

Q1) Ans. Primary reason for choosing the right data structure is.

- 1) Efficiency \rightarrow the choice of data structure directly impacts the efficiency of algorithm. A well-chosen data structure can significantly reduce time and space complexity. For example, using a hash table for quick lookup or a priority queue for efficient sorting.
- 2) memory usage \rightarrow Different data structures have varying memory footprint. Efficient memory usage is crucial for large data sets or resource-constrained environments.
- 3) Algorithm design \rightarrow the choice of data structure often dictates the design and logic of the algorithms. Certain algorithms are inherently suited to specific data structures.

4) Ease of Implementation → Some data structures are simpler to implement than others. Choosing a simpler data structure can lead to faster development time and easier debugging.

5) Problem solving suitability → Different data structures are different suited for different problem domains.

For example, graphs are ideal for representing relations and networks, while trees are useful for hierarchical data.

* Categorization of data structures:

- * Int : Represents Integer values.
- * Float : Represents floating point number.
- * char : Represents single characters.
- * bool : Represents Boolean value (true and false).

* Linear secondary data structures

- * stack : Follows a LIFO (Last-In-First-out)
- * queue : Follows a FIFO (First-In-First-out)

① Ans

1-c

Non-linear secondary data structure

tree = represent hierarchical relationship between nodes.
graph = represent a network of nodes connect edge.

Key point

- Primary data structure are the fundamental building block.
- Linear secondary data structure have sequential arrangement
- Non-linear data structure have complex relationships between element (:-)

(Q2) Ans

(2a)

An AVL tree (name after its Inventors, Adelson-Velskii and Landis) is a self balancing binary search tree where the height of two subtree of any node differ by at most one. This property ensures that the tree maintains logarithmic height, leading to efficient search, Insertion deletion, operations.

* Construct an AVL tree for the sequence :-

20, 30, 10, 50, 40, 70, 80, 60

1) Insertion of 20

→ create a root node with value 20.

2) Insertion of 30

→ 30 is greater than 20. So it becomes right child of the root.

3) Insertion of 10

→ 10 is less than 20. So it becomes left child of the root.

4) Insertion of 50.

- 50 Is greater than 30. so it become the right child of 30.

5) Insertion of 40.

- 40 Is greater than 30 but less than 50 so it become left child of 50.

6) Insertion of 70.

- 70 Is greater.

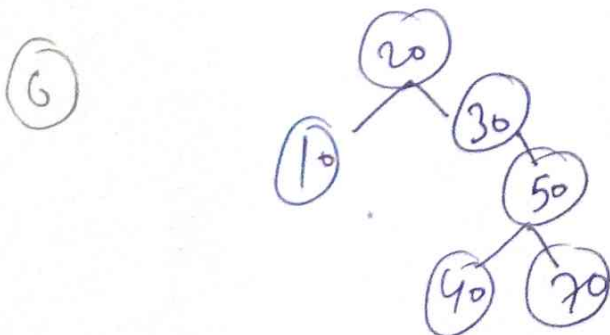
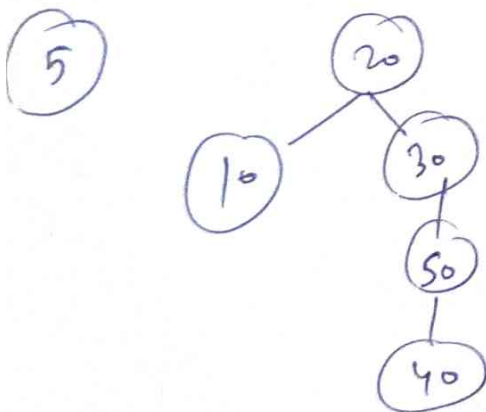
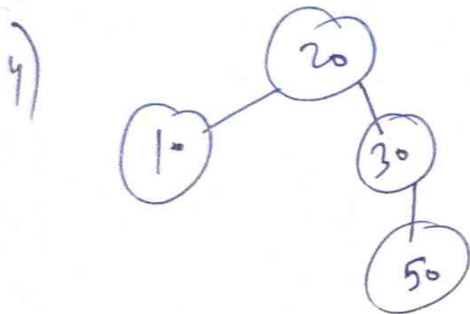
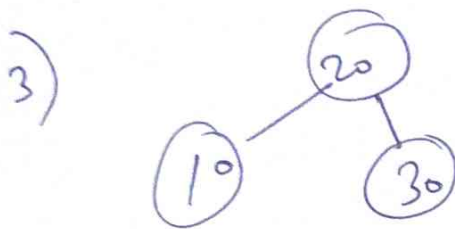
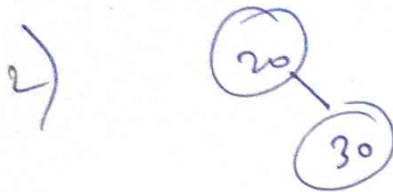
7) Insertion of 80.

- 80 Is greater than 70. so it become the right child of 70.

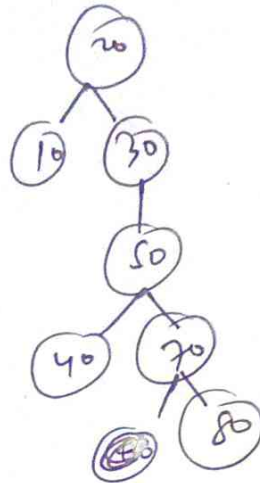
8) Insertion of 60.

- 60 Is greater than 50 but less than 70. so it become the left child of 70.

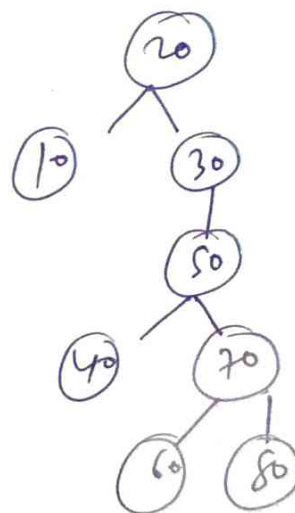
① How explain by using diagram - AVL tree 2-C



Final AVL tree



8) Final AVL tree



3 (a) Ans

Ans Insertion Sort Algorithm

3-a

→ Insertion Sort is a simple sorting algorithm that works by iteratively building a sorted array one element at a time. It starts with the second element and compares it with the element before it, shifting them to the right until the correct position is found for the current element. This process continues for each element in the array, gradually building the sorted portion.

→ Time complexity

- * Best case : $O(n)$ when the array is already sorted.
- * Average case : $O(n^2)$ when the elements are in random order.
- * Worst case : $O(n^2)$, when the array is sorted in reverse order.

(*) Efficiency → Insertion sort is most efficient for small array or when the array is partially sorted. It is also a good choice when memory write expensive as it minimizes the number of write accesses. (3-6)

(*) Sorting the given sequence using Insert sort.

Step 1

[47, 12, 1, 68, 3]

Step 2

[12, 47, 1, 68, 3] (12 is smaller than 47, so it's shifted to the left.)

Step 3

[1, 12, 47, 68, 3] (1 is smaller than 12 and 47, so it's shifted to the left most position.)

Step 4

[1, 12, 47, 68, 3] (68 is already in the correct position.)

(3-c)

step 5

[1, 3, 12, 47, 68] (3 is smaller than 12, 47 and 68 so it's shifted to the correct position.)

* Final sorted array

[1, 3, 12, 47, 68]

Don

(3-c)

step 5

[1, 3, 12, 47, 68] (3 is smaller than 12, 47 and 68
so it's shifted to the correct position.)

* Final sorted array

[1, 3, 12, 47, 68]

Ans

Ans 4 Ans

4-a

→ Recursion Involves a function calling itself directly or Indirectly TO understand how Recursion works under the hood . it's helpful to visualize it using a Stack data structure .

* → The following is recursive function to calculate the factorial of a number .

Python

```
def factorial (n):
```

```
    If  $n == 0$ :
```

```
        Return 1
```

```
    else :
```

```
        Return  $n * \text{factorial}(n-1)$  (lets trace the execution of factorial (3):)
```

* (1)

step ①

factorial (3) is called the function pushes the current value of $n(3)$ and the return address onto the stack .

If the call factorial (2)

Step 2

(4-1)

Factorial 2 Is called the function pushes the current value of $n(2)$ and the return the Address of the onto the stack.

If the call factorial (1).

Step 3

Factorial (1) Is called -
the function pushes the current value of $n(1)$ and the return Address on to the stacks.

If the factorial (0)

Step (4)

Factorial (0) Is called.
the base case Is reach. and the function return 1.

Step (5)

Factorial (1) pops the return Address and 1 from the stack.

if multiple 1 to 1 and return 1

step 6

(1-E)

factorial(2) pops the return Address and 1 from the stack.
it multiplies 2 by 1 and return 2.

step 7

factorial(3) pops the return Address and 2 from the stack.
it multiplies 3 by 2 and return 6.
Visual Representation:

stack (top to bottom)

3, return Address.
2, return Address.
1, return Address.
0, return Address.
1
1
2
6

⑤ 7/11/21

step ① Initia all distance by ∞ except node.

distance $\Rightarrow [0, \infty, \infty, \infty, \infty, \infty]$

step ② Initiate visited array

③ Initilize all element to false -

visited = [false, false, false, false, false, false]

step ③

Find the node with minimum distance.

→ In the first iteration, the source node has smallest distance (0)

step 4

visited[0] = true.

step 5

for node A

* Distance B through A = distance[0] + 6 = 6

* " C " A = distance[0] + 5 = 5

* update distance[1] to 6 and distance[2] to 5

Step 6 Repeat steps 3-5 until nodes are visited.

Iteration 2

* Node c has minimum distance (5).

* marks c as visited

* update distance B and D through c.

Iteration 3

⊗ Node B has minimum distance 6.

⊗ mark B as visited

⊗ update distance D and E through B.

Iteration 4

⊗ Node D has the minimum distance (7).

mark D as visited.

update E and F through D.

Iteration 5

* Node E has the minimum distance (9).

* mark F as visited

Final distance array = $[0, 6, 5, 7, 9, 5]$

⑤ Shortest path

S to A \rightarrow A (Distance 6)

S to B \rightarrow C \rightarrow B (Distance 6)

S to C \rightarrow S \rightarrow C (Distance 5)