Module-5

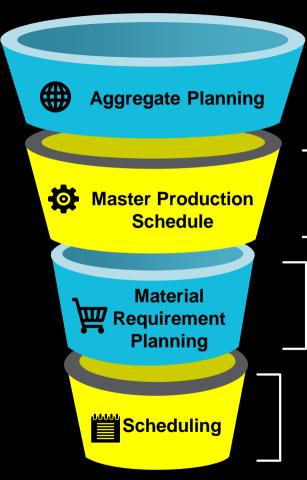
Production Scheduling and Sequencing





- 5.1 Scheduling: Inputs for scheduling, loading and scheduling devices, factors influencing scheduling, scheduling techniques, use of Gantt Charts and basic scheduling problems. Project scheduling by using elements of network analysis –PERT & CPM, cost analysis & crashing, resource leveling
- **5.2 Sequencing:** Product sequencing, dispatching, progress report & expediting and control. Johnson's Rule for optimal sequence of N jobs on 2 machine. Process n Jobs on 3 Machines (n/3 problem) and Jackson Algorithm. Processing of 2 Jobs on m Machine (2/m) problem





Keeping in view the estimated future demand of the final product, aggregate planning is done for long time horizon usually for 1-3 years.

Long term plan is broken down in master production schedules for shorter time period comprising of the complete information about the quantity and time of different products to be produced.

On the basis of Master production schedule, demand for the raw material, components etc (known as secondary demand) are estimated under the material requirement planning system.

Finally, very short term schedules are prepared which establish both the timing and the use of resources within a firm.





- Inputs for scheduling
- Loading and scheduling devices
- Factors influencing scheduling
- Scheduling techniques
- Use of Gantt Charts
- Basic scheduling problems.
- Project scheduling by using elements of network analysis
 - PERT & CPM
 - Cost analysis & crashing
 - Resource leveling





- Scheduling process involves the decision making regarding the allocation of available capacity or resources. Thus, the process can be called as time-phased plans or schedule of activities.
- Scheduling is concerned with preparation of machine loads and fixation of starting and completion dates for each of the operations. Machines have to be loaded according to their capability of performing the given task and according to their capacity. Thus the duties include:
 - Loading, the machines as per their capability and capacity.
 - Determining the start and completion times for each operation.
 - To coordinate with sales department regarding delivery schedules.
- Detailed scheduling determines start times, finish times and work assignments for all jobs at each work centre. Calendar times are specified when job orders, employees, and materials (inputs), as well as job completion (outputs), should occur at each work centre. By estimating how long each job will take to complete and when it is due, schedulers can establish start and finish dates and develop the detailed schedule.





- The production-schedules are developed by performing the following functions:
 - Loading
 - Sequencing
 - Scheduling
- A production schedule is the time table that specifies the times at which the jobs in a production department will be processed on various machines.
- The schedule gives the starting and ending times of each job on the machines on which the job has to be processed.
- Last stage of planning before production occurs.





- Meet customer due dates
- Minimize job lateness
- Minimize response time
- Minimize completion time
- Minimize time in the system
- Minimize overtime
- Maximize machine or labor utilization
- Minimize idle time
- Minimize work-in-process inventory





- Process Industry
 - Linear programming
 - EOQ with non-instantaneous replenishment
- Mass Production
 - Assembly line balancing
- Project
 - Project –scheduling techniques (PERT, CPM)
- Batch Production
 - Aggregate planning
 - Master scheduling
 - Material requirements planning (MRP)
 - Capacity requirements planning (CRP)





- 1. Bill of Material (BOM) & Blue prints (Drawings) shows kind of item required and detailed work to be carried out.
- 2. Master Production Schedule (MPS) shows priority and quantity of finished products, due dates, quantity of raw materials
- 3. Route sheet shows operations and machines to be scheduled and processing times
- 4. Inventory Records shows availability of materials & tools and time required for procurement of items not in stock.
- 5. Machine-Load chart shows the quantity of work already scheduled on various machines and the amount of spare (remaining) capacity available for use.





- Machine loading is the process of converting operation schedule into practices in conjunctions with routing.
- This process is assigning specific jobs to machines, men, or work centers based on relative priorities and capacity utilization.
- Loading ensures maximum possible utilization of productive facilities and avoid bottleneck in production.
- It's important to either overloading or under loading the facilities, work centers or machines to ensure maximum utilization of resources.





- Loading devices
 - Machine load chart
- Scheduling devices
 - Gantt charts
 - Milestone chart
 - Progress chart
 - Networks
 - Earned values
 - Line of balance



Factors influencing scheduling

External Factors

- 1. Customers demand
- 2. Customers delivery dates
- 3. Stock of goods already lying with the dealers & retailers.

Internal Factors

- 1. Stock of finished good with firm
- 2. Time interval to manufacture each component, subassembly and then assembly.
- 3. Availability of equipments & machinery their capacity & specification.
- 4. Availability of materials
- 5. Availability of manpower
- 6. Manufacturing facilities Power, MH devices, work-bench area
- 7. Feasibility of economic production run EOQ



Scheduling Approaches

There are mainly two types of approaches which are commonly used:

- 1. Forward scheduling: In forward scheduling, the scheduler schedules all activities forward in time.
 - (a) Jobs are given earliest available time slot in operation;
 - (b) Usually excessive WIP results.
- 2. Backward scheduling: In backward scheduling, the scheduler begins with a planned date and moves backward in time.
 - (a) Start with due date and work backward through operations reviewing lead times;
 - (b) Less WIP but must have accurate lead time.





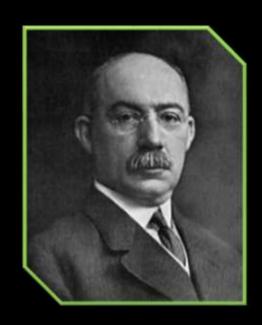
- Graphs-
 - Gantt Chart Job shop
 Job shop
- Diagram-
 - Network diagram
 - CPM
 - PERT

PROJECTS



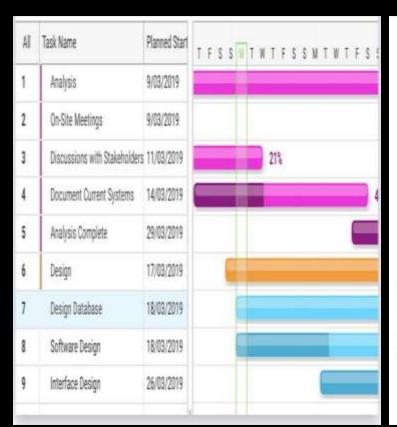


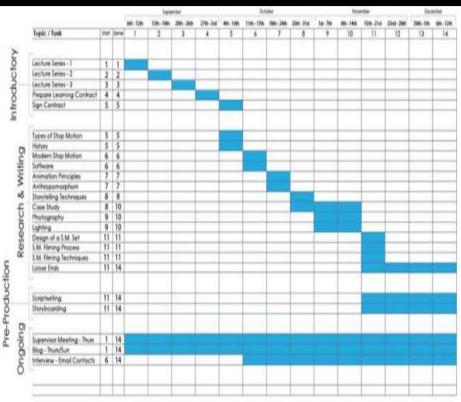
- A Gantt chart is a type of bar chart that illustrates a project schedule, named after its inventor, Henry Gantt
- This chart lists the tasks to be performed on the vertical axis, and time intervals on the horizontal axis
- The Gantt progress chart graphically displays the current status of each job or activity relative to its scheduled completion date
- To illustrate the relationship between project activities & time
- To show the multiple project activities on one chart
- To provide a simple & easy to understand representation of project scheduling





Gantt Charts - sample







Steps to Creating a Gantt Chart

- 1. Determine Project start date and deadline
- 2. Gather all information surrounding the list of activities within a project the Work Breakdown Structure may be useful for this
- 3. Determine how long each activity will take
- 4. Evaluate what activities are dependant on others
- 5. Create Graph shell including the timeline and list of activities
- 6. Using either Forward Scheduling or Backward Scheduling Begin to add bars ensuring to include dependencies and the full duration for each activity



Gantt Chart- Example

Consider a project on market survey of households. Do the following for this project-

- a) Enumerate all the activities
- b) Write down the logical sequence of the activities (in terms of immediate predecessors).
- c) Get the estimate for the time required by each activity.
- d) Draw Gantt chart.





Activity	Description	Immed iate Predec essor	ion
А	Plan Survey	-	3
В	Hire Personnel	A	5
С	Design Questionnaire	A	10
D	Train Personnel	В	7
E	Select Household	C,D	4
F	Print Questionnaire	С	5
G	Conduct Survey	E,F	15
н	Analyze Results	G	5

Time Activities	5	i 10	15	5 20	25	30	35	5 40
Plan Survey								
Hire Personnel								
Design Questionnaire								
Train Personnel								
Select Household								
Print Questionnaire								
Conduct Survey								
Analyze Results								



Advantages of Gantt Chart

- A useful tool for displaying time-based information within a project
- Very simple to create
- They provide a useful overview of project activities, a good starting point for project planning
- The charts are widely used and understood
- There exists several PC software packages that allow you to build Gantt Charts





Limitations of Gantt Chart

- It does not help identifying the key activities which are important for project completion in time.
- It does not permit identification of important stages in the completion of the project.
- The time (duration) estimates of the activities are made well in advance, and therefore, are likely to involve considerable amount of uncertainty. But uncertainties cannot be taken into account in scheduling activities using a Gantt chart.
- Utility of this chart becomes limited, especially in projects having a large number of activities.
- The Gantt Chart does not explain the reasoning behind the chosen duration of each activity
- The Gantt Chart is very difficult to update when changes to the project plan take place. This
 makes it time consuming and results in long-term planning being very difficult
- Gantt Charts encourage a one-step approach to planning this prevents flexibility in project planning
- As Gantt Charts are difficult to update manually, they can often become obsolete
- The charts do not consider project costs or resources.





Basic scheduling problems

- Bar Chart
- Network analysis consisting of three different closely resembling methods. namely:
 - Precedence diagram method (PDM)
 - Critical Path Method (CPM)
 - Program evaluation and review technique (PERT)
- Line of Balance (LOB)



Project

What is a project?

Project is an interrelated set of activities that has a definite starting and ending point resulting in to an unique product. Few examples of project are-

- Constructing a bridge, dam, highway or building
- Producing an aero plane, missile or rocket
- Introducing a new product
- Installation of a large computer system
- Construction of a ship
- Maintenance of major equipment/plant
- Commissioning of a power plant
- Conducting national election



Steps in Project scheduling

Managing a project (regardless of its size and complexity) requires identifying every activity to be undertaken and planning- when each activity must begin and end in order to complete the overall project in time. Typically all projects involve the following steps:

- Description of the project
- Development of network diagram
- Insertion of time of starting/ending of each activity
- Analysis of the network diagram.
- Development of the project plan
- Exception of the project
- Periodically assessment of the progress of project



Project scheduling

- Network analysis
 - CPM Critical Path Method
 - PERT Program Evaluation & Review Technique
- Crashing

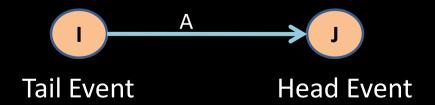


Terminologies used in network diagram

Activity: An activity means work/job. it is a time consuming process. it is represented by an arrow (→) in the network diagram as Tail → head



 Event: An event is a specific instant of time → marks the "start" and "end" of an activity



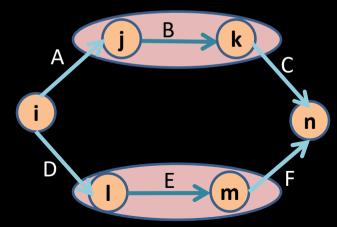


- Duration (d): Duration is the estimated or actual time required to complete a task or an activity.
- **Predecessor activity**: Activities that must be completed immediately prior to the start of another activity are called predecessor activities.
- Successor activity: Activities that cannot be started until one or more of other activities are completed but immediately succeed them are called successor activities.
- **Dummy activity**: An activity which does not consume any resource but merely depicts the dependence of one activity on other is called dummy activity. It is introduced in a network when two or more parallel activities have the same start and finish nodes. Shown by dotted arrow line.

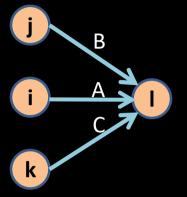
Serial activities flow from one to the next



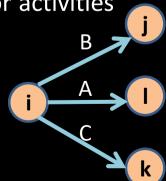
Concurrent activities are accomplished together.



Merge activities have two or more immediate predecessor



Burst activities have two or more successor activities





- Total project time: Time to complete the project. In other words, it is the duration of critical path.
- Earliest start time (ESi): It is the earliest possible time at which an activity can start. it is calculated by moving from 1st to last event in the network diagram.
- Latest start time (LS): It is the latest possible time by which an activity can start.
- Earliest finish time (EFj): It is the earliest possible time at which an activity can finished/end.
- Latest finish time (LFi): It is the last event time of the head event. It is calculated by moving backward in the network diagram.
- Float/slack: Slack is with reference to an event. Float is with reference to an activity.
- Total float: (Latest finish time- Earliest start time) Activity duration
- Free float: (Earliest finish time- Earliest start time) Activity duration.
- **Critical path**: the longest possible continuous pathway taken from the initial event to the terminal event. It determines the total calendar time required for the project; and, therefore, any time delays along the critical path will delay the reaching of the terminal event by at least the same amount.
- *Critical activity*: An activity that has total float equal to zero. An activity with zero float is not necessarily on the critical path since its path may not be the longest.

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Float/Slack



- It may be observed that for every critical activity in a network, the earliest start and latest start time are the same.
- This is so since the critical activities cannot be scheduled later than their earliest schedule time without delaying the total project duration, they do not have any flexibility in scheduling.
- Since there exists only one path through the network that is the longest i.e critical path, the other paths must either be equal or shorter.
- However, non-critical activities do have some flexibility i.e. these activities can be delayed for some time without affecting the project duration.
- Therefore, there are activities that can be completed before the time when they are actually needed.
- The time between the scheduled completion date and the required date to meet critical path is referred as the slack/float time.
- The activities on the critical path have zero slack/float time, i.e. any delay in these activities will delay the project completion.

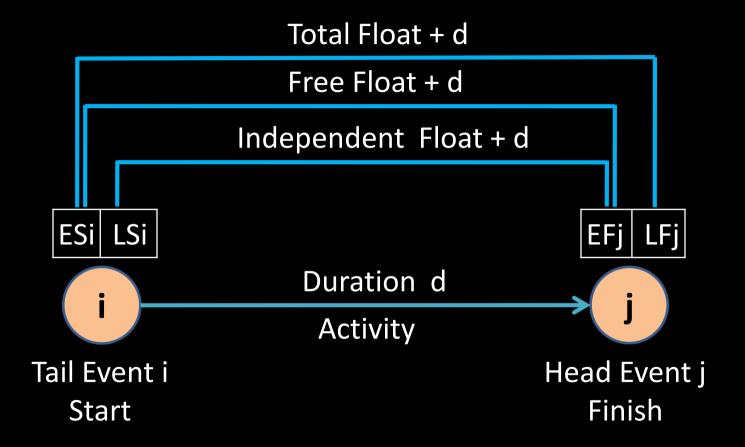


- Float or Slack = (Time available for completion of activity) - (Time necessary to complete the same) = (LST - EST) or (LFT - EFT)
- This flexibility is termed as slack in case of an event and as float in case of an activity
- Slack is used with PERT and Float is used with CPM
- The terms "slack" and "float" are often used interchangeably. However, the essential difference between the terms is that slack is typically associated with inactivity, while float is associated with activity. Slack time allows an activity to start later than originally planned, while float time allows an activity to take longer than originally planned.
- The activities on the critical path have zero slack/float time, i.e. any delay in these activities will delay the project completion.
- > The use of slack/float time provides better resource scheduling.
- It is also used as warning sign i.e. if available slack begins to decrease then activity is taking longer than anticipated.



- Positive slack would indicate ahead of schedule; negative slack would indicate behind schedule; and zero slack would indicate on schedule.
- Thus, the difference between the length of a given path and the length of the critical path is known as slack/float. Knowing where slack/float is located helps managers to prioritize allocation of scarce resources and direct their efforts to control activities.
- Hence , *float* or *slack* is a measure of the excess time and resources available to complete a task.
- It is the amount of time that a project task can be delayed without causing a delay in any subsequent tasks (*free float*) or the whole project (*total float*).
- Independent Float: It is the amount of time by which the start of an activity can be delayed without affecting earliest start time of an immediate following activities assuming that the preceding activity has finished at its latest finish time.
 - = (EST of head event LST of tail event) Activity duration.

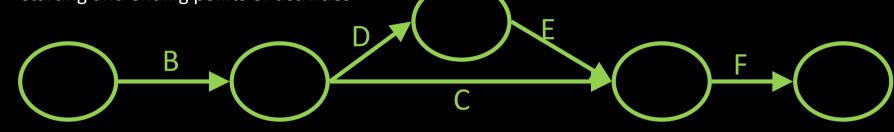




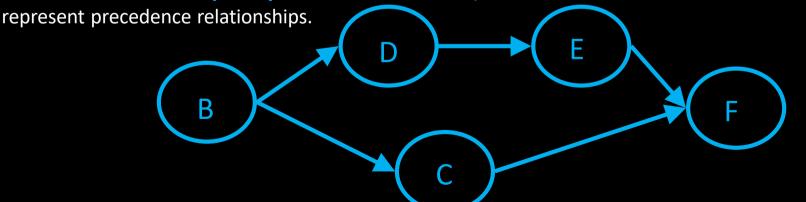




Activities On Arc (AOA)- Arrows are used to represent activities or tasks. Nodes represent starting and ending points of activities



Activities On Node (AON)- Nodes are used to represent activities or tasks, while arrows



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- Forward pass determines the earliest times (ES- Early Start) each activity can begin and the earliest it can be completed (EF- Early Finish).
- > There are three steps for applying the forward pass:
 - Add all activity times along each path as we move through the network (ES + d = EF)
 - ➤ Carry the EF time to the activity nodes immediately succeeding the recently completed node. That EF becomes the ES of the next node, unless the succeeding node is a merge point
 - At a merge point, the largest preceding EF becomes the ES for that node (because the earliest the successor can begin is when all preceding activities have been completed)





- ➤ The goal of the backward pass is to determine each activity's Late Start (LS) and Late Finish (LF) times.
- There are three steps for applying the backward pass:
 - \triangleright Subtract activity times along each path through the network (LF d = LS).
 - ➤ Carry back the LS time to the activity nodes immediately preceding the successor node. That LS becomes the LF of the next node, unless the preceding node is a burst point.
 - ➤ In the case of a burst point, the smallest succeeding LS becomes the LF for that node (because the latest the predecessor can finish is when any one of the successor activities should start)

Project scheduling - network analysis

Guidelines for Network Construction-

- The network should have a unique starting node (tail event) and unique completion node (head event).
- No activity should be represented by more than one arrow (→) in the network.
- No two activities should have the same starting node and same ending node.
- The flow of the diagram should be from left to right.
- Dummy activity is an imaginary activity indicating precedence relationship only. duration of dummy activity is zero.
- The length of arrow bear no relationship to activity time.
- The arrow in a network identifies the logical condition of dependence.
- The direction of arrow indicates the direction of work flow.

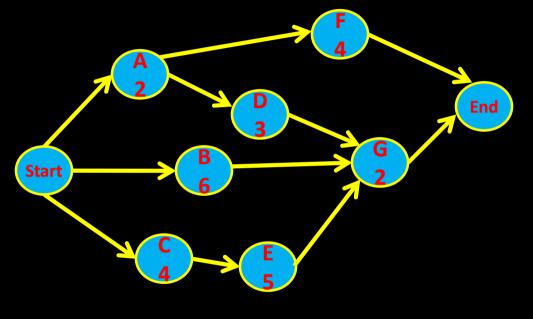
- All networks are constructed logically or based on the principal of dependency.
- No event can be reached in a project before the completion of precedence activity.
- Every activity in the network should be completed to reach the objective.
- No set of activities should form a circular loop.
 Arrows should not be crossed unless it is completely unavoidable.
- Arrows should be kept straight & not curved or bent.
- Angle between arrows should as large as possible.
- Each activity must have a tail or head event...
- Once the diagram is complete the nodes should be numbered from left to right. It should then be possible to address each activity uniquely by its tail & head event.

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Example- AON

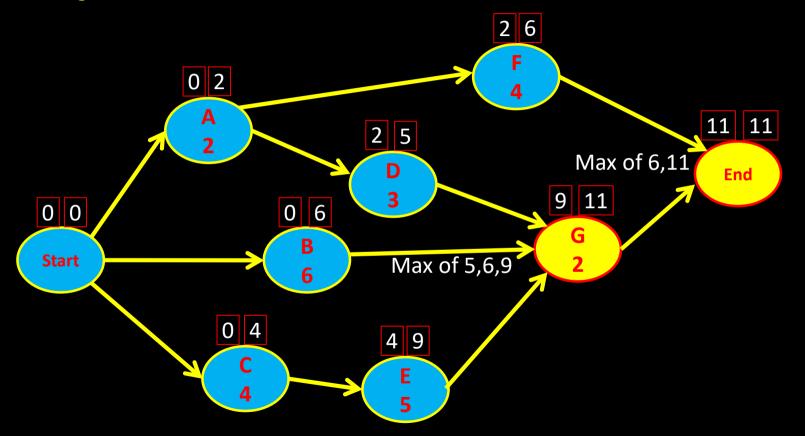


Activity	Predecessor	Duration
Α	-	2
В	-	6
С	-	4
D	А	3
Е	С	5
F	А	4
G	B,D,E	2



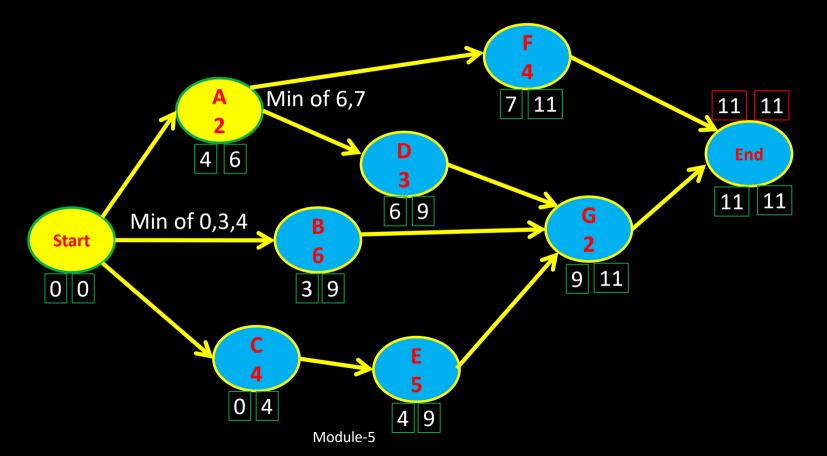






Example- Backward Pass

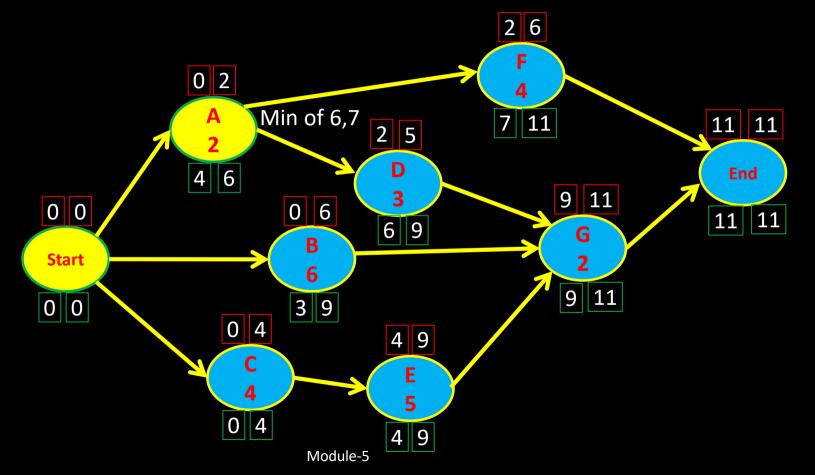




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Example-Summary





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EST = Earliest start time

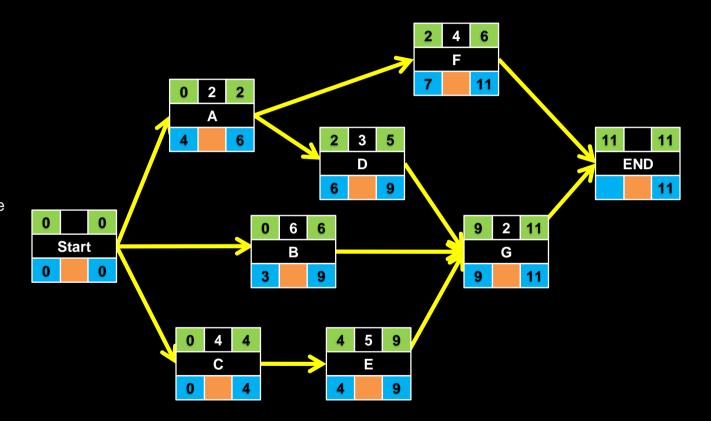
EFT = Earliest finish time

LST = Latest start time

LFT = Latest finish time

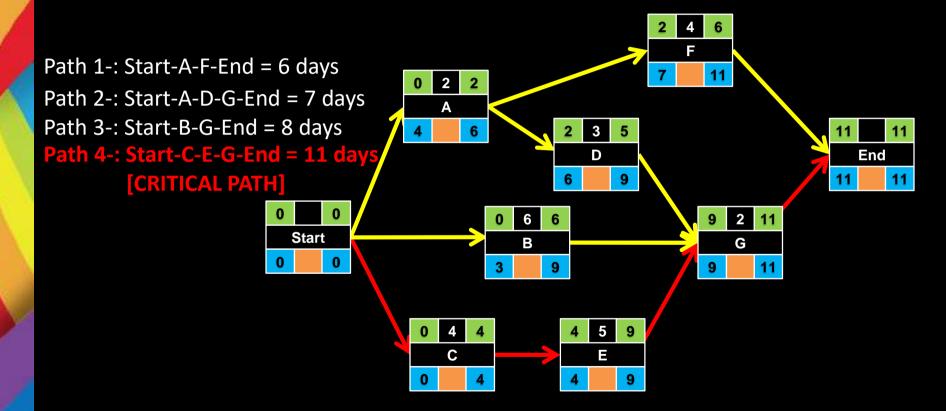
DR = Duration

TF = Total Float













Always slack is calculated for AON network

Activity	Duration	EST	EFT	LST	LFT	SLACK (ST-ST or FT-FT)
А	2	0	2	4	6	4
В	6	0	6	3	9	3
С	4	0	4	0	4	0
D	3	2	5	6	9	4
Е	5	4	9	4	9	0
F	4	2	6	7	11	5
G	2	9	11	9	11	0



Example- AOA

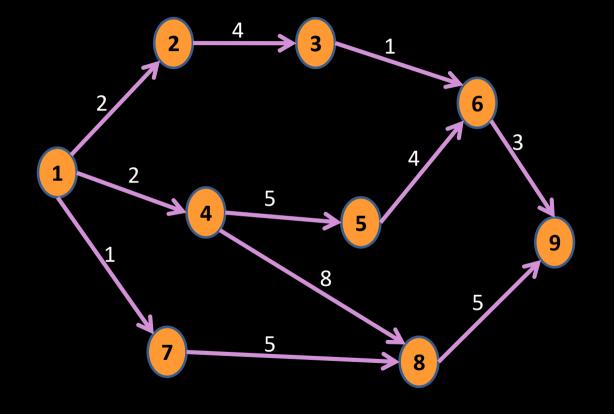
A project schedule has the characteristics shown in table. Construct the network and locate the critical path. Calculate the various time estimates and floats.

Activity	Duration
1-2	2
1-4	2
1-7	1
2-3	4
3-6	1
4-5	5
4-8	8
5-6	4
6-9	3
7-8	5
8-9	5





Activity	Duration
1-2	2
1-4	2
1-7	1
2-3	4
3-6	1
4-5	5
4-8	8
5-6	4
6-9	3
7-8	5
8-9	5



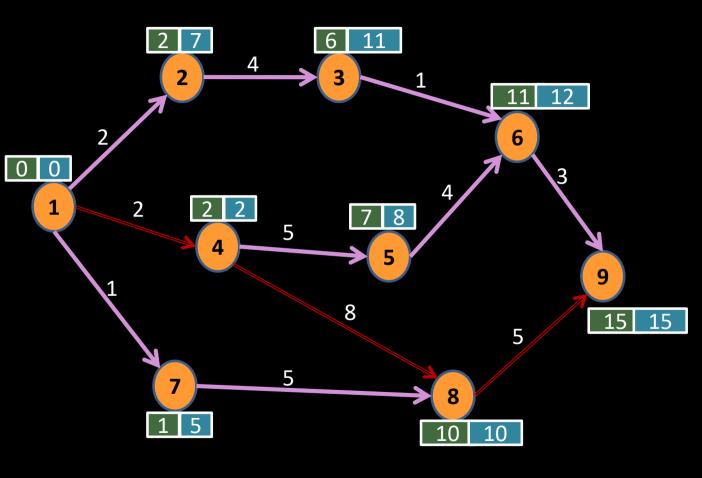


Earliestand Latesttimecalculation

Critical path –

1-4-8-9

ProjectDuration=15 days



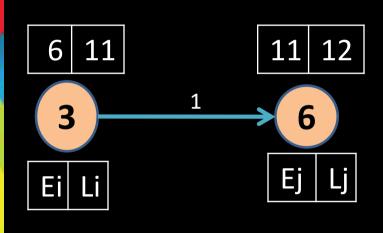


Activity	Duration	EST	EFT (EST+ Du)	LST (LFT-Du)	LFT	Total float	Free float FF	Independent float
1-2	2	0	2	5	7	5	0	0
1-4	2	0	2	0	2	0	0	0
1-7	1	0	1	4	5	4	0	0
2-3	4	2	6	7	11	5	0	-5
3-6	1	6	7	11	12	5	4	-1
4-5	5	2	7	3	8	1	0	-1
4-8	8	2	10	2	10	0	0	0
5-6	4	7	11	8	12	1	0	-1
6-9	3	11	14	12	15	1	1	0
7-8	5	1	6	5	10	4	4	0
8-9	5	10	15	10	15	0	0	0



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- Total Float = (Lj-Ei)-Dij = (12-6)-1= 5
- Free Float = (Ej-Ei)- Dij= (11-6)-1 = 4
- Independent Float = (Ej-Li)-Dij= (11-11)-1 = -1

Advantages of CPM



- It shows the graphical view of the project.
- It discovers and makes dependencies visible.
- It helps in project planning, scheduling, and controlling.
- It helps in contingency planning.
- It shows the critical path, and identifies critical activities requiring special attention.
- It helps you assign the float to activities and flexibility to float activities.
- It shows you where you need to take action to bring project back on track.
- To shorten the planned critical path of a project by:
 - Pruning (Trimming and cutting) critical path activities
 - "Fast tracking" (To do more things in the same time in order to finish a job earlier than normal or planned.)
 - "Crashing the critical path" (Shortening the durations of critical path activities by adding resources).





- Because the critical path method is an optimal planning tool, it always assumes that all resources are available for the project at all times.
- It does not consider resource dependencies.
- There are chances of misusing float or slack.
- Less attention on non-critical activities, though sometimes they may also become critical activities.
- Projects based on the critical path often fail to be completed within the approved time duration.





PERT planning involves the following steps:

- 1. Identify the specific activities and milestones.
- 2. Determine the proper sequence of the activities.
- 3. Construct a network diagram.
- 4. Estimate the time required for each activity.
- 5. Determine the critical path.
- 6. Update the PERT chart as the project progresses.





- Optimistic time: The minimum possible time required to accomplish an activity (to) or a path (O), assuming everything proceeds better than is normally expected
- *Pessimistic time*: The maximum possible time required to accomplish an activity (tp) or a path (P), assuming everything goes wrong (but excluding major catastrophes).
- Most likely time: The best estimate of the time required to accomplish an activity (tm) or a path (M), assuming everything proceeds as normal.
- Expected time: The best estimate of the time required to accomplish an activity (te) or a path (TE), accounting for the fact that things don't always proceed as normal (the implication being that the expected time is the average time the task would require if the task were repeated on a number of occasions over an extended period of time.

$$te=(to+4tm+tp)\div6$$

PERT- Probability to complete project

 In order to find out the project duration, the expected task time for each activity is to be determined using the formula

$$te = to + 4tm + tp$$

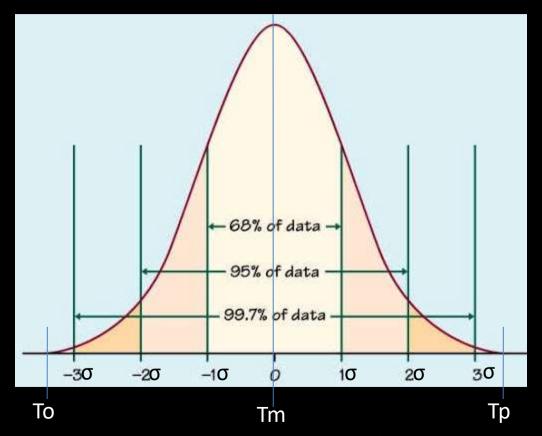
In order to find out the probability of completion in a given day, standard deviation (σ) for the critical path is to be determined using the formula $\sigma^2 = \frac{1}{2} \left[\frac{1}{2} \right]^2$

We assume that the distribution for the total duration of project is normal. Then
the std normal variate for desired time(scheduled Time) D is given by

Z= Scheduled Time (D)- Expected Time (Te) =
$$Z = \frac{D-Tc}{\sigma}$$







- •We know that the project duration for Critical Path (by network construction), we call it Te.
- •We also know to calculate the SD for the Critical Path.
- •We are to find the probability of completing the project at a certain duration we call this D.



Standard Normal Probabilities

Table entry

Table entry for z is the area under the standard normal curve to the left of z.

	*									
z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.4	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0002
-3.3	.0005	.0005	.0005	.0004	.0004	.0004	.0004	.0004	.0004	.0003
-3.2	.0007	.0007	.0006	.0006	.0006	.0006	.0006	.0005	.0005	.0005
-3.1	.0010	.0009	.0009	.0009	.0008	.0008	.0008	.0008	.0007	.0007
-3.0	.0013	.0013	.0013	.0012	.0012	.0011	.0011	.0011	.0010	.0010
-2.9	.0019	.0018	.0018	.0017	.0016	.0016	.0015	.0015	.0014	.0014
-2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0019
-2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.0026
-2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.003€
-2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	.0049	.0048
-2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	.0066	.0064
-2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089	.0087	.0084
-2.2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116	.0113	.0110
-2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150	.0146	.0143
-2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192	.0188	.0183
-1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244	.0239	.0233
-1.8	.0359	.0351	.0344	.0336	.0329	.0322	.0314	.0307	.0301	.0294
-1.7	.0446	.0436	.0427	.0418	.0409	.0401	.0392	.0384	.0375	.0367
-1.6	.0548	.0537	.0526	.0516	.0505	.0495	.0485	.0475	.0465	.0455
-1.5	.0668	.0655	.0643	.0630	.0618	.0606	.0594	.0582	.0571	.0559
-1.4	.0808	.0793	.0778	.0764	.0749	.0735	.0721	.0708	.0694	.0681
-1.3	.0968	.0951	.0934	.0918	.0901	.0885	.0869	.0853	.0838	.0823
-1.2	.1151	.1131	.1112	.1093	.1075	.1056	.1038	.1020	.1003	.0985
-1.1	.1357	.1335	.1314	.1292	.1271	.1251	.1230	.1210	.1190	.1170
-1.0	.1587	.1562	.1539	.1515	.1492	.1469	.1446	.1423	.1401	.1379
-0.9	.1841	.1814	.1788	.1762	.1736	.1711	.1685	.1660	.1635	.1611
-0.8	.2119	.2090	.2061	.2033	.2005	.1977	.1949	.1922	.1894	.1867
-0.7	.2420	.2389	.2358	.2327	.2296	.2266	.2236	.2206	.2177	.2148
-0.6	.2743	.2709	.2676	.2643	.2611	.2578	.2546	.2514	.2483	.2451
-0.5	.3085	.3050	.3015	.2981	.2946	.2912	.2877	.2843	.2810	.2776
-0.4	.3446	.3409	.3372	.3336	.3300	.3264	.3228	.3192	.3156	.3121
-0.3	.3821	.3783	.3745	.3707	.3669	.3632	.3594	.3557	.3520	.3483
-0.2	.4207	.4168	.4129	.4090	.4052	.4013	.3974	.3936	.3897	.3859
-0.1	.4602	.4562	.4522	.4483	.4443	.4404	.4364	.4325	.4286	.4247
-0.0	.5000	.4960	.4920	.4880	.4840	.4801	.4761	.4721	.4681	.4641

Standard Normal Probabilities

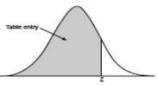


Table entry for z is the area under the standard normal curve to the left of z.

z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
0.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	-5714	.5753
0.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
0.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
0.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
0.5	,6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
0.6	.7257	7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
0.7	7580	.7611	7642	.7673	.7704	.7734	.7764	.7794	.7823	7852
0.8	.7881	7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
0.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998





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Z(+)	Probability (Pr)(%)	Z(-)	Probability (Pr)(%)
0	50.0	0	50.0
+0.1	53.98	-0.1	46.02
+0.2	57.93	- 0.2	42.07
+0.3	61.79	- 0.3	38.21
+0.4	65.54	-0.4	34.46
+0.5	69.15	- 0.5	30.85
+0.6	72.57	-0.6	27.43
+0.7	75.80	- 0.7	24.20
+0.8	78.81	-0.8	21.19
+0.9	81.59	- 0.9	18.41
+1.0	84.13	- 1.0	15.87
+1.1	86.43	-1.1	13.57
+1.2	88.49	- 1.2	11.51
+1.3	90.32	- 1.3	9.68
+1.4	91.92	- 1.4	8.08
+ 1.5	93.32	- 1.5	6.68
+1.6	94.52	-1.6	5.48
+ 1.7	95.54	- 1.7	4.46
+1.8	96.41	- 1.8	3.59
+1.9	97.13	- 1.9	2.87
+2.0	97.72	- 2.0	2.28
+2.1	98.21	- 2.1	1.79
+2.2	98.61	-2.2	1.39
+ 2.3	98.93	- 2.3	1.07
+2.4	99.18	- 2.4	0.82
+2.5	99.38	- 2.5	0.62
+2.6	99.53	- 2.6	0.47
+ 2.7	99.65	- 2.7	0.35
+2.8	99.74	- 2.8	0.26
+2.9	99.81	- 2.9	9.19
+3.0	99.87	- 3.0	0.13



Example of PERT

A project consists of the following activities and time estimates.

Activity	Optimistic time (to),day	Pessimistic time (tp), day	Most likely time (tm), day
1-2	3	15	6
1-3	2	14	5
1-4	6	30	12
2-5	2	8	5
2-6	5	17	11
3-6	3	15	6
4-7	3	27	9
5-7	1	7	4
6-7	2	8	5

- a) What is the project duration?
- b) What is the probability that the project will be completed in 27 days?





 In order to find out the project duration, the expected task time for each activity is to be determined using the formula

$$te = to + 4tm + tp$$

In order to find out the probability of completion in a given day, standard deviation (σ) for the critical path is to be determined using the formula

$$\sigma^2 = \left[\frac{\text{tp-to}}{6} \right]^2$$

So the required data are presented in the table of next slide





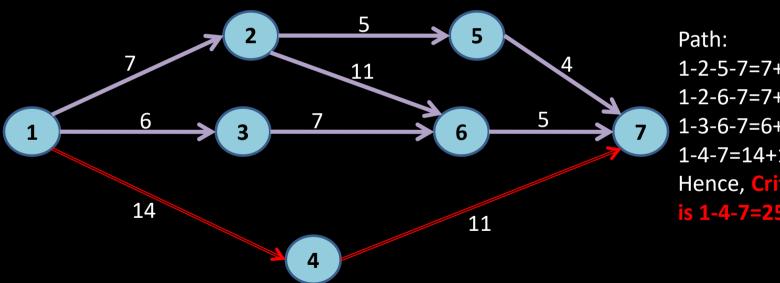
So the required data are presented in the Following

Activity	to	tp	tm	te	σ^2
1-2	3	15	6	7	4
1-3	2	14	5	6	4
1-4	6	30	12	14	16
2-5	2	8	5	5	1
2-6	5	17	11	11	6
3-6	3	15	6	7	4
4-7	3	27	9	11	16
5-7	1	7	4	4	1
6-7	2	8	5	5	1





Using the expected time (te) value, the network is drawn as shown below.







- a) 1-4-7 is critical path. The duration of project
 - = 14+11= 25 days.
- b) The sum of variances along the critical path
 - = 16+16 = 32.

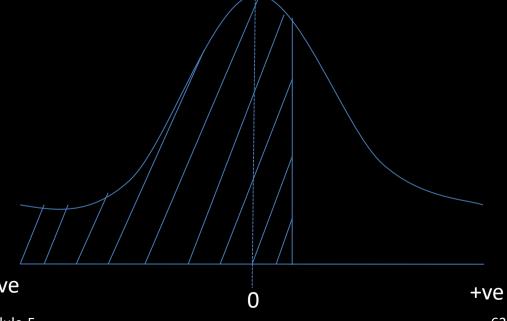
Now the standard deviation, $\sigma = \sqrt{\sigma^2} = \sqrt{32} = 5.656$ Expected project duration, Te = 25 days

Solution-PERT

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- Given D = 27 day.
- With reference to Normal Distribution Curve

$$Z = \frac{D - Te}{\sigma} = \frac{27 - 25}{5.656} = 0.35$$







- From Normal Distribution Table, for Z = 0.35, the fraction of (shadow) area = 0.637 i.e., 63.68%
- So probability of completion of project in 27 days is 63.68%
- [Note: If probability of completion of project will be given and the due date (D) will be asked to find out, then backward calculation can give the result].





- PERT (Program Evaluation and Review Technique) compels managers to plan, which helps them see how the pieces fit together.
- Each subordinate manger has to plan the events for which he or she is responsible.
- It concentrates on critical elements that may need correction.
- It makes possible a kind of forward-looking control.
- The network system with its subsystems enables managers to aim reports and pressure for action at the right spot and level in the organization structure at the right time.





- Because of its emphasis on "activity-time" to its operation, PERT is not useful when no reasonable estimates of time schedule can be made.
- Another disadvantage has been its emphasis on time only but not on costs.



Differences bet PERT & CPM

SI No.	PERT	СРМ
1.	PERT is a probabilistic model with uncertainty in activity duration. activity duration is calculated from to, tp & tm by relation te = (to+4tm+tp)/6	CPM is a deterministic model with well known activity duration
2.	It is an event oriented approach	It is an activity oriented approach
3.	PERT terminology uses word like network diagram event and slack	CPM terminology sues word like arrow diagram nodes and floats
4.	The use of dummy activity is required for representing the proper sequencing	No dummy activity
5.	PERT basically does not demarcate between critical and noncritical activity	CPM maks the critical activity
6.	PERT is applied in projects where resources are always available	CPM in applied to projects where minimum overall cost is the prime importance.
7.	PERT is suitable in defense project & R &D, where activity time can't be readily predicted	7. Suitable for plant maintenance, civil construction projects etc. where activity duration is known.

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- Generally costs are divided into two
 - direct costs
 - indirect costs
- Direct costs- Direct costs are associated with the physical construction of the project including
 - Materials,
 - Equipment,
 - Labor and
 - Subcontractor (if exists)
- Indirect costs They are generally broken down into two categories:
 - head office overhead and
 - general conditions (project or site overhead)





- Crashing an activity refers to taking special costly measures to reduce the duration of an activity below its normal value.
- These special measures might include using overtime, hiring additional temporary help, using special timesaving materials, obtaining special equipment, etc.
- **Crashing the project** refers to crashing a number of activities in order to reduce the duration of the project below its normal value.





- Crashing a project means the process of accelerating an activity or multiple activities to shorten the overall duration of a project.
- By adding additional people, equipment, or man-hours, a project manager can shorten an activity's duration.
- If the activity affected is critical, the project will be shortened as well.
- Activities are crashed for different reasons:
 - An activity may need to be completed by a specific date for contractual reasons.
 - Some activities can be accomplished more economically during a certain time of the year, encouraging managers to accelerate preceding activities.





Crashing of a network can be done in following steps:

1. Critical path:

Find the normal critical path and identify the critical activity.

2. Cost slope:

- Calculate the cost slope for the different activities by using the formula.
- Cost slope = [Crash cost-Normal cost]/[Normal time- Crash time]
- The cost slope indicates the extra cost required to expedite an activity per unit time.

• 3. Ranking:

 Rank the activities in the ascending order of cost slope. The activity having the minimum cost slope have to be crashed first, crash the selected activity to its minimum duration.



Crashing Steps

• 4. Crashing:

 Crash the activities in the critical path as per the ranking i.e., activity having lower cost slope would be crashed first to the maximum extent possible. Calculate the new direct cost by cumulative adding the cost or crashing to the normal cost.

5. Parallel crashing:

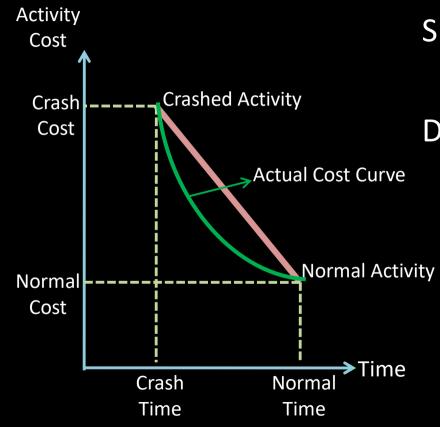
 As the critical path duration is reduced by the crashing in step 3, other paths also become critical, i.e., we get parallel critical path. This means that project duration can be reduced duly by simultaneous crashing or activity on the parallel critical path.

• 6. Total cost:

 Crashing as per steps 3 and 4, one reaches a point when further crashing is either not possible or does not result in the reduction or crashing or project duration. For the different project durations total cost is found up to total cost is got by adding corresponding fixed cost to the direct cost, and the direct cost is got by adding the expediting crashing cost commutative to the normal cost.







Slop = <u>Crash Cost-Normal Cost</u> Normal Time-Crash Time

Direct Cost =

Direct cost of previous Crashing

[Crashing Cost slop X Crashing Time] of current crashing



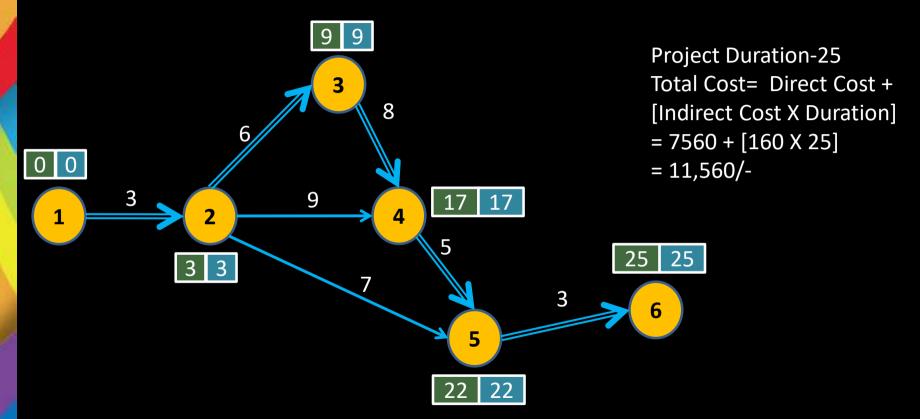
Crashing- Example

The following table gives data on normal cost and time, crash cost and time for a project. The indirect cost is Rs. 160/day. Determine optimum project duration and corresponding minimum cost.

Activity	Nor	mal	Crash		
	Time	Cost	Time	Cost	
1-2	3	360	2	400	
2-3	6	1440	4	1620	
2-4	9	2160	5	2380	
2-5	7	1120	5	1600	
3-4	8	400	4	800	
4-5	5	1600	3	1770	
5-6	3	480	2	760	











0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25

1 2 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25

2 4 *

2 5 *

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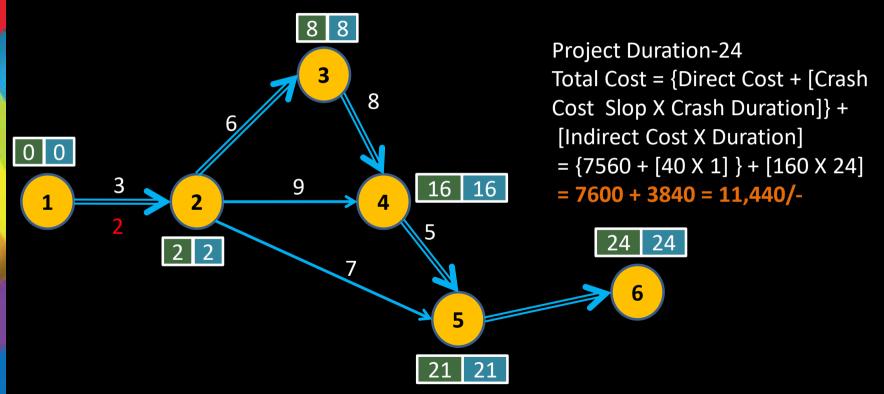
A otivity	Nor	mal	Cra	Slon=AC/AT		
Activity	Time	Cost	Time	Cost	Slop=ΔC/ΔT	
1-2	3	360	2	400	40	1
2-3	6	1440	4	1620	90	3
2-4	9	2160	5	2380	55	
2-5	7	1120	5	1600	240	
3-4	8	400	4	800	100	4
4-5	5	1600	3	1770	85	2
5-6	3	480	2	760	280	5

Total Normal Cost = 7560





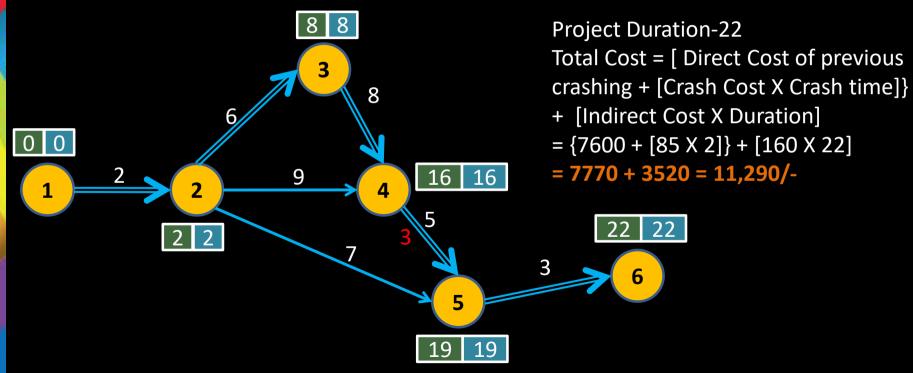
1. Crashing Activity 1-2: As min. slop is 40 for activity 1-2, we will Crash it first







2. Crashing Activity 4-5: As next min. slop is 85 for activity 4-5, we will Crash it now

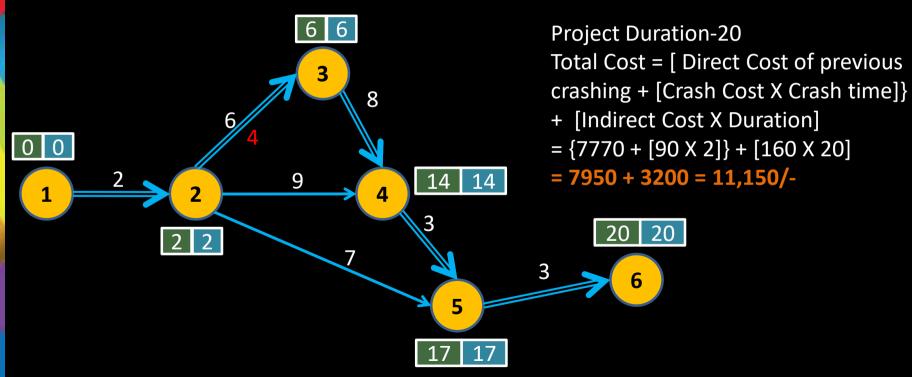


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3. Crashing Activity 2-3: As next min. slop is 90 for activity 2-3, we will Crash it now

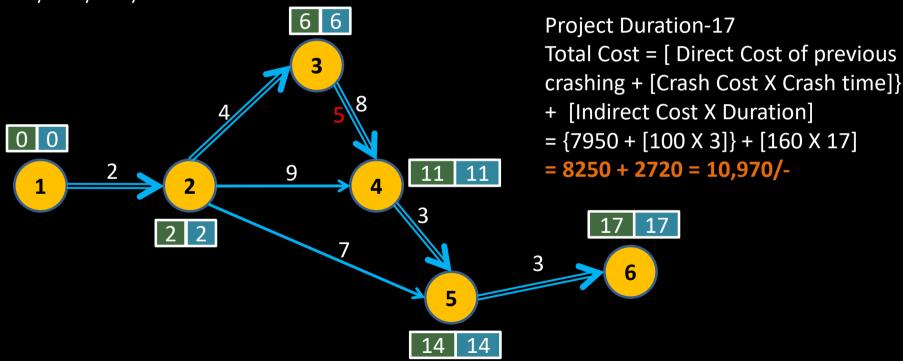


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Crashing-Solution

4. Crashing Activity 3-4: As next min. slop is 100 for activity 3-4, we will Crash it now. If we crash 3-4 fully by 4 days then CP will be changed. Therefore to maintain original CP containing 3-4, we will crash it by 3 days only

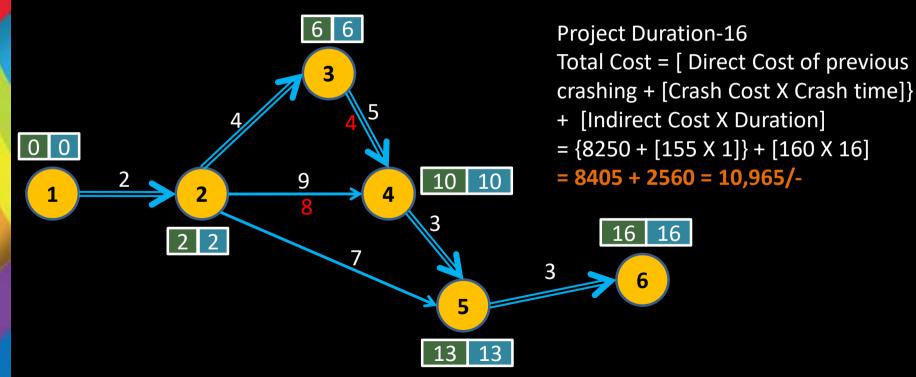






Crashing-Solution

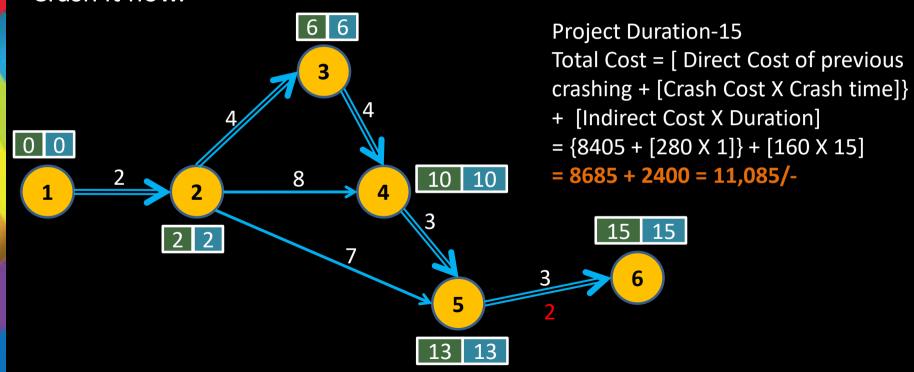
5. Crashing Activity 2-4 & 3-4: If we crash 2-3 & 3-4 simultaneously by 1 day then total cost (100+55=155) which is less than indirect cost 160. so we can crash both together







6. Crashing Activity 5-6: As next min. slop is 280 for activity 5-6, we will Crash it now.



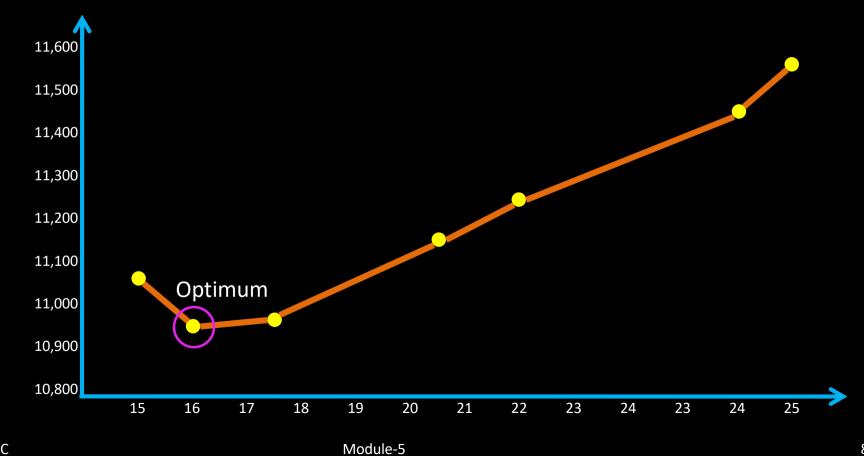


Crashing-Solution

Crashed Activity	Days saved	Project duration	Direct project cost	Over heads 160Xduration	Total project cost
None	-	25	7560	4000	11650
1-2	1	24	7600	3840	11440
4-5	2	22	7770	3520	11250
2-3	2	20	7950	3200	11150
3-4	3	17	8250	2720	10970
3-4, 2-4	1	16	8405	2560	10965
5-6	1	15	8685	2400	11085

Crashing-Solution





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Resource Leveling

- Resource leveling is a technique used to examine unbalanced use of resources (usually people or equipment) over time, and for resolving over-allocations or conflicts resulting from scheduling certain tasks simultaneously. Such conflicts are:
 - more resources such as machines or people are needed are available, or
 - a specific person is needed in both tasks, the tasks will have be rescheduled concurrently or even sequentially to manage the constraint.
- It is used to balance the workload of primary resources over course of the project[s], usually at the expense of one of traditional triple constraints (time, cost, scope)



Resource Leveling

- Resource leveling helps an organization to make use of the available resources to the maximum. The idea behind resource leveling is to reduce wastage of resources i.e., to stop over-allocation of resources. Resource leveling techniques provide a means of distributing resource usage over time to minimize the period-by-period variations in manpower, equipment, or money expended.
- The essential idea of resource leveling centers about the rescheduling of activities within the limits of available float to achieve better distribution of resource usage.



Resource Leveling -Example

A subcontractor needs to install flooring in two areas:

Area 1: This area has old vinyl tile that must be removed and replaced with new vinyl tile.

Area 2: This area has a concrete slab that needs to be topped with ceramic tile. This simple project is broken into the activities shown in the following table,

Activity	Description	Predecessor	Duration	Worker
А	Purchase and deliver material	-	5	2
В	Remove old vinyl tile	-	7	4
С	Install ceramic tile	А	3	3
D	Install new vinyl tile	A,B	5	3
Е	Clean-up inspect	C,D	2	2



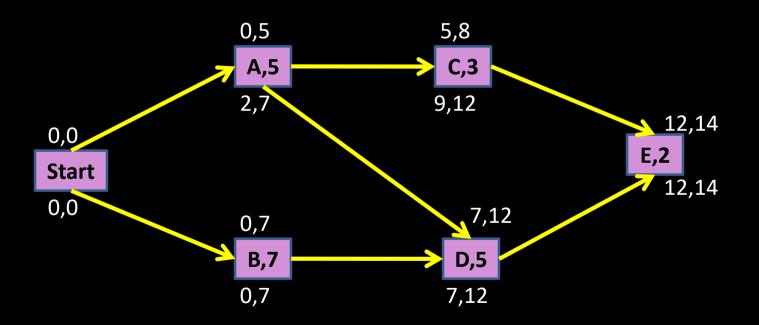
Resource Leveling - Solution

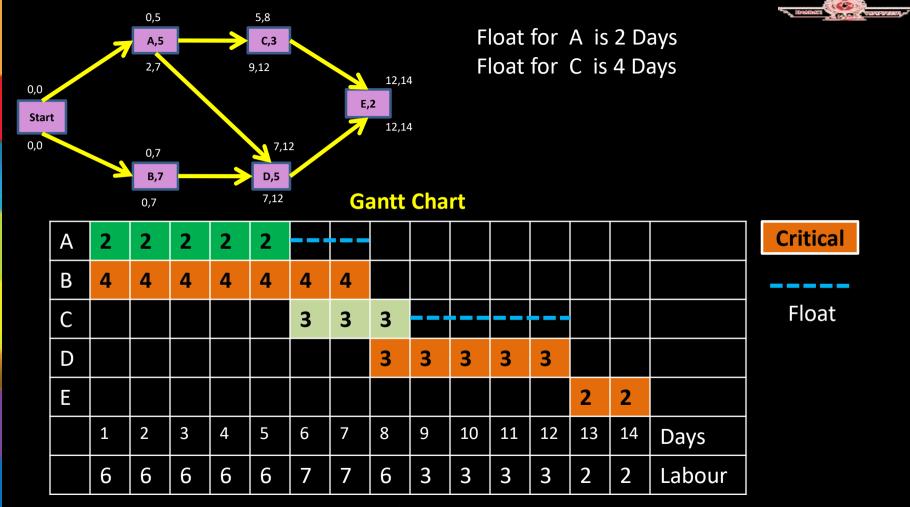
- 1. Draw the precedence network and perform the CPM calculations.
- 2. Allocate the required resources, then level them so that the subcontractor does not use more than six laborers at any time.
- 3. Find ways to improve the labor usage profile. For the sake of simplicity, assume that any laborer can perform any task.



Resource Leveling - Solution

Network diagram

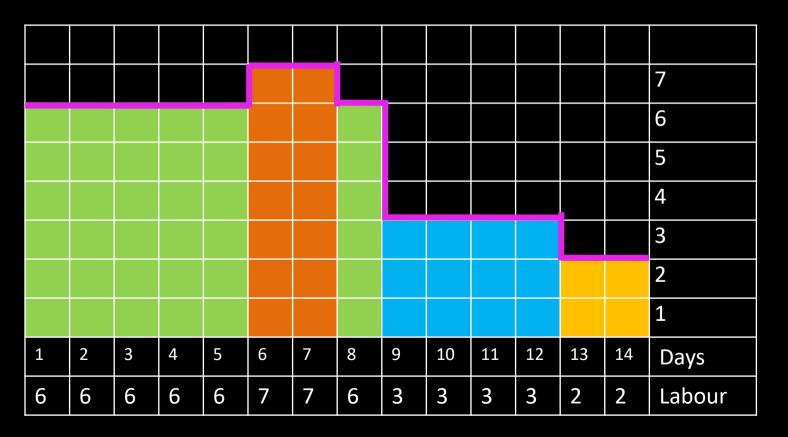




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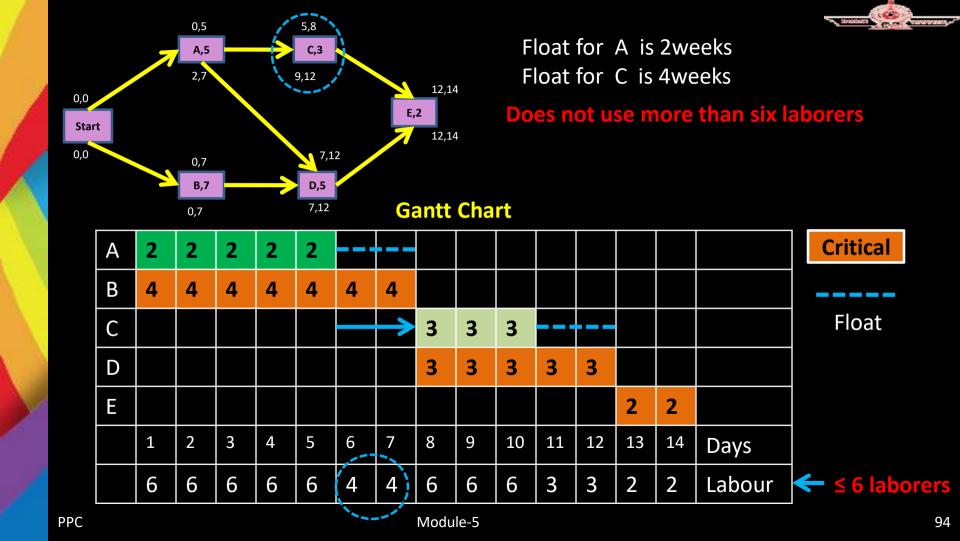




Resource Profile of Example

Does not use more than six laborers

														7
														6
														5
														4
														3
														2
														1
1	2	3	4	5	6	7	8	9	10	11	12	13	14	Days
6	6	6	6	6	7	7	6	3	3	3	3	2	2	Labour





Resource Profile of Example

Does not use more than six laborers

														7
														6
														5
														4
														3
														2
														1
1	2	3	4	5	6	7	8	9	10	11	12	13	14	Days
6	6	6	6	6	4	4	6	6	3	3	3	2	2	Labour





- Product sequencing
- Dispatching
- Progress report & expediting and control.
- Johnson's Rule for optimal sequence of
 - N jobs on 2 machine
 - Process n Jobs on 3 Machines (n/3 problem) and
 - Jackson Algorithm
 - Processing of 2 Jobs on m Machine (2/m) problem





- Sequencing: the process of determining the job order on machines or work centers
 - Also known as priority sequencing
- Priority rules: the rules used in obtaining a job sequence
 - Can be simple or complex
 - Can use one or more pieces of information
 - Common rules shown on next slide





- Prioritize jobs assigned to a resource
- If no order specified use first-come firstserved (FCFS)
- Many other sequencing rules exist
- Each attempts to achieve to an objective

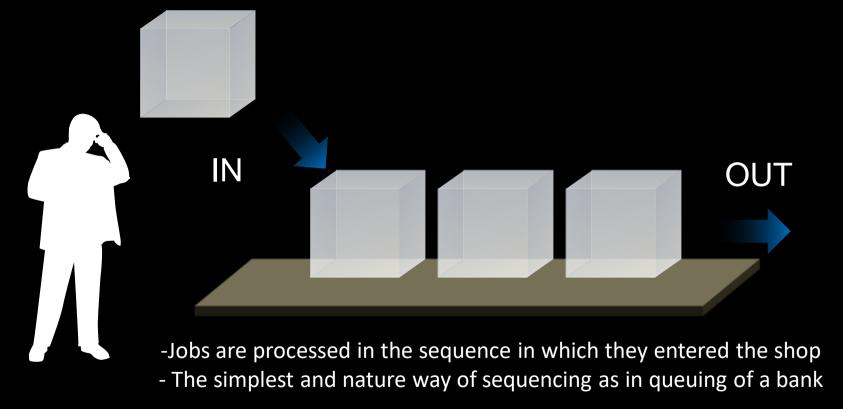




- 1. FCFS first-come, first-served
- LCFS last come, first served
- 3. SPT shortest processing time
- 4. EDD earliest due date
- 5. CR critical ratio
- 6. LWR Least Work remaining
- 7. FOR Fewest Operation Remaining
- 8. SL Slack Time
- 9. ST/O Slack time per operation
- 10. NQ Next Queue
- 11. LSU Least set –up



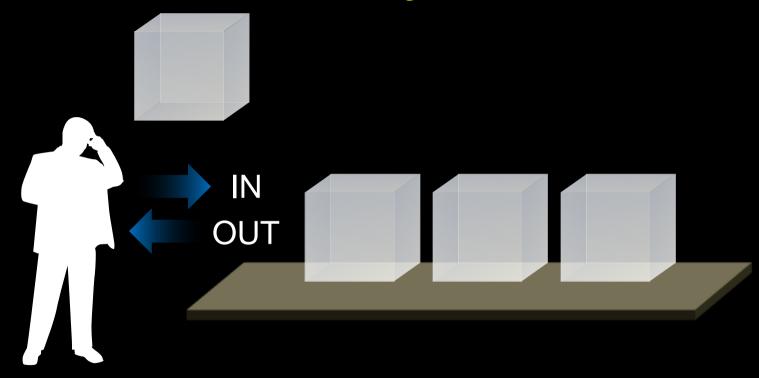




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- 3. SPT (shortest processing time)
 - Jobs are sequenced in increasing order of their processing time
 - The job with shortest processing time is first, the one with the next shortest processing time is second, and so on
- 4. EDD (earliest due date) Jackson Algorithm
 - Jobs are sequenced in increasing order of their due dates
 - The job with earliest due date is first, the one with the next earliest due date is second, and so on





- 5. CR (Critical ratio)
 - Critical ratio is the remaining time until due date divided by processing time;
 - Scheduling the job with the smallest CR next;
 - -CR provides the balance between SPT and EDD, such that the task with shorter remaining time and longer processing time takes higher priority;
 - CR will become smaller as the current time approaches due date, and more priority will be given to one with longer processing time;
 - For a job, if the numerator of its CR is negative (the job has been already later), it is naturally scheduled next; 6. If more than one jobs are later, higher priority is given to one that has shorter processing time (SPT).
- 6. Least work remaining (LWR) It is an extension of SPT. It indicates that work be scheduled according to the processing time remaining before the job is considered to be complete.





- 7. Fewest operations remaining (FOR) It is another form of SPT. It sequences jobs based on the number of successive operations remaining until the job is considered.
- 8. Slack time (ST) Slack is determined by subtracting the sum of set-up and processing times from the time remaining until the job due date. Jobs are processed in order of the smallest amount of slack.
- 9. Slack time per operation (ST/O) The slack time is divided by the number of operations remaining until the job is complete with the smallest values being scheduled first.

Sequencing methods



- 10.Next queue (NQ) It depends on the machine utilization. It considers queues at each of the succeeding work centers at which the jobs will go.
- 11. Least set –up (LSU) It maximizes utilization. Least set-up selects first the job minimizes changeover time on given machine.



Sequencing – Example 1

The processing time for five jobs and their due dates are given for a single machine scheduling is given below in table. Determine:

- 1. The sequence
- 2. Total completion time
- 3. Average completion time
- 4. Average number of jobs in the system and
- 5. Average job lateness using the following priority sequencing rules
 - I. Shortest Processing time (SPT)
 - II. Earliest due date (EDD)
 - III. Longest processing time (LPT)
 - IV. Compare the above characteristics for the three sequencing rules

Job (j)	1	2	3	4	5
Processing Time (tj) hrs	9	7	5	11	6
Due date (in days) (dj)	16	20	25	15	40



Sequencing – Solution 1

Shortest Processing time (SPT) – As per the rule, the job with shortest processing time is scheduled first immediately followed by the next lowest processing time and so on.

Job Sequence	Processing time (tj) days	Flow time (Ft) days	Due Date (dj) days	Job lateness (days)
3	5	5	25	0
5	6	11	40	0
2	7	18	20	0
1	9	27	16	11
4	11	38	15	23
Total	38	99		34



Sequencing – Solution 1

Various Characteristics are:

- I. Total completion time (flow time)= 38 days
- II. Average completion time
 - = Total flow time/No. of jobs = 99/5 = 19.8 days
- III. Average number of jobs in the system
 - = Total flow time/ Total Process time (completion)
 - = 99/38 = 2.61 jobs
- IV. Average job lateness
 - = Total Job lateness/ No. of jobs
 - = 34/5 = 6.8 days



Earliest Due Date (EDD) – As per the rule, priority is given to the job with earliest due date. Arranging the jobs as per the EDD rules gives following table.

Job Sequence	Processing time (tj) days			Job lateness (days)
4	11	11	15	0
1	9	20	16	4
2	7	27	20	7
3	5	32	25	7
5	6	38	40	0
Total	38	128		18



Various Characteristics are:

- I. Total completion time (flow time)= 38 days
- II. Average completion time
 - = Total flow time/No. of jobs = 128/5 = 25.6 days
- III. Average number of jobs in the system
 - = Total flow time/ Total Process time (completion)
 - = 128/38 = 3.37 jobs
- IV. Average job lateness
 - = Total Job lateness/ No. of jobs
 - = 18/5 = 3.6 days



Longest Processing Time (LPT) – As per the rule, priority is given to the job with longest processing time. Arranging the jobs as per the LPT rules gives following table.

Job Sequence	Processing time (tj) days			Job lateness (days)
4	11	11	15	0
1	9	20	16	4
2	7	27	20	7
5	6	33	40	0
3	5	38	25	13
Total	38	129		24



Various Characteristics are:

- I. Total completion time (flow time)= 38 days
- II. Average completion time
 - = Total flow time/No. of jobs = 129/5 = 25.8 days
- III. Average number of jobs in the system
 - = Total flow time/ Total Process time (completion)
 - = 129/38 = 3.39 jobs
- IV. Average job lateness
 - = Total Job lateness/ No. of jobs
 - = 25/5 = 4.8 days



Comparison of Priority rules

Priority rule	Total Completion time (days)	Average Completion time (days)	Average no. of jobs in the system	Average Job Lateness
SPT	38	19.8	2.61	6.8
EDD	38	25.6	3.37	3.6
LPT	38	25.8	3.39	4.8



Sequencing – Example 2

The following jobs are waiting to be processed in a turning shop on 23rd July 2020. The estimates of the time needed to complete the jobs are as follows in the table. Sequence the job based on minimum critical ratio.

Jobs (j)	Due Date	Processing time (days)
1	31 st July	9
2	2 nd August	6
3	16 th August	24
4	29 th July	5
5	30 th August	30





- The Critical ratio is computed as
- Critical Ratio (CR) = Time remaining for due date of the job
 Time needed to complete the job
 - = <u>Time remaining</u>
 Work remaining
- As per the critical ration rule, a job with the minimum critical ratio is given the first preference, i.e., the lower is the critical ratio. Higher is it's priority.
- The denominator of CR, i.e., the time needed to complete the job includes the processing time remaining plus the transfer time plus the estimated waiting time remaining for the job to go through before it is completely processed.





Job Sequence	Due Date	Processing time (Tr) days the job in days (Tn)		Critical Ratio CR=Tn/Tr
1	31 st July	9	8	8/9=0.89
2	2 nd August	6	10	10/6=1.167
3	16 th August	24	24	24/24=1.00
4	29 th July	5	6	6/5=1.20
5	30 th August	30	38	38/30=1.27





- CR<1 means that job is already late
- CR=1 indicates that the job is on schedule
- CR>1 indicates that the job has some slack available to it.
- From the table, job 1 has lowest CR and has to be processed first and job 2 has highest CR and it is scheduled last
- The sequence is

1 3 4 5 2



Expediting and Control

- Control phase is effected by dispatching, inspection and expediting materials control, analysis of work-in-process. Finally, evaluation makes the PPC cycle complete and corrective actions are taken through a feedback from analysis. A good communication, and feedback system is essential to enhance and ensure effectiveness of PPC.
- Expediting: This is the control tool that keeps a close observation on the progress of the work. It is logical step after dispatching which is called 'follow-up'. It coordinates extensively to execute the production plan.
- Expediting is a process of tracking a job's progress and taking special
 actions to move it through the facility. In tracking a job's progress, special
 action may be needed to keep the job moving through the facility on time.
 Manufacturing or service operations disruptions-equipments breakdowns,
 unavailable materials, last-minute priority changes, require managers to
 deviate from plans and schedules and expedite an important job on a
 special handling basis.





- Progressing function can be divided into three parts, i.e., follow up of materials, follow up of work-in-process and follow up of assembly.
- The duties include: (a) Identification of bottlenecks and delays and interruptions because of which the production schedule may be disrupted. (b) To devise action plans (remedies) for correcting the errors. (c) To see that production rate is in line with schedule.





- It is concerned with starting the processes.
- It gives necessary authority to start a particular work, which has already being planned under Routing and scheduling.
- For starting the work, essential orders and instructions are given. Therefore, the complete definition of dispatching → "Released of order and instructions for the starting of production for any item in accordance with the route sheet and scheduled chart.



Function of Dispatching

- 1. After dispatching is done, required materials are moved from stores to m/c(s) and from operation to operation.
- 2. Authorizes to take work in hand as per schedule.
- 3. To distribute m/c loading and schedule charts route sheets and other necessary instructions and forms.
- 4. To issue inspection orders, clearly stating the type of inspection required at various stages.
- 5. To order too section for issuing proper tools, jigs, fixtures and other essential articles.



Forms used in Dispatching

Following are some of the more common forms used in dispatching.

- 1. Work orders: while starting the production, work orders are issued to departments to commence the desired lot of product.
- 2. Time cards: Each operator is supplied with this card in which he mentions the time taken by each operation and other necessary information's. there are helpful for wage payment.
- 3. Inspection Tickets: These tickets are sent to the inspection department which shows the quality of work required and stages at which inspection is to be carried out.
- 4. Move Tickets: These tickets are used for authorizing over the movement of material from store to shop and from operation to operation.
- 5. Tool & Equipment Tickets: It authorizes the tool department that new tools, gauges, jigs, fixtures and other required equipment may be issued to shop.

Johnson's Algorithm



- The general sequencing problem is stated as 'N' jobs (1,2,3....n) to be processed through 'M' machines (m₁,m₂,m₃....m_n) at a time by following , order of processing (precedence) and a given processing time, with minimizing elapsed(idle) time.
- Johnson's algorithm is the technique for minimizing completion time for a group of jobs to be processed in optimal sequence.





Johnson's algorithm is used for:

- 1. N jobs and 2 machines
- 2. N jobs and 3 machines

Assumptions -

- 1. No machines can process more than one job at a time
- 2. Processing times are independent of processing job
- 3. Each job once started once one machine is continued till completion on it
- 4. Time involved in moving a job from one machine to another is negligibly small





Steps:

- 1. List time required to process each job at each machine. Set up a one-dimensional matrix to represent desired sequence with # of slots equal to # of jobs.
- 2. Select smallest processing time at either machine.
 - If that time is on machine 1, put the job as near to beginning of sequence as possible.
 - If smallest time occurs on machine 2, put the job as near to the end of the sequence as possible. Remove the job from the list.
- 3. Remove the job from the list.
- 4. Repeat steps 2-3 until all slots in matrix are filled & all jobs are sequenced.



Five jobs are to be processed on two machines M1 and M2 in the order M1M2. Processing time in hours are given below in the table.

Job	Machine Centre-1	Machine Centre-2
А	5	6
В	16	5
С	8	2
D	9	17
Е	4	6

Determine the sequence that minimizes total elapsed time. Find out the total elapsed time and idle time, if any, on M2.



Job	Machine Centre-1	Machine Centre-2
А	5	6
В	16	5
С	8	2
D	9	17
Е	4	6



The minimum processing time, 2, is given by Job C on Machine 2. So, Schedule Job C in the end.

Job	Machine Centre-1	Machine Centre-2
А	5	6
В	16	5
	8	
D	9	17
Е	4	6





The minimum processing time, 2, is given by Job C on Machine 2. So, Schedule Job C in the end.

Job	Machine Centre-1	Machine Centre-2
А	5	6
В	16	5
	8	
D	9	17
Е	4	6

С



After removing job C, the minimum processing time, 4, is given by Job E on Machine 1. So, Schedule Job E in the beginning.

Job	Machine Centre-1	Machine Centre-2
А	5	6
В	16	5
D	9	17
E	4	6

E C



Job E is removed. Now, there is a tie. Minimum processing time is given by Jobs A and B. Break ties arbitrarily. Schedule one of Job A or Job B.

Job	Machine Centre-1	Machine Centre-2
А	5	6
В	16	5
D	9	17

E A C

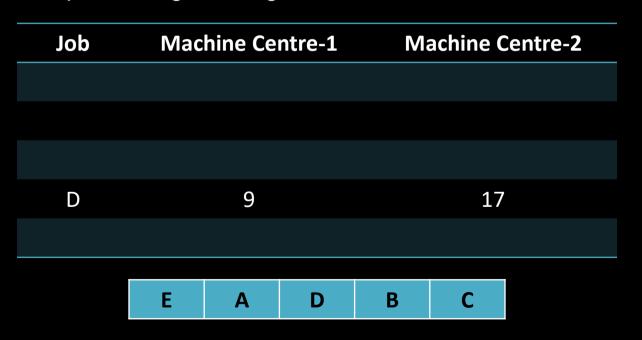


Job A is chosen arbitrarily. Job A is scheduled in the beginning, because its minimum time is given on Machine 1. Beginning means position 2 because position 1 is taken

Job	Mac	hine Ce	ntre-1	Ma	achine C	entre-2
В		16			5	
D		9			17	
	Ε	Α		В	С	



Next, Job B is scheduled. It's scheduled in the end, because its minimum processing time is given on Machine 2.





The sequencing is complete after assigning the remaining Job D to the remaining position. Next, the make span is computed.

E A D B C



To compute the elapsed time:

- 1. The starting time of machine M₁ is assumed as 0.00
- 2. The machine M2 starts processing job 2 only when it comes out of machine M1 after completion. So it is idle for 1 hour in the start till job comes to it from machine 1.
- 3. The minimum total elapsed time is 40 hrs to process all the 5 jobs through two machines M1 and M2

The idle time on machine M1 = 4+1+2 = 7 hrs.



				N	Machine
Job		Machine Centre-2	Optimal sequence	In	Proces sing
Α	5	6			time
В	16	5	Е	0	4
С	8	2	Α	4	5
D	9	17	D	9	9
			В	18	16
Е	4	6	5		
			C	34	8

	Λ	/lachine N	VI1	M	lachine N	V12	Idle
Optimal sequence	In	Proces sing time	Out	In	Proces sing time	Out	time M2
Ε	0	4	4	4	6	10	4
А	4	5	9	10	6	16	-
D	9	9	18	18	17	35	2
В	18	16	34	35	5	40	-
С	34	8	42	42	2	44	2

The minimum total elapsed time is 44 hrs to process all the 5 jobs through two machines M1 and M2. The idle time on machine M1 = 4+2+2 = 8 hrs.

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N Jobs on 3 machines (N/3)

Conditions to be satisfied to solve N/3 problems by Johnson's Methods:

- 1. Each job has to go through all the three machines M1,M2,M3.
- 2. The smallest processing time on machine M1 ≥ Largest processing time on machine M2
- 3. The smallest processing time on machine M3 ≥ Largest processing time on machine M2

If either or both of these conditions are satisfied then the given problem can be solved by Johnson's algorithm.





Steps:

- 1. Convert the 3 machine problem in to 2 machine problem by introducing two fictitious machines G and H.
 - Gi =M1i=M2i
 - Hi = M2i=M3i (i=1,2,3...n)
- 2. Once the problem is converted in to N/2 problem, the sequence is determined by Johnson's algorithm for N/2 problem
- 3. For the optimal sequence determined, find out the minimum total elapsed time associated with machines.



N Jobs on 3 machines (N/3)

Breaking Rules:

- 1. If there are equal smallest processing time one for each machine, place the job on machine 1, first in the sequence and one in machine 2 last in the sequence.
- 2. If the equal smallest time are both for machine 1, select the job with lower processing time in machine 2 for placing first in the sequence.
- 3. If equal smallest times are both for machine 2, select the one with lower processing time in machine 1, for placing last in the sequence.



N Jobs on 3 machines (N/3)

Seven jobs are to be processed through 3 machines M1, M2 and M3 in the order M1,M2,M3. The processing times are given in hrs. to process each one of the 3 jobs through all the machines find the optimal sequence of the jobs. Also find the minimum total elapsed time and idle times on M2 and M3.

Jobs	M1	M2	M3
Α	3	4	6
В	8	3	7
С	7	2	5
D	4	5	11
Ε	9	1	5
F	8	4	6
G	7	3	12





Step-1: Check for conditions to be satisfied

- Minimum processing time on M1 = 3
- Minimum processing time on M3 = 5
- Maximum processing time on M2 = 5

Condition 1:

- Min. time on M1 ≥ Max. time on M2
- Here 3 ≥ 5, so condition 1 is satisfied

Condition 2:

- Min. time on M3 ≥ Max. time on M2
- Here 5 = 5, so condition 2 is satisfied
- Hence this problem can be solved by Johnson's algorithm

Jobs	M1	M2	M3
А	3	4	6
В	8	3	7
С	7	2	5
D	4	5	11
Е	9	1	5
F	8	4	6
G	7	3	12





Step-2: Convert N/3 problem in to N/2 problem by assuming fictitious machines G and H.

$$G = M1i + M2i$$
 and $H = M2i + M3i$

Jobs	Gi	Hi
А	7	10
В	11	10
С	9	7
D	9	16
Е	10	6
F	12	10
G	10	15



N Jobs on 3 machines (N/3)

Step-3: Determine the sequence using N/2 procedure.

- Minimum processing time is 6 for job E and is associated with machine H. So process job E last in the sequence.

Jobs	Gi	Hi
А	7	10
В	11	10
С	9	7
D	9	16
E	10	6
F	12	10
G	10	15
		E





Jobs	Gi	Hi
А	7	10
В	11	10
	9	7
D	9	16
F	12	10
G	10	15







Jobs	Gi	Hi
В	11	10
D	9	16
F	12	10
G	10	15





N Jobs on 3 machines (N/3)

Minimum time is 10 associated with

- 1. Machine Gi for Job G. so do the job g next in the sequence
- 2. Tie between job F and job B for machine Hi . As per the rule job B should be processed last

Jo	bs		Gi		Hi		
	В		11		10		
	F		12		10		
G 10		15					
Α	D	G	F	В	С	E	





	Λ	Machine M1		Ma	Machine M2		Idle	N	Machine M3		
Optimal sequence	In	Proces sing time	Out	In	Proc essi ng time	Out	time M2	In	Proces sing time	Out	Idle time M2
Α	0	3	3	3	4	7	3	7	6	13	7
D	3	4	7	7	5	12	-	13	11	24	-
G	7	7	14	14	3	17	2	24	12	36	-
F	14	8	22	22	4	26	5	36	6	42	-
В	22	8	30	30	3	33	4	42	7	49	-
С	30	7	37	37	2	39	4	49	5	54	-
Е	37	9	46	46	1	47	7	54	5	59	-
							25				7

Min. total elapsed time=59 hrs., Idle time of M2=25 hrs, idle time of M3=7 hrs

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- For these types of problems, there are two jobs J1, J2 each of which has to be processed on m machines M1, M2, ..., Mm with different sequences of machines for processing each of the jobs.
- Each machine can perform only one job at a time. The exact or expected processing times on all the given machines are known.
- The objective is to find a sequence of processing the jobs, which minimizes the total elapsed time from the start of the first job to the completion of the last job.





- A problem of this type can be solved with the help of graphical method.
- We have to use the following steps in this method:
- Step 1:Represent the processing times of job 1 on different machines along the x-axis and processing times of job 2 on different machines along the y-axis.
- Step 2: Draw the vertical/horizontal lines through processing times as given in Step 1 and shade the common area for processing of two jobs on the same machine at different times since each machine can perform only one job at a time.



2 Jobs on M machines (2/m)

Step 3: Starting from the origin, we move diagonally, horizontally or vertically through various stages of completion of the processing of both the jobs through different machines at the same time until all the processing times are finished. If both the jobs are being processed simultaneously at different machines at the same time, we move diagonally. If Job 2 is under process at any machine and Job 1 is idle, i.e., Job 1 is waiting to be processed at the same machine through which Job 2 is being processed, we move vertically; and we move horizontally when Job 1 is being processed and Job 2 is idle.

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2 Jobs on M machines (2/m)

- Step 4: An optimal sequence for the jobs is the shortest line consisting of combinations of horizontal, vertical and diagonal (451) lines from the origin. Since both the jobs are being processed simultaneously on the diagonal line, effort should be made to select a path on which diagonal movement is maximum.
- So, we first try to move diagonally but keep in mind that diagonal movement through the blocked out (shaded) areas is not allowed since both the jobs cannot be processed simultaneously on a machine. Then horizontal or vertical movement is chosen keeping in view that total elapsed time should be minimum. The elapsed time can be obtained by adding the idle time for either job to the processing time for that job.

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2 Jobs on M machines -Example

- A machine shop has five machines A, B, C, D and E. Two jobs must be processed through each of these machines. The time (in hours) taken on each of these machines and the necessary sequence of jobs through the shops are given in table below.
- Use the graphical method to obtain the total minimum elapsed time.

Job 1	Sequence	Α	В	С	D	Е
	Time	2	4	3	6	6
Job 2	Sequence	С	А	D	Е	В
	Time	4	6	3	3	6



2 Jobs on M machines -Solution

- We are given the job sequences and processing time of 2 jobs at 5 machines. We follow the graphical method to find the minimum total elapsed time from starting the first job at the first machine to completion of the second job at the last machine.
- We first represent the processing time of job 1 on different machines, i.e, 2, 4, 3, 6, 6 along the x-axis and the processing time of job 2, i.e., 4, 6, 3, 3, 6 along the y-axis.





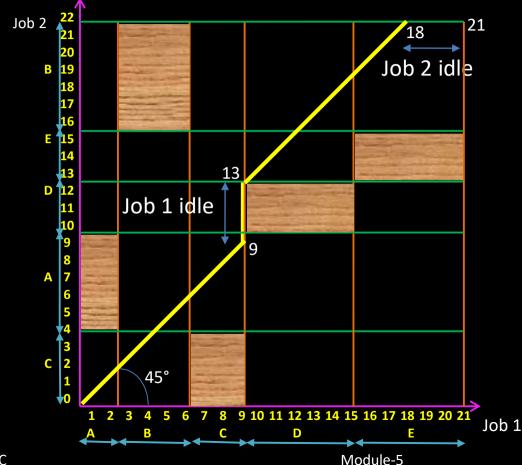
- Then we draw the vertical lines through processing times of Job 1. We draw the first vertical line at 2 hrs, the second at 2 + 4 = 6 hrs, the third at 6 + 3 = 9 hrs, and so on.
- Similarly, we draw the horizontal lines through processing times of Job 2. We draw the horizontal lines at 4, 10, 13, 16 and 22 hrs in this case. We now shade the common area for processing of jobs 1 and 2 on one machine at the same time as each machine can perform only one job at a time.

In this case we find the common areas to be:

- i. between 0 to 2 hours on the x-axis and 4 to 10 hours on the y-axis for machine A,
- ii. between 2 to 6 hours on the x-axis and 16 to 22 hours on the y-axis for machine B,
- iii. between 6 to 9 hours on the x-axis and 0 to 4 hours on the y-axis for machine C,
- iv. between 9 to 15 hours on the x-axis and 10 to 13 hours on the y-axis for machine D,
- v. between 15 to 21 hours in the x-axis and 13 to 16 hours on the y-axis for machine E.



2 Jobs on M machines -Solution



Total Idle time for Job 1 is 13-9 = 4 hrs. Total Idle time for Job 2 is 21-18 = 3 hrs.

The total elapsed time for Job 1 is 21 + 4 = 25 hours. The total elapsed time for job 2 is 22 + 3 = 25 hours

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2 Jobs on M machines -Solution

- We now have to find an optimal sequence for processing of the jobs 1 and 2, i.e., the shortest line consisting of combinations of horizontal, vertical and diagonal (45°) lines from the origin. For this, we start from the origin and move diagonally first up to the point (9, 9) since both the jobs 1 and 2 are being processed simultaneously.
- After being processed through machines A, B and C, job 1 becomes idle since job 2 is being
 processed in machine A and it is then being processed in machine D. Therefore, we move
 vertically which means Job 2 is under process and Job 1 is idle. The idle time for job 1 is 4
 hours in this case.
- Again we move diagonally up to the point (18, 22) since both the jobs 1 and 2 are being processed simultaneously. At this stage, job 2 is completed but job 1 is being processed through machine E. Therefore, we move horizontally, which means Job 1 is being processed and Job 2 is idle. The idle time for job 2 is 3 hours since job 1 is processed through machine E between 15 to 21 hours.
- In this case, the idle time for job 1 is found to be 4 hours. Therefore, the total elapsed time for Job 1 is 21 + 4 = 25 hours. Similarly, the idle time for job 2 is seen to be 3 hours when job 1 was under processing between 18 to 21 hrs and the processing for job 2 had been completed. Therefore, the total elapsed time for job 2 is 22 + 3 = 25

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2 Jobs on M machines -Practice

- Using the graphical method, calculate the minimum time needed to process job 1 and job 2 on five machines A, B, C, D and E, that is, for each machine find the job which should be done first. Also calculate the total time needed to complete both jobs.
 - 1. Job 1 Sequence : A B C D E Time (in hrs) : 1 2 3 5 1
 - 2. Job 2 Sequence : C A D E B Time (in hrs) : 3 4 2 1 5
- 2. Use the graphical method to minimize the time required to process the following jobs on the machines, that is, for each machine specify the job that should be done first. Also calculate the total elapsed time for completing both jobs.
 - 1. Job 1 Sequence : A B C D E Time (in hrs) : 6 8 4 12 3
 - 2. Job 2 Sequence : B C A D E Time (in hrs) : 10 8 6 4 12