

Todays Content: Pre-requisites: Recursion

- Back Tracking
- All numbers
- Subset sum
- Generate all permutations

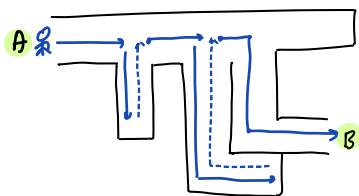
} Happy New Year Everyone

- Will share my
- : Heaps: 2
- : Greedy

Notes + pen links in message

Backtracking: Generating all solutions using recursion: Backtracking

Maze:



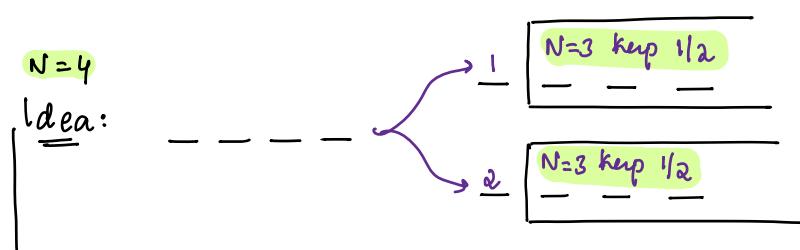
- 1) All Subsets
- 2) All permutations
- 3) All Combinations

Idea: Generating solutions, choose path but we cannot go any further, come back & take another path.

18) Given N digits print all N digit numbers formed only by 1 & 2
in increasing order of numbers

N:2 :	<u>1</u> <u>1</u>	N:3 :	<u>1</u> <u>1</u> <u>1</u>
	<u>1</u> <u>2</u>		<u>1</u> <u>1</u> <u>2</u>
	<u>2</u> <u>1</u>		<u>1</u> <u>2</u> <u>1</u>
	<u>2</u> <u>2</u>		<u>1</u> <u>2</u> <u>2</u>
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			<u>2</u> <u>2</u> <u>1</u>
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Idea: 1. Using queue.
 : Please Queue notes
2. Using bit manipulations

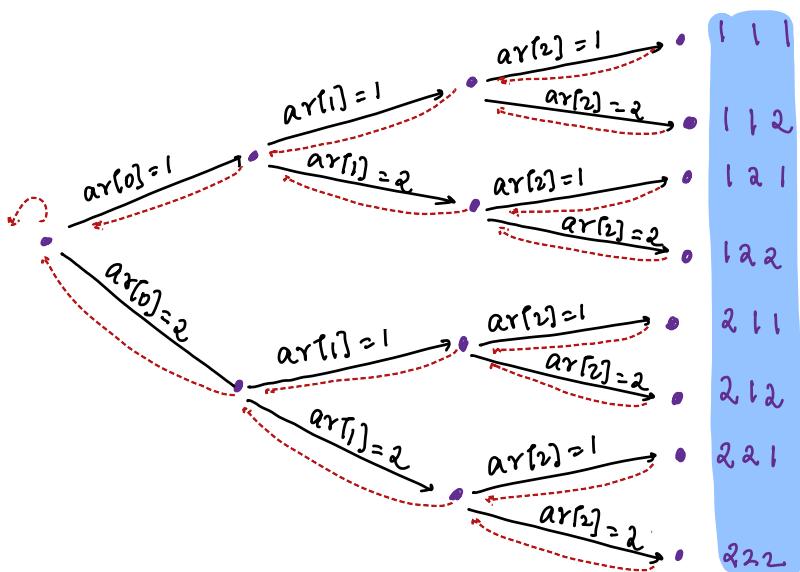


// Generate all n digit numbers using recursion: Backtracking

Tracing : $N=3$

End of path

0 1 2 3 $ary[3] = \begin{matrix} 0 & 1 & 2 \\ 2 & 2 & 2 \end{matrix}$



func:

→ current present we are at

- parameters: $ar[N]$ i \rightarrow size can indicate end
- Subproblems: 2
how many subproblem a single problem has $2 \times 2 \times 2 \times \dots = 2^N$ N digit numbers
- return type: void

10: 25 pm

void printAll(int ar[], int i, int N) { TC: $O(2^N \times N)$ SC: $O(N + N)$

```
if (i == N) {  
    print ar[]  
    return;  
}
```

```
// At ith index choice  
ar[i] = 1  
printAll(ar, i+1, n)  
ar[i] = 2  
printAll(ar, i+1, n)
```

main() {

```
int ar[N] = {0}  
printAll(ar, 0, N)
```

↳ Every function call will have its own copy
(e.g. N : pass by value)

All functions will use same array.
: pass by reference

→ arr[] → map → pass an object it's pass
→ list → → by reference
int ar[] = new int[]
HashMap<int, int> = new HashMap<>
ArrayList<int> = new ArrayList<>

: primitive datatypes

: int / float / double / long ...

array ↗ call stack
size ↘

```
main() {  
    int ar[3] = {0};  
    printAll(ar, 0, 3)  
}
```

ar[3] = {1} }

```
void printAll(ar[], i=0, N=3)  
if (i == N) { print ar[] return; }  
ar[i] = 1  
printAll(ar, i+1, n)  
ar[i] = 2  
printAll(ar, i+1, n)
```

3

printAll

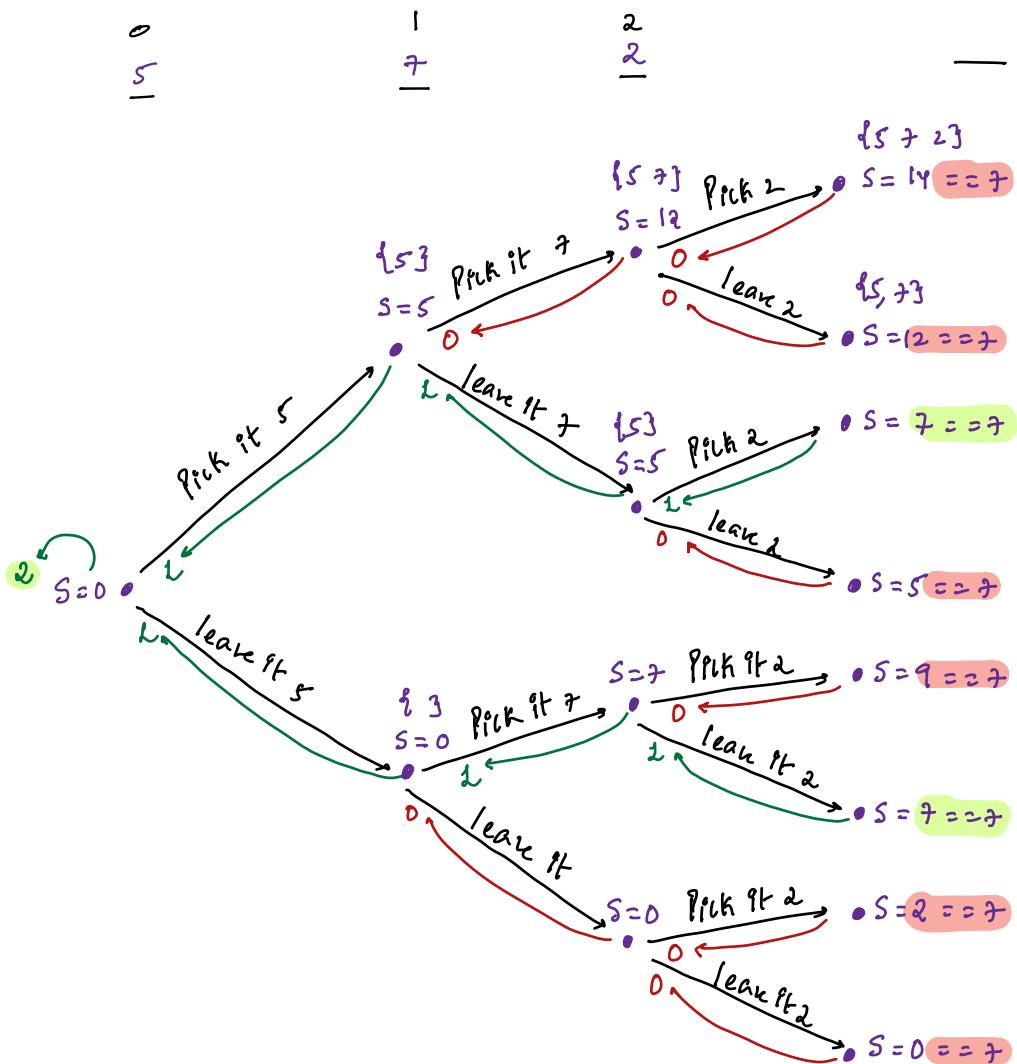


Q) Given $\text{arr}[N]$ elements, count of subsets with sum == k

Ex1: $\text{arr}[3] = \{ 5, 7, 2 \}$ $k=7$, ans=2

Subsets: $\{5, 2\} \{7\}$

Idea: Generate all subset sums == k
 : backtracking



Parameters: arr[N], i, N, sum, k

SubProblems: 2

return type: int : count of subsets

int countSubSumC(int arr[], int N, int k, int i, int sum) {

 if (i == N) {
 if (sum == k) { return 1 }
 else { return 0 }
 }

$\left\{ \begin{array}{l} TC: 2^N * 1 \\ SC: O(N): \text{Stack size} \end{array} \right.$

// At i^{th} index choices

undoping update on sum
[
 sum = sum + arr[i] // Picking i^{th} ele sum gets updated
 int $c_1 = \text{countSubSum}(arr, N, k, i+1, \text{sum})$ // Subsets with sum = k
 sum = sum - arr[i] // Leave i^{th} ele sum we are reducing
 int $c_2 = \text{countSubSum}(arr, N, k, i+1, \text{sum})$ // Subsets with sum = k
 return $c_1 + c_2$
]

Note: In back tracking

: variable updates

fun(— , — , —)

: undo updates in above variable

// Given arr[N] distinct elements print all permutations:
 \downarrow
 $\text{arr[3]} = \{6, 9, 14\}$

} Backtracking
 all arrangements

Permutations / arrangements } for n elts = $\frac{N \times N-1 \times N-2 \times N-3 \times \dots \times 1}{N!}$
 \downarrow
 $\begin{array}{ccc} 6 & 9 & 14 \\ \underline{-} & \underline{-} & \underline{-} \\ 6 & 14 & 9 \end{array}$

$\begin{array}{ccc} 9 & 6 & 14 \\ \underline{-} & \underline{-} & \underline{-} \\ 9 & 14 & 6 \end{array}$ parameters: arr[], i, N

$\begin{array}{ccc} 9 & 14 & 6 \\ \underline{-} & \underline{-} & \underline{-} \\ 14 & 6 & 9 \end{array}$ subproblems: At i^{th} index we swap with all indices from $[i, N-1]$

$\begin{array}{ccc} 14 & 9 & 6 \\ \underline{-} & \underline{-} & \underline{-} \end{array}$ return type: void

void allpermute(int arr[], int N, int i){

if ($i == n$) {
 print(arr[]);
 return;
}}

TC: $(N! * N)$

SC: $O(N)$

// At i^{th} index choices = Swap i^{th} index = $[i, N-1]$

$j = i; j < n; j++$ } // choices

// at $arr[i]$ we want $arr[j]$

Swap $arr[i] \leftrightarrow arr[j]$ // fix i^{th} index with $arr[j]$

allpermute(arr, N, i+1)

Swap $arr[i] \leftrightarrow arr[j]$ // undo update

$$\text{ar}[3] = \{6 \ 9 \ 14\}$$

tn
0

$$\underline{0} : \underline{0} \mid 2$$

1 : 1 2

$$\frac{2}{4} : \frac{2}{4}$$



0 1 2
6 9 14?

11

1

1

111

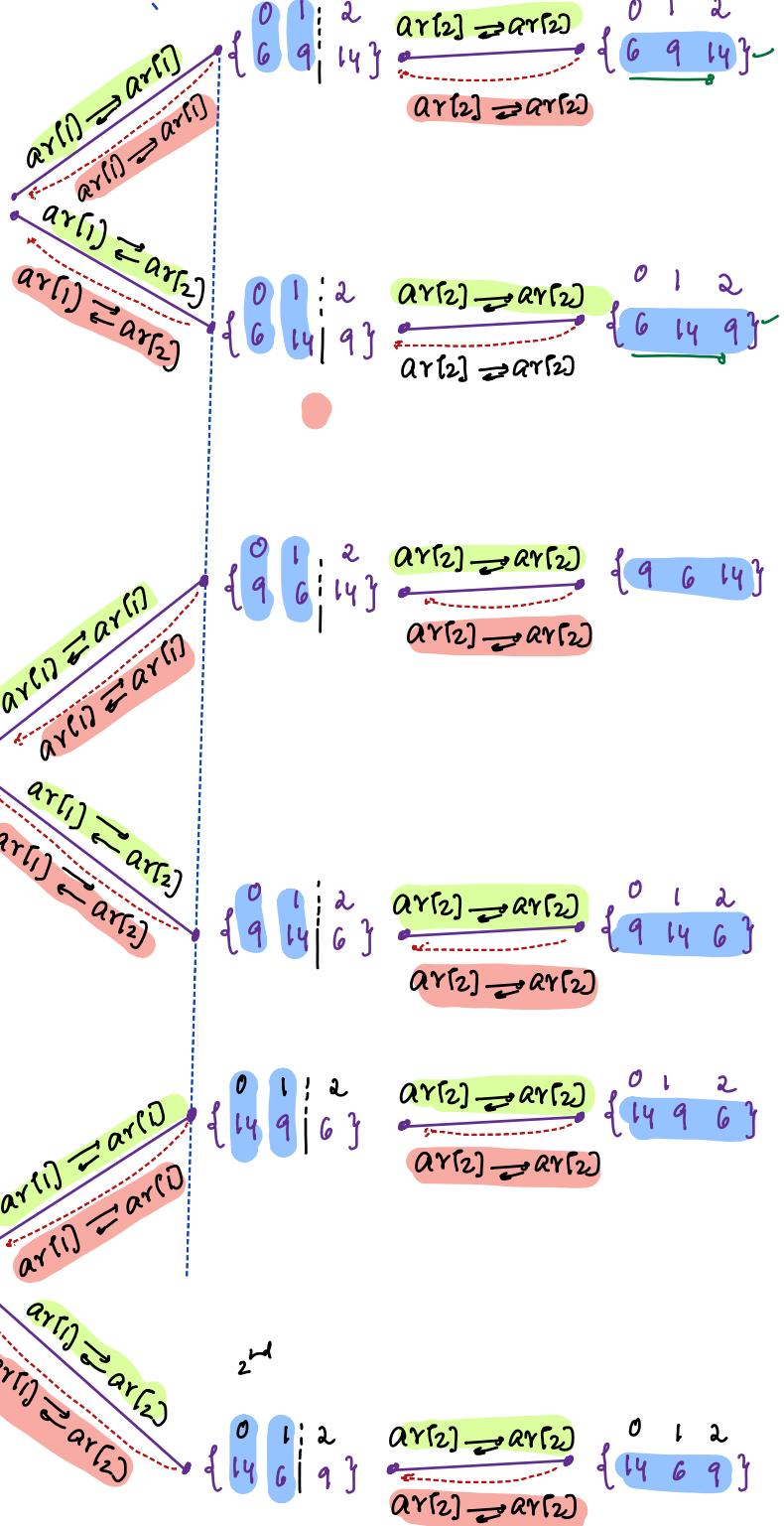
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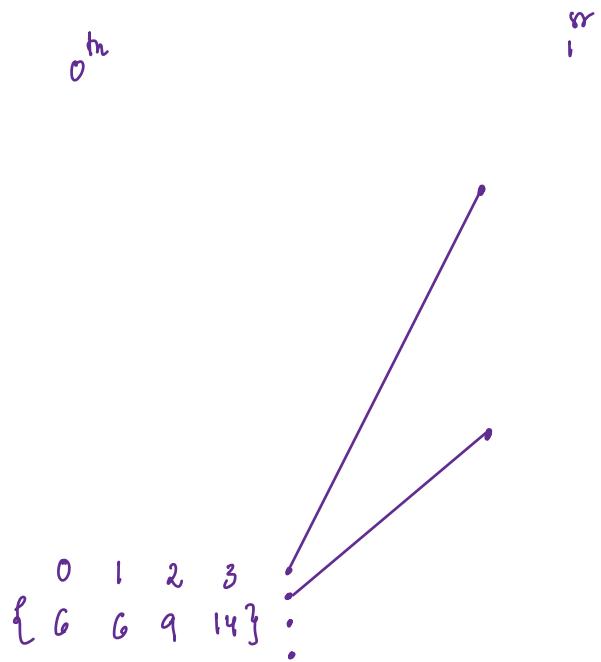
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2



Permutations with Repetition : TODD array duplicates, get all distinct permutations

$$arr[4] = \{ 6 \ 6 \ 9 \ 14 \}$$



$$ar[4] = \{6, 6, 9, 14\}$$

$$\{6:2, 9:1, 14:1\}$$

0 1 2 3

