## **ASSIGNMENT-1**

## EE24BTECH11057-SHIVAM SHILVANT\*

- 9) The slope of tangent to curve y = f(x) at (x, f(x)) is 2x + 1. If the curve passes through the point (1, 2), then the area bounded by curve, the x axis and the line x = 1 is
  - a)  $\frac{5}{6}$
  - b)  $\frac{6}{5}$
  - c)  $\frac{1}{6}$
  - d) 6
- 10) If  $f(x) = \frac{x}{\sin x}$  and  $g(x) = \frac{x}{\tan x}$ , where  $0 < x \le 1$ , then in this interval (1997-2 Marks)
  - a) both f(x) and g(x) are increasing functions.
  - b) both f(x) and g(x) are decreasing functions.
  - c) f(x) is an increasing function.
  - d) g(x) is an increasing function.
- 11) The function  $f(x) = \sin^4 x + \cos^4 x$  increases if (1999-2 Marks)
  - a)  $0 < x < \frac{\pi}{8}$
  - b)  $\frac{\pi}{4} < x < \frac{3\pi}{8}$
  - c)  $\frac{3\pi}{8} < x < \frac{5\pi}{8}$
  - d)  $\frac{5\pi}{8} < x < \frac{3\pi}{4}$
- 12) Consider the following statements in S and (2000S)
  - S: Both sin x and cos x are decreasing functions in the interval  $(\frac{\pi}{2}, \pi)$  If a differentiable function decreases in a interval (a, b), then its derivative also decreases in (a, b).

Which of the following is true?

- a) Both S and R are wrong.
- b) Both S and R are correct, but R is not the correct explanation of S.
- c) S is correct and R is correct explanation for S.

- d) S is correct and R is wrong.
- 13) Let  $f(x) = \int e^x (x-1)(x-2) dx$ . Then f decreases in the interval

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- a)  $(-\infty, -2)$
- b) (-2, -1)
- (1,2)
- d)  $(2, +\infty)$
- 14) If normal to curve y = f(x) at the point (3,4)makes an angle  $\frac{3\pi}{4}$  with the positive x-axis, then f'(3) =(2000S)
  - a) -1
  - b)  $-\frac{3}{4}$

  - c)  $\frac{4}{3}$  d) 1
- 15) Let  $f(x) = \begin{cases} |x|, & \text{for } 0 < |x| \le 2 \\ 1, & \text{for } x = 0 \end{cases}$  then at x = 0, (2000S)
  - a) a local maximum
  - b) no local maximum
  - c) a local minimum
  - d) no extremum
- 16) For all  $x \in (0, 1)$ (2000S)
  - a)  $e^x < 1 + x$
  - b)  $\log_e (1 + x) < x$
  - c)  $\sin x > x$
  - d)  $\log_e x > x$
- 17) If  $f(x) = xe^{x(1-x)}$ , then f(x) is (2001S)a) increasing on  $\left[-\frac{1}{2}, 1\right]$ 
  - b) decreasing on R
  - c) increasing on R
  - d) decreasing on  $\left[-\frac{1}{2}, 1\right]$
- 18) The triangle formed by tangent to curve f(x) = $x^2+bx-b$  at the point (1, 1) and the coordinate axes, lies in the first quadrant. If its area is 2,

then the value of b is

(2001S)

- a) -1
- b) 3
- c) -3
- d) 1
- 19) Let  $f(x) = (1 + b^2)x^2 + 2bx + 1$  and let m(b)be the minimum value of f(x). As b varies, the range of m(b) is (2001S)
  - a) [0, 1]
  - b)  $(0, \frac{1}{2}]$
  - c)  $\left[\frac{1}{2}, 1\right]$
  - d) (0, 1]
- 20) The length of a longest interval in which the function  $3 \sin x - 4 \sin^3 x$  is increasing,

is (2002S)

- a)  $\frac{\pi}{3}$
- b)  $\frac{\pi}{2}$
- c)  $\frac{3\pi}{2}$
- d)  $\pi$
- 21) The point(s) on the curve  $y^3 + 3x^2 = 12y$  where the tangent is vertical, is(are) (2002S)
  - a)  $\left(\pm \frac{4}{\sqrt{3}}, -2\right)$
  - b)  $\left(\pm\sqrt{\frac{11}{3}},1\right)$
  - (0,0)
  - d)  $\left(\pm \frac{4}{\sqrt{3}}, 2\right)$
- 22) In [0,1] Lagranges Mean Value theorem is NOT applicable to (2003S)
  - a)  $f(x) = \begin{cases} \frac{1}{2} x, & x < \frac{1}{2} \\ \left(\frac{1}{2} x\right)^2, & x \ge \frac{1}{2} \end{cases}$ b)  $f(x) = \begin{cases} \frac{\sin x}{x}, & x \ne 0 \\ 1, & x = 0 \end{cases}$

  - c) f(x) = x|x|
  - d) f(x) = |x|

- 23) Tangent is drawn to ellipse  $\frac{x^2}{27} + y^2 = 1$  at  $\left(3\sqrt{3}\cos\theta,\sin\theta\right)$  (where  $\theta\in\left(0,\frac{\pi}{2}\right)$ ). Then the value of  $\theta$  such that sum of intercepts on axes made by this tangent is minimum, is (2003S)
  - a)  $\frac{\pi}{3}$
  - b)  $\frac{\pi}{6}$
  - c)  $\frac{\pi}{8}$
  - d)  $\frac{\pi}{4}$