PART1

Defining Constants and Equations

1.0 INTRODUCTION

The U.S. Standard Atmosphere, 1976 is an idealized, steady-state representation of the Earth's atmosphere from the surface to 1000 km, as it is assumed to exist in a period of moderate solar activity.

For heights from the surface to 51 geopotential kilometers (km), the tables of this standard are identical with those of the U.S. Standard Atmosphere, 1962 (COESA 1962) and are based on traditional definitions.

These definitions, especially for heights below 20 km, do not necessarily represent an average of the vast amount of atmospheric data available today from observations within that height region.

For heights from 51 km to 84.852 km (i.e., 51.413 to 86 geometric kilometers), the tables are based upon the averages of present-day atmospheric data as represented by the traditional type of defining parameters.

These include the linearly segmented temperature-height profile, and the assumption of hydrostatic equilibrium, in which the air is treated as a homogeneous mixture of the several constituent gases.

At greater heights, however, where dissociation and diffusion processes produce significant departures from homogeneity, the definitions governing the Standard are more sophisticated than those used at lower altitudes.

In this high-altitude regime, the hydrostatic equation, as applied to a mixed atmosphere, gives way to the more general equation for the vertical component of the flux for individual gas species (Colegrove et al., 1965; Keneshea and Zimmerman, 1970), which accounts for the relative change of composition with height.

This flux equation simplifies to the hydrostatic equation for the special case when the atmospheric gases remain well mixed, as is the situation below 86 km.

The temperature-height profile between 86 and 1000 km is not expressed as a series of linear functions, as at lower altitudes.

Rather, it is defined in terms of four successive functions chosen not only to provide a reasonable approximation to observations, but also to yield a continuous first derivative with respect to height over the entire height regime.

Observational data of various kinds provide the basis for independently determining various segments of this temperature-height profile.

The observed temperatures at heights between 110 and 120 km were particularly important in imposing limits on the selection of the temperature-height function for that region, while the observed densities at 150 km and above strongly influenced the selection of both the temperature and the extent of the low-temperature isothermal layer immediately above 86 km.

In spite of the various independent data sets upon which the several temperature-height segments are based, it is desirable, for purposes of mathematical reproducibility of the tables of this Standard, to express the temperature in a series of consecutive height functions from the surface to 1000 km, with the expression for each successive function depending upon the endpoint value of the preceding function, as well as upon certain terms and coefficients peculiar to the related height interval.

This total temperature-height profile applied to the fundamental continuity models (i.e., the hydrostatic equation and the equation of motion), along with all the ancillary required constants, coefficients, and functions, defines the U.S. Standard Atmosphere, 1976.

The specification of this definition without any justification in terms of observed data is the purpose of Section 1.

1.1 INTERANTIONAL SYSTEM OF UNITS

The 1976 U. S. Standard Atmosphere is defined in terms of the International System (SI) of Units (Mechtley 1973).

A list of the symbols, names, and the related quantities of the applicable basic and derived SI units, as well as of the nonstandard metric units and the English unit employed in this Standard is presented in Table 1.

1.2 BASIC ASSUMPTIONS AND FORMULAS

1.2.1 Adopted Constants.

For purposes of computation, it is necessary to establish numerical values for various constants appropriate to the Earth's atmosphere.

The adopted constants are grouped into three categories.

Category I includes those constants which are common to many branches of the physical and chemical sciences, and are here considered to be fundamental constants.

Some of these may be multivalued, as in the case of M, representing the molecular weight of the i-th gas species.

Category I includes three single-valued and one multivalued constant.

The Boltzmann constant, $k = 1.380622 \times 10^{-23} \,\text{Nm/K}$, is theoretically equal to the ratio $\frac{R^*}{N_A}$, and has a value, consistent with the carbon-12 scale, as cited by Mechtley (1973).

The Avogadro constant, $N_A = 6.022169 \times 10^{26} \, \mathrm{kmol}^{-1}$, is consistent with the carbon-12 scale and is the value cited by Mechtley (1973).

The gas constant, $R^* = 8.31432 \times 10^3 \,\mathrm{N \cdot m/(kmol \cdot K)}$, is consistent with the carbon-12 scale, and is the value used in the 1962 Standard.

This value is not exactly consistent with the cited values of k and N_A .

Category IIC on stants

The set of values of fractional-volume concentrations F_i , listed in Table 3, is assumed to represent the relative concentrations of the several gas species comprising dry air at sea level.

These values are identical to those given in the 1962 Standard (COESA 1962), and except for minor modifications based upon CO2 measurements by Keeling (1960), these values are the same as those given by Glueckauf (1951), and are based upon the earlier work of Paneth (1939).

The quantity g_0 (= 9.80665 m/s²) represents the sea-level value of the acceleration of gravity adopted for this Standard.

The dimensional constant g'_0 , selected to relate the standard geopotential meter to geometric height, is numerically equal to g_0 , but with appropriately different dimensions.

This constant implicitly defines one standard geopotential meter as the vertical increment through which one must lift one kilogram to increase its potential energy by 9.80665 joules.

The geometric length of this vertical increment varies inversely with the height-dependent value of g.

Each of the members of the set of geopotential-height values H_b , listed in Table 4, represents the base of one of eight successive atmospheric layers.

The pairs of values of H_b and $L_{M,b}$ are based partly on tradition and partly on present-day observations. The first five of these pairs are identical to those of the first five layers of the 1962 Standard, while the remaining two values of both H_b , and $L_{M,b}$ have been newly selected to provide a reasonable fit to the presently available atmospheric data.

The first two values of the related sets have their origin in one of the earliest aeronautical standard atmospheres (Toussaint 1919), and were approximated in the first U.S. Standard Atmosphere (Diehl 1925).

Each member of the set of seven gradients $L_{M,b} = \frac{dT}{dH}$ [i.e., of molecular scale temperature T_M (Minzner and Ripley 1956) with respect to geopotential H] listed in Table 4 represents the fixed value appropriate throughout its related layer, H_b to H_{b+1} .

The standard sea-level atmospheric pressure P_0 equal to 1.013250×10^5 Pa (or N/m²) was adopted in 1947 in Resolution 164 of the International Meteorological Organization, and corresponds to the pressure exerted by a column of mercury 0.760 m high, having a density of 1.35951×10^4 kg/m³ and subject to an acceleration due to gravity of 9.80665 m/s². This equivalency definition was adopted by the International Commission on Weights and Measures in 1948.

The effective Earth's radius for purposes of calculating geopotential at any latitude is readily obtained from equations given by Harrison (1968).

The value of r_0 (= 6356.766 km) used in this Standard corresponds to the latitude for which $g = 9.80665 \,\mathrm{m/s^2}$.

The standard sea-level temperature T_0 is 288.15 K. This value is based upon two international agreements. The first of these is Resolution 192 of the International Commission for Air Navigation, which in 1924 adopted 15° C as the sea-level temperature of the International Standard Atmosphere.

This value has been retained unchanged in all known standard atmospheres since that date.

The second agreement is that of the 1954 Tenth General Conference on Weights and Measures, which set the fixed point of the Kelvin temperature scale at the triple-point temperature 273.16 K, which is 0.01 K above the ice-point temperature at standard sea-level pressure.

The Sutherland constant, $S = 110 \,\mathrm{K}$, (Hilsenrath et al. 1955) is a constant in the empirical expression for dynamic viscosity.

The quantity, $\beta = 1.458 \times 10^6 \,\mathrm{kg/(s \cdot m \cdot K^{1/2})}$, (Hilsenrath et al. 1955) is a constant in the expression for dynamic viscosity.

The ratio of specific heat of air at constant pressure to the specific heat of air at constant volume is a dimensionless quantity with an adopted value $\gamma = 1.400$.

This is the value adopted by the Aerological Commission of the International Meteorological Organization, in Toronto in 1948.

The mean effective collision diameter σ (= 3.65 × 10⁻¹⁰ m) of molecules is a quantity that varies with gas species and temperature.

The adopted value is assumed to apply in a dry, sea-level atmosphere.

Above 85 km, the validity of this value changes.

The quantity a represents a set of five values of species-dependent coefficients listed in Table 6. Each of these values is used in a particular function for designating the height-dependent, molecular-diffusion coefficient D_i for the related gas species. (See b_i below.)

The quantity b_i represents a set of five values of species-dependent exponents listed in Table 6. Each of these values is used, along with the corresponding value of a_i , in eq (8) for designating the height-dependent, molecular-diffusion coefficient for the related gas species. The particular values of a_i and b_i adopted for this Standard have been selected to yield a height variation of D, assumed to be realistic.

The quantity $K_7 = 1.2 \times 10^7 \,\mathrm{m}^2/\mathrm{s}$ is the adopted value of the eddy-diffusion coefficient K at $Z_1 = 86 \,\mathrm{km}$ and in the

height interval from 86 up to 197 km. Beginning at 91 km and extending up to 115 km, the value of K is defined by:

(11b) At 115 km the value of K equals K_{10}

The quantity $K_{10} = 0.0 \,\mathrm{m^2/s}$ is the adapted value of the eddy-diffusion coefficient at $Z_{10} = 120$ and highest for the height interval from 115 km to 1000 $\mathrm{m^2/s}$.

The two-valued set of gradients $L_{s,x}$, listed in Table 5, are specifically selected for the Standard to represent available observations. Each of these two values of $L_{s,x}$ is associated with the entire extent of a corresponding layer whose base is Z_s , where the top is Z_{s+1} .

The quantity $N(O)_0$, (= 8.6 × 10^{13} m⁻³), is the number density of atomic oxygen assigned for this Standard to exist at Z = 86 km. This value is used, along with other number densities of atomic oxygen, hydrogen atom, and densities of N_2 , O_2 , Ar, and He at 86 km. (See Appendix A.)

The quantity, $N(H)_{\infty}$, (= 1.0 × 10¹⁰ m⁻³) is the assigned number density of atomic hydrogen at height $Z_{\infty} = 500$ km, and is used as the reference value in computing the height profile of atomic hydrogen

between 150 and 1000 km.

The quantity w_i represents the fifth set of the six sets of constants described along with q above.

The quantity W_i represents the sixth set of the six sets of constants described along with q above.

The quantity Z_s represents the altitude. The values of Z_s for l equal to 7 through 12. The values of Z_s and Z_{s+1} correspond successively to the top of the successive layers characterized by successive linear segments of the adopted temperature-height function for this Standard. The value Z_{10} is the reference height for the atomic oxygen calculation, while the value Z_{10+1} represents the top of the region for which the tabular values of the Standard are given. These values of Z_s , along with the designation of the type of temperature-height function associated with the first four of these values, plus the related values of $L_{s,x}$ for the two segments having a linear temperature-height function, are listed in Table 5.

The quantity a_i represents a set of six adopted species-dependent thermal-diffusion coefficients listed in Table 6. The quantity $\sigma^* = (10^{-3} \text{ K/cm})$ is a term that is chosen as a compromise between the classical "least flux" flux for $T_0 \sim 100 \text{ K}$, with corrections to take into account deviations from a Maxwellian velocity distribution at the critical level, (Brinkman 1971) and the effects of electronic exchange with R^+ and O^- in the plasmapshere (Tinsley 1970).

1.2.2 EQUILIBRIUM CONDITIONS

The air is assumed to be dry, and at heights sufficiently below 86 km, the atmosphere is assumed to be homogeneously mixed, with a relative molecular composition leading to a constant mean molecular weight M.

If the air is treated as a perfect gas, the total pressure P, temperature T and total density ρ at any point in the atmosphere are related by the equation of state, i.e., the perfect gas law, one form of which is

$$P = \rho \cdot R^* \cdot \frac{T}{M} \tag{1}$$

where R^* is the universal gas constant.

An alternate form of the equation of state, in terms of the total number density N and the Avogadro constant N_A , is

$$P = N \cdot \frac{R^*}{N_A} \cdot T = N \cdot k \cdot T \tag{2}$$

This form represents the summation of P_i , the partial pressures of the individual gas species, where P_i is related to the number density of the *i*-th gas species in the following expression:

$$P_i = n_i \cdot k \cdot T \tag{3}$$

where k is the Boltzmann constant.

Within the height region of complete mixing, the atmosphere is assumed to be in hydrostatic equilibrium, and to be horizontally stratified so that dP, the differential of pressure, is related to dz, the differential of geometric height, by the relationship

$$dP = -\rho \cdot g \cdot dz \tag{4}$$

where g is the height-dependent acceleration of gravity.

The relation between eqs (1) and (4) yields another form of the hydrostatic equation, which can be as

basis for the low-altitude pressure calculation:

$$\frac{dP}{P} = -\frac{g \cdot M}{R^* \cdot T} \cdot dz \tag{5}$$

Above 86 km, the hydrostatic equilibrium of the atmosphere gradually breaks down as diffusion and vertical transport of individual gas species lead to the need for a dynamically adjusted model including diffusive separation.

Under these conditions it is convenient to express the height variations in the atmospheric number density in terms of the vertical component of the flux of the molecules of individual gas species (Colgrove et al. 1966). In terms of the *i*-th gas species, this expression is

$$n_i \cdot v_i + D_i \left(\frac{dn_i}{dz} + \frac{n_i}{T} \cdot \frac{dT}{dz} + \frac{n_i}{M} \cdot \frac{dM}{dz} + \frac{g \cdot n_i \cdot m_i}{R^* \cdot T} \right) + K \left(\frac{dn_i}{dz} + \frac{n_i}{T} \cdot \frac{dT}{dz} + \frac{g \cdot n_i \cdot m_i}{R^* \cdot T} \right) = 0$$
 (6)

The function K is defined differently in each of three height regions:

1. For $86 \le Z < 95$ km,

$$K = K_7 = 1.2 \times 10^2 \,\mathrm{m}^2/\mathrm{s}$$
 (7a)

2. For $95 \le Z < 115$ km,

$$K = K_7 \cdot \exp\left[1 - \frac{400}{400 - (Z - 95)^2}\right] \tag{7b}$$

3. For $115 \le Z < 1000$ km,

$$K = K_{10} = 0.0 \,\mathrm{m}^2/\mathrm{s} \tag{7c}$$

The function D_i is defined by

$$D_i = \frac{a_i}{\Sigma n_i} \cdot \left(\frac{T}{273.15}\right)^{b_i} \tag{8}$$

where a_i and b_i are the species-dependent constants defined in Table 6, while T and Σn_i are both altitude-dependent quantities which are specified in detail below. The values of D_i , determined from these altitude-dependent quantities and the defined constants a_i and b_i , are plotted in Figure 1 as a function of altitude, for each of four species, O, O₂, Ar, and He. The value of D_i for atomic hydrogen, for heights just below 150 km, is also shown in Figure 1. This same figure contains a graph of K as a function of altitude. It is apparent that, for heights sufficiently below 90 km, values of D_i are negligible compared with K, while above 115 km, the reverse is true. In addition, it is known that the flux velocity v_i for the various species becomes negligibly small at altitudes sufficiently below 90 km.

The information regarding the relative magnitudes V_i , D_i , and K permits us to consider the application of eq (6) in each of several regimes.

One of these regimes is for heights sufficiently below 90 km, such that v_i and D_i are both extremely small compared with K. Under these conditions, eq (6) reduces to the following form of the hydrostatic equation:

$$\frac{dn_i}{n_i} + \frac{dT}{T} = -\frac{g \cdot M}{R^* \cdot T} \cdot dZ. \tag{9}$$

Since the left-hand side of this equation is seen through eq (3) to be equal to dP_i/P_i , eq (9) is seen to be the single-gas equivalent to eq (5). Consequently, while eq (6) was designed to describe the

assumed equilibrium conditions of individual gases above 86 km, it is apparent that eq (6) also describes such conditions below that altitude, where the partial pressure of each gas comprising the total pressure varies in accordance with the mean molecular weight of the mixture, as well as in accordance with the temperature and the acceleration of gravity. Nevertheless, eq (5), expressing total pressure, represents a convenient step in the development of equations for computing total pressure versus geometric height, when suitable functions are introduced to account for the altitude variation in T, M, and g.

It has been customary in standard-atmosphere calculations, to effectively eliminate the variable portion of the acceleration of gravity from eq (5) by the transformation of the independent variable Z to geopotential altitude H, thereby simplifying both the integration of eq (5) and the resulting expression for computing pressure. The relationship between geometric and geopotential altitude depends upon the concept of gravity.

1.2.3 Gravity and Geopotential Altitude

Viewed in the ordinary manner, from a frame of reference fixed in the earth, the atmosphere is subject to the force of gravity. The force of gravity is the resultant (vector sum) of two forces:

- 1. the gravitational attraction in accordance with Newton's universal law of gravitation, and
- 2. the centrifugal force, which results from the choice of an earthbound, rotating frame of reference.

The gravity field, being a conservative field, can be derived conveniently from the gravity potential energy per unit mass, that is, from the geopotential Φ . This is given by

$$\Phi = \Phi_G + \Phi_C \tag{10}$$

where Φ_G is the potential energy, per unit mass, of gravitational attraction, and Φ_C is the potential energy, per unit mass, associated with the centrifugal force. The gravity, per unit mass, is

$$g = \nabla \Phi \tag{11}$$

where $\nabla \Phi$ is the gradient (ascendant) of the geopotential.

The acceleration due to gravity is denoted by g and is defined as the magnitude of g; that is,

$$g = |\mathbf{g}| = |\nabla \phi|. \tag{12}$$

When moving along an external normal from any point on the surface ϕ_0 , to a point on the surface $\phi_1 + d\phi$, close to the first surface, so that $\phi_1 = \phi_0 + d\phi$, the incremental work performed by shifting a unit mass from the first surface to the second will be

$$d\phi = g \cdot dZ. \tag{13}$$

Hence,

$$\phi = \int_0^Z g \cdot dZ. \tag{14}$$

The unit of measurement of geopotential is the standard geopotential meter (m'), which represents the work done by lifting a unit mass 1 geometer meter, through a region in which the acceleration of gravity is uniformly 9.80665 m/s².

The geopotential ϕ of any point with respect to mean sea level (assumed zero potential), expressed in geopotential meters, is defined as geopotential altitude.

Therefore, geopotential altitude H is given by

$$H = g_0^{-1} \int g \cdot dZ. \tag{15}$$

and is expressed in geopotential meters (m') when the unit geopotential g_0^{-1} is set equal to 9.80665 m'/s².

With geopotential altitude defined as in eq (15), the differential of H(dH) may be expressed as

$$g \cdot dH = g \cdot dZ. \tag{16}$$

This expression is used in eq (5) to reduce the number of variables prior to its integration process by leading to an expression for computing pressure as a function of geopotential height.

The inverse square law of gravitation provides an expression for g as a function of altitude with sufficient accuracy for most model-atmosphere computations:

$$g = g_0 \left(\frac{r_0}{r_0 + Z}\right)^2. \tag{17}$$

where r_0 is the effective radius of the Earth at a specific latitude as given by Lambert's equations (List 1963).

Such value of r_0 takes into account the centrifugal acceleration at the particular latitude.

For this Standard, the value of r_0 is taken as 6.356766×10^6 m, consistent with the adopted value of $g_0 = 9.80665 \,\mathrm{m/s}^2$ for the sea-level value of the acceleration of gravity.

The variation of g as a function of geometric altitude is depicted in Figure 2.

Integration of eq (15), after substitution of eq (17) for g, yields

$$H = g_0 \cdot \frac{r_0}{g_0 \cdot r_0 + Z} \cdot \frac{r_0 \cdot Z}{r_0 + Z}.$$
 (18)

or

$$Z = \frac{r_0 \cdot H}{r_0 - H}.\tag{19}$$

where $\gamma = g/g_0 = 1$ m'/m.

Differences between geopotential altitudes obtained from eq (18) for various values of Z, and those computed from the more complex relationship used in developing the U.S. Standard Atmosphere, 1962, are small. For example, values of H computed from eq (18) are approximately 0.2, 3.4, and 33.5 m greater at 90, 150, and 700 km, respectively, than those obtained from the relationship used in the 1962 Standard.

The transformation from Z to H in eq (18) makes it unnecessary to utilize the variation of T as well as any variation in M between the surface and 86 km. Also, we have defined a term of H. It is convenient therefore to determine the sea-level value of M as well as the extent of the height dependence of this quantity between the surface and 86 km. Therefor.

this low-altitude regime, the two variables T and M are combined with the constant \bar{M} , into a single variable T_M , which is then defined as a function of H.

1.2.4 MEAN MOLECULAR WEIGHT.

The mean molecular weight \bar{M} of a mixture of gases is by definition

$$\bar{M} = \frac{\sum (n_i \cdot M_i)}{\sum n_i} \tag{20}$$

where n_i and M_i are the number density and defined molecular weight, respectively, of the *i*th gas species. In that part of the atmosphere between the surface and about 86 km altitude, mixing is dominant, and the effect of diffusion and photochemical processes upon \bar{M} is negligible. In this re- gion the fractional composition of species F_i is assumed to remain constant at the defined value F_i , and \bar{M} remains constant at its sea-level value \bar{M}_0 . For these conditions n_i is equal to the product of F_i times the total number density N, so that eq (20) may be rewritten as

$$\bar{M} = \frac{\sum [F_i \cdot N \cdot M_i]}{\sum [F_i \cdot N]} = \frac{\sum [F_i \cdot M_i] \cdot N}{\sum [F_i] \cdot N} = \frac{\sum [F_i \cdot M_i]}{\sum F_i}$$
(21)

The right-hand element of this equation results from the process of factoring N out of each term of both the numerator and the denominator of the preceding equation, so that in spite of the altitude dependence of N, \bar{M} is seen analytically to equal \bar{M}_0 over the entire altitude region of complete mixing.

When the defined values of F_i , and M_i (from table 3) are introduced into eq (21), \bar{M}_0 is found to be 28.9644 kg/kmol. At 86 km (84.852 km), however, the defined value of atomic-oxygen number density (8.6 x 10^{13} /m³) is seen in Appendix A to lead to a value of $\bar{M} = 28.9522$ kg/kmol, about 0.04 percent less than \bar{M}_0 .

To produce a smooth transition from this initial value at sea level to that at 86 km, it has been arbitrarily defined at intervals of 0.5 km for altitudes between 70.000 and 84.852 km, in terms of the ratio \bar{M}/\bar{M}_0 , as given in table 7. These ratio values have been interpolated from those initially selected for intervals of kinetic temperature between 80 and 86 km to satisfy the boundary conditions of $\bar{M}=\bar{M}_0=28.9644$ kg/kmol at 80 km, and $\bar{M}=28.9522$ at 86 km, and to satisfy a condition of smoothly decreasing first differences in \bar{M} within this height interval of 80 to 86 km.

These arbitrarily assigned values \bar{M}/\bar{M}_0 may be used for correcting a number of parameters of this Standard if the tabulations are to correctly fit the model in the fifth and perhaps in the fourth significant figures within this height region.

This after-the-fact correcting is required because these values of \bar{M} were not included in the program used for computing the tables of this Standard below 86 km, and hence, the tabulations of some of the properties may show a discontinuity of up to 0.04 percent between 85.5 and 86 km. This situation exists particularly for four properties: in addition to molecular weight, i.e., kinetic temperature, total number density, mean free path, and collision frequency.

For these five parameters the discrepancy in the tables between 80 and 86 km can readily be removed by simply multiplying or dividing the tabulated values of T, M, and L by the corresponding values of \bar{M}/\bar{M}_0 from the tabulated values of \bar{M} and dividing by the corresponding values of \bar{M}_0 .

Three other properties, dynamic viscosity, kinematic viscosity, and thermal conductivity, which are

tabulated only for heights below 86 km, have similar discrepancies for heights immediately below 86 km.

These values are not so simply corrected, however, because of the empirical nature of their respective defining functions. Rather, these quantities must be recalculated, in terms of a suitably corrected set of values of T, if the precision correct values are desired for geometric altitudes between 80 and 86 km.

1.2.5 MOLECULAR-SCALE-TEMPERATURE VS. GEOPOTENTIAL ALTITUDE (1.0 to 44.8525 KM)

The molecular-scale temperature T_M (Minzner et al. 1958) at a point is defined as the product of the kinetic temperature T times the ratio of \bar{M}_0 to \bar{M} , where \bar{M} is the mean molecular weight of air at that point, and \bar{M}_0 is 28.9644, the mean sea-level value of \bar{M} discussed above. Analytically,

$$T_M = T \cdot \frac{\bar{M}_0}{\bar{M}}. (22)$$

When T is expressed in the Kelvin scale, T_M is also expressed in the Kelvin scale.

The principle value of the parameter T_M is that it combines the variable portion of M with the variable T into a single new variable, in a manner somewhat similar to the combining of the variable portion of g with Z to form the new variable H.

When both of these transformations are introduced into (5), and when T_M is expressed as a linear has an exact integral. Under these conditions, the computation of P versus H becomes a simple process not requiring numerical integration. Traditionally, standard atmospheres have defined temperature as a linear function of height to eliminate the need for numerical integration in the computation of pressure versus height. This Standard follows the tradition to heights up to 86km, and the function T_M versus H is expressed as a series of seven successive linear equations. The general form of these linear equation is

$$T_M = T_{M,b} + L_{M,b} \cdot (H - H_b) \tag{23}$$

with the value of subscript b ranging from 0 to 6 in accordance with each of seven successive layears. The value of $T_{M,b}$ for the first layer (b=0) is 288.15K, identical to T_0 , the sea-level value of T, since at this level $M=M_0$. With this value of $T_{M,b}$ defined, and the set of six values of H_0 and the six corresponding value of $L_{M,b}$ defined in table 4, the function T_M of H is completely defined from the surface to 84.8520 km' (86 km). A graph of this function compared with the similar function of the 1962 Standard in figure 3. From the surface to the 51 – km' altitude, this profile is identical to that of the 1962 Standard. The profile from 51 to 84.8520km' was selected by Task Group I, and addreviated table of thermodynamic properties of the atmosphere based upon this profile were published by Kantor and Cole (1973).

1.2.6 KINETIC TEMPERATURE VERSUS GEOMETRIC ALTTUDE