

### Contraste tratamento

$\theta_1 = 0$  para  $\theta = \alpha, \beta$ .

$$X = \begin{bmatrix} \mu & \alpha_1 & \alpha_2 & \alpha_3 & \beta_1 & \beta_2 & \gamma_{11} & \gamma_{21} & \gamma_{31} & \gamma_{12} & \gamma_{22} & \gamma_{32} \\ 1 & 1 & . & . & 1 & . & 1 & . & . & . & . & . \\ 1 & . & 1 & . & 1 & . & . & 1 & . & . & . & . \\ 1 & . & . & 1 & 1 & . & . & . & 1 & . & . & . \\ 1 & 1 & . & . & . & 1 & . & . & . & 1 & . & . \\ 1 & . & 1 & . & . & 1 & . & . & . & . & 1 & . \\ 1 & . & . & 1 & . & 1 & . & . & . & . & . & 1 \end{bmatrix} \Rightarrow X = \begin{bmatrix} \mu & \alpha_2 & \alpha_3 & \beta_2 & \gamma_{22} & \gamma_{32} \\ 1 & . & . & . & . & . \\ 1 & 1 & . & . & . & . \\ 1 & . & 1 & . & . & . \\ 1 & . & . & 1 & . & . \\ 1 & 1 & . & 1 & 1 & . \\ 1 & . & 1 & 1 & 1 & 1 \end{bmatrix}$$

$\underbrace{\hspace{1.5cm}}_{\alpha_1 = 0} \quad \underbrace{\hspace{1.5cm}}_{\beta_1 = 0} \quad \underbrace{\hspace{1.5cm}}_{X_\mu} \quad \underbrace{\hspace{1.5cm}}_{X_{\mu:\alpha}} \quad \underbrace{\hspace{1.5cm}}_{X_{\mu:\beta}} \quad \underbrace{\hspace{1.5cm}}_{X_{\mu:\gamma}}$

### Contraste soma zero

$\theta_k = -\sum_{i=1}^{k-1} \theta_i$  para  $\theta = \alpha, \beta$  e  $k$  é o número de níveis.

$$X = \begin{bmatrix} \mu & \alpha_1 & \alpha_2 & \alpha_3 & \beta_1 & \beta_2 & \gamma_{11} & \gamma_{21} & \gamma_{31} & \gamma_{12} & \gamma_{22} & \gamma_{32} \\ 1 & 1 & . & . & 1 & . & 1 & . & . & . & . & . \\ 1 & . & 1 & . & 1 & . & . & 1 & . & . & . & . \\ 1 & . & . & 1 & 1 & . & . & . & 1 & . & . & . \\ 1 & 1 & . & . & . & 1 & . & . & . & 1 & . & . \\ 1 & . & 1 & . & . & 1 & . & . & . & . & 1 & . \\ 1 & . & . & 1 & . & 1 & . & . & . & . & . & 1 \end{bmatrix} \Rightarrow X = \begin{bmatrix} \mu & \alpha_1 & \alpha_2 & \beta_1 & \gamma_{11} & \gamma_{21} \\ 1 & 1 & . & 1 & 1 & . \\ 1 & . & 1 & 1 & . & 1 \\ 1 & -1 & -1 & 1 & -1 & -1 \\ 1 & 1 & . & -1 & -1 & . \\ 1 & . & 1 & -1 & . & -1 \\ 1 & -1 & -1 & -1 & 1 & 1 \end{bmatrix}$$

$\underbrace{\hspace{1.5cm}}_{X_\mu} \quad \underbrace{\hspace{1.5cm}}_{X_{\mu:\alpha}} \quad \underbrace{\hspace{1.5cm}}_{X_{\mu:\beta}} \quad \underbrace{\hspace{1.5cm}}_{X_{\mu:\gamma}}$

$\underbrace{\hspace{1.5cm}}_{\beta_2 = -\beta_1} \quad \underbrace{\hspace{1.5cm}}_{\alpha_3 = -(\alpha_1 + \alpha_2)}$

### Contraste de Helmert

$(u-1)\theta_u = -\sum_{i=1}^{u-1} \theta_i$  para  $\theta = \alpha, \beta$  sendo  $u = 2, \dots, k$  e  $k$  é o número de níveis.

$$X = \begin{bmatrix} \mu & \alpha_1 & \alpha_2 & \alpha_3 & \beta_1 & \beta_2 & \gamma_{11} & \gamma_{21} & \gamma_{31} & \gamma_{12} & \gamma_{22} & \gamma_{32} \\ 1 & 1 & . & . & 1 & . & 1 & . & . & . & . & . \\ 1 & . & 1 & . & 1 & . & . & 1 & . & . & . & . \\ 1 & . & . & 1 & 1 & . & . & . & 1 & . & . & . \\ 1 & 1 & . & . & . & 1 & . & . & . & 1 & . & . \\ 1 & . & 1 & . & . & 1 & . & . & . & . & 1 & . \\ 1 & . & . & 1 & . & 1 & . & . & . & . & . & 1 \end{bmatrix} \Rightarrow X = \begin{bmatrix} \mu & \alpha_1 & \alpha_2 & \beta_1 & \gamma_{11} & \gamma_{21} \\ 1 & -1 & -1 & -1 & 1 & 1 \\ 1 & 1 & -1 & -1 & -1 & 1 \\ 1 & . & 2 & -1 & . & -2 \\ 1 & -1 & -1 & 1 & -1 & -1 \\ 1 & 1 & -1 & 1 & 1 & -1 \\ 1 & . & 2 & 1 & . & 2 \end{bmatrix}$$

$\underbrace{\hspace{1.5cm}}_{X_\mu} \quad \underbrace{\hspace{1.5cm}}_{X_{\mu:\alpha}} \quad \underbrace{\hspace{1.5cm}}_{X_{\mu:\beta}} \quad \underbrace{\hspace{1.5cm}}_{X_{\mu:\gamma}}$

$\underbrace{\hspace{1.5cm}}_{-\beta_1 = \beta_2} \quad \underbrace{\hspace{1.5cm}}_{-(\alpha_1 + \alpha_2) = 2\alpha_3} \quad \underbrace{\hspace{1.5cm}}_{-\alpha_1 = \alpha_2}$