

STUDENT PORTOFOLIO



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Department & Specialization: NWC CSE IT

SEM – 5th

Subject – 18CSC301J FORMAL LANGUAGE & AUTOMATA

FACULTY – Dr. P Balaji Srikanth (102776)

FIA Assignment: 1

PR2011030100666 Salwana Kurni

Q.

let the statement $P(n)$ given as

$P(n): 2^{2n} - 1$ is divisible by 3, for every natural number n .

We observe that $P(1)$ is true

$$\text{Since } 2^2 - 1 = 4 - 1 = 3$$

1 is divisible by 3.

Assume that $P(n)$ is true for some natural number n

i.e, $P(n): 2^{2n} - 1$ is divisible by 3

$$\therefore P(n): 2^{2n} - 1 = 3k \text{ where } k \in \mathbb{N}$$

Now, to prove that $P(n+1)$ is true

$$\text{we have } P(n+1): 2^{2(n+1)} - 1$$

$$= 2^{2n+2} - 1$$

$$= 2^{2n} \cdot 2^2 - 1$$

$$= 2^{2n} \cdot 4 - 1$$

$$= 3 \cdot 2^{2n} + 3k - 1 = 3m$$

Thus $P(n+1)$ is true, here even $P(n)$ is true hence, by principle of mathematical induction natural number n .

Q.

By induction on n , As a base case is $n=5$ then we have
test $5^2 = 25 < 32 = 2 \cdot 16$

So, claim holds

Inductive step, assume for n

$n > 5$ that $n^2 < 2n$, then we have
that $(n+1)^2 = n^2 + 2n + 1$

Since $n > 5$, we have -

$$(n+1)^2 = n^2 + 2n + 1$$

$$< n^2 + 2n + n \quad (\text{since } 1 < n)$$

$$= n^2 + 3n$$

$$(3n < n \leq n^2)$$

$$< n^2 + n^2$$

$$= 2n^2$$

So $(n+1)^2 < 2n^2$, now by own

inductive

$$n^2 < n^2$$

Thus -

$$(n+1)^2 < 2n^2$$

$$= 2n+1$$

Worksheet - 111

Shivam Kumar
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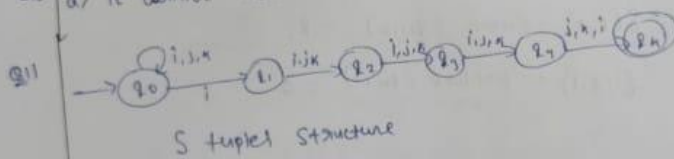
- 1.
- 2.
- 3.

$$mq \Rightarrow \begin{matrix} 1 \rightarrow b \\ 2 \rightarrow c \\ 3 \rightarrow d \\ 4 \rightarrow d \end{matrix}$$

$2x^2 + 3x + 1 = 0$
 $x = \frac{-3 \pm \sqrt{9 - 8}}{4}$
 $x = \frac{-3 \pm 1}{4}$
 $x = \frac{-3 + 1}{4} = \frac{-2}{4} = \frac{-1}{2}$
 $x = \frac{-3 - 1}{4} = \frac{-4}{4} = -1$
 $\therefore x = \frac{-1}{2}, -1$
 $\therefore \frac{1}{x} = -2, -1$
 $\therefore \frac{1}{x} + 1 = -1, 0$
 $\therefore \frac{1}{x} + 1 = 0$
 $\therefore \frac{1}{x} = -1$
 $\therefore x = -1$
 $\therefore \frac{1}{x} + 1 = -1$
 $\therefore \frac{1}{x} = -2$
 $\therefore x = -\frac{1}{2}$
 $\therefore x = -1, -\frac{1}{2}$

Worksheet II

- Q1. i) Finite set of decimal numbers
Q2. d) logical rules
Q3. a) FSM has unique output state
Q4. b) 2
Q5. a) $(0+1)^*000(0+1)^*$
Q6. d) The recognising power is same
Q7. d) 4
Q8. b) move to different output state for same input
Q9. c) $(0^*10^*10^*)^*10$
Q10. a) It cannot match second half and first half



Q12

$$E\text{-closure}(q_0) = \{q_0, q_2\} \rightarrow \textcircled{A}$$

$$\delta(A, 0) = E\text{-close}(\delta(\{q_0, q_2\}, 0), 0)$$

$$= E\text{-close}(\emptyset \cup \{q_3\}, 0) = \{q_3\} \rightarrow \textcircled{B}$$

$$\delta(A, 1) = E\text{-close}(\delta(\{q_0, q_2\}, 1), 1)$$

$$= E\text{-close}(\{q_1, q_4\}, 1)$$

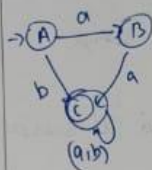
$$= \{q_1, q_4\} \rightarrow \textcircled{C}$$

$$\delta(B, 0) = E\text{-close}(\delta(\{q_3\}, 0), 0) = E\text{-close}(\{q_2\}, 0)$$

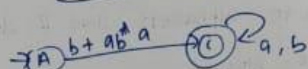
$$= \{q_2\} \rightarrow \textcircled{D}$$

$$\delta(B, 1) = \emptyset$$

12



eliminate B



$$RE = (\emptyset + (b + ab^*a)(a+b)^*\emptyset)^*$$

$$(b + ab^*a)(a+b)^*$$

$$= (b + ab^*a)(a+b)^*$$

Alternatively Rij method can also be used

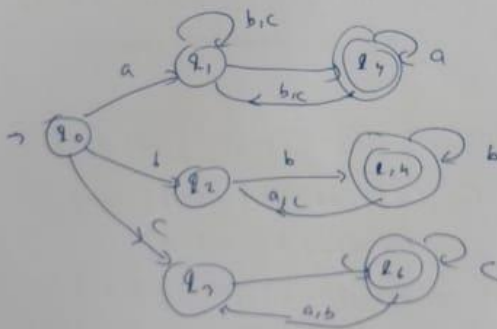
Wankhede - 111

Shivam Kulkarni

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Set-0

1. a) Proof by counter example
2. b) I Denote alphabets and I^+ denotes strings
3. b) positive closure
4. d) language that accepts strings has aaa as substring
5. b) NFA is more expensive than DFA
6. c) only \emptyset indicates no transition between two states
7. c) $S = T$
8. d) a and ϵ
9. c) $a^* \times \epsilon \rightarrow 2^{\mathbb{N}}$
10. b) only I is true
- 11.



Unit 5

1. Assume $H = \text{Head}$ $T = \text{Tail}$

List $R = (T, H, HTH, TT)$

List $S = (TH, TH, HT, T)$

Now we have to find out a sequence that string formed by R and S are identical such a sequence is 1, 2, 1, 3, 3, 4
Hence from the R and S list.

1	2	1	3	3	4	1	2	1	3	3	4
T	H	T	HT	HT	T	TH	TH	HT	HT	T	T

or

Take ms

Take the combination 1, 2, 1, 3, 3, 4

by concatenation strings in the series

$w_1, w_2, w_1, w_2, w_3, w_4 = H, H, H, H, H, H$

$T, H, T, HT, HT, T = TH, TH, HT, HT, T, T$

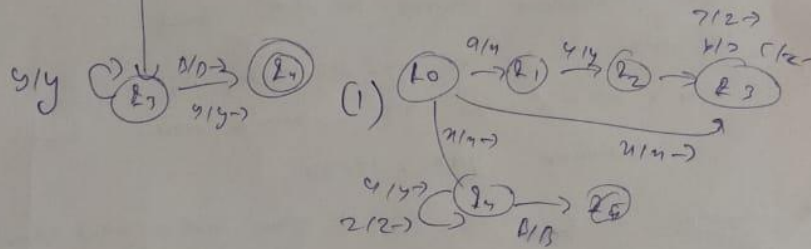
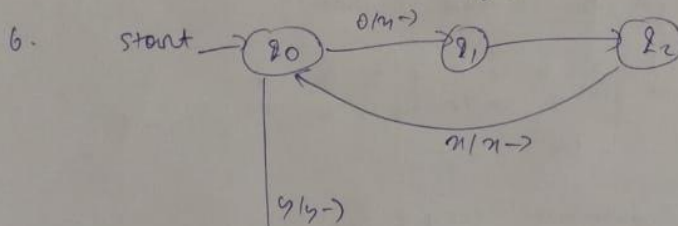
Instance $Y_{RPS} = 121334$

4. Counting Sort takes $O(n+k)$ time and $O(n+k)$ space, where n is the number of items were sorting and k is the number of possible values.

We iterate through the input items twice - once to populate away both iterate are $O(n)$ time. Additionally we iterate through counts once to fill in next index, which is $O(k)$ time. The algorithm allocate 3 additional array, one for count one for next index and one for the output. The first two are $O(k)$ space and the final one is $O(n)$ space.

Unit-4

1. True
2. True
3. D) 7
4. A) left
5. A) Both S_1 and S_2 are true.




(2)

multitape (multitape) Turing machine
multi Dimensional Turing machine
Serial Turing machine
tape TM

(3)

State	0	1	Symbol	Y	R
q_0	$(q_1, 1, R)$	-	-	(q_3, Y, R)	-
q_1	$(q_2, 0, R)$	(q_0, Y, L)	(q_1, Y, R)	-	-
q_2	$(q_1, 0, L)$	$(q_0, 1, R)$	(q_2, Y, L)	-	-
q_3	-	-	-	$(q_3, 1, R)$	(q_4, R, R)
q_4	-	-	-	-	-

<p>Matching One Or More Repetitions</p> <p>Easy, Max Score: 20, Success Rate: 99.48%</p>	★	Solved ✓
<p>Matching Ending Items</p> <p>Easy, Max Score: 20, Success Rate: 97.22%</p>	★	Solved ✓
<p>Matching Word Boundaries</p> <p>Easy, Max Score: 20, Success Rate: 96.93%</p>	★	Solved ✓
<p>Capturing & Non-Capturing Groups</p> <p>Easy, Max Score: 20, Success Rate: 98.97%</p>	★	Solved ✓
<p>Alternative Matching</p> <p>Easy, Max Score: 20, Success Rate: 94.12%</p>	★	Solved ✓
<p>Matching Same Text Again & Again</p> <p>Easy, Max Score: 20, Success Rate: 97.98%</p>		Solved ✓
<p>Backreferences To Failed Groups</p> <p>Easy, Max Score: 20, Success Rate: 94.65%</p>		Solved ✓

<p>Branch Reset Groups</p> <p>Easy, Max Score: 20, Success Rate: 95.25%</p>	★	Solved ✓
<p>Forward References</p> <p>Easy, Max Score: 20, Success Rate: 89.30%</p>	★	Solved ✓
<p>Positive Lookahead</p> <p>Easy, Max Score: 20, Success Rate: 99.47%</p>	★	Solved ✓
<p>Negative Lookahead</p> <p>Easy, Max Score: 20, Success Rate: 97.13%</p>	★	Solved ✓
<p>Positive Lookbehind</p> <p>Easy, Max Score: 20, Success Rate: 98.47%</p>	★	Solved ✓
<p>Negative Lookbehind</p> <p>Easy, Max Score: 20, Success Rate: 97.84%</p>	★	Solved ✓
<p>Detect HTML links</p> <p>Medium, Max Score: 10, Success Rate: 73.19%</p>	★	Solved ✓

STATUS

- ☐ Solved
- ☐ Unsolved

DIFFICULTY

- ☐ Easy
- ☐ Medium
- ☐ Hard

SUBDOMAINS

- ☐ Introduction
- ☐ Character Class
- ☐ Repetitions
- ☐ Grouping and Capturing
- ☐ Backreferences
- ☐ Assertions
- ☐ Applications

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- ☐ Assertions
- ☐ Applications

<h3>Detect HTML Tags</h3> <p>Easy, Max Score: 10, Success Rate: 93.26%</p>	★	Solved ✓
<h3>Find A Sub-Word</h3> <p>Easy, Max Score: 10, Success Rate: 90.34%</p>	★	Solved ✓
<h3>Alien Username</h3> <p>Easy, Max Score: 10, Success Rate: 95.33%</p>	★	Solved ✓
<h3>IP Address Validation</h3> <p>Easy, Max Score: 10, Success Rate: 91.37%</p>	★	Solved ✓
<h3>Find a Word</h3> <p>Medium, Max Score: 15, Success Rate: 87.84%</p>	★	Solved ✓
<h3>Detect the Email Addresses</h3> <p>Medium, Max Score: 15, Success Rate: 88.44%</p>	★	Solved ✓
<h3>Detect the Domain Name</h3> <p>Medium, Max Score: 15, Success Rate: 89.76%</p>	★	Solved ✓

STATUS

- ☒ Solved
- ☐ Unsolved

DIFFICULTY

- ☐ Easy
- ☐ Medium
- ☐ Hard

SUBDOMAINS

- ☐ Introduction
- ☐ Character C
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