

Central Limit Theorem Assignment

Q.1.

$$\mu = 10$$

$$\sigma = 4$$

$$n = 100$$

Value is < 9

$$z = \frac{x - \mu}{\frac{\sigma}{\sqrt{n}}}$$

$$z = \frac{9 - 10}{\frac{4}{\sqrt{100}}} = \frac{-1}{\frac{4}{10}} = \underline{\underline{-2.5}}$$

in z table value = .0062

Q.2

$$\text{mean } \mu = 50$$

$$\sigma = 15$$

$$n = 10$$

~~$$z = \frac{x - \mu}{\frac{\sigma}{\sqrt{n}}}$$~~

Q.3

$$\mu = 2.4$$

$$\sigma = 2.0$$

$$n = 100$$

$$\frac{2}{\sqrt{100}}$$

Q.4

$$Z = \frac{98 - 96}{\frac{16}{\sqrt{35}}} = \frac{2}{\frac{16}{5.9}} = \frac{2}{2.70} = .74$$
$$= \underline{\underline{.7704}}$$

Q.5.

(a) $Z = \frac{\bar{x} - \mu}{\sigma} = \frac{6.8 - 6}{1} = .2$

$$= \underline{\underline{.5793}}$$

(b) $Z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}} = \frac{6.2 - 6}{\frac{1}{\sqrt{100}}} = .2 \times 10 = \underline{\underline{2}}$

$$.9772$$

Q.6 =

$$Z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}} = \frac{6.2 - 6}{\frac{1}{\sqrt{100}}} = \underline{\underline{.9772}}$$

If we do the male the 60% of the men will not be included.

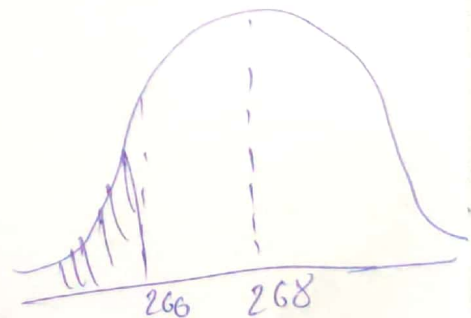
Q.7.

$$n = 25$$

$$\sigma = 15$$

$$\mu = 260$$

$$Z_{\text{sn}} = \frac{260 - 268}{\frac{15}{\sqrt{25}}} = \frac{-8}{\frac{15}{5}} = \frac{-8}{3} = -2.66$$
$$= \underline{\underline{.0039}}$$



Q.8

From above observation we can say that .0039 is less than 1%. So 260 days per mean is unusually low. So it does affect the health.

Q.9

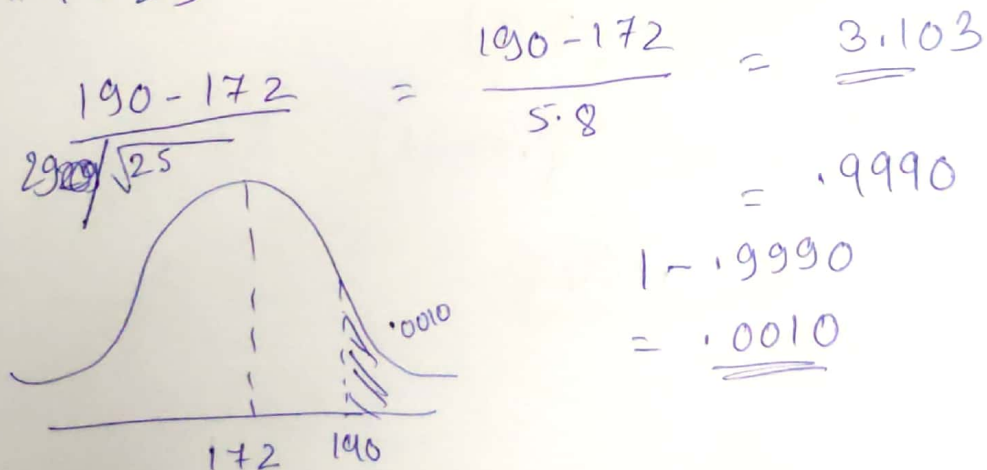
$$\mu = 172$$

$$\sigma = 29$$

$$(a) \quad z = \frac{190 - 172}{29} = .621 = \text{table} = .7324$$

it says. one randomly selected
~~table = .2673~~ $\therefore 1 - .7324$
 $= \underline{\underline{.2673}}$

$$(b) \quad n = 25$$



(c)

$$\text{mean. } \frac{4750}{25} = \underline{\underline{190}}$$

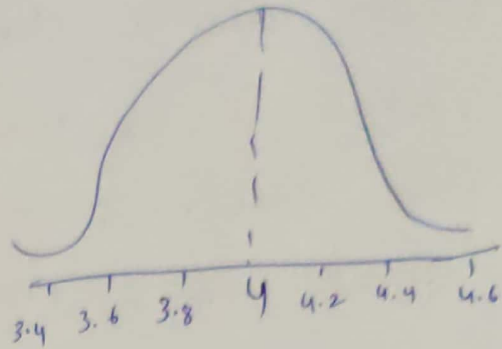
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Q. 10

$$\mu = 4.0$$

$$\sigma = 1.5$$

$$n = 50$$



$$\frac{\sigma}{\sqrt{n}} = \frac{1.5}{\sqrt{50}} = \underline{\underline{.2121}}$$

if 3.5 & 3.8

$$P\left(\frac{3.5 - 4.0}{.2121}\right)$$

$$-.94$$

$$P\left(\frac{3.8 - 4.0}{.2121}\right)$$

$$-2.36$$

so if between 3.5 & 3.8

$$\text{the } (-.94) - (-2.36)$$

$$= (.1736) - (.0091)$$

$$= \underline{\underline{.1645}}$$

Q. 11

$$\mu = 23.1$$

$$\sigma = 3.1$$

$$n = 6$$

$$n = 27$$

$$Z = \frac{27 - 23.1}{\frac{3.1}{\sqrt{6}}} = 3.08$$

$$1 - .9990 = .0010$$

Q. 12

$$\mu = 21.50$$

$$\sigma = 2.22$$

$$n = 8$$

$$Z_1 = \frac{20 - 21.50}{\frac{2.22}{\sqrt{8}}} = \frac{-1.5}{.78} = -1.92$$
$$= .0274$$

$$Z_2 = \frac{23 - 21.50}{.78} = \frac{1.5}{.78} = 1.92$$
$$= .9726$$

$$Z_1 - Z_2 = .9726 + .0274$$

$$= .9998$$

a.13

$$\mu = 75$$

$$\sigma = 5$$

$$(a) \quad z = \frac{83 - 75}{5} = 1.6$$

$$z = .9452$$

$$p = 1 - z$$

$$= 1 - .9452$$

$$= \underline{\underline{.0548}}$$

$$(b) \quad \frac{83 - 75}{5/\sqrt{5}} = \frac{83 - 75}{2.23} = 3.57$$

$$z = .9999$$

$$p = 1 - z$$

$$= 1 - .9999$$

$$= \underline{\underline{.0001}}$$

Q.14

$$\mu = 28.3$$

$$\sigma = 2.3$$

$$n = 10$$

$$x = 27$$

$$z = \frac{27 - 28.3}{\frac{2.3}{\sqrt{10}}} = \frac{-1.3}{.727} = -1.788$$

$$z = \underline{\underline{1.0375}}$$