

Solving optimization by Hand

Our final Model is in the form of

$$\text{Sales} = 6.75 + 0.0191 \times TV + 0.02886 \times \text{Radio} + 0.001086 \times TV \times \text{Radio} \longrightarrow (1)$$

Interaction term

$$\text{Given } TV + \text{Radio} = 300$$

$$\text{Sub } \text{Radio} = 300 - TV \text{ in eq (1)}$$

$$\text{Sales} = 6.75 + 0.0191 \times TV + 0.02886 \times (300 - TV) + 0.001086 \times TV \times (300 - TV)$$

$$\text{Sales} = 6.75 + 0.0191 \times TV + 8.658 - 0.02886 TV + 0.3258 TV - 0.001086 (TV)^2$$

$$f(x) = \text{Sales} = 15.408 + 0.316 TV - 0.001086 (TV)^2 \longrightarrow (3)$$

Solving First order condition

$$f'(x) = 0$$

$$0.3161 - 2 \times 0.001086 \times TV = 0$$

$$0.3161 - 0.002172 \times TV = 0 \longrightarrow (2)$$

$$\frac{0.3161}{0.002172} = TV$$

$$TV = 145.534 \text{ units}$$

$$\text{Radio} = 300 - 145.534$$

$$\text{Radio} = 154.465 \text{ units}$$

~~Here~~

After solving eq (2) (2^{nd} order diff)

$$f''(x) = -0.002172 \text{ which is } < 0$$

\therefore TV, Radio are maximum points

TV budget must be \$145,534 dollars

and Radio budget must be \$154,465 dollars

to maximize the sales

Sub TV value in (3)

$$\text{Sales} = 15.408 + 0.3151 \times 145.534 - 0.001086 \times (145.534)^2$$

$$\text{Sales} = 38.14 \text{ units}$$

This prediction ^{of sales} is high compared to existing sales value.

-The maximum sales value for the existing data is 27 units.