

Todays Content :

- i^{st} smaller on left $\rightarrow i^{st}$ smaller on right
- i^{st} larger on left $\rightarrow i^{st}$ larger on right
- Area of histogram
- Sum of Max of every subarray

1st smaller element on left side

Given $ar[n]$, for every ele $ar[i]$ find nearest smaller element on left side.

nearest ele @ $ar[i]$

↳ distance between indices

Ex1: $ar[6] = [4, 5, 2, 10, 3, 12]$

$ans[6] = [-1, 4, -1, 2, 2, 3]$

0	1	2	3	4	5
4	5	2	10	3	12

Ex2: $ar[8] = [4, 6, 10, 11, 7, 8, 3, 5]$

$ans[8] = [-1, 4, 6, 10, 6, 7, -1, 3]$

Ideal: for every element, iterate on left & get 1st smaller on left side

int[] smallerleft(int ar[n]) { TC: O(N²) SC: O(1)

int ans[n] = {-1} // if no smaller, it should be -1

i=0; i < n; i++) {

// find 1st smaller for $ar[i]$?

j = i-1; j >= 0; j-- {

// $ar[j]$ is 1st smaller?

if ($ar[j] < ar[i]$) {

 ans[i] = ar[j];

 break;

N^2 : optimization

↳ $N \log N$: sorting *

: Binary search *

N times?

{ → target

 → search space

 → discard or not *

Note: doubts/ideas: public chat

Ex1: $arr[12] = [5, 8, 11, 14, 7, 10, 13, 6, 9, 10, 2, 5]$

$ans[12] = [-1, 5, 8, 11, 5, 7, 10, 5, 6, 9, -1, 2]$

5
2
~~X~~
~~X~~
~~X~~
~~X~~
~~X~~
~~X~~
~~X~~
~~X~~

Container: $\text{top}()$, $\text{push}()$: at top $\text{pop}()$: top element

↳ Stack:

Ex2: $arr[8] = [0, 1, 2, 3, 4, 5, 6, 7]$
 $arr[8] = [4, 6, 10, 11, 6, 8, 3, 5]$

$ans[8] = [-1, 4, 6, 10, 4, 6, -1, 3]$

5
3
~~X~~
~~X~~
~~X~~
~~X~~
~~X~~
~~X~~

```
int[] stiSmaller(int ar[N]) { TC: 2^n = O(N) SC: O(N)
```

```
int ans[n] = {-1}
```

```
Stack<int> st;
```

```
i=0; i < n; i++) {
```

```
//ar[i] find ith smaller
```

```
while(st.size() >= st.top() >= ar[i]) {
```

```
    st.pop()
```

top cannot be ans bcz
we are removing

```
if(st.size() > 0) {
```

```
    ans[i] = st.top();
```

```
    st.push(ar[i]);
```

```
}
```

Nearest smaller index on left

ar[8] = 0 1 2 3 4 5 6 7
 4 6 10 11 7 8 3 5

ans[8] = -1 0 1 2

0 | 1 | 2 | 3 |

```
int[] stiSmallerIndex(int ar[N]) { TC: O(N) SC: O(N)}
```

```
int ans[n] = {-1}
```

```
Stack<int> st;
```

```
i=0; i < n; i++) {
```

```
//ar[i] find ith smaller
```

```
while(st.size() >= ar[st.top()] >= ar[i]) {
```

```
    st.pop()
```

```
} if(st.size() > 0) {
```

```
    ans[i] = st.top();
```

```
    st.push(i); //only push index
```

```
}
```

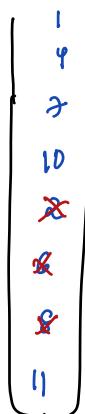
ToDo: ith small index on right:

Iterate from n-1 → 0

2) Nearest Greater on left side

Ex: $ar[8] = [11, 8, 6, 2, \underline{10}, 7, 4, 1]$

$ans[8] = [-1, 11, 8, 6, 11, 10, 7, 4]$



```
int[] it greater left(int ar[n]) {
```

```
    int ans[n] = {-1};
```

```
    stack<int> st;
```

```
    i = 0; i < n; i++) {
```

```
        // ar[i] find ir smaller
```

```
        while(st.size() >= 0 & ar[i] <= ar[st.top()]) {
```

```
            st.pop();
        }
```

```
        if(st.size() >= 0) {
```

```
            ans[i] = st.top();
```

```
            st.push(ar[i]);
```

top cannot be ans bcz
we are removing

$ar[st.top()] <= ar[i]$

// i^r greater than left

st.push(i)

```
    return ans;
```

Note: i^t greater index on right:

iterate from right to left

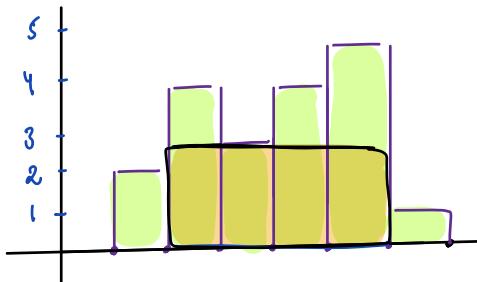
10:16 → 10:25 pm

Histogram Area:

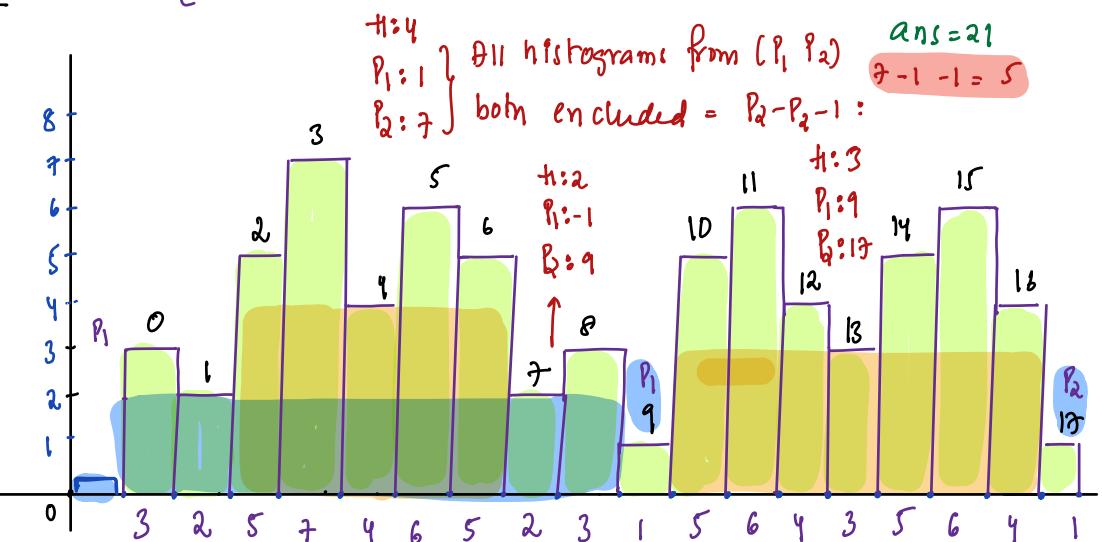
Given Continuous block of histogram find max Rectangular area

Note: Every histogram is of width = 1 which can be present within in histograms

$$\text{Ex1: } \text{ar}[c] = \{2, 4, 3, 4, 5, 1\} \text{ area} = 12$$



$$\text{Ex2: } \text{ar}[] = \{3, 2, 5, 7, 4, 6, 5, 2, 3, 1, 5, 6, 4, 3, 5, 6, 4, 1\}$$



Obs1: Height of a rectangle should be one of the height of histogram

Ideal: for every histogram height take it as rectangle height

: Iterate on right q get first small index whose value is $\text{rectangle height} = P_2$

: Iterate on left q get first small index whose value is $\text{rectangle height} = P_1$

: area = min(ans, ($P_2 - P_1 - 1$) * height) // current rectangular height

int Rectarea(int hist[n]) { TC: O(N+N+N) = O(N) SC: O(n+n) = O(N)

int left[] = stsmall index left(hist[7])

// if no smaller on left initialize with -1

int right[] = ^{fr}small index right(hist[7])

// if no smaller in right initialize with N

area = 0

i = 0; i < n; i++) { // consider every histogram rectangle height

int h = hist[i] // height of histogram

// ^{fr}small index on left & ^{fr}small index in right

int p₁ = left[i]

int p₂ = right[i]

area = max(area, $(p_2 - p_1 - 1) * h$)

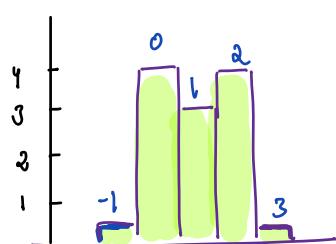
3

return area;

3

Edge Case:

$$\text{Ex: arr[3] = } \begin{matrix} 0 & 1 & 2 \\ 4 & 3 & 4 \end{matrix}$$



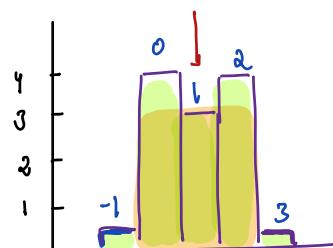
p₁: left: -1 | -1 | 1

p₂: right : 1 | -1 | -1

{p₂ - p₁ - 1} : 1 | -1 | -3

wPath : 1 | -1 | -3

{It cannot be negative}



p₁: left: -1 | -1 | 1

p₂: right : 1 | 3 | 3

wPath : 1 | 3 | 1

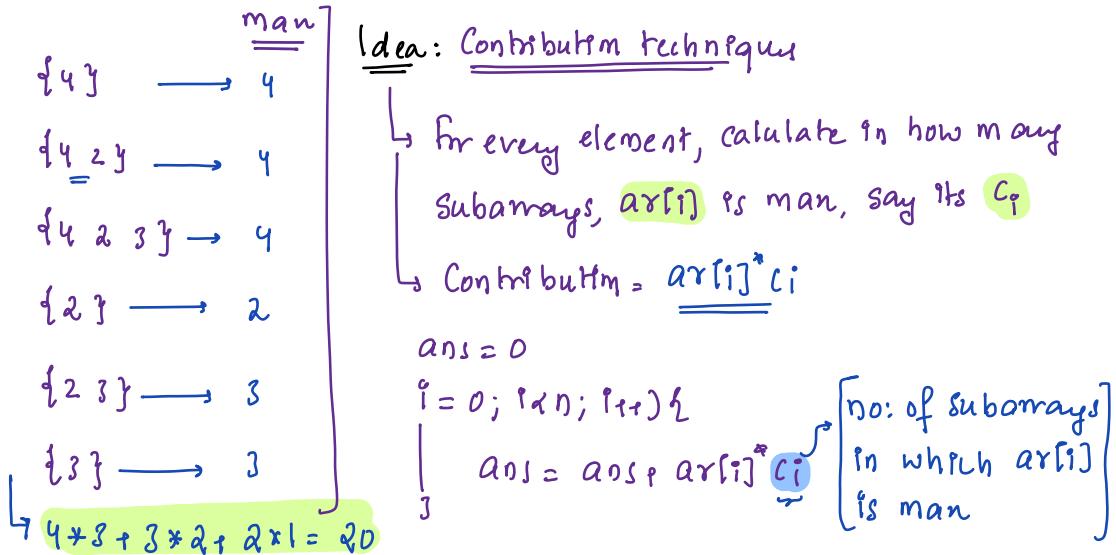
$$3 - (-1) - 1 \\ 3 + 1 - 1 = 2$$

①

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Q8) Given $\text{arr}[N]$ distinct elements sum of man of every subarray

Ex: $\text{arr}[3] = \{4, 2, 3\}$ ans = 20



Ex1: $\text{arr}[7] = \{1, 3, 2, 6, 4, 3, 8\}$

	0	1	2	3	4	5	6	7	8	9
P_1	10	10	8	5	6	6	7	8	9	10
$S = i - P_1$	5	4	2	1	0	1	2	3	4	5
$i [l = P_2 - i]$	6	7	8	9	10	11	12	13	14	15
P_2	1	2	3	4	5	6	7	8	9	10

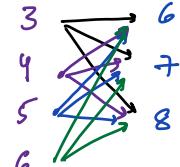
s e # count of subarrays = 12

$S = i - P_1$ # $l = P_2 - i$ # $c_g = s * e = (P_2 - P_1) * (P_2 - i)$

$P_1 = i^{th}$ greater index in left
Initialize with -1

$P_2 = i^{th}$ greater index in right

Initialize with N



`int minSub(int arr[N])` ↳ **TC: O(N) SC: O(N)**

{
 |
 | TODO
 | }
 |

→ Sum of min of every subarray : TODO ✓

→ If elements are not distinct: {**Edge Case**}

 → Sum of max of every subarray : TODO ✓

 → Sum of min of every subarray : TODO ✓

→ **golang:**

- o → Struct
- o → pointers
- o → pointers as member in struct
- o → linked list in go-lang

Doubts: