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EE24BTECH11058 - P.Shiny Diavajna

Question: Using vectors, prove that the points $\begin{pmatrix} 2 & -1 & 3 \end{pmatrix}$, $\begin{pmatrix} 3 & -5 & 1 \end{pmatrix}$ and $\begin{pmatrix} -1 & 11 & 9 \end{pmatrix}$ are collinear.

Solution:

Variable	Description
$\begin{pmatrix} 2 & -1 & 3 \end{pmatrix}$	Point A
$\begin{pmatrix} 3 & -5 & 1 \end{pmatrix}$	Point B
$(-1 \ 11 \ 9)$	Point C

TABLE 0: Variables Used

$$(B - A \quad C - A)^{\mathsf{T}} = \begin{pmatrix} 1 & -4 & -2 \\ -3 & 12 & 6 \end{pmatrix}$$

$$\xrightarrow{R_2 = R_2 + 3R_1} \begin{pmatrix} 1 & -4 & -2 \\ 0 & 0 & 0 \end{pmatrix}$$

rank = number of non-zero rows i.e. rank =1

therefore,

A, B, C are collinear.

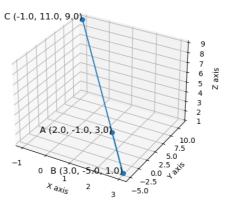


Fig. 0.1: Plot of points A,B and C