

↳ Sughest

↳ DTU grad.

↳ 5* on codechef. (ICPC) ^{→ yellow} _{→ CP}

↳ Content creator. {CP, graph, Hashmap} → 21m views
↳ Per coding

↳ 3 yrs+ teacher

↳ SDE & Instructor

↳ Advanced batch exp.

Today's agenda

↳ N sorted array

↳ Given 2 sorted array find K smallest pair sum

Q) Given 2D $\text{mat}[N][M]$, every row is sorted, merge entire data into 1D sorted list and return sorted list.

Ex: $\text{mat}[4][6]$

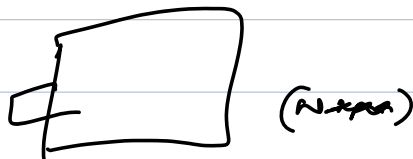
2	7	10	17	25	34
-6	0	1	8	11	16
3	4	6	14	21	26
7	10	14	19	23	27

//idea1

↳ Insert all the elements in a dynamic array and sort.

T.C: $O(N \times M) + (N \times M) \log(N \times M)$
 \Downarrow
 $O(N \times M \log(N \times M))$

-6 0 1 2 3 4 6 7 7



$(N \times M)$

$N \times M \log(N \times M)$

↳ 2000+

1000
 \downarrow
 kcode

1000
 \downarrow
 cc + ef

11 Pointer approach

	0	1	2	3	4	5
0	X	^{P1} 7	10	17	25	34
1	X	X	X	^{P2} 8	11	16
2	^{P3} 3	4	6	14	21	26
3	^{P4} 7	10	14	19	23	27

idea:

N Pointers, every iteration Point
Pointer with min val and move
that Pointer.

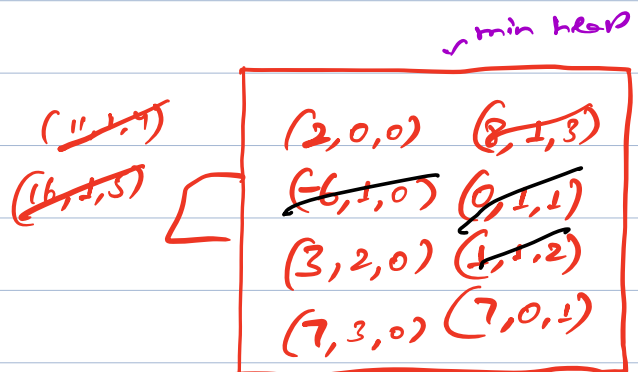
ans: -6 0 1 2

How to implement?

	0	1	2	3	4	5
0	2	7	10	17	25	34
1	-6	0	1	8	11	16
2	3	4	6	14	21	26
3	7	10	14	19	23	27

rem: (2,0,0)

-6 0 1 2



Pair f
int val;
int row;
int col;
Comparator

// Pseudo Code

```
void merge (int mat[N][M]) {
```

```
    minheap <- Pair (int val, int row, int col) >> mh;
```

```
    for (int i=0; i<N; i++) {
```

```
        mh.insert (Pair (mat[i][0], i, 0));
```

```
    }
```

```
    while (mh.size() > 0) {
```

```
        Pair rem = mh.getmin();
```

```
        mh.deletemin();
```

```
        int v = rem.val;
```

```
        int r = rem.row;
```

```
        int c = rem.col;
```

```
        Print (v);
```

```
        if (c+1 < M) {
```

```
            mh.insert (Pair (mat[r][c+1], r, c+1));
```

```
        }
```

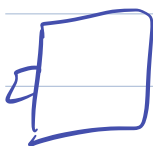
```
    }
```

```
    T.C:  $O(N \times M \log N)$ 
```

```
    S.C:  $O(N)$ 
```

```
}
```

log \rightarrow size of PQ

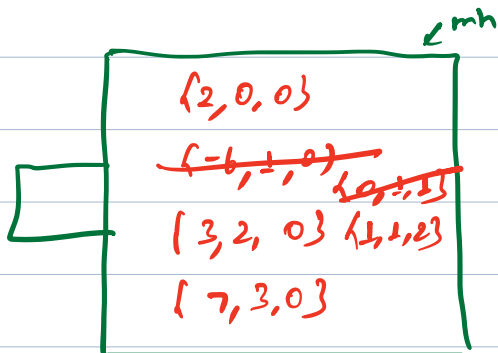


\rightarrow on the basis of val

dry run

$m=6$

	0	1	2	3	4	5
0	2	7	10	17	25	34
1	-6	0	1	8	11	16
2	3	4	6	14	21	26
3	7	10	14	19	23	27



$rem: \{0, 1, 1\}$

$v: 0$
 $r: 1$
 $c: 1$

```
void merge (int mat[N][M]) {
```

```
    minHeap <- Pair<int val, int row, int col>> mh;
```

```
    for (int i=0; i<N; i++) {
```

```
        mh.insert (Pair(mat[i][0], i, 0));
```

```
    }
```

```
    while (mh.size() > 0) {
```

\nearrow on the basis of val

```
        Pair rem = mh.getmin();
```

```
        mh.deleteMin();
```

```
        int v = rem.val;
```

```
        int r = rem.row;
```

```
        int c = rem.col;
```

```
        Print(v);
```

```
        if (c+1 < M) {
```

```
            mh.insert (Pair(mat[r][c+1], r, c+1));
```

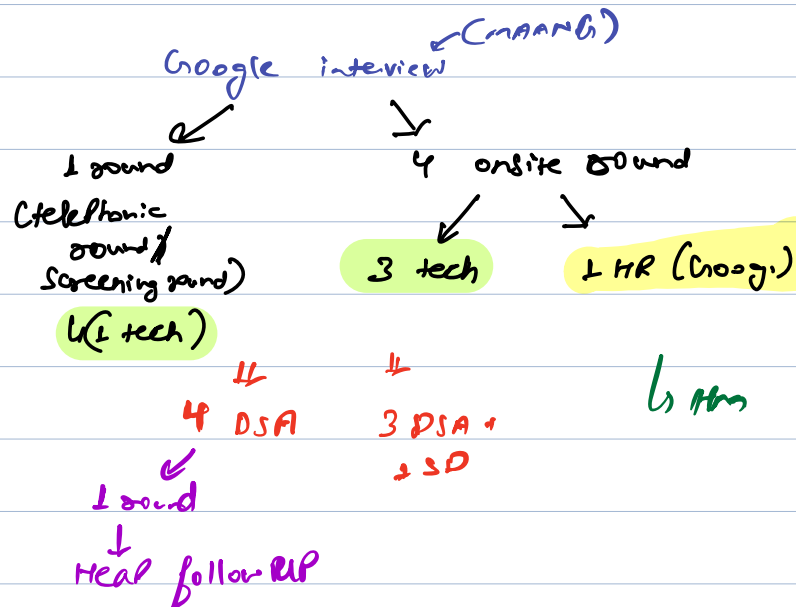
```
        }
```

```
    }
```

3

-6 0

10:15 PM \leftarrow



Q) K Smallest Pair Sums:

↳ Given 2 sorted arrays, Print K Smallest Pair Sums, a single pair only 1 time.

$K=5$

$a[i]$	0	1	2	3	4
$a[i]$	2	5	8	11	13

$b[j]$	0	1	2	3	4	5	6
$b[j]$	3	7	9	12	15	16	20

Pairs	:	Sum	i	j
1	:	5	0	0
2	:	8	1	0
3	:	9	0	1
4	:	11	0	2
5	:	11	2	0

Idea

↳ Create all the Pairs and Store in a list, Sort that and Print K Smallest Pairs.

5 9 11 14 17 18 22

↓
Sort ()

T.C : $O(N*m) + O(N*m \log(N*m))$
+ $O(K)$

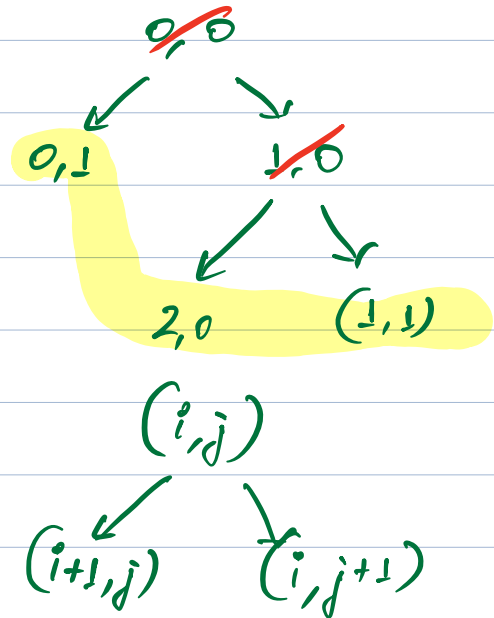
$a[s]:$ ⁰2 ¹5 ²8 ³11 ⁴13

$k=5$

$b[t]:$ ⁰3 ¹7 ²9 ³12 ⁴15 ⁵16 ⁶20

Pairs	:	Sum	i	j
1		5	0	0
2		8	1	0
3		9	0	1
4		11	0	2
			\downarrow 1,2	\downarrow 0,3

~~(5, 0, 0)~~ ~~(11, 0, 2)~~
~~(9, 0, 1)~~ (14, 1, 2)
~~(8, 1, 0)~~ (14, 0, 3)
 (11, 2, 0) (12, 1, 1)



↳ To take care of duplicacy

↳ hashset

<String>

"i @ j"

// Pseudo code

```
void KPairs (int a[], int b[], int k) {
```

```
    minheap < Pair {val, i, j} > mh;
```

```
    HashSet <String> hs;
```

```
    mh.insert (Pair (a[0]+b[0], 0, 0));  
    hs.insert (0 + " " + 0);
```

```
    for (int i = 0; i < k; i++) {
```

```
        Pair sem = mh.getMin();
```

```
        mh.deleteMin();
```

```
        // int val = sem.val;
```

```
        // i = sem.i      // j = sem.j
```

```
        Print (val);
```

```
        if (i+1 < n && hs.search((i+1) + " " + j)) == false) {
```

```
            mh.insert(a[i+1]+b[j], i+1, j);
```

```
            hs.insert((i+1) + " " + j);
```

```
        }
```

```
        if (j+1 < m && hs.search(i + " " + j+1)) == false) {
```

```
            mh.insert(a[i]+b[j+1], i, j+1);
```


hs.insert((i) + " " + (j+1));

T.C: $O(K * \log(K))$

mh.insert(pair(a[i]+b[j], 0, 0));
hs.insert(0 + " " + 0);

Dry run

K=3

a[s]: 2 5 8 11 13

b[s]: 3 7 9 12 15 16 20

mh:

{5, 0, 0}
{8, 1, 0}
{9, 0, 1}

hs:

"0 0"	"1 0"	"0 1"
-------	-------	-------

```
for(int i=0; i<K; i++){
    pair sem = mh.getmin();
    mh.deleteMin();
    //int val = sem.val;
    //i = sem.i    //j = sem.j
    Print(val);
}
```

```
if (i+1 < N && hs.search((i+1) + " " + j) == false){
    mh.insert(a[i+1] + b[j], i+1, j);
    hs.insert((i+1) + " " + (j+1));
}

if (j+1 < M && hs.search(i + " " + (j+1)) == false){
    mh.insert(a[i] + b[j+1], i, j+1);
    hs.insert((i) + " " + (j+1));
}

sem = {5, 0, 0}
```

5 8

↳ 1 add PQ

(1 sem → 2 add) → K times

→ 1 + 2 ⇒ K addⁿ

↳ Pseudo code

Doubt session

class Pair {

int val;

int row;

int col;

}

PriorityQueue<Pair> mh = new PriorityQueue<>() {

Comparator (Pair a, Pair b) {

return a.val - b.val;

}

}

Pair n1 = new Pair (a[b] + b[b], 0, 0);

mh.insert(n1);

bubble sort

{-1, 0, 1}

↑

Arrays.sort(a)

Comparator (Pair a, Pair b) {

return a.val - b.val

→ 1
0
1

```

    }
    return a.n - b.n > 1
}

```

$a[5]: (2, 5) (5, 7) (4, 11) (3, 11)$
 $(4, 15) (8, 12)$

```

Pair {
    int m;
    int n;
}

```

```

void bubbleSort (int arr[], int N) {

```

```

    for (int i = 0; i < N - 1; i++) { // no. of iter.

```

```

        for (int j = 0; j <= N - 2 - i; j++) {

```

```

            if (arr[j] > arr[j + 1]) {
                // swap(arr[j], arr[j + 1]);

```

```

            }
        }
    }
}

```

3