

Huazhong University  
of Science & Technology

# Electronic Circuit of Communications

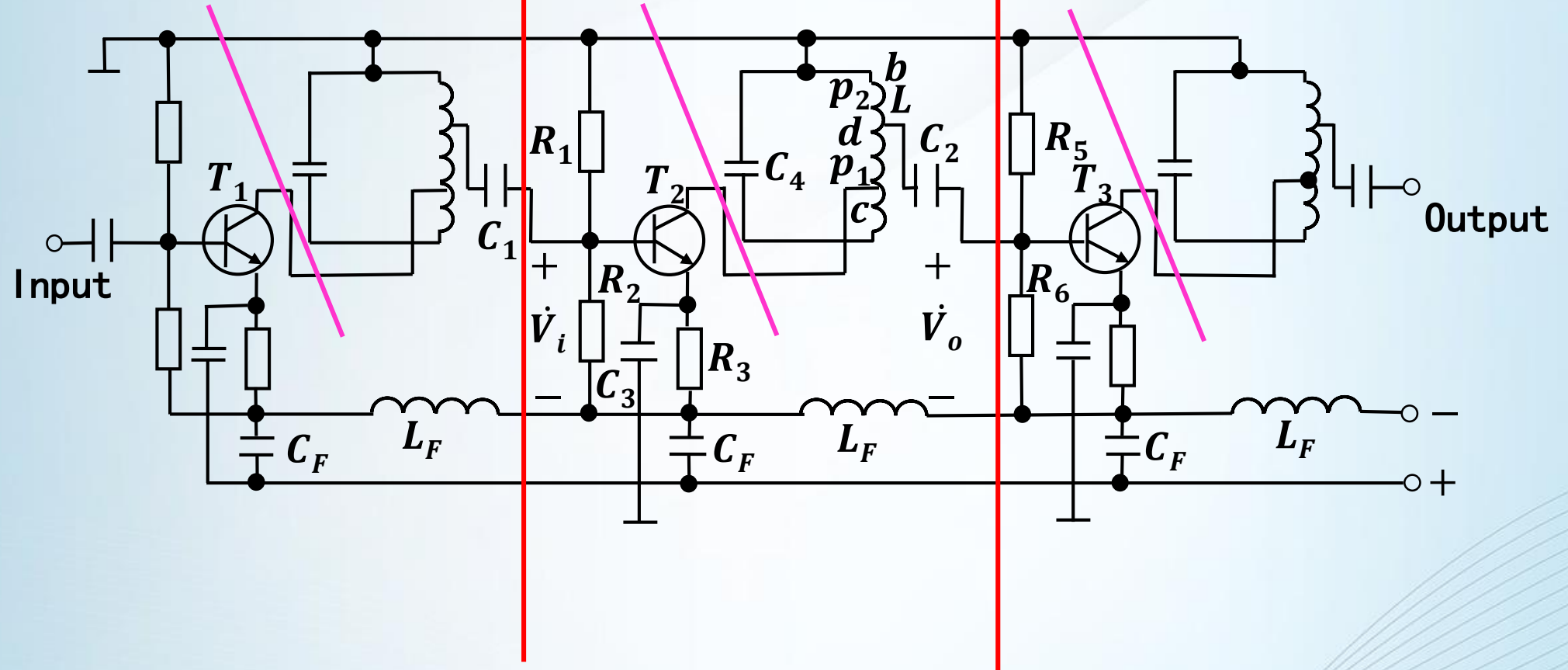
School of Electronic Information  
and Communications

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# Multiple Stage Amplifier

# Multiple Stage Small Signal Amplifier



Divide and Conquer

## (1) *m*-stage Gain

➤ Amplifier with *m* stages,  $A_{V_1}$ 、 $A_{V_2}$  ·····  $A_{V_m}$ , respectively

$$\text{m-stage Gain: } A_m = A_{V_1} \cdot A_{V_2} \cdot \cdots \cdots A_{V_m}$$

➤ If every stage has equal  $A_{V_1}$

$$A_m = A_{V_1}^m$$

## (2) $m$ -stage Bandwidth $(2\Delta f_{0.7})_m$

If equal stage gain:

$$A_m = A_V^m$$

$$\frac{A_m}{A_{m0}} = \frac{1}{\left( \sqrt{1 + \left( \frac{Q_L}{f_0} 2\Delta f \right)^2} \right)^m} = \frac{1}{\sqrt{2}}$$

$\Rightarrow$  Total bandwidth:  $(2\Delta f_{0.7})_m = \sqrt{2^{\frac{1}{m}} - 1} \cdot 2\Delta f_{0.7}$

1-stage gain

Factor  $< 1$ ,  $X = \sqrt{2^{\frac{1}{m}} - 1}$

**Note:**

➤ Total Bandwidth  $<$  Single Bandwidth

### (3) $m$ -stage Selectivity (Rectangle Coefficient)

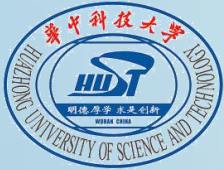
$$\frac{A_m}{A_{m0}} = \frac{1}{\left( \sqrt{1 + \left( \frac{Q_L}{f_0} 2\Delta f \right)^2} \right)^m} = 0.1$$

$$\Rightarrow (2\Delta f_{0.1})_m = \sqrt{100^{\frac{1}{m}} - 1} \cdot 2\Delta f_{0.7}$$

$$\Rightarrow K_{r0.1} = \frac{(2\Delta f_{0.1})_m}{(2\Delta f_{0.7})_m} = \frac{\sqrt{100^{\frac{1}{m}} - 1}}{\sqrt{2^{\frac{1}{m}} - 1}}$$

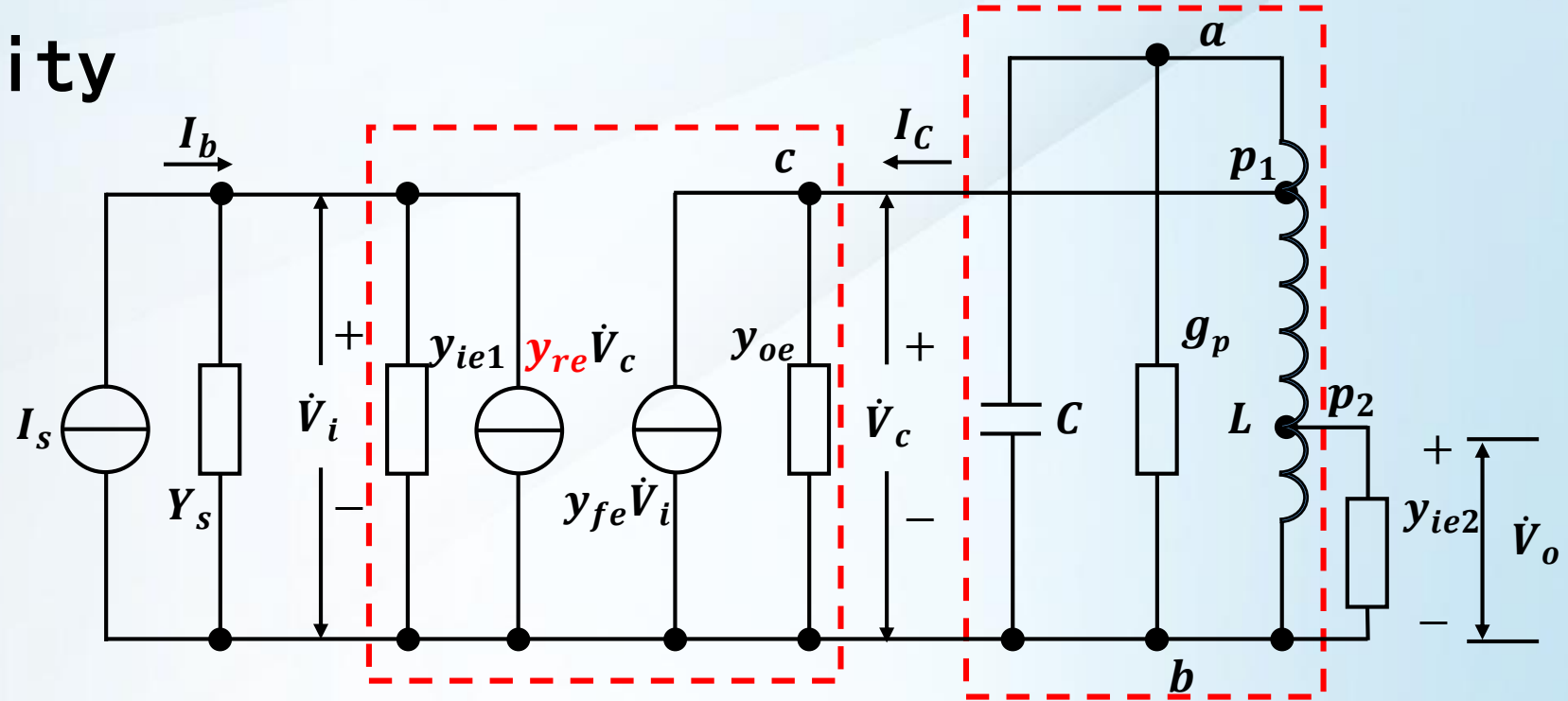
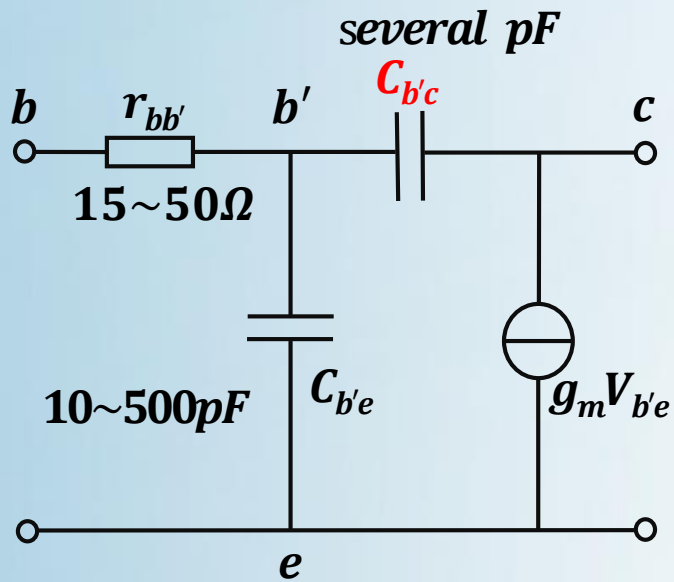
Note: Far away from ideal 1

$m$	1	2	3	4	5	6	7	8	9	10
$K_{r0.1}$	9.9499	4.6613	3.7430	3.3805	3.1886	3.0703	2.9902	2.9324	2.8888	2.8547



# Instability

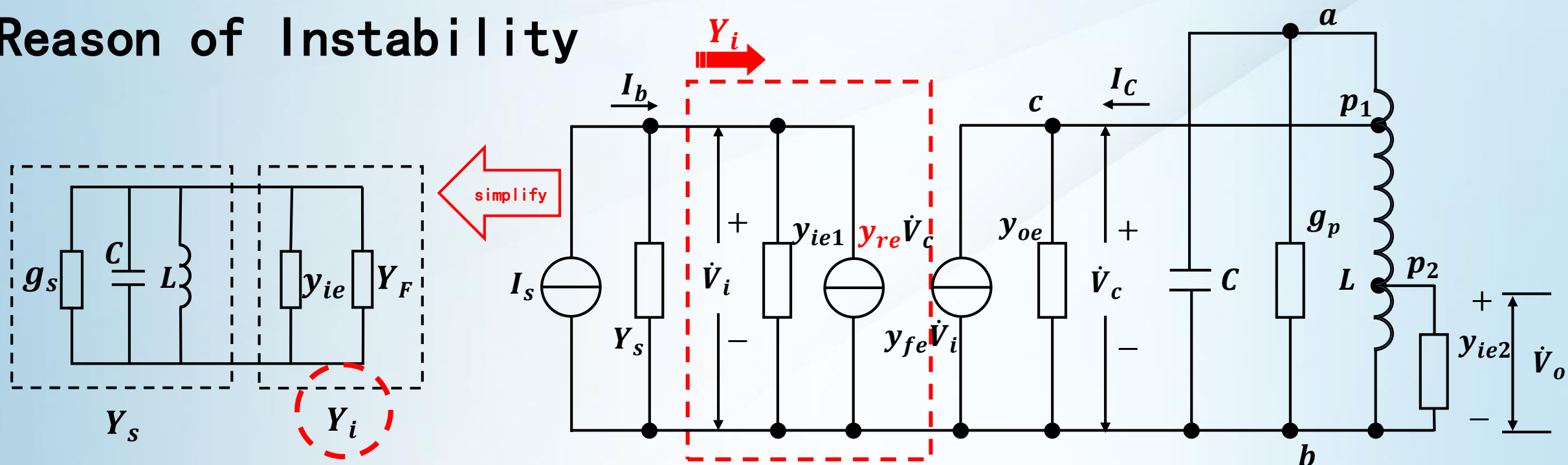
# Reason of Instability



- Hybrid  $\pi$ :  $C_{b'c} \neq 0 \rightarrow \text{Bi-directional} \rightarrow \text{Instable}$
- Y parameter:  $y_{re} \neq 0$



# Reason of Instability



➤ Consider  $g_\Sigma$  of  $Y_s + Y_i$

$$g_\Sigma = g_s + g_{ie} + g_F$$

$$\Rightarrow g_F \text{ (function of frequency)} < 0 \quad \rightarrow g_\Sigma = 0$$

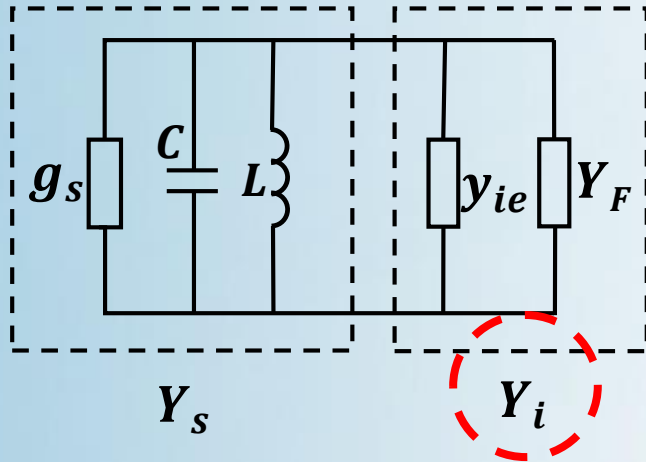
$$\Rightarrow Q_L = \frac{\omega_0 C_\Sigma}{g_\Sigma} \rightarrow \infty$$

Amplifier disabled

$$Y_i = y_{ie} - \frac{y_{fe} y_{re}}{y_{oe} + Y'_L} = y_{ie} + Y_F$$

$$Y_F = g_F + jb_F$$

# Condition of Instability



If  $Y_s + Y_i = 0$ ,  $g_\Sigma = 0$  Instable

$$Y_s + Y_i = Y_s + y_{ie} - \frac{y_{fe}y_{re}}{y_{oe} + Y'_L} = 0 \Rightarrow \frac{(Y_s + y_{ie})(y_{oe} + Y'_L)}{y_{fe}y_{re}} = 1$$

$y_{re} \uparrow$ , Feedback  $\uparrow$ , Left equation  $\downarrow$ , Close to 1  $\rightarrow$  Instable  
 $y_{re} \downarrow$ , Feedback  $\downarrow$ , Left of equation  $\uparrow \rightarrow$  Stable

**Stability Coefficient**  $S = \frac{(Y_s + y_{ie})(y_{oe} + Y'_L)}{y_{fe}y_{re}}$

If  $S = 1$ , Instable

If  $S \gg 1$ , Stable ( $S = 5 \sim 10$ )

## Relation between $A_{V_o}$ and $S$

$$\text{If } S = 5, \quad (A_{V_o})_s = \sqrt{\frac{|y_{fe}|}{2.5\omega_0 C_{re}}}$$

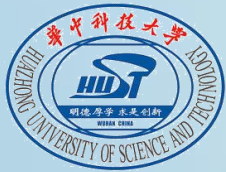
$$A_{V_o} \leq (A_{V_o})_s$$

**Note:**

①  $f \uparrow \quad (A_{V_o})_s \downarrow$

② Choose bigger  $\frac{|y_{fe}|}{C_{re}}$

③  $(A_{V_o})_s$  only consider inner feedback, not outside feedback



# Solutions

**Clue:**

$y_{re} \neq 0$  (  $C_{b'c} \neq 0$  )  $\Rightarrow$  Bi-directional Device

$\Rightarrow$  Unidirectionalize

1

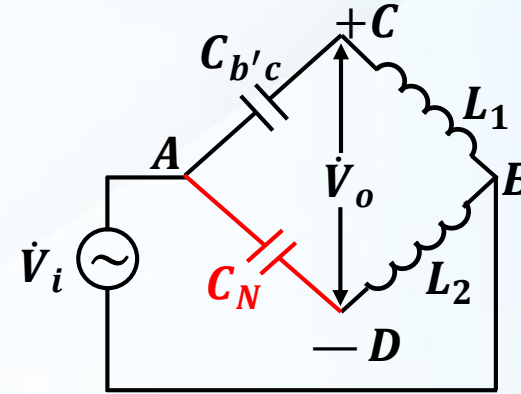
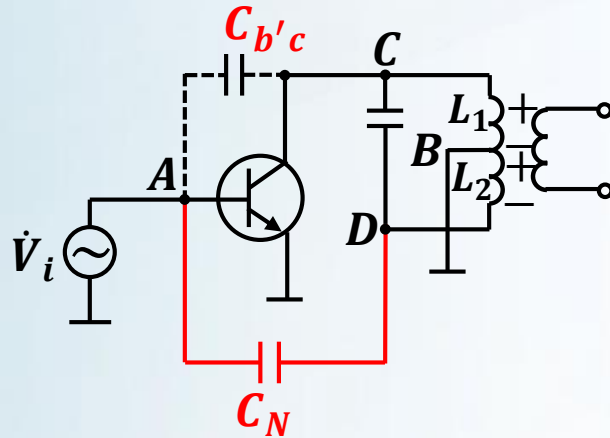
**Neutralization**

2

**Mismatch**

# (1) Neutralization:

- To add  $C_N$  to construct bridge



- Balanced Bridge,  $CD$  ( $\dot{V}_0$ ) does not feedback to  $AB$
- Balanced Bridge, impedance ratio are same

$$\therefore \frac{\omega L_1}{\omega L_2} = \frac{\frac{1}{j\omega C_{b'c}}}{\frac{1}{\omega C_N}} \Rightarrow C_N = \frac{L_1}{L_2} C_{b'c}$$

Output not affect input

## (2) Mismatch:

Gain↓ Stability↑

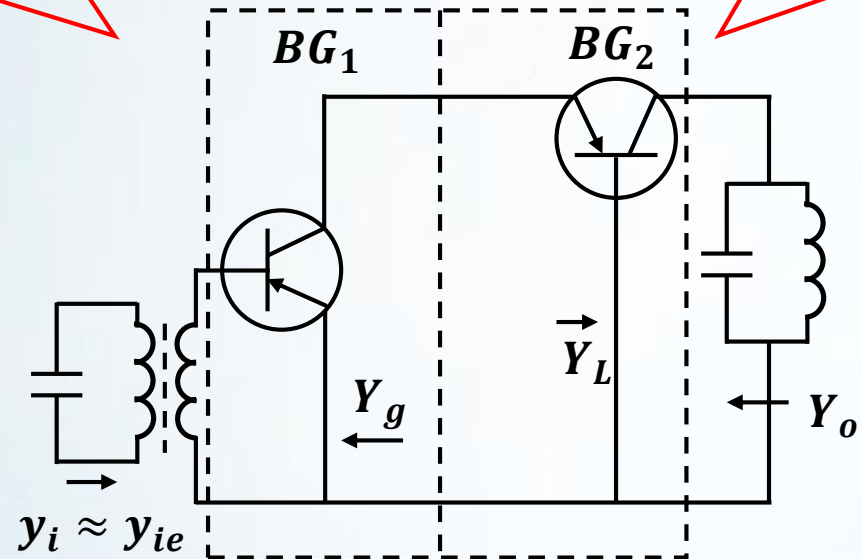
➤ Clue: Mismatch  $\Rightarrow$  Output  $\downarrow \Rightarrow$  Feedback  $\downarrow \Rightarrow$  Stable

Common Emitter

$r_{in} \uparrow ; r_{out} \uparrow$

Common Base

$r_{in} \downarrow ; r_{out} \uparrow$



Darlington



### (3) Comparisons

#### ➤ Neutralization

Pros: Simple, High Gain

Cons: ① not for wideband amplifier  
② not effective for changes of temperature  
③ not suitable for batch production

#### ➤ Mismatch

Pros: ① wideband amplifier  
② effective for changes of many factors  
③ suitable for batch production

Cons: gain ↓