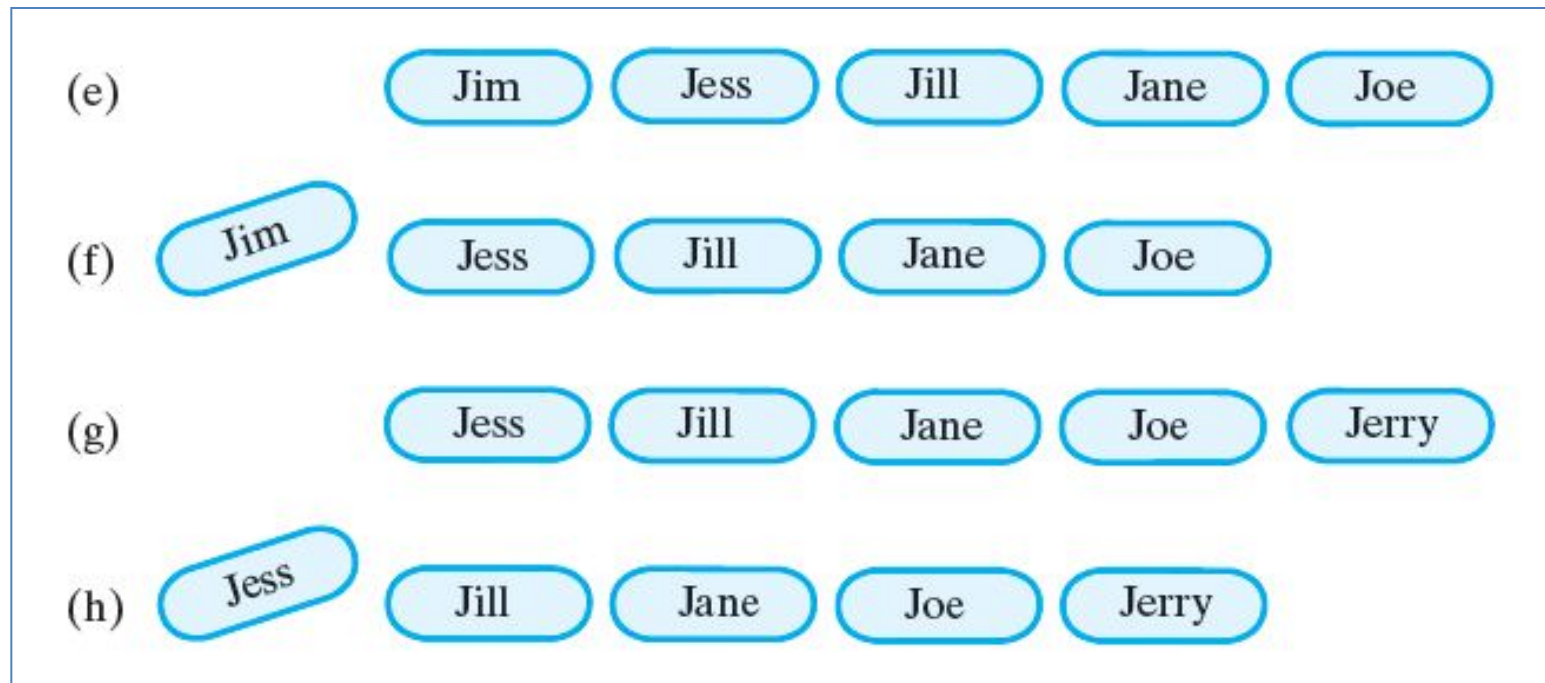
Jim

Jess

Jill

Jane

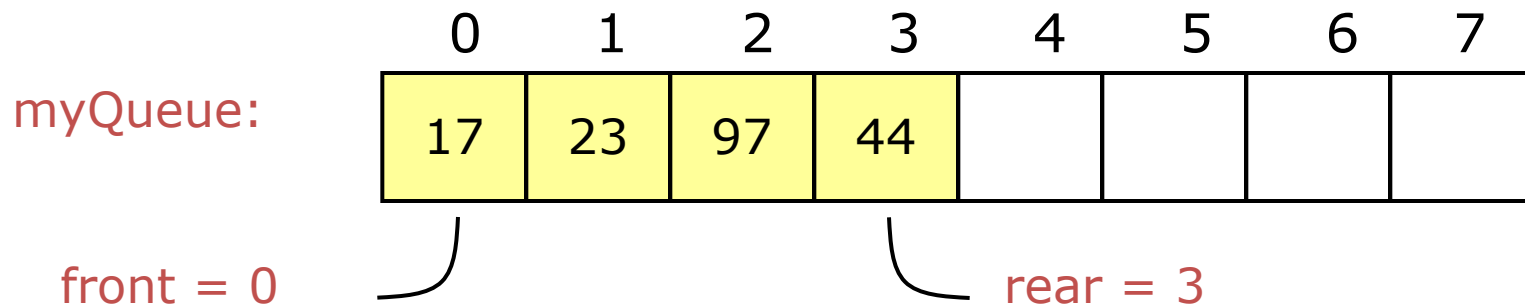
A queue of strings after (a) enqueue adds *Jim*;
(b) enqueue adds *Jess*; (c) enqueue adds *Jill*;
(d) enqueue adds *Jane*;



A queue of strings after (e) enqueue adds *Joe*; (f) dequeue retrieves and removes *Jim*; (g) enqueue adds *Jerry*; (h) dequeue retrieves and removes *Jess*;

Queue

- A **queue** is a first in, first out (**FIFO**) data structure
- This is accomplished by inserting at one end (the **rear**) and deleting from the other (the **front**)



- **To insert:** put new element in location **4**, and set **rear** to **4**
- **To delete:** take element from location **0**, and set **front** to **1**

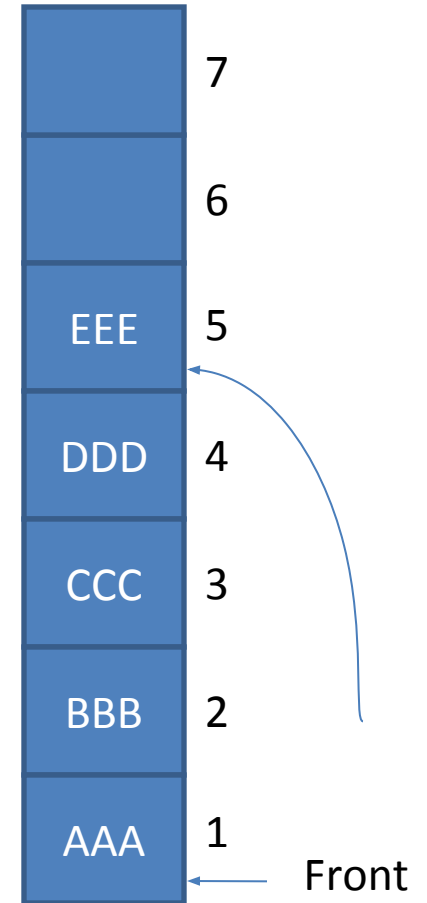
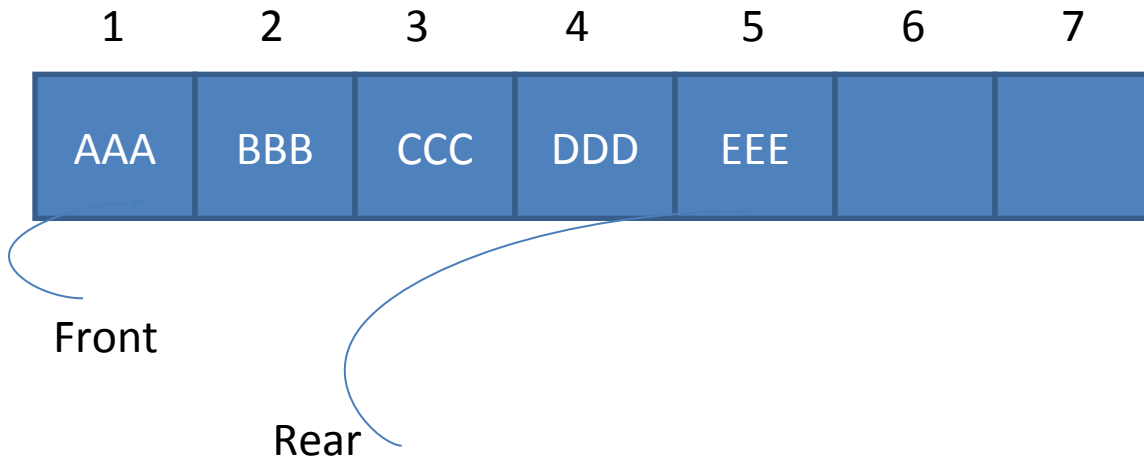
Queue

- **Two basic operations** are associated with queue:
- **“Insert”** operation is used to insert an element into a queue.
 - Called *enqueue operation*
- **“Delete”** operation is used to delete an element from a queue.
 - Called *dequeue operation*

Queue

Example:

Queue: AAA, BBB, CCC, DDD, EEE



Queue

- **rear** is the location in which the data element is to be **inserted**.
- **front** is the location from which the data element is to be **removed**.
- When queue is empty
 - $\text{rear} = -1$
 - $\text{front} = -1$
- Adding an element in queue will increase the value of **rear**
 - $\text{rear} = \text{rear} + 1;$
- Removing an element in queue will increase the value of **front**
 - $\text{front} = \text{front} + 1;$

Array implementation of queue

Queue empty $\text{rear} = -1$ $\text{front} = -1$



Array implementation of queue

Queue empty $\text{rear} = -1$ $\text{front} = -1$



Add 10, $\text{rear} = 0$ $\text{front} = 0$



Array implementation of queue

Queue empty $\text{rear} = -1$ $\text{front} = -1$



Add 10, $\text{rear} = 0$ $\text{front} = 0$



Add 20, $\text{rear} = 1$, $\text{front} = 0$



Array implementation of queue

Queue empty $\text{rear} = -1$ $\text{front} = -1$



Add 10, $\text{rear} = 0$ $\text{front} = 0$



Add 20, $\text{rear} = 1$, $\text{front} = 0$



Add 30, $\text{rear} = 2$, $\text{front} = 0$



Array implementation of queue

Queue empty $\text{rear} = -1$ $\text{front} = -1$



Add 10, $\text{rear} = 0$ $\text{front} = 0$



Add 20, $\text{rear} = 1$, $\text{front} = 0$



Add 30, $\text{rear} = 2$, $\text{front} = 0$



Add 40, $\text{rear} = 3$, $\text{front} = 0$



Array implementation of queue

Add 40, rear=3, front=0

10	20	30	40			
----	----	----	----	--	--	--

Remove, rear=3, front=1

	20	30	40			
--	----	----	----	--	--	--

Array implementation of queue

Add 40, rear=3, front=0

10	20	30	40			
----	----	----	----	--	--	--

Remove, rear=3, front=1

	20	30	40			
--	----	----	----	--	--	--

Remove, rear=3, front=2

		30	40			
--	--	----	----	--	--	--

Array implementation of queue

Add 40, rear=3, front=0

10	20	30	40			
----	----	----	----	--	--	--

Remove, rear=3, front=1

	20	30	40			
--	----	----	----	--	--	--

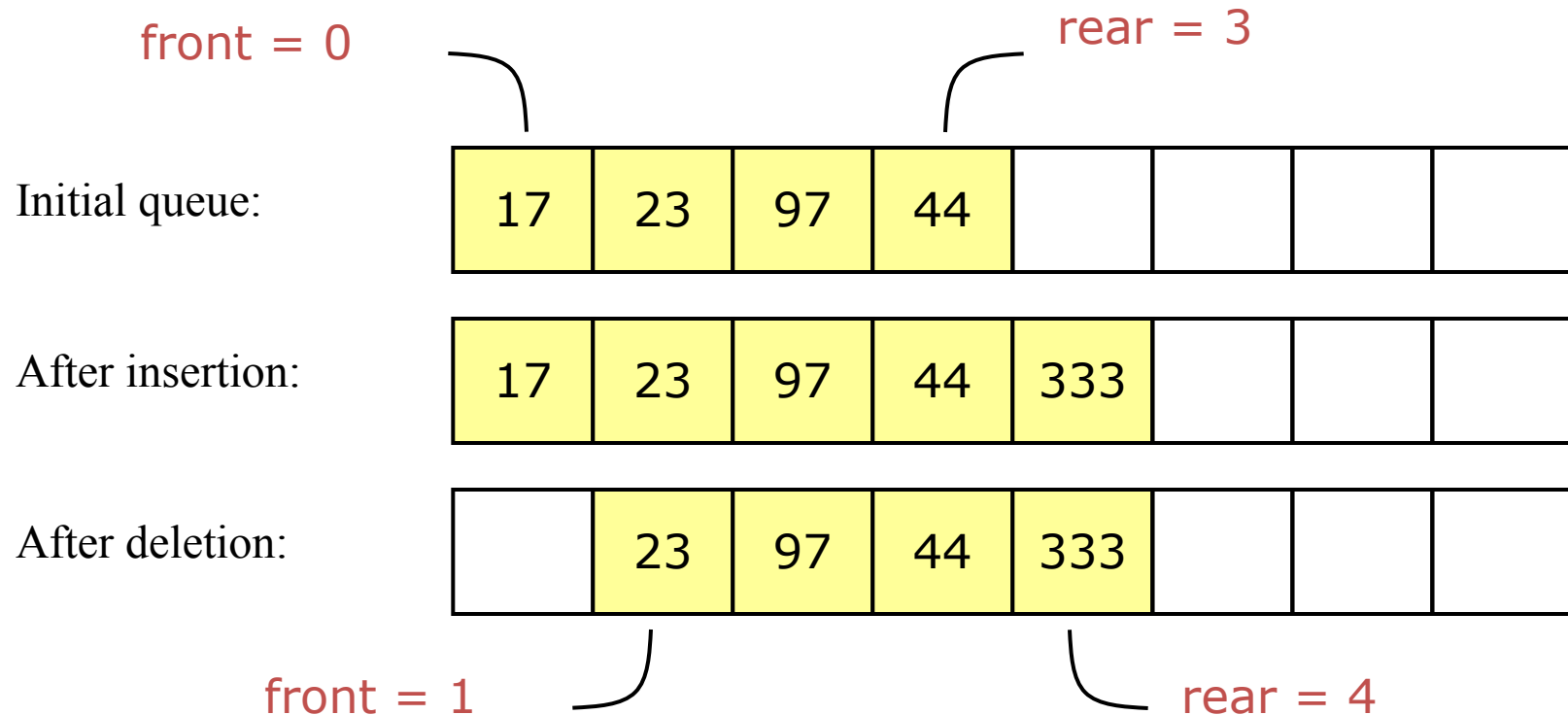
Remove, rear=3, front=2

		30	40			
--	--	----	----	--	--	--

Add 60, rear=4, front=2

		30	40	60		
--	--	----	----	----	--	--

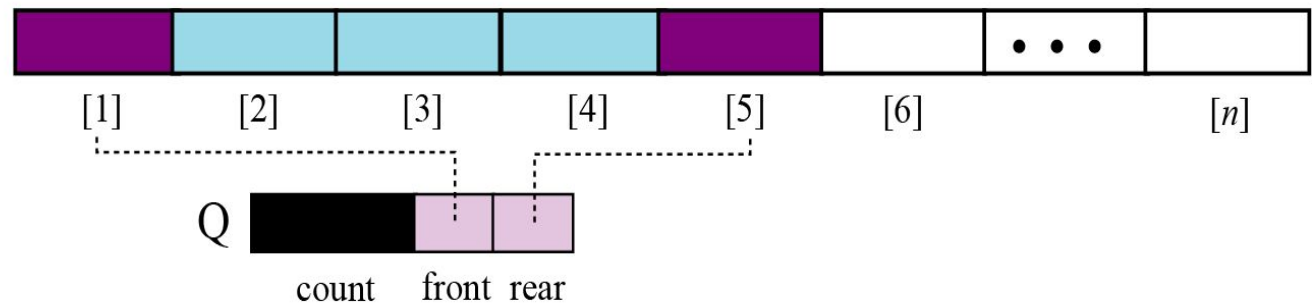
Queue



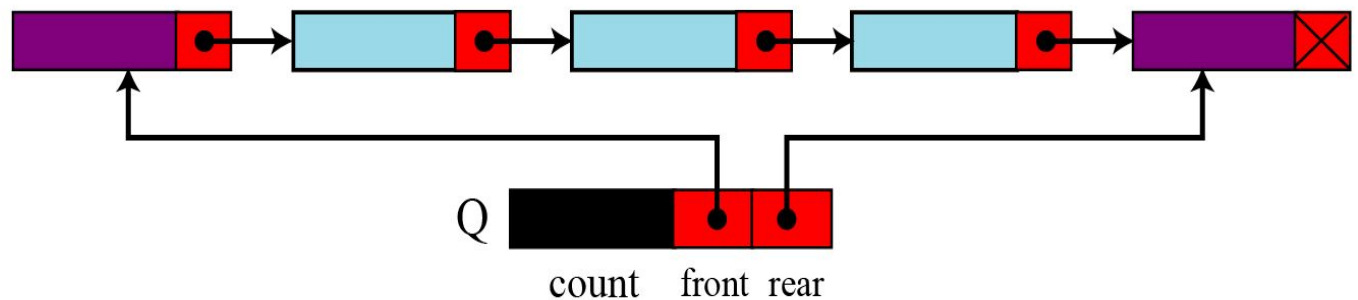
- Notice how the array contents “crawl” to the right as elements are inserted and deleted
- This will be a problem after a while!

Queue

b. Array
implementation



c. Linked list
implementation



Insert Operations in Linear Queue

- **Rear** is the location in which the data element is to be **inserted**.
- **Front** is the location from which the data element is to be **removed**.
- Here N is the maximum size of the Queue

```
1. If Rear = N then Print: Overflow and  
   Return.                      /*...Queue already  
   filled..*/  
2. Set Rear := Rear +1  
3. Set Queue[Rear] := Item  
4. Return.
```

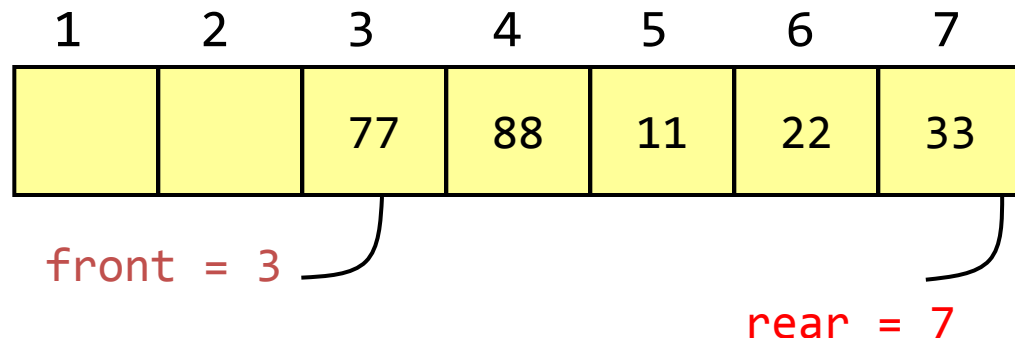
Delete Operations in Linear Queue

- **Rear** is the location in which the data element is to be **inserted**.
- **Front** is the location from which the data element is to be **removed**.
- Here N is the maximum size of the Queue

```
1. If Front = N+1 then Print: Underflow and Return.  
/*...Queue Empty*/  
2. Set Item := Queue[Front]  
3. Set Front := Front + 1  
4. Return.
```

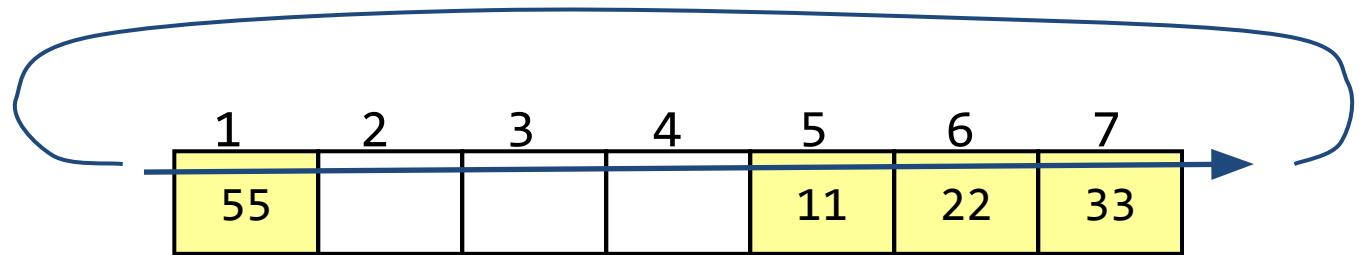
Problem

- Once the queue is full, rear has already reached the Queue's rear most position
- Even though few elements from the front are deleted and some occupied space is relieved,
- it is not possible to add anymore new elements

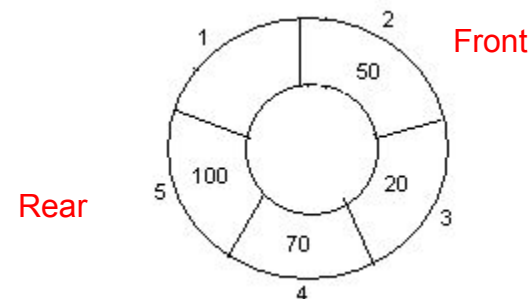


Circular queue

- We can treat the array holding the queue elements as circular (joined at the ends)



- Once the Queue is full the "First" element of the Queue becomes the "Rear" most element, if and only if the "Front" has moved forward



Drawback of Linear Queue

- Once the queue is full, even though few elements from the front are deleted and some occupied space is relieved, it is not possible to add anymore new elements, as the rear has already reached the Queue's rear most position.

Circular Queue

- This queue is not linear but circular.
- Its structure can be like the following figure:
- In circular queue, once the Queue is full the "First" element of the Queue becomes the "Rear" most element, if and only if the "Front" has moved forward. otherwise it will again be a "Queue overflow" state.

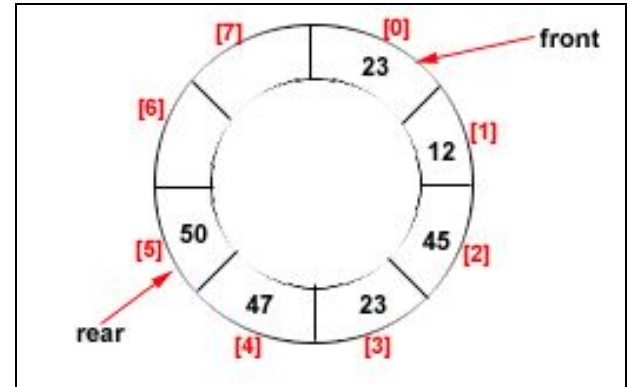


Figure: Circular Queue having Rear = 5 and Front = 0

For Insert Operation

- **Rear** is the inserting location
- **Front** is the removing location.
- Here N is the maximum size of the Cqueue
- **Initailly Rear = 0 and Front = 0.**

1. If $\text{Front} = 0$ and $\text{Rear} = 0$
then Set $\text{Front} := 1$ and go to step 4.
2. If $\text{Front} = 1$ and $\text{Rear} = N$ or $\text{Front} = \text{Rear} + 1$
then Print: "Circular Queue Overflow" and Return.
3. If $\text{Rear} = N$ then Set $\text{Rear} := 1$ and go to step 5.
4. Set $\text{Rear} := \text{Rear} + 1$
5. Set $\text{CQueue}[\text{Rear}] := \text{Item}$.
6. Return

For Delete Operation

- **Rear** is the inserting location
- **Front** is the removing location.
- Here N is the maximum size of the Cqueue
- Front element is assigned to Item, initially, Front = 1.

```
1. If Front = 0 then
    Print: "Circular Queue Underflow" and Return.    /*..Delete
without Insertion
2. Set Item := CQueue [Front]
3. If Front = N then Set Front = 1 and Return.
4. If Front = Rear then Set Front = 0 and Rear = 0 and Return.
5. Set Front := Front + 1
6. Return.
```

For Delete Operation

Delete-Circular-Q(CQueue, Front, Rear, Item)

Here, CQueue is the place where data are stored. Rear represents the location in which the data element is to be inserted and Front represents the location from which the data element is to be removed. Front element is assigned to Item. Initially, Front = 1.

1. If Front = 0 then

Print: "Circular Queue Underflow" and Return. /*..Delete without Insertion

2. Set Item := CQueue [Front]

3. If Front = N then Set Front = 1 and Return.

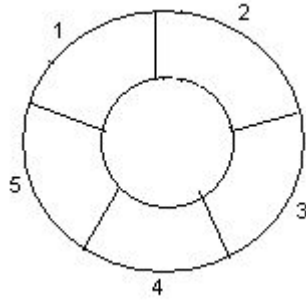
4. If Front = Rear then Set Front = 0 and Rear = 0 and Return.

5. Set Front := Front + 1

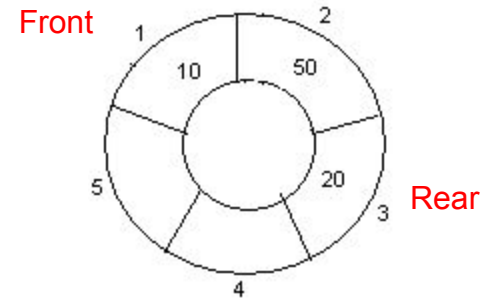
6. Return.

Circular queue

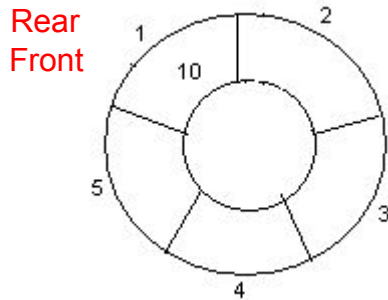
1. Initially, Rear = 0, Front = 0.



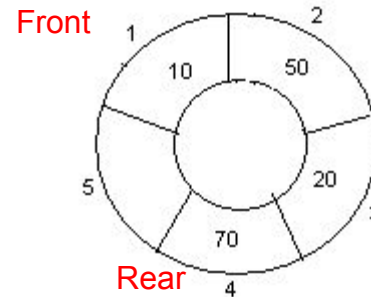
4. Insert 20, Rear = 3, Front = 1.



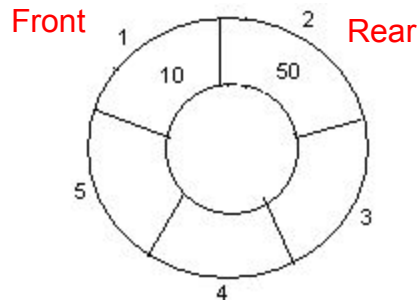
2. Insert 10, Rear = 1, Front = 1.



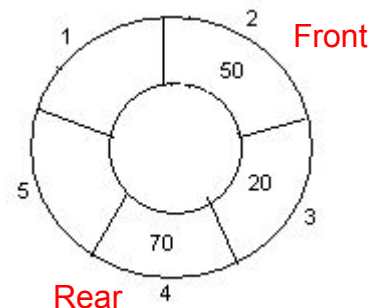
5. Insert 70, Rear = 4, Front = 1.



3. Insert 50, Rear = 2, Front = 1.

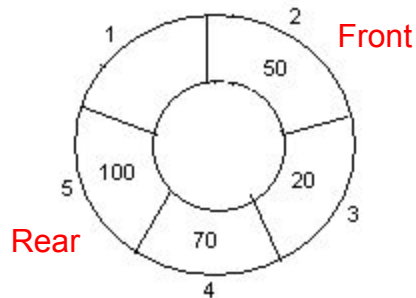


6. Delete front, Rear = 4, Front = 2.

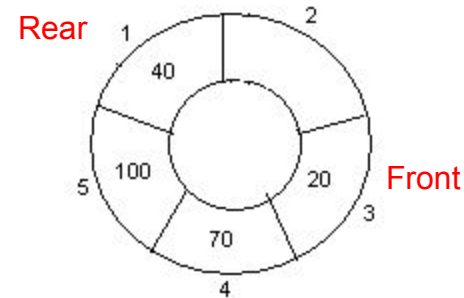


Circular queue

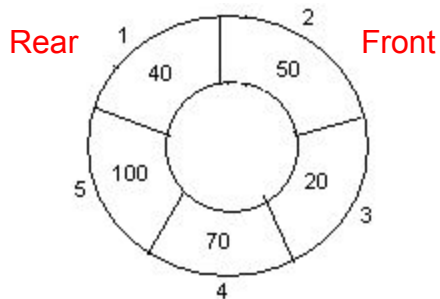
7. Insert 100, Rear = 5, Front = 2.



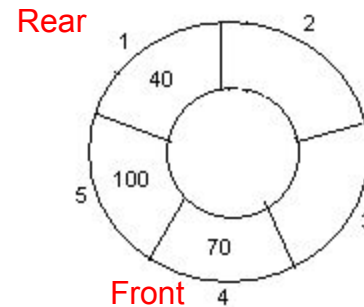
10. Delete front, Rear = 1, Front = 3.



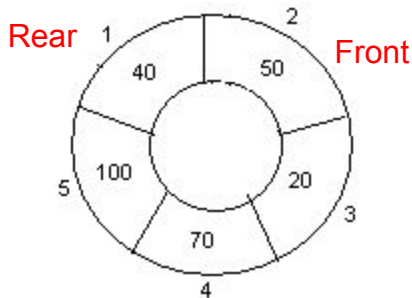
8. Insert 40, Rear = 1, Front = 2.



11. Delete front, Rear = 1, Front = 4.



9. Insert 140, Rear = 1, Front = 2.
As $\text{Front} = \text{Rear} + 1$, so Queue overflow.



12. Delete front, Rear = 1, Front = 5.

