

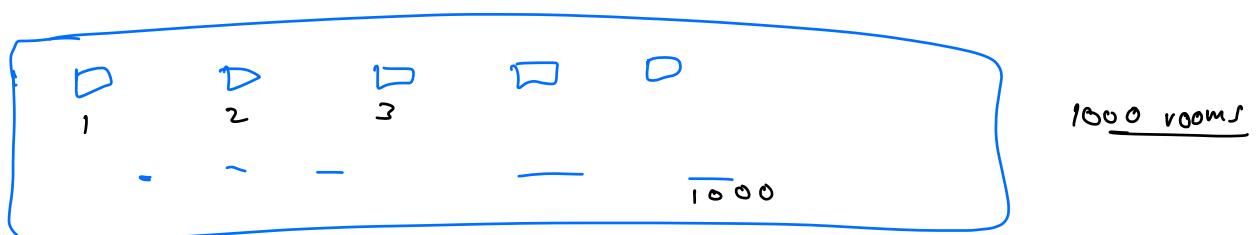
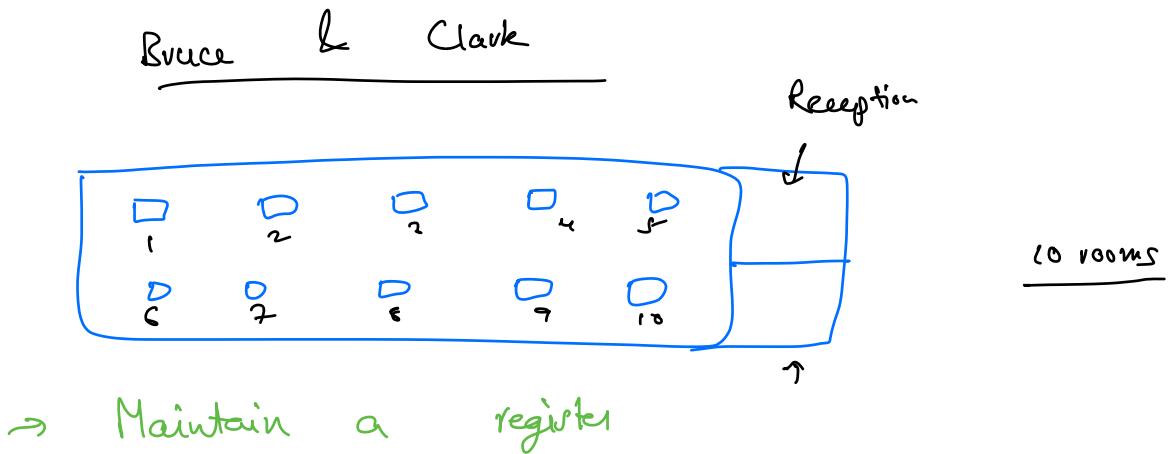
Hashing 1

Agenda

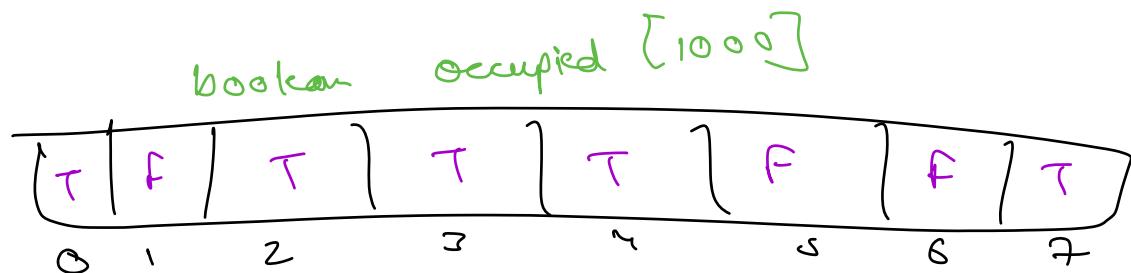
- ✓ Introduction
- {• Frequency Count
- First Non Repeating Element
- Subarray with sum=0

Arrays

What is Hashing ?



boolean array



Covid Pandemic

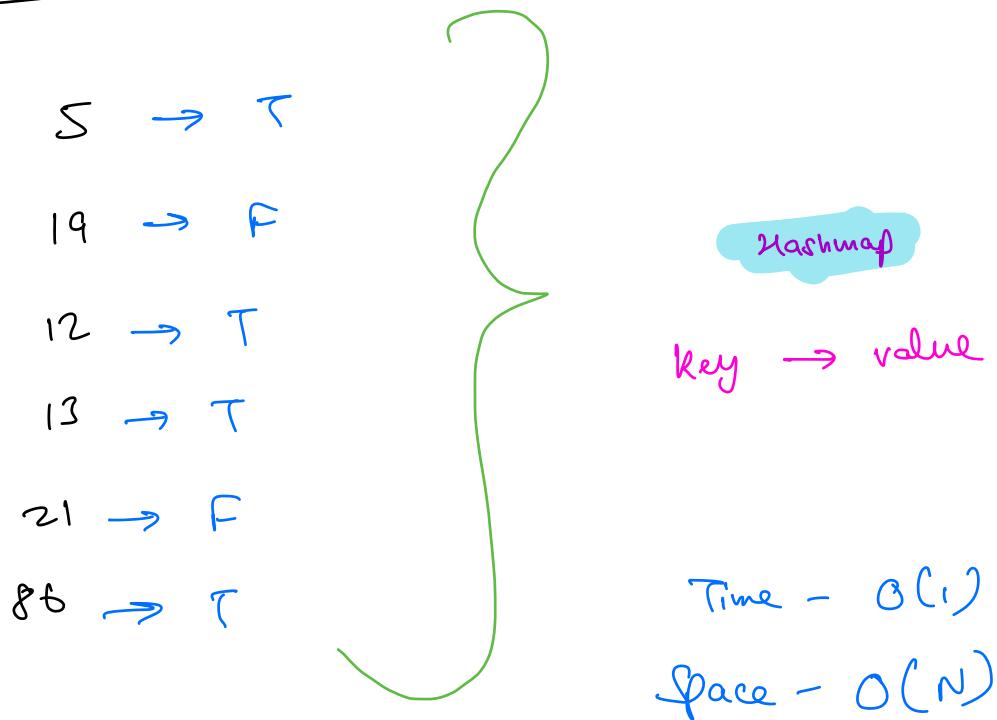
Went to a numerologist.

Lucky Numbers between $[1, 10^9]$

Numbers - 5, 9, 12, 13, 21, 25, ..., 1002,
 $10^5, 10^6, 10^7$ -

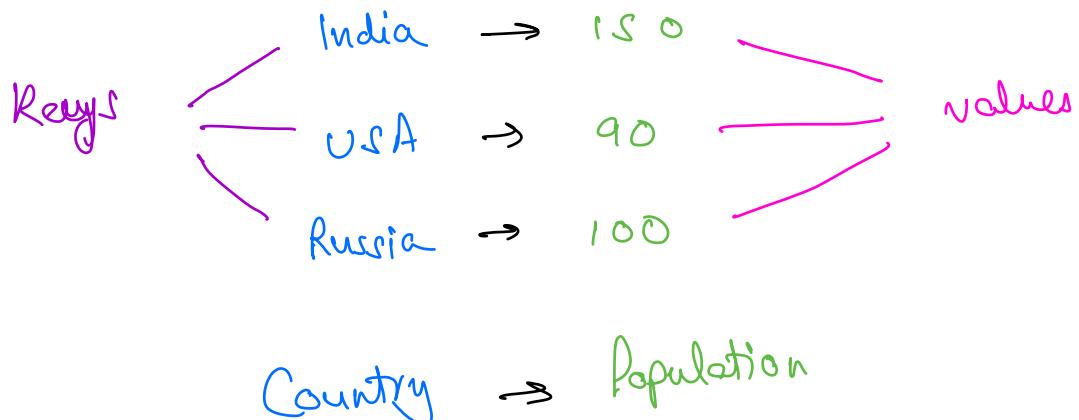
boolean occupied $[10^9]$ \leftarrow very large space

Advantage: $O(1)$ time
fast access



Understanding key-value

Q1. Store population of every country



HashMap <str , int >

Q2. No of states in each country

India → 29
USA → 50
Russia → 60

Keys values

HashMap <str , int >

Q3. For every country, store all state names

Country → list [states]

HashMap < str, Array < str > >

Q4. For every country, store population of each state.

Country → HashMap < string, int >
Population of each state

India → {
Punjab: 1000 >
TN: 2000
Kerala: 3000
}

Hashmap Operations

{ insert(Key, value)
 search(Key)
 remove(Key)
 update(key, newValue)
 size() = No of entries

India → 29

USA → 50

Russia → 60

Time : $O(1)$

Space : N operations $\rightarrow \Theta(N)$ space

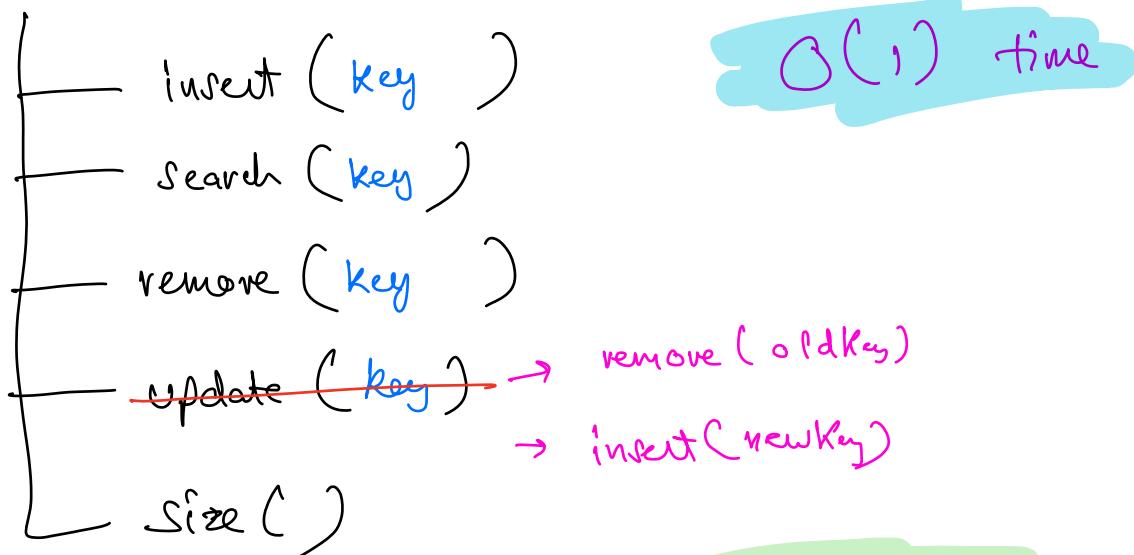
Internal Implementation
(Hashing)

Advanced
Batch

HashSet Operations

It only stores keys.

{ 2, 5, 1, 6, 7, 8 }



Unique Keys

1, 1, 2, 3, 2, 2, 3, 4, 4, 4, 4

Quiz 1

↳ { 1, 2, 3, 4 }

Arrays

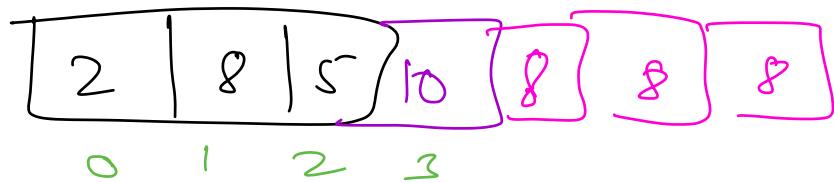
- Ordered DS
- Indexing
- Duplicate data

Set

- Unordered DS
- No indexing
- Unique keys

→ Time Complexities
- $O(N)$

→ Time Complexities
- $O(1)$



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2, δ_1 ,
S
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Language Implementation

	<u>Java</u>	<u>Python</u>	<u>C++</u>
<u>Hashmap</u>	HashMap	dict	unordered_map
<u>Hashset</u>	HashSet	set	unordered_set

Q1 Frequency of Numbers

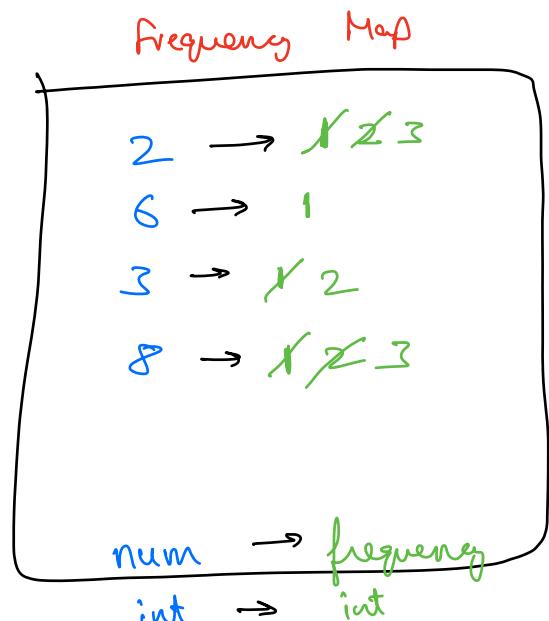
Given N array elements & Q queries. For each query find frequency of each element in array.

$$arr[10] = \{2, 6, 3, 8, 2, 8, 2, 3, 8\}$$

Q = 4
query
2 : 3
8 : 3
3 : 2
5 : 0

Brute Force

- 1) For each query, iterate & get the count.



TC: O(Q * N)

SC: O(1)

Optimised Approach

HashMap <int, int> freq;

// Iterate & store the frequencies

for (i=0; i<N; i++) {

// Insert ar[i] in my hashmap

if (ar[i] in freq)

update value by +1

else

insert (ar[i] → 1)

}

// Answer the queries

for (i=0; i<Q; i++) {

query = input()

if (query is in freq)

print(freq[query])

else

print(0)

}

Java

```

● ● ●
import java.util.Scanner;
import java.util.HashMap;

public class Frequency {
    public static void main(String[] args) {
        int[] arr = { 2, 5, 6, 1, 7, 8, 9, 2, 7, 5, 10, 8 };
        HashMap<Integer, Integer> freq = new HashMap<Integer, Integer>();

        for (int i = 0; i < arr.length; i++) {
            if (freq.containsKey(arr[i])) {
                freq.put(arr[i], freq.get(arr[i]) + 1);
            } else {
                freq.put(arr[i], 1);
            }
        }

        // Answer Q queries
        Scanner sc = new Scanner(System.in);
        int Q = sc.nextInt();
        while (Q-- > 0) {
            int query = sc.nextInt();
            if (freq.containsKey(query)) {
                System.out.println(freq.get(query));
            } else {
                System.out.println(0);
            }
        }
    }
}

```

Python

```

● ● ●
arr = [2, 5, 6, 1, 7, 8, 9, 2, 7, 5, 10, 8]

freq = {} ← did
for i in range(len(arr)):
    if arr[i] in freq:
        freq[arr[i]] += 1
    else:
        freq[arr[i]] = 1
} O(N)

# Answer Q queries
Q = int(input())
for _ in Q:
    query = int(input())
    if query in freq:
        print(freq[query])
    else:
        print(0)
} O(Q)

```

Time = $O(N+Q)$
 Space = $O(N)$

Break Hill 10:21 PM

Q2 Find the first non repeating element.



Example 1

Quiz 2

$$ar[6] = 1 \ 2 \ 3 \ 1 \ 2 \ 5$$

$1 \rightarrow 2$

$2 \rightarrow 2$

$3 \rightarrow 1$

$5 \rightarrow 1$

Ans = 3

Example 2

$$ar[8] = 4 \ 3 \ 3 \ 2 \ 5 \ 6 \ 4 \ 5$$

$4 \rightarrow 2$

$3 \rightarrow 2$

$2 \rightarrow 1$

$5 \rightarrow 2$

$6 \rightarrow 1$

Ans = 2

Example 3

$$ar[7] = 2 \ 6 \ 8 \ 4 \ 7 \ 2 \ 9$$

Ans = 6

Idea & Pseudocode

Brute force - N^2

- 1) Construct the frequency map
- 2) Iterate over the array, get the first element with freq = 1

TC : $O(N)$

SC : $O(N)$

Java

```
import java.util.HashMap;

public class FirstNonRepeating {
    public static void main(String[] args) {
        int[] arr = { 1, 2, 3, 1, 2, 5 };
        HashMap<Integer, Integer> freq = new HashMap<Integer, Integer>();
        for (int i = 0; i < arr.length; i++) {
            if (freq.containsKey(arr[i])) {
                freq.put(arr[i], freq.get(arr[i]) + 1);
            } else {
                freq.put(arr[i], 1);
            }
        }

        for (int i = 0; i < arr.length; i++) {
            if (freq.get(arr[i]) == 1) {
                System.out.println(arr[i]);
                break;
            }
        }
    }
}
```

Python

```
arr = [1, 2, 3, 1, 2, 5]

freq = {}

for i in range(len(arr)):
    if arr[i] in freq:
        freq[arr[i]] += 1
    else:
        freq[arr[i]] = 1

for i in range(len(arr)):
    if freq[arr[i]] == 1:
        print(arr[i])
        break
```

Q3 Given N array elements, find no. of distinct elements.

Example 1

$\text{arr}[5] = 3 \quad 5 \quad 6 \quad 5 \quad 4$

$\left\{ \begin{array}{l} 3, 5, 6, \\ 4 \end{array} \right\} \Rightarrow 4$

Example 2

Quiz 3

$\text{arr}[7] = \underline{6} \quad \underline{3} \quad \underline{7} \quad 3 \quad \underline{8} \quad 6 \quad \underline{9}$

$\left\{ \begin{array}{l} 6, 3, \\ 7, 8, 9 \end{array} \right\} \Rightarrow 5$

Hashset

```
Hashset<int> hs;
for (i=0; i<N; i++) {
    hs.insert(arr[i])
}
return hs.size()
```

Java

```
●●●●●  
import java.util.Arrays;  
import java.util.HashSet;  
  
public class UniqueElements {  
    static int countOfUnique(Integer[] arr) {  
        HashSet<Integer> set = new HashSet<Integer>();  
        for (int i = 0; i < arr.length; i++) {  
            set.add(arr[i]);  
        }  
        return set.size();  
    }  
  
    static int countOfUniqueShort(Integer[] arr) {  
        HashSet<Integer> set = new HashSet<Integer>(Arrays.asList(arr));  
        return set.size();  
    }  
  
    public static void main(String[] args) {  
        Integer[] arr = { 6, 2, 4, 7, 4, 4, 2, 6, 1 };  
        System.out.println(countOfUnique(arr));  
  
        System.out.println(countOfUniqueShort(arr));  
    }  
}
```

Python

```
●●●●●  
def countOfUnique(arr):  
    s = set()  
    for i in range(len(arr)):  
        s.add(arr[i])  
    return len(s)  
  
def countOfUniqueShort(arr):  
    s = set(arr)  
    return len(s)  
  
arr = [6, 2, 4, 7, 4, 4, 2, 6, 1]  
print(countOfUnique(arr))  
print(countOfUniqueShort(arr))
```

$\text{TC} : \mathcal{O}(n)$
 $\text{SC} : \mathcal{O}(n)$

Q4 Given N array elements, check if they are all distinct or not.

Example 1

2 5 4 9 \Rightarrow True

Example 2

2 9 8 2 6 \Rightarrow False

Example 3

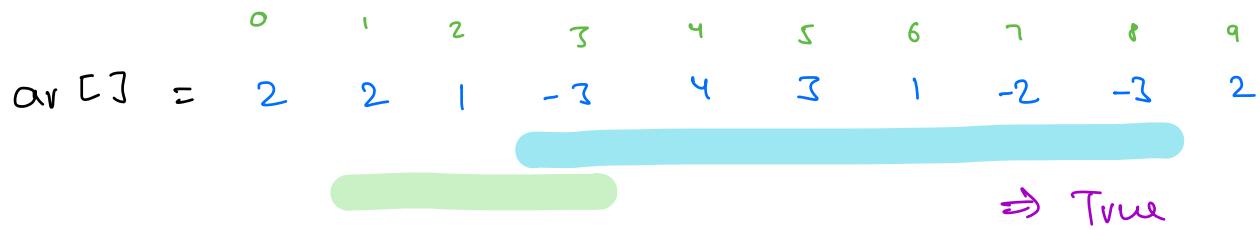
5 8 6 10 8 6
 \Rightarrow False

if (countOfUnique(arr) == N)
 return True

else

 return False

Q5 Given N array elements, check if there exists a subarray with sum=0.



$$\text{No of subarrays} = \frac{N(N+1)}{2}$$

Quiz 4

Idea

- 1) For every subarray, check if $\text{sum} = 0$
↳ $O(N^3)$
- 2) optimisation: Carry forward
↳ $O(N^2)$
- 3) Prefix Sum

Quiz 5

$$\text{sum}[L \dots R] = \text{pf}[R] - \text{pf}[L-1]$$

	0	1	2	3	4	5	6	7	8	9
$\text{ar}[i] =$	2	2	1	-3	4	3	1	-2	-3	2
$\text{pf}[i] =$	2	4	5	2	6	9	10	8	5	7

$$\text{pf}[2] = 5 = \text{sum}[0 \dots 2]$$

$$\text{pf}[8] = 5 = \text{sum}[0 \dots 8]$$

$$\Rightarrow 5 = \text{sum}[0 \dots 2] + \text{sum}[3 \dots 8]$$

$$\Rightarrow 5 = 5 + \text{sum}[3 \dots 8]$$

$$\Rightarrow 5 - 5 = \text{sum}[3 \dots 8]$$

$$\Rightarrow 0 = \text{sum}[3 \dots 8]$$

$$pf[0] = 2 = \text{sum}[0 \quad 0]$$

$$pf[3] = 2 = \text{sum}[0 \quad 3]$$

$$\Rightarrow 2 = \text{sum}[0 \quad 0] + \text{sum}[1 \quad z]$$

$$\Rightarrow 2 = 2 + \text{sum}[1 \quad z]$$

$$\Rightarrow 2 - 2 = \text{sum}[1 \quad z]$$

$$\Rightarrow 0 = \text{sum}[1 \quad z]$$

Idea

If we have repetition in the prefix
sum array, ans \rightarrow True

- 1) Construct pf [] away ← TODO
- 2) Create a hashset & insert all values of pf [] in it.
- 3) if (hs.size () < N or (0 in hs))

Repetition → True

 else

No repetition → False

This will NOT WORK

	0	1	2	3
arr [] =	-1	4	-3	2
pf [] =	-1	3	0	2

pf [2] = 0 \Rightarrow sum [0 2] = 0

Java

```
● ● ●  
boolean checkSubarrayWithZeroSum(int[] arr) {  
    HashSet<Integer> s = new HashSet<Integer>();  
  
    int prefixSum = arr[0];  
    s.add(prefixSum);  
  
    for (int i = 1; i < arr.length; i++) {  
        prefixSum += arr[i];  
        s.add(prefixSum);  
    }  
  
    if (s.size() < arr.length || s.contains(0)) {  
        return true;  
    }  
  
    return false;  
}
```

Python

```
● ● ●  
def checkSubarrayWithZeroSum(arr):  
    s = set()  
  
    prefixSum = arr[0]  
    s.add(prefixSum)  
  
    for i in range(1, len(arr)):  
        prefixSum += arr[i]  
        s.add(prefixSum)  
  
    if len(s) < len(arr) or (0 in s):  
        return True  
  
    return False
```

TC : $O(N)$

SC : $O(N)$

Doubts

Thank
You

Keys → immutable
int, str, tuple, float, bool
~~list, set, dict~~

values → Anything

Good
Night

Thank
You

Wednesday