

$$(tg(\frac{1}{x}))' = \frac{1}{(\cos(\frac{1}{x}))^2} \cdot \frac{((-1) \cdot 1)}{x^2}$$