

MTP 290-Problem Set 8
Numerical Integration

1. Use Simpson rule to evaluate

(a) $\int_0^{\pi/3} \cos^2 x \, dx.$

(b) Use your answer to part (a) to deduce an approximate value of integral $\int_0^{\pi/3} \sin^2 x \, dx.$

2. Use Simpson's rule with 5 ordinates to find an approximate value for the integral

$$\int_4^6 \frac{1}{3 - \sqrt{x}} \, dx.$$

3. Approximate the integral of $f(x)=x^3$ on the interval $[1,2]$ by using composite Simpson's method

(a) with four sub intervals,

(b) with eight sub intervals,

(Which approximation is much closer to the correct answer)

(c) Compute the true error in both the cases.

4. Using Trapezoidal Rule and Simpson's rule with $n=4$ to approximate the value of the following integral and compute the true errors and approximation errors

$$\int_0^2 e^{x^2} \, dx.$$

5. Evaluate the following integral by using one point Gauss quadrature and compute the true error.

$$\int_0^{\pi/2} x \sin x \, dx$$

6. Redo Problem 5 by using two point Gauss quadrature formula.