

Todays Content:

- Sorting Basics , Stable Sorting
- Selection Sort
- Bubble Sort
- Merge Sort
 - a) Merge 2 sorted arr[]
 - b) Merge 2 sorted arr[] in single arr[]

Sorting: arranging data in increasing order based on parameter

1 2 3 5 7 : inc, parameter = value

9 6 3 2 1 : dec, parameter = value

1 7 2 9 24 : inc based on no. of factors
↓ ↪ ↪ ↪ ↪
1 2 2 3 8

Why sorting: Searching becomes easier

Stable/unstable: When 2 data points have same parameter

value & their relative order is same after sorting {Stable sorting Algo}
→ parameter

: sort data increasing order based on marks

Name	Marks
Mohit	0
Aman	100
Shrest	45
kajal	32
Aayush	45
Aditya	92

Name	Marks
Mohit	0
kajal	32
Shrest	
Aayush	
Shrest	
Aayush	

Case-I sort A Case-II sort B

↓

Stable Sorting

Ex2: arr[5] = 1 5 2 6 2

Stable / Not

After Sort 1 = 1 2 2 5 6 : Stable

After Sort 2 = 1 2 2 5 6 : Unstable

Inplace Sorting: If sorting algo takes O(1) space in that case it is considered as Inplace sorting algo

(Q) Given $\text{arr}[N]$ elements, find k^{th} smallest elements: {repeat}



Return $\text{arr}[k-1]$ index element, when $\text{arr}[]$ sorted?

$\text{arr}[8] =$	0	1	2	3	4	5	6	7	8	$k=3$	$k=4$	$k=7$	$k=2$	$k=1$
	2	8	4	-1	6	7	5	10	-1	2	4	7	5	-1

Idea: Sort $\text{arr}[]$ & return $\text{arr}[k-1]$ $\text{TC: } O(N \log N)$

Idea2: Iterate in $\text{arr}[]$ find min keep it at its correct pos
repeat above proc k times $\text{TC: } O(N^k)$ $\text{SC: } O(1)$

$k=4:$

$\text{arr}[8] =$	0	1	2	3	4	5	6	7	8	$i=0$	\min	ind	$\text{swap}(- -)$
	2	8	5	-1	6	7	4	10	-1		-1	3	$\text{swap}(\text{arr}[3], \text{arr}[0])$
											-1	8	$\text{swap}(\text{arr}[8], \text{arr}[1])$
													$\text{swap}(\text{arr}[3], \text{arr}[2])$
													$\text{swap}(\text{arr}[6], \text{arr}[5])$
													return arr[2]

Selection Sort (int $\text{arr}[N]$, int k) { $\text{TC: } O(N^k)$ $\text{SC: } O(1)$ }

$i = 0; i < N; i = i + 1\{$

// Iterate from $[i, N-1]$ & calculate min & ind

$\min = \text{arr}[i], \text{ind} = i$

$j = i; j < n; j + +\{$

if ($\text{arr}[j] < \min$) {

$\min = \text{arr}[j], \text{ind} = j$

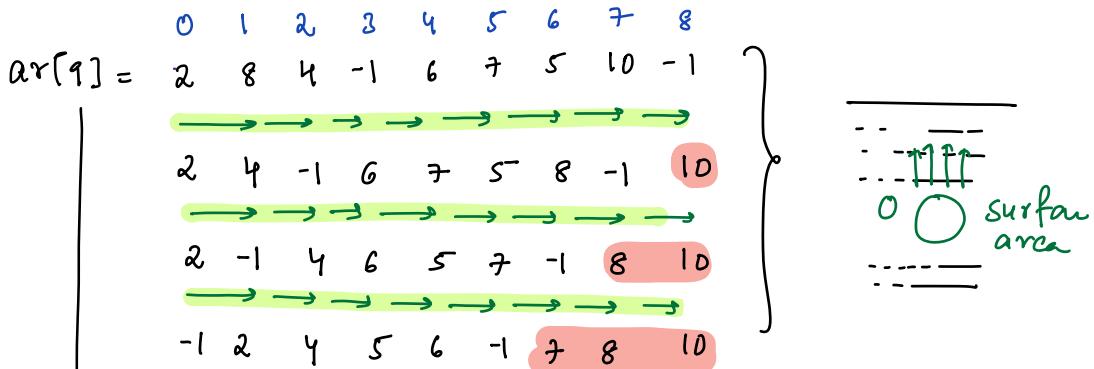
$\text{swap}(\text{arr}[\text{ind}], \text{arr}[i]) // \text{swap do on your own}$

Inplace sorting algorithm

Ex: 	0	1	2	3	\min	ind
	2	4	2	1	1	3
	1	4	2	2	2	2
	1	2	4	2	2	3
	1	2	2	4		

make it.
not stable algo \rightarrow TODO stable

Q8) $\text{arr}[N]$, we can only swap adj^g elements sort $\text{arr}[]$ inc



Repeat above proc N times to make entire data sorted

bubbleSort (int arr[N]) { TC: O(N²) SC: O(1) }

↳ in-place sorting algo

i = 0; i < N; i++) {

 int c = 0 → TODO: modification possible

 j = 0; j < N-1; j++) { → incorrect order

 if (arr[j] > arr[j+1]) { f = N-1 ⇒ arr[N-1] & arr[N] }

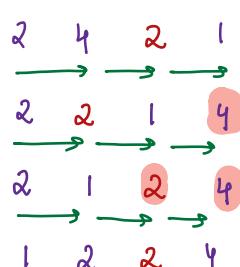
 swap(arr[j] & arr[j+1])

 c = c + 1

 }

 if (c == 0) { break } → 10:25 → 10:35 break

Ex: Stability



Stable sorting algo

Note:

arr[5]: 0 1 2 3 4
3 | 6 10 8

→ → → →

1 3 6 8 10 : 2 swaps

→ → → →

1 3 6 8 10 : 0 swaps

In a iteration Swap = 0, data is already sorted so, break

38) Given 2 sorted arrays, $a[N]$, $b[M]$, create $c[N \times M]$
which contains overall sorted data

$$\underline{\underline{C_1}}: a[4] = \{ 7 \ 10 \ 11 \ 14 \} \quad a[3] = \{ 3 \ 6 \ 10 \}$$

$$b[8] = \{ 3 \ 8 \ 9 \} \quad b[2] = \{ 5 \ 9 \}$$

$$c[7] = \{ 3 \ 7 \ 8 \ 9 \ 10 \ 11 \ 14 \} \quad c[5] = \{ 3 \ 5 \ 6 \ 9 \ 10 \}$$

Ideas 1: $a[N] \rightarrow c[] : O(N)$
 $b[M] \rightarrow c[] : O(M)$

Idea 2: $\cdot x_1 \rightarrow p_1$ // Copy remaining ele

$$\text{En: } a[4]: \left\{ \begin{array}{c} 0 \\ 7 \\ 10 \end{array} \quad \begin{array}{c} 1 \\ 11 \end{array} \quad \begin{array}{c} 2 \\ 14 \end{array} \quad \begin{array}{c} 3 \end{array} \right.$$

$b[3] : \{ 3 \quad 8 \quad 9 \}$ } $\frac{p_2 \rightarrow p_2 \rightarrow p_2}{0 \quad 1 \quad 2} \text{out of array}$

$$c[7] : \{ 3, 7, 8, 9, 10, 11, 14 \}$$

$$Q_n: \quad \begin{array}{c} p_1 \rightarrow p_1 \rightarrow p_1 \rightarrow p_1 \rightarrow p_1 \\ 0 \quad 1 \quad 2 \quad 3 \quad \{ \text{out-of-array} \} \\ a[4]: \quad \{ \quad 2 \quad 8 \quad 10 \quad 14 \} \end{array}$$

$b[5] := \{ 3, 7, 16, 20, 24 \}$

$$C_{[9]} : \left\{ \begin{array}{cccccccccc} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 \\ 2 & 3 & 7 & 8 & 10 & 14 & 16 & 20 & 24 \end{array} \right\}$$

`int[] merge2(int a[N], int b[M]) TC: O(N+M) SC: O(1)`

$$P_1 = 0, P_2 = 0, P_3 = 0$$

`int c[N+M]`

\rightarrow // Both P_1 & P_2 should be in order

`while (P1 < N & P2 < M) { // we break, if one of array completed`

`if (a[P1] <= b[P2]) { // a[P1] should come first`

$$c[P_3] = a[P_1], P_1 = P_1 + 1, P_3 = P_3 + 1$$

$\left| \begin{array}{l} 3 \\ \text{else} \\ 3 \end{array} \right.$

$$c[P_3] = b[P_2], P_2 = P_2 + 1, P_3 = P_3 + 1$$

$\left| \begin{array}{l} 3 \\ \end{array} \right.$

`// copy remaining elements`

`while (P1 < N) { // elements in a[] are left out`

$$c[P_3] = a[P_1], P_1 = P_1 + 1, P_3 = P_3 + 1$$

$\left| \begin{array}{l} 3 \end{array} \right.$

`while (P2 < M) { // elements in b[] are left out`

$$c[P_3] = b[P_2], P_2 = P_2 + 1, P_3 = P_3 + 1$$

$\left| \begin{array}{l} 3 \end{array} \right.$

`return c[]`

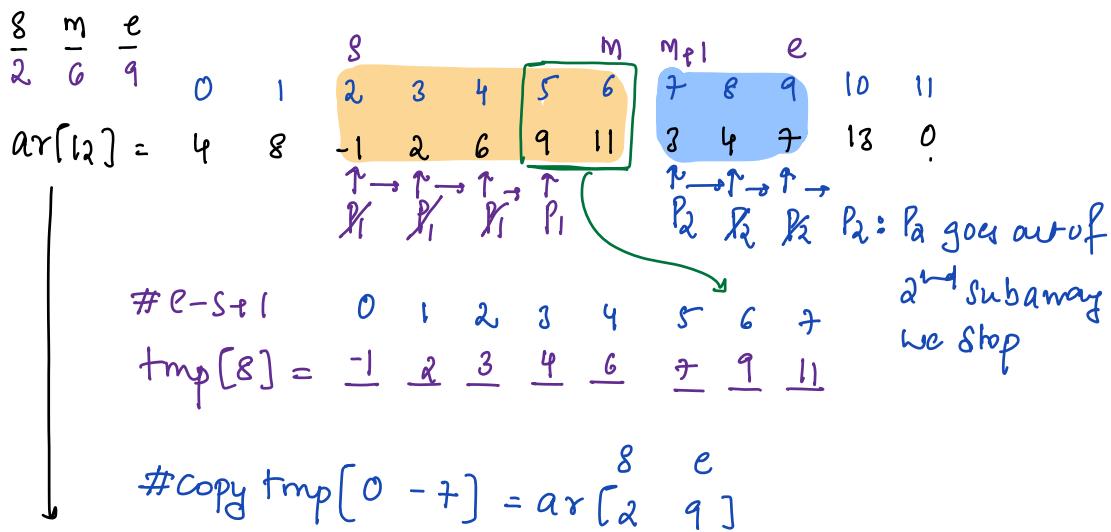
$\left| \begin{array}{l} 3 \end{array} \right.$

Q) Given $ar[N]$ elements & 3 indices, s, m, e

and Subarray $[s \dots m]$ is sorted

Subarray $[m+1 \dots e]$ is sorted

Sort subarray from $[s \dots e]$?



$$ar[12] = [4, 8, -1, 2, 3, 4, 6, 7, 9, 11, 13, 0]$$

PseudoCode:

given $ar[s \dots m]$ sorted & $ar[m+1, e]$ is sorted, sort $\{s \rightarrow e\}$

void merge(int A[], int s, int m, int e) { Tc: O(n) Sc: O(n)

$$P_1 = s, P_2 = m+1, P_3 = 0$$



int c[e-s+1]

\downarrow // Both P₁ & P₂ should be in order

while (P₁ <= m && P₂ <= e) { // we break, if one of array completed

if (a[P₁] <= a[P₂]) { // a[P₁] should come first

$$c[P_3] = a[P_1], P_1 = P_1 + 1, P_3 = P_3 + 1$$

3
else

$$c[P_3] = a[P_2], P_2 = P_2 + 1, P_3 = P_3 + 1$$

3

// copy remaining elements

while (P₁ <= m) { // elements in a[] are left out

$$c[P_3] = a[P_1], P_1 = P_1 + 1, P_3 = P_3 + 1$$

3

while (P₂ <= e) { // elements in b[] are left out

$$c[P_3] = a[P_2], P_2 = P_2 + 1, P_3 = P_3 + 1$$

3

// copy $c[0 \dots j] \rightarrow ar[s \dots e]$

$$i = s, j = 0$$

while (i <= e) {

$$ar[i] = c[j], i = i + 1, j = j + 1$$

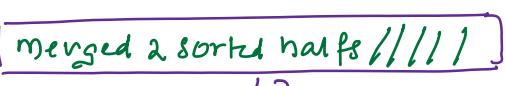
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Q) Given $\text{arr}[N]$ Sort them, no inbuilt sort

$$\begin{array}{c} \text{N} \\ \hline \underline{\underline{100}} \end{array}$$

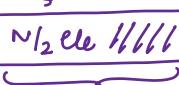
TC: iterations

Case-I:  : $O(N^2) = 10^4$

Case-II:  : $\left[\frac{N}{2}\right]^2 \times 2 + N$

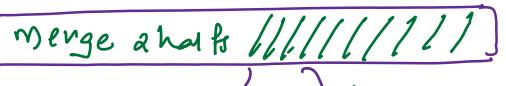
$\xleftarrow{\text{merge } = N}$


 $\left[\frac{N}{2}\right]^2$

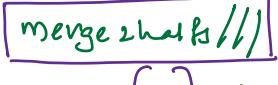

 $\left[\frac{N}{2}\right]^2$

: $\frac{N^2}{2} + N \Rightarrow$

: $\frac{10^4}{2} + 100 \Rightarrow 5100$

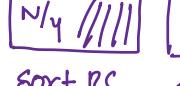
Case-III:  : $\left[\frac{N^2}{4}\right]4 + 2N$

\xleftarrow{N}


 $\left[\frac{N}{2}\right]^2$

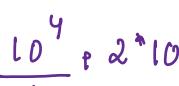

 $\left[\frac{N}{2}\right]^2$

: $\frac{N^2}{4} + 2N$


 $\left[\frac{N}{4}\right]^2$


 $\left[\frac{N}{4}\right]^2$


 $\left[\frac{N}{4}\right]^2$


 $\left[\frac{N}{4}\right]^2$

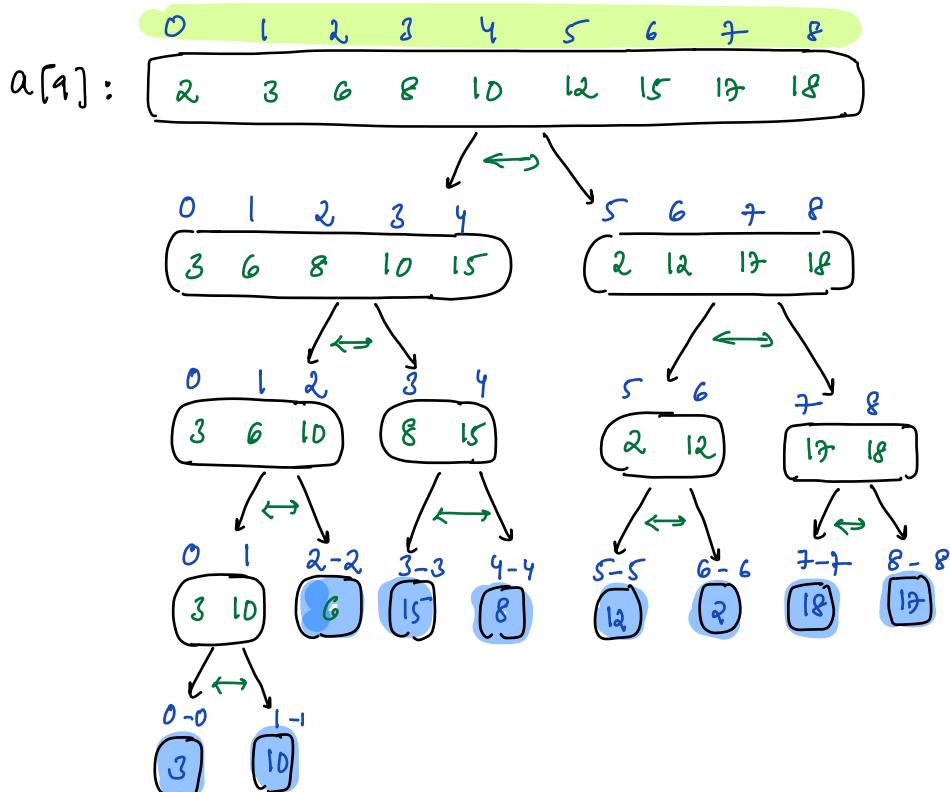
: $N = 100$

: $\frac{10^4}{4} + 2 * 100$

: 2700

Obs: keep dividing arr[] until it has only single element
q start merging \rightarrow { Idea of Merge Sort }

Idea: MergeSort

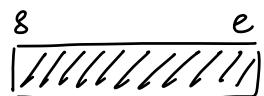


Ass: Given $\text{arr}[]$, sort subarray from $[s-e]$

// pass by reference, same array from

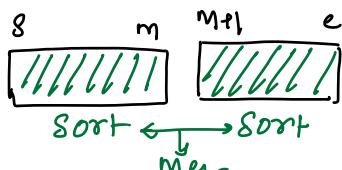
void mergeSort($\text{int arr}[]$, int s , int e) { function calls

if ($s == e$) { // single element
 return;



$$m = (s+e)/2$$

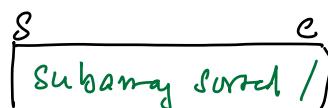
$$m = (s+e)/2$$



mergeSort(arr, s, m) : $f(N/2)$

mergeSort($\text{arr}, m+1, e$) : $f(N/2)$

merge(arr, s, m, e) : N



$$f(N) = 2f(N/2) + N \quad f(1) = 1$$

$Tc: O(N \log N)$

$Sc: O(N)$

$$f(N) = f(N/2) + f(N/2) + N$$

$$f(N) = 2f(N/2) + N \quad f(1) = 1$$

$$\xrightarrow{\quad} \boxed{f(N/2) = 2f(N/4) + N/2}$$

$$= 2 \left[2f(N/4) + N/2 \right] + N$$

$$= 4f(N/4) + 2N = 2^2 f(N/2^2) + 2N$$

$$\boxed{f(N/4) = 2f(N/8) + N/4}$$

$$= 4 \left[2f(N/8) + N/4 \right] + 2N$$

$$= 8f(N/8) + 3N = 2^3 f(N/2^3) + 3N$$

$$\boxed{f(N/8) = 2f(N/16) + N/8}$$

$$= 8 \left[2f(N/16) + N/8 \right] + 3N$$

$$= 16f(N/16) + 4N = 2^4 f(N/2^4) + 4N$$

After k Substitutions =

$$f(N) = 2^k f(N/2^k) + kN \rightarrow f(1) = 1$$

$$\frac{N/2^k}{2^k} = 1 \Rightarrow 2^k \geq N \Rightarrow k = \log_2^N$$

$$Nf(1) + \log_2^N N \in O(N \log N)$$

$$\underline{f(N) = O(N \log N)}$$

Beginer → May 22 Java Monday -1

Intermediate → Jun 22 Intermediate Morning -1

Raise it in support & get recordings