



University of Tehran  
College of Engineering  
School of Electrical and Computer  
Engineering (ECE)  
School of Mechanical Engineering  
(ME)



## **Mechatronics & Robotics**

**Homework 2:**  
Kinematic Modeling of Robotic Arms

***Teaching Assistants:***

Navid Razaghi  
Parsa Namazian

**Deadline: 8 April 2024 (20 Farvardin), 23:59**

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## Problem 1: Wrist Robot (20 points)

Consider the following 6-degree-of-freedom robot. The third joint is a prismatic joint.

- Find D-H parameters for this robot.
- According to the above part, find  $Q_i$  and  $\vec{a}_i$ .
- $P_W = \begin{bmatrix} x_w \\ y_w \\ z_w \end{bmatrix}$  is wrist point of the robot. Calculate it.

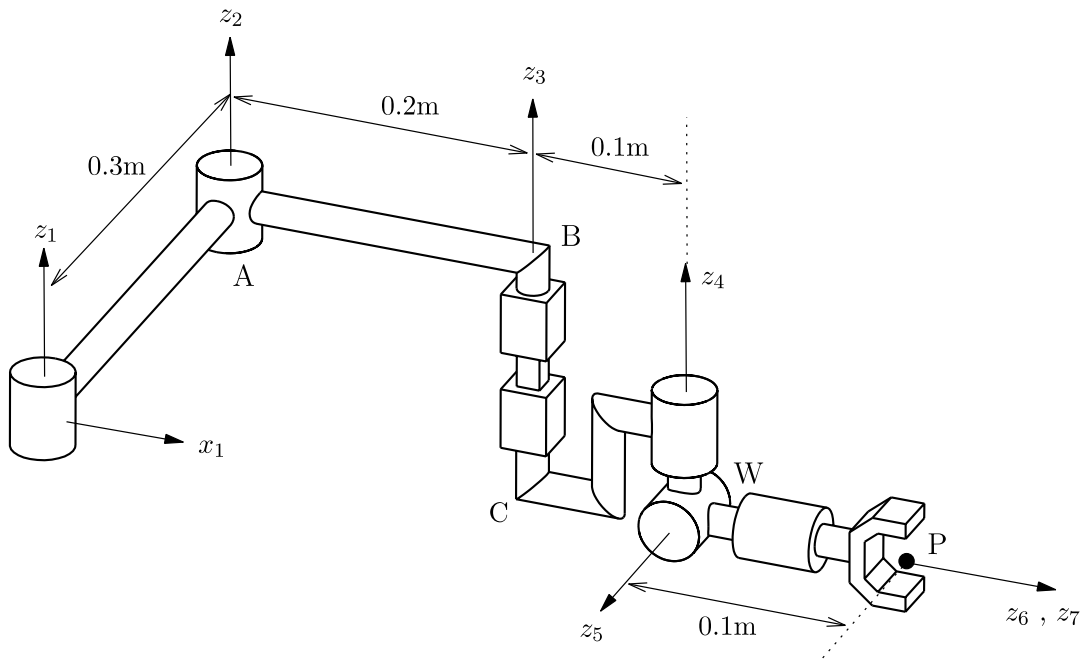


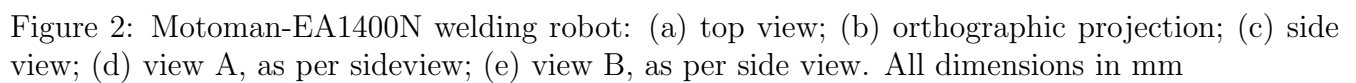
Figure 1: 6-DOF robot

**Problem 2: Motoman-EA1400N Welding Robot (20 points)**

The following figure is the data sheet of the Motoman-EA1400N welding robot.

- Under the assumption that the operation point of the robot is located along the axis of the 6th joint, on the flange indicated in view A, produce a table with Denavit-Hartenberg parameters of the robot.
- Is this robot decoupled?
- Form the FKP for this manipulator.

N.B.: All lengths are indicated in mm. It is strongly recommended to sketch the robot at an arbitrary posture in order to ease the definition of the DH coordinate frames.

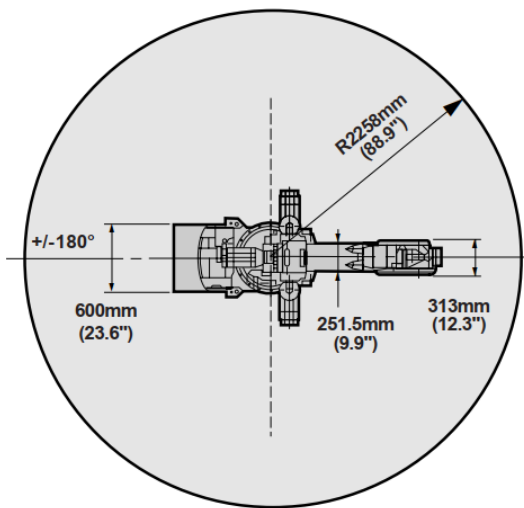


### Problem 3: FANUC S-420i (20 points)

The data sheet of FANUC robot known as S-420i is attached.

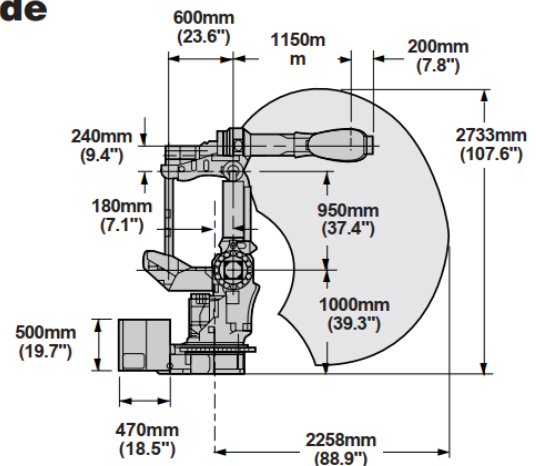
- According to the datasheet, form the DH parameters and solve the FKP.
- Is this robot decoupled? Solve the IKP for this manipulator. Find the number of answers to the IKP.
- Solve the FKP and IKP using MATLAB's Robotics Toolbox and verify your answers in the previous item. To verify them, given a sine wave profile to the actuators, solve the FKP using the equations and toolbox. The answers must be the same. Do it vice versa for the IKP.

# S-420*i* S Top



Top view

## Side



Side view

Figure 3: S420-i

### Problem 4: IKP (20 points)

Consider the following three-degree-of-freedom robot, where all axes of rotation are at an angle of 90 degrees.

- Find the table of D-H parameters by drawing the axes corresponding to each joint.
- According to the previous part, find the  $\vec{a}_i$  vectors and  $Q_i$  matrices related to each link.
- According to the previous part, obtain the forward kinematics problem.
- According to the above part, solve the inverse kinematics problem for  $\theta_1$  and  $\theta_3$  by referring to the two equations that are solved to obtain the value of these joints. (It means two equations in which there is no  $\theta_2$  term and it is possible to calculate the indicated values by forming a system of equations)

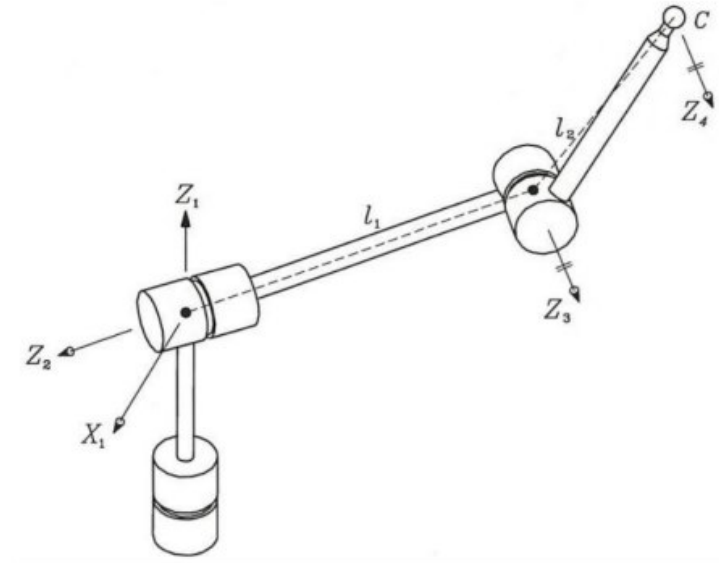


Figure 4: 3-DOF Robot

## Homework Guidelines and Instructions

- The deadline for sending this exercise will be until the end of Monday, April 8th.
- This time cannot be extended and you can use time grace if needed.
- The implementation must be in Python programming language and your codes must be executable and uploaded along with the report.
- This exercise is done by one person.
- If any similarity is observed in the work report or implementation codes, this will be considered as fraud for the parties.
- Using ready-made codes without mentioning the source and without changing them will constitute cheating and your practice score will be considered zero.
- If you do not follow the format of the work report, you will not be awarded the grade of the report.
- Handwritten exercise delivery is not acceptable.
- All pictures and tables used in the work report must have captions and numbers.
- A large part of your grade is related to the work report and problem solving process.
- Please upload the report, code file and other required attachments in the following format in the system: `HW1_[Lastname]_[StudentNumber].zip`  
For example, the: `HW1_Ezati_12345678.zip`
- If you have questions or doubts, you can contact the assistants through the following e-mail with the subject HW2-Mechatronics. Stay in touch educationally:
  - `Navid.Razaghi@ut.ac.ir` (Navid Razaghi)
  - `PNamazian@ut.ac.ir` (Parsa Namazian)
- Be happy and healthy