

*Dr. Shirin Glander*

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# ***Statistical Genetics: Analyses with R***

Here comes a dedication

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## *List of Figures*

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## ***Preface***

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Hi there, this is my great book.

---

### ***Why read this book***

It is very important...

---

### ***Structure of the book***

Chapters ?? introduces a new topic, and ...

---

### ***Software information and conventions***

I used the *knitr* package and the *bookdown* package to compile my book.  
My R session information is shown below:

```
sessionInfo()
```

```
## R version 3.4.0 (2017-04-21)
## Platform: x86_64-w64-mingw32/x64 (64-bit)
## Running under: Windows 7 x64 (build 7601) Service Pack 1
```

```
##  
## Matrix products: default  
##  
## locale:  
## [1] LC_COLLATE=English_United States.1252  
## [2] LC_CTYPE=English_United States.1252  
## [3] LC_MONETARY=English_United States.1252  
## [4] LC_NUMERIC=C  
## [5] LC_TIME=English_United States.1252  
##  
## attached base packages:  
## [1] stats      graphics  grDevices  utils      datasets  
## [6] methods    base  
##  
## loaded via a namespace (and not attached):  
## [1] compiler_3.4.0  backports_1.0.5 bookdown_0.3  
## [4] magrittr_1.5     rprojroot_1.2   tools_3.4.0  
## [7] htmltools_0.3.5 rstudioapi_0.6  yaml_2.1.14  
## [10] Rcpp_0.12.10     stringi_1.1.5   rmarkdown_1.5  
## [13] knitr_1.15.1     stringr_1.2.0   digest_0.6.12  
## [16] evaluate_0.10
```

Package names are in bold text (e.g., **rmarkdown**), and inline code and filenames are formatted in a typewriter font (e.g., `knitr::knit('foo.Rmd')`). Function names are followed by parentheses (e.g., `bookdown::render_book()`).

---

## Acknowledgments

A lot of people helped me when I was writing the book.

Frida Gomam  
on the Mars

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## ***About the Author***

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I am a bioinformatician at the University Hospital of Münster in Germany, where I'm responsible for Next Generation Sequencing analysis. I've earned my PhD from the University of Münster, where I worked on the link between flowering time and immune defense in plants using quantitative genetics and RNA-sequencing. My overarching interest has been evolutionary biology and genetics. At the moment, I am mainly working on questions relating to immunology - specifically inflammation, immune tolerance and auto-inflammatory diseases.

I'm a big fan of R and I write a blog<sup>1</sup> where I explore different data sets and techniques in R. I also teach ballroom and Latin dance courses.

You can find me and my package for gene expression analysis (exprAnalysis) on Github<sup>2</sup>.

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<sup>1</sup><https://shiring.github.io/>

<sup>2</sup><https://github.com/ShiringG>



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## ***The basics of R***

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- introduce the basics of R or at a minimum provide a set of resources that can be used to learning R prior to starting this book



# 1

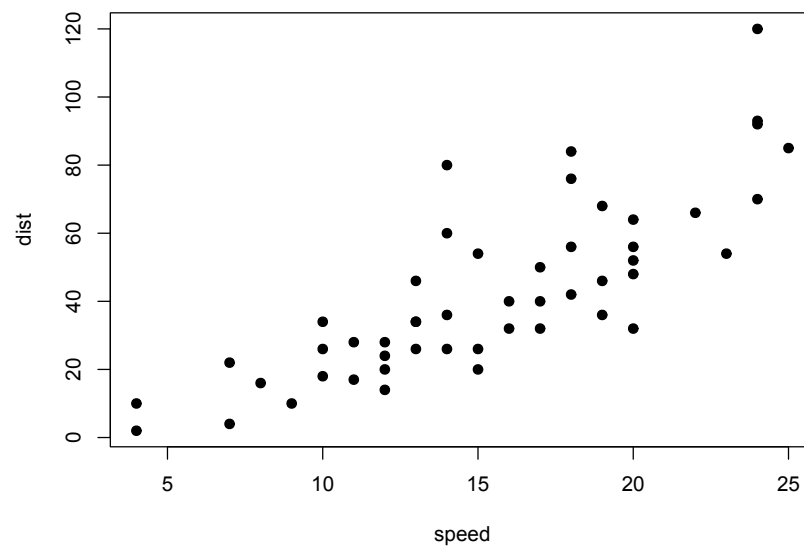
## *Introduction to Statistical Genetics*

Now unplug your Internet cable, and start doing some serious work.

We have a nice figure in Figure 1.1, and also a table in Table 1.1.

```
par(mar = c(4, 4, 1, .1))  
plot(cars, pch = 19)
```

```
knitr::kable(  
  head(iris), caption = 'The boring iris data.',  
  booktabs = TRUE  
)
```



**FIGURE 1.1:** Hello World!

**TABLE 1.1:** The boring iris data.

Sepal.Length	Sepal.Width	Petal.Length	Petal.Width	Species
5.1	3.5	1.4	0.2	setosa
4.9	3.0	1.4	0.2	setosa
4.7	3.2	1.3	0.2	setosa
4.6	3.1	1.5	0.2	setosa
5.0	3.6	1.4	0.2	setosa
5.4	3.9	1.7	0.4	setosa

More chapters to come in 02-foo.Rmd, 03-bar.Rmd, ...



## **2**

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### *Evolutionary Genetics*

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#### **2.1** *Evolution of genetic systems*

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#### **2.2** *Phylogenetics*

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#### **2.3** *Game Theory*

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#### **2.4** *Genetic Algorithms*

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#### **2.5** *Evolutionary Algorithms*



# 3

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## *Population Genetics*

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### **3.1** *Hardy-Weinberg*

---

### **3.2** *Linkage Disequilibrium*



# 4

## Quantitative Genetics

### 4.1 QTL analysis

Quantitative Trait Loci (QTL) are regions in the genome that are associated with variation in a quantitative trait. Quantitative traits are phenotypes that can be measured on a continuous scale, like height, weight, etc.

QTL analysis (or QTL mapping) is typically done on experimental populations to find genes which contribute to the heritability of traits. Phenotype and genetic marker data are collected from every individual in the population. The general concept of QTL mapping is that we can then calculate the correlation between genotypes and phenotypes at each marker position and test whether they show a statistically significant association.

Let's consider the famous example of [Doebley and Stec \(1991\)](#), who assessed the variation of traits that discriminate commercial maize from its native relative teosinte. Teosinte is much smaller than maize as we know it today and one teosinte plant produces many ears, each of which has only two rows of seeds. But even though maize and teosinte look so completely different, they are still able to produce viable offspring together. [Doebley and Stec \(1991\)](#) utilized this and crossed the two plant species to produce an F1 generation, which were in turn self-pollinated. The resulting F2 population of maize-teosinte-hybrids showed a wide range of intermediate parental morphologies. Each of the F2 offspring was then genotyped at 58 locations in the genome, so that the quantitative trait information on morphology could be correlated with the genetic map. This analysis revealed that most of the morphological variation between maize and teosinte were the result of changes in only a handful of genes, one of which is the *tb1* (*teosinte branched 1*) gene.

#### 4.1.1 Recombinant Inbred Lines (RILs)

RILs are experimental sister populations that have been produced by a very specific back-crossing scheme. The process is similar to Doebley and Stec's crossing of maize and teosinte: two homozygous parents are crossed to produce an F1 generation. Following the laws of genetics, each offspring's genome consists of a random combination of parental alleles and crossover (or recombination) events. Depending on the design, F1 offspring are usually either selfed or mated with a sibling to introduce another level of genetic recombination. The final generation is then inbred for many generations to obtain a collection of homozygous sister lines, each with a unique mosaic genome of parental alleles (Pollard, 2012).

#### 4.1.2 QTL analysis in R

##### 4.1.2.1 The “*qtl*” package

The best established R package for QTL mapping is Karl Broman's *qtl* package<sup>1</sup> (Broman et al., 2016). It implements several techniques for finding QTLs, like Hidden Markov Models (HMM), interval mapping, Haley-Knott regression and multiple imputation. It is very well documented and comes with extensive example data and code.

Here, I will introduce you to a basic QTL mapping workflow using the examples given in the package documentation and refer you to more complex analysis options where applicable.

##### 4.1.2.1.1 \*

#### Installation and loading the package

If this is the first time you are using the *qtl* package, you need to install it from CRAN. The following line of code checks whether you already have the package, and if not installs it.

---

<sup>1</sup><http://www.rqtl.org/>

```
pkg = "qtl"
if (system.file(package = pkg) == "") install.packages(pkg)
```

You can then load the package:

```
library(qtl)
```

#### 4.1.2.1.2 \*

#### Loading the data

I will be using the example data on murine hypertension that is provided in the package ([Sugiyama et al., 2001](#)). The **summary()** function shows you the main properties of the data:

```
data(hyper)
summary(hyper)
```

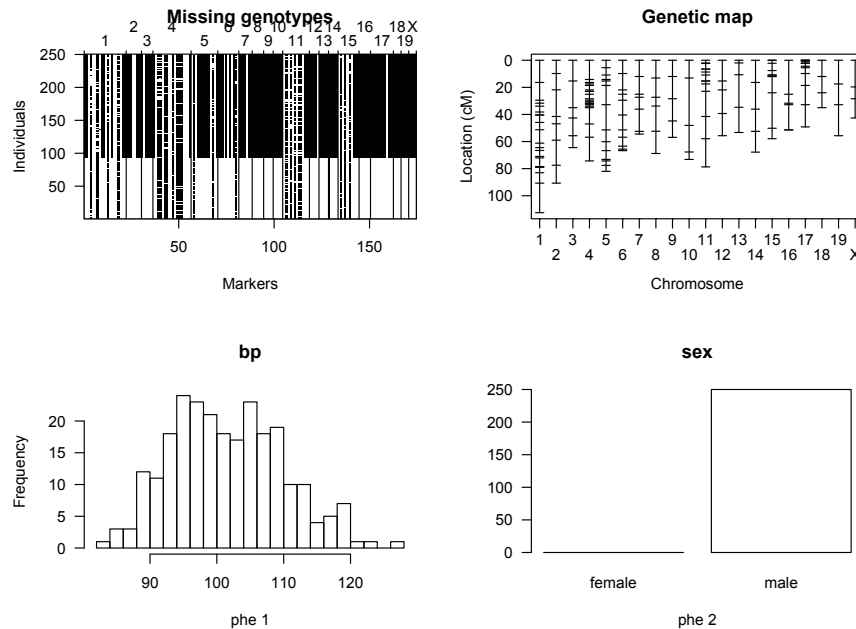
```
##      Backcross
##
##      No. individuals:    250
##
##      No. phenotypes:    2
##      Percent phenotyped: 100 100
##
##      No. chromosomes:   20
##      Autosomes:         1 2 3 4 5 6 7 8 9 10 11 12 13
##                        14 15 16 17 18 19
##      X chr:             X
##
##      Total markers:     174
##      No. markers:       22 8 6 20 14 11 7 6 5 5 14 5 5
##                        5 11 6 12 4 4 4
##      Percent genotyped: 47.7
##      Genotypes (%):
##      Autosomes:         BB:50.1  BA:49.9
```

```
##          X chromosome:      BY:53.0  AY:47.0
```

The **plot()** function produces plots showing missing genotypes, the marker positions and the distribution of phenotypes or traits. This will give you a first idea of your data.

The package manual<sup>2</sup> includes a description of various additional plotting functions, which I won't cover here. I also advise to examine each object with **head()** or **summary()** after you ran a function to get a feel for your data and the various steps you are taking in the analysis.

```
plot(hyper)
```



#### 4.1.2.1.3 \*

### Genetic map estimation

<sup>2</sup><http://www.rqtl.org/tutorials/rqtltour.pdf>



Before we proceed with the analysis, I typically recommend to replace the existing genetic map with an estimated one to reduce the potential errors. The genetic map represents all markers on a chromosome in a linear fashion. The `est.map()` function applies a Hidden Markov Model (Lander and Green, 1987) to estimate the map with an assumed genotyping error rate (`error.prob`).

Here, we can also specify the mapping function (`map.function`) that we want to use to convert genetic distance to recombination fraction. The distance between two markers is usually given as a unit of genetic linkage, called *centimorgan* (cM). One cM represents the distance with an average of 0.01 crossover events in one generation (i.e. 1% recombination). However, this representation of distance underestimates the actual recombination fraction, which is inherently not additive. With increasing distance the chance of double crossovers increases, so that they are in a way “invisible” to the traditional estimation of recombination distance.

Another reason why genetic maps based on recombination are biased is crossover interference, which describes the phenomenon that a crossover event reduces the likelihood of another recombination event occur close by.

To correct for such biases, we can choose from the following mapping functions:

- **Haldane’s** is the simplest mapping function and assumes a Poisson distribution for crossover events and does not consider interference.
- **Kosambi’s** mapping function also considers interference and double crossovers but it can not calculate joint recombination probabilities for more than three loci.
- **Carter-Falconer’s** mapping function can be extended to more complex interference rates.
- **Morgan’s** mapping function assumes complete interference.

The two most widely used mapping functions are Haldane’s (the default) and Kosambi’s. For this example, using Haldane’s should be sufficient. Because our example is a backcross, we can assume no interference, meaning that all crossovers are independent (Lynch and Walsh, 1998).

```
newmap <- est.map(hyper, error.prob = 0.0001, map.function = "haldane")
hyper <- replace.map(hyper, newmap)
```

We can now estimate the recombination fractions between all pairs of markers. The **est.rf()** function also calculates the LOD scores. LOD stands for “likelihood of the odds” and is a measure of linkage. In QTL mapping we calculate LOD scores for the genetic markers and a threshold, above which we consider a QTL statistically significant in its association with the trait.

```
hyper <- est.rf(hyper)
```

The **calc.errorlod()** function calculates the genotyping errors according to [Lincoln and Lander \(1992\)](#). We can see which markers have an error LOD above a certain threshold (cutoff) with the **top.errorlod()** function.

```
hyper <- calc.errorlod(hyper, error.prob = 0.0001)
te <- top.errorlod(hyper, cutoff = 3)
te
```

```
##   chr  id  marker errorlod
## 1   4 102 D4Mit288    3.325
## 2   4 107 D4Mit111    3.262
## 3   4 216 D4Mit214    3.261
## 4  11  57 D11Mit82    3.021
## 5  11 118 D11Mit82    3.021
```

```
hyper.clean <- hyper
for(i in 1:nrow(te)) {
  chr <- te$chr[i]
  id <- te$id[i]
  mar <- te$marker[i]
  hyper.clean$geno[[chr]]$data[hyper$pheno$id == id, mar] <- NA
}
```

### Finding QTLs

Now, we can proceed with the central step: mapping the QTLs.

Because the individuals in QTL studies are genotyped at specific marker locations throughout the genome, we inherently have to deal with the missing information about genotypes between markers. Hidden Markov Models (HMM) can help us overcome this problem by calculating genotype probabilities between markers based on the joint genotype distribution.

We first need to calculate these genotype probabilities using the ***calc.genoprob()*** function. We can define several parameters, like step size, the amount of error we want to allow for, the mapping function and step width. Here, we want to calculate genotype probabilities for every cM (step = 1), with a fixed step width and an error probability of 0.0001. As above, we are again using Haldane's mapping function.

```
hyper.clean <- calc.genoprob(hyper.clean, step = 1, error.prob = 0.0001, map.function = "haldane")
```

The simplest QTL model, we can run is single-QTL marker regression or interval mapping using the ***scanone()*** function.

These simple methods can give a good estimation of QTLs but they can also introduce bias, especially with multiple QTL in close proximity. More advanced mapping approaches, like Composite Interval Mapping (CIM) are discussed later on.

The first parameter we want to specify is the phenotype(s) and model (e.g. parametric or non-parametric) for mapping. Here, we want to use the first phenotype, i.e. the first column in our phenotype matrix, which follows a normal distribution. We can see the phenotype matrix by calling:

```
hyper.clean$pheno
```

Then, we need to specify the mapping algorithm we want to use. We can

choose from several options. Here, I will only present the practical implications for each method. For a full discussion of the mathematical principles, see [Lynch and Walsh \(1998\)](#).

- **Marker regression:** Marker regression is by far the simplest approach to QTL mapping. Here, we calculate the association between phenotype and genotype at each marker position independently.

Because it is so simple, marker regression is seldom recommended to use. With interval mapping, a phenotype  $\sim$  genotype association analysis is performed for each flanking marker pair independently. This improves the approximation and gives confidence regions around QTL.

- **EM (Expectation-Maximization) algorithm:** EM is usually applied to maximum likelihood (ML) analyses of mixed models. It is an iterative process of calculating conditional probabilities and updating the ML estimates. This process is repeated until the estimates converge ([Lander and Botstein, 1989](#)). If we have a reasonably dense marker map, the EM algorithm will converge on the global maximum.
- **(Extended) Haley-Knott regression:** Haley-Knott regression uses a simpler model than the EM algorithm ([Haley and Knott, 1992](#)). The extended Haley-Knott regression also considers variance is therefore gives improved approximations. Haley-Knott regression can give good approximations of the likelihood profiles for ML interval mapping but with more complex cases, it can be heavily biased.
- **Multiple imputation:** This method uses multiple rounds of imputing the unknown genotypes between markers and combines them into a final imputation model ([Sen and Churchill, 2001](#)). This allows us to perform a simple analysis of variance at each position in the genome. Multiple imputation needs much more computational power than simpler methods and will usually not outperform them with single-QTL models (it is much more advantageous with more complex multi-QTL models, however).

Here, I will show QTL mapping examples for the EM algorithm and for multiple imputation:

```
# EM algorithm
out.em <- scanone(hyper.clean, pheno.col = 1, model = "normal", method = "em")
```

The multiple imputation method requires the use of the *sim.geno()* function before we call the mapping function. It calculates the joint genotype distribution based on the available marker information and uses it to perform the imputation of missing genotypes. With the *n.draws* parameter, we define how many imputations will be run. The more imputations steps we run, the more precise the genotypes but with increasing cost of computational time and power.

```
hyper.clean <- sim.geno(hyper.clean, step = 1, n.draws = 100, error.prob = 0.0001, map.function = map.function)
out.imp <- scanone(hyper.clean, pheno.col = 1, model = "normal", method = "imp")
```

Now that we have a LOD score for each marker position, we want to know which positions are significantly associated with the phenotype. To determine this, we will use the *scanone()* function again, but this time we want to calculate the genome-wide LOD score threshold with a permutation test. Above this threshold we can consider a QTL to be statistically significant. Here, I am using a similar call as before, but I am specifying that we want to use 1000 permutations.

```
operm.imp <- scanone(hyper.clean, pheno.col = 1, model = "normal", method = "imp", n.perm = 1000)

## Doing permutation in batch mode ...
```

The *summary()* function will tell us our genome-wide LOD score threshold for a given significance value (here 0.05).

```
lod <- summary(operm.imp, alpha = 0.05)
lod
```

```
## LOD thresholds (1000 permutations)
##      lod
## 5% 2.28
```

And now we can also refine our QTL results by including the significance

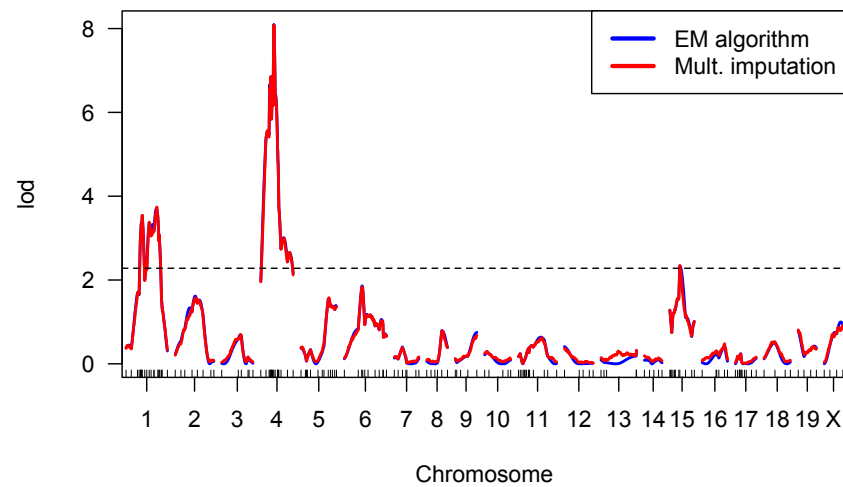
threshold. This will give us the LOD score and estimated p-values for each marker above the threshold, around which we can now assume to have found a QTL for our trait of interest.

```
summary(out.imp, perms = operm.imp, alpha = 0.05, pvalues = TRUE)
```

```
##           chr   pos   lod  pval
## c1.loc98    1 101.3 3.74 0.001
## D4Mit164    4  41.6 8.09 0.000
## D15Mit152   15  37.3 2.34 0.043
```

Now that we have our QTL, we can plot them with the *plot()* function. Here, I am plotting the results from both, the EM algorithm and the multiple imputation method. As expected, they do not differ much. The horizontal dotted line shows the genome-wide LOD threshold and our two significant QTL pop up nicely on chromosomes 1 and 4.

```
plot(out.em, col = "blue")
plot(out.imp, col = "red", add = TRUE)
abline(h = lod[1], lty = 2)
legend("topright", c("EM algorithm", "Mult. imputation"), col = c("blue", "red"), lty = 1, lwd
```



4.1.2.1.5 \*

QTL interaction mapping

4.1.2.1.6 \*

Covariates in QTL models

4.1.2.2 *QTL Analysis using Bayesian Interval Mapping ("qtlbim" package)*

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4.2 *Gene x Environment interactions*

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4.3 *Variance and heritability*





# 5

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## *Genetics of complex diseases*

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### **5.1 Genome Wide Association Studies (GWAS)**

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### **5.2 Pedigree analysis**



# 6

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## *Genetic Epidemiology*

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### **6.1** *Infection models*



# A

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## *More to Say*

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Yeah! I have finished my book, but I have more to say about some topics.  
Let me explain them in this appendix.

To know more about **bookdown**, see <https://bookdown.org>.



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## ***Bibliography***

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