

1) The domain of the function $f(x) = \sin^{-1} [2x^2 - 3] + \log_2 (\log_{1/2} (x^2 - 5x + 5))$ where $[t]$ is the greatest integer function, is :

- a) $\left(-\sqrt{\frac{5}{2}}, \frac{5-\sqrt{5}}{2}\right)$
- b) $\left(\frac{5-\sqrt{5}}{2}, \frac{5+\sqrt{5}}{2}\right)$
- c) $\left(1, \frac{5-\sqrt{5}}{2}\right)$
- d) $\left(1, \frac{5+\sqrt{5}}{2}\right)$

2) Let S be the set of all (α, β) , $\pi < \alpha, \beta < 2\pi$, for which the complex number $\frac{1-i \sin \alpha}{1-2i \cos \beta}$ is purely real. Let $Z_{\alpha\beta} = \sin 2\alpha + i \cos 2\beta$, $(\alpha, \beta) \in S$. Then $\sum_{(\alpha, \beta) \in S} \left(iZ_{\alpha\beta} + \frac{1}{iZ_{\alpha\beta}}\right)$ is equal to:

- a) 3
- b) $3i$
- c) 1
- d) $2 - i$

3) If α, β are the roots of the equation $x^2 - \left(5 + 3\sqrt{\log_3 5} - 5\sqrt{\log_5 3}\right) + 3\left(3^{(\log_3 5)^{\frac{1}{3}}} - 5^{(\log_5 3)^{\frac{2}{3}}} - 1\right) = 0$ then the equation, whose roots are $\alpha + \frac{1}{\beta}$ and $\beta + \frac{1}{\alpha}$,

- a) $3x^2 - 20x - 12$
- b) $3x^2 - 10x - 4$
- c) $3x^2 - 10x + 2$
- d) $3x^2 - 20x + 16$

4) Let $A = \begin{pmatrix} 4 & -2 \\ \alpha & \beta \end{pmatrix}$ If $A^2 + \gamma A + 18I = 0$, then $\det(A)$ is equal to

- a) -18
- b) 18
- c) -50
- d) 50

5) If for $p \neq q \neq 0$, the function $f(x) = \frac{\sqrt[7]{p(729+x)}-3}{\sqrt[3]{729+qx}-9}$ is continuous at $x=0$, then :

- a) $7pqf(0) - 1 = 0$
- b) $63qf(0) - p^2 = 0$
- c) $21qf(0) - p^2 = 0$
- d) $7pqf(0) - 9 = 0$

6) Let $f(x) = 2 + |x| - |x - 1| + |x + 1|$, $x \in \mathbf{R}$ Consider

$$(S1) : f'\left(-\frac{3}{2}\right) + f'\left(-\frac{1}{2}\right) + f'\left(\frac{1}{2}\right) + f'\left(\frac{3}{2}\right) = 2$$

$$(S2) : \int_{-2}^2 f(x) dx = 12 \text{ Then,}$$

- a) both (S1) and (S2) are correct
- b) both (S1) and (S2) are wrong
- c) only (S1) is correct
- d) only (S2) is correct

7) Let the sum of an infinite G.P. , whose first term is a and the common ratio is r , be 5. Let the sum of its first five terms be $\frac{98}{25}$. Then the sum of the first 21 terms of an AP, whose first term is $10ar$, n^{th} term is a_n and the common difference is $10ar^2$ is equal to :

- a) $21a_{11}$
- b) $22a_{11}$
- c) $15a_{16}$
- d) $14a_{16}$

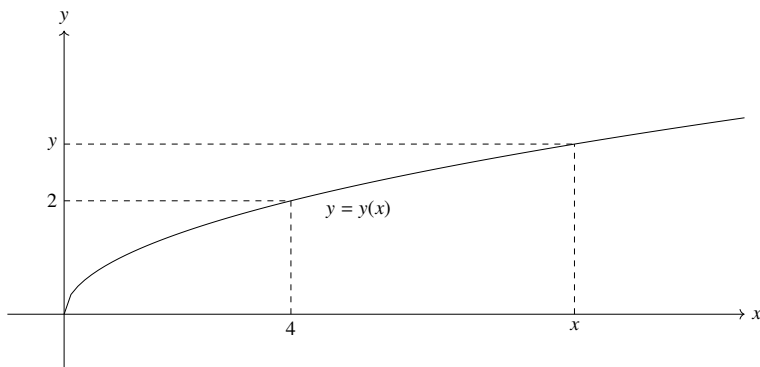
8) The area of the region enclosed by $y \leq 4x^2$, $x^2 \leq 9y$ and $y \leq 4$, is equal to :

- a) $\frac{40}{3}$
- b) $\frac{56}{3}$
- c) $\frac{112}{3}$
- d) $\frac{80}{3}$

9) $\int_0^2 \left([2x^2 - 3x] + \left[x - \frac{1}{2} \right] \right) dx$ where $[t]$ is the greatest integer function, is equal to :

- a) $\frac{7}{6}$
- b) $\frac{9}{12}$
- c) $\frac{31}{12}$
- d) $\frac{5}{2}$

10) Consider a curve $y = y(x)$ in the first quadrant as shown in the figure. Let the area A_1 is twice the area A_2 . Then the normal to the curve perpendicular to the line $2x - 12y = 15$ does **NOT** pass through the point.



- a) (6, 21)
- b) (8, 9)

- c) $(10, -4)$
 d) $(12, -15)$
- 11) The equation of the sides AB, BC and CA of a triangle ABC are $2x+y=0$, $x+py=39$ and $x-y=3$ respectively and $\mathbf{P}(2, 3)$ is its circumcentre. Then which of the following is NOT true:
- a) $(AC)^2 = 9p$
 b) $(AC)^2 + p^2 = 136$
 c) $32 < \text{area}(\triangle ABC) < 36$
 d) $34 < \text{area}(\triangle ABC) < 38$
- 12) A Circle C_1 passes through the origin \mathbf{O} and has diameter 4 on the positive x -axis. The line $y=2x$ gives a chord OA of a circle C_1 . Let C_2 be the circle with OA as a diameter. If the tangent to C_2 at the point \mathbf{A} meets the x -axis at \mathbf{P} and y -axis at \mathbf{Q} , then $QA : AP$ is equal to :
- a) $1 : 4$
 b) $1 : 5$
 c) $2 : 5$
 d) $1 : 3$
- 13) If the length of the latus rectum of a parabola, whose focus is (a, a) and the tangent at its vertex is $x+y=a$, is 16, then $|a|$ is equal to
- a) $2\sqrt{2}$
 b) $2\sqrt{3}$
 c) $4\sqrt{2}$
 d) 4
- 14) If the Length of the perpendicular drawn from the point $\mathbf{P}(a, 4, 2)$, $a > 0$ on the line $\frac{x+1}{2} = \frac{y-3}{3} = \frac{z-1}{-1}$ is $2\sqrt{6}$ units and $\mathbf{Q}(\alpha_1, \alpha_2, \alpha_3)$ is the image of the point \mathbf{P} in this line, then $a + \sum_{i=1}^3 \alpha_i$ is equal to :
- a) 7
 b) 8
 c) 12
 d) 14
- 15) If the line of intersection of the planes $ax+by=3$ and $ax+by+cz=0$, $a > 0$ makes an angle 30° with the plane $y-z+2=0$, then the direction cosines of the line are :
- a) $\frac{1}{\sqrt{2}}, \frac{1}{\sqrt{2}}, 0$
 b) $\frac{1}{\sqrt{2}}, -\frac{1}{\sqrt{2}}, 0$
 c) $\frac{1}{\sqrt{5}}, -\frac{2}{\sqrt{5}}, 0$
 d) $\frac{1}{2}, -\frac{\sqrt{3}}{2}, 0$