

Today's Content

- ↳ Currency exchange
- ↳ fractional knapsack
- ↳ Greedy Properties
- ↳ Activity Selection
- ↳ job Scheduling

→ to use the mon demon, if you can

Indian Currency: 1, 2, 5, 10, 20, 50, 100, 200, 500, 2000

Cash: 5548 → min number of Coins/notes to get required Cash?
↳ multiples of same coins are allowed.

Notes/coins	Count	leftout	
2000	2	→	1548
500	3	→	48
20	2	→	8
5	1	→	3
2	1	→	1
1	<u>1</u>	→	0
	10		

Will it always work?
↓
NOPE

$0 \leq \text{Notes}[i-1] * 2 \leq \text{Money}[i]$

Currency: 1 10 18

Money: 20 → min coins required?

18
1
1 } 3

optimal scenario
10
10 } 2

Q) Fractional Knapsack

↳ you can consume K kg of vegetables, you can eat any integral amount of item. Max Protein you can get?

Vegetables		Eating complete item Protein gained	max 70 kg consumption		Protein/kg
			min kg		
Tomato	20 kg	200 P			10 P/kg - 20 = 200P
Apples	15 kg	180 P	5 kg → 250P	5 kg → 100P	12 P/kg - 15 = 180P
Onion	50 kg	250 P	20 kg → 200P	10 kg → 150P	5 P/kg
Chicken	10 kg	150 P		12 kg → 132P	15 P/kg - 12 = 150P
Potato	25 kg	200 P		15 kg → 180P	8 P/kg - 8 = 64P
Mango	12 kg	132 P		20 kg → 200P	11 P/kg - 12 = 132P
Seafood	5 kg	100 P		8 kg → 64P	20 P/kg - 5 = 100P
				826 P	826 P

Greedy Properties:

- ① for min/max related Problems.
 - ↳ binary search
 - ↳ dp
 - ↳ greedy
- ② 2 pointers

→ greedy will

(i) Based on what Parameter we want to apply greedy.

(iii) Check the approach by coming up with counter examples.

↳ atleast one counter

example.

Tomato \rightarrow 5 kg \rightarrow 50 P

Apple \rightarrow 6 kg \rightarrow 600 P

7 kg		Protein/kg
using smallest wt.		
5 kg	\rightarrow 50 P	100 P/kg \rightarrow 1 \rightarrow 100 P
2 kg	\rightarrow 200 P	100 P/kg \rightarrow 6 \rightarrow 600 P
<u>250 P</u>		<u>610 P</u>

↳ Solve Problems by "locally optimal choices" at (greedy)

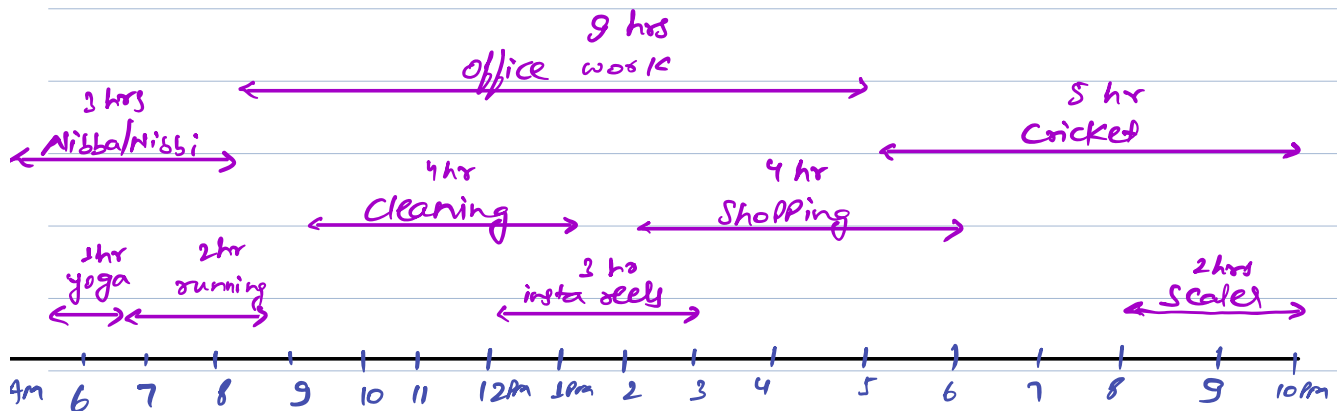
each Step, and this is giving you the final best answer.

D) Activity Selection

↳ max Count of task you can do.

Note: ① Start a task, we need to complete.

② At any point of time, single task.



① min duration task first.

yoga, scales, running, insta reels

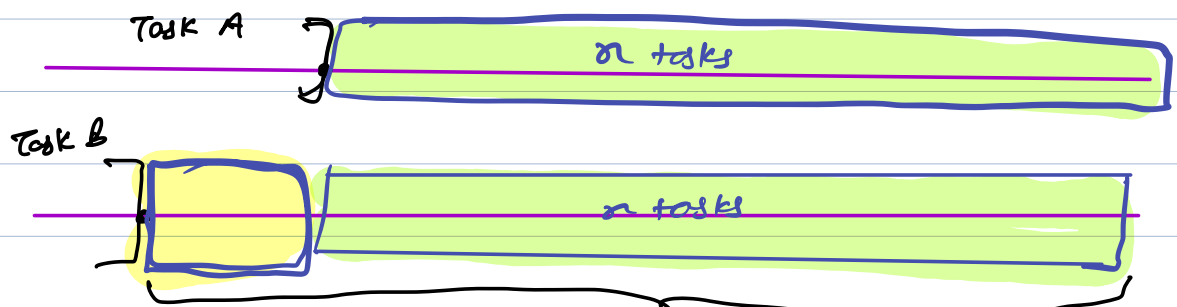
② Starting early

Nibba/Nissi, office work, cricket

③ ending early ✓

↳ yoga, running, cleaning, shopping, scales

Correctness:



$\geq n$ tasks

↳ By picking ending early tasks, we are leaving more slots to do more tasks.

Non-overlapping intervals?!

Algorithm:

↳ ① Sort all the tasks on the basis of end time.

② get all non-overlapping task.

Job Scheduling

Given n tasks to complete

→ Deadline assigned for each task, day on or before we can do task.

→ Payment assigned to each task.

→ on any given day we can perform only 1 task and Each task take 1 day to finish.

→ find max payment we can get.

Ex1:

Job	deadline day	Payment
a	3	100
b	1	19
c	2	27
d	1	25
e	3	30

Parameter
 ↓
 Payment (i)
 ↓
 deadline (ii)
 ↓
 Payment + deadline (iii)

<u>c</u>	<u>e</u>	<u>a</u>	→ 157
1	2	3	

Job	deadline day	Payment
a	3	100
b	1	19
c	2	27
d	2	25
e	1	30

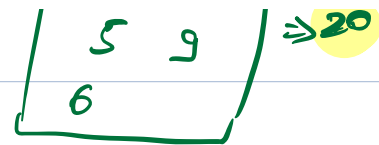
<u>e</u>	<u>d</u>	<u>a</u>
	2	

Ex2:

Job	deadline day	Payment
a	3	5
b	1	1
c	3	6
d	2	3
e	3	9

Job: b d a c e
 dead: 1 2 3 3 3
 Pay: 1 3 5 6 9

1 2



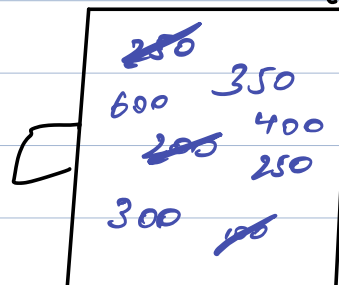
Ex2: Tasks: 1 2 3 4 5 6 7 8 9 10
 dead: 2 1 1 1 4 5 4 5 5 2
 money: 200 250 200 350 300 100 250 600 400 150

Sort on the basis of deadline

dead: 1 1 1 2 2 4 4 5 5 5 ⁱ
 money: 250 200 350 200 150 300 250 100 600 400

350

1900 ←



// Pseudo code;

↳ ① Sort the data on the basis of deadline

↳ ② Iterate and pick the jobs if Payment is better

↓
Pain of discipline or Pain of regret

Ex: arr = {-1, -2, -3}

b = 5

①

{-1, ~~-2~~, ~~-3~~}
 -4, ~~-6~~
 -6, ~~-8~~
 -12



{~~-1~~, ~~-2~~, ~~-3~~}
 ~~-4~~, -4, -6
 ~~-8~~
 -4

↳ -4 = ans

-4 < -1

✓