## **Θ Paradox** (private beta)

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This paper engages with proving the existence of a theoretical paradox that are based on fundamentals of math concepts.

### **Introduction:**

This experiment shows us a theoretical paradox of the relationship between an angle,  $\theta$ , made by a stretched line from two stationary points on a line from time t = 0s to t = ts. (refer to figure 1)

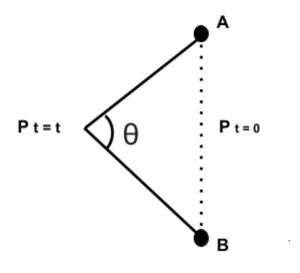


Figure 1

## **Hypothesis**

#### Part 1:

Assume that 'A' and 'B' are two stationary points on a single plane, separated by a constant distance 'x' (only considering 2D now), which are joined by a line 'AB', which is an infinitely stretchable line.

At a time t = 0s -- which is the initial time -- the angle  $\theta$  between the points is 180 degrees ( $\pi$  rad).

At a time t = t, i.e. when the line is stretched from a specific point (point of stretching) and the angle is made between the points 'A' and 'B', opposite to the direction of stretch of line which is always < 180 degrees ( $\pi$  rad) and a perpendicular distance, say 'y' is made from the point used for stretching to the final destination at time t = t (which would be y).

(refer to figure 2.1 and 2.2)

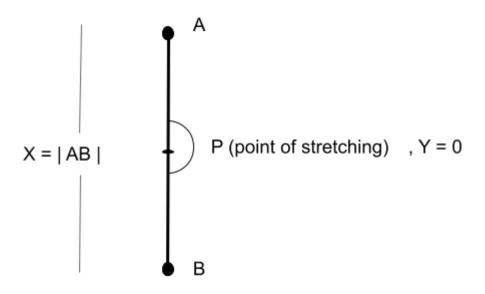


Figure 2.1, Initial state of line

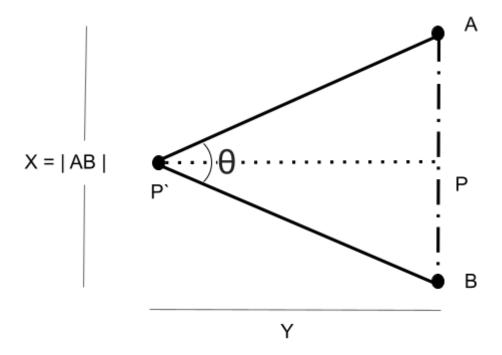


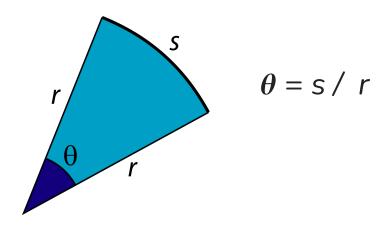
Figure 2.2, final state at a time t = t,  $\theta < 180$ 

As long as  $\mathbf{y}$  is stretched the angle  $\theta$  is always < 180. The graph of the relation between angle as a function of distance from  $\mathbf{P}$  to goes similar to that of a  $f(x) = 1/\log(x)$  graph.

From figure 2.2, we get <u>(eq 1)</u>:

$$\theta \approx AB/PB = AB/PA = x/PB$$

It is known that central angle in a circle subtended by an arc length (in radian) = Arc length / radius



When a circle has an infinite radius, a tangent to a part of the circle would be parallel to the circle, passing through the circle itself. Therefore, **A** 

# CIRCLE WITH AN INFINITE RADIUS IS A STRAIGHT LINE.

When the line (stretchable line between points A and B taken above) is stretched so that the magnitude of the perpendicular vector distance between the initial point of stretching and the final point is infinite, the angle **AP'B** is 0 degrees. (refer to figure 3)

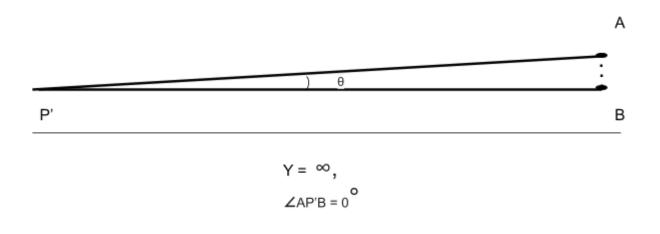


Figure 3

The above picture shows P' extended from a point P, which is the midpoint of AB (taken for ease of solving).

The above image is also scaled to pictorially represent an infinite distance. The magnitude of AB is still X units and will always be throughout.

#### Math:

From figure 3,  $y = \infty$ .

=>  $\theta = AB / P'B$  ... [ circle with infinite radius is a line ]

Assuming AB to be a part of a circle with its radius =  $y = \infty$ ,

$$\theta = AB / P'B = x / P'B$$

$$\theta = x / \infty = 0 \qquad \text{... [Any number divided by infinity is equal to 0]}$$

Since the distinct parts of the lines, namely **P'A** and **P'B** from the point **P'** are originating from the same point and since  $\theta = 0$  (angle between P'A and P'B), it is safe to say that these are the same lines when  $y = \infty$ . i.e. the lines **P'A** = **P'B** and are both one and the same and they start and end at the same point **P'** and **P**, respectively.

BUT we've always had a stationary distance separating these lines, 'x' which is not

changing throughout the process, which is never going to be  $\mathbf{0}$  even when the distance  $\mathbf{y} = \mathbf{w}$ .

$$=> 0 < x \le \infty$$
  
 $=> \theta \ne 0$ , or  $\theta > 0$ 

But  $\theta$  is 0 at an infinite value for y which make rise a Paradox.