
 Marwadi University <small>Marwadi Chandarana Group</small> 	Marwadi University Faculty of Engineering and Technology Department of Information and Communication Technology	
Subject: DAA (01CT0512)	AIM: Implementing the Exponential (Power) function to calculate x^n using Divide and Conquer Approach	
Experiment No: 3	Date:	Enrolment No: 92301733046

Theory:

The exponential (power) function calculates x^n , where x is the base and n is the exponent. This operation can be done in different ways, each with different time and space requirements.

1. Iterative (Naive) Approach:

- This method multiplies the base x by itself n times in a loop. It is easy to implement but has a time complexity of $O(n)$ in the worst case, as it performs n multiplications. The space complexity is $O(1)$ because it uses only a fixed number of variables.

2. Divide and Conquer (Unoptimized, $O(n)$):


- This approach splits the problem into smaller subproblems by dividing n by 2 each time. However, it recalculates the same subproblem several times, leading to unnecessary work and a worst-case time complexity of $O(n)$. The recursion depth lowers the space requirement to $O(\log n)$.

3. Divide and Conquer (Optimized, $O(\log n)$):

- This version improves efficiency by calculating $\text{power}(x, n/2)$ once and reusing the result. This dramatically reduces the number of multiplications, resulting in a worst-case time complexity of $O(\log n)$ and a space complexity of $O(\log n)$ due to recursion depth.

These three approaches show the balance between simplicity and efficiency in algorithm design. They illustrate how techniques like result reuse can greatly improve performance.

Programming Language: Python

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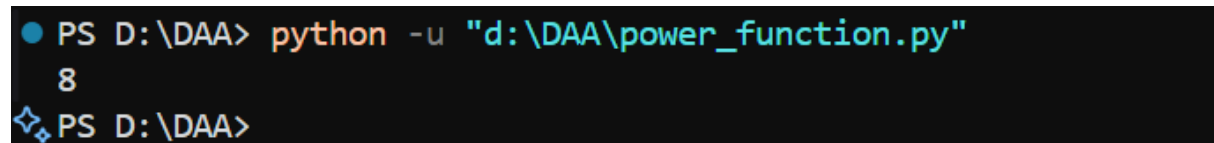
1) Exponential Function using Iterative (Naive) Approach

Code:

```
def power_iterative(x, n):
    result = 1
    for i in range(n):
        result *= x
    return result
```

```
print(power_iterative(2, 3))
```

Output:



```
PS D:\DAA> python -u "d:\DAA\power_function.py"
8
PS D:\DAA>
```

Space complexity: $O(1)$

Justification: The algorithm uses only a fixed number of variables (result, x, n, and the loop counter), without any recursion or additional data structures. As a result, the space complexity remains constant at $O(1)$ for all cases.



Time complexity:

Best case time complexity: $O(1)$

Justification: The best case occurs when $n = 0$. In this situation, the loop does not execute, and the function directly returns 1. This results in a constant-time operation with a time complexity of $O(1)$.

Worst case time complexity: $O(n)$

Justification: The worst case occurs when $n > 0$. Here, the loop runs exactly n times, performing one multiplication per iteration. Therefore, the total number of operations grows linearly with n , giving a time complexity of $O(n)$.

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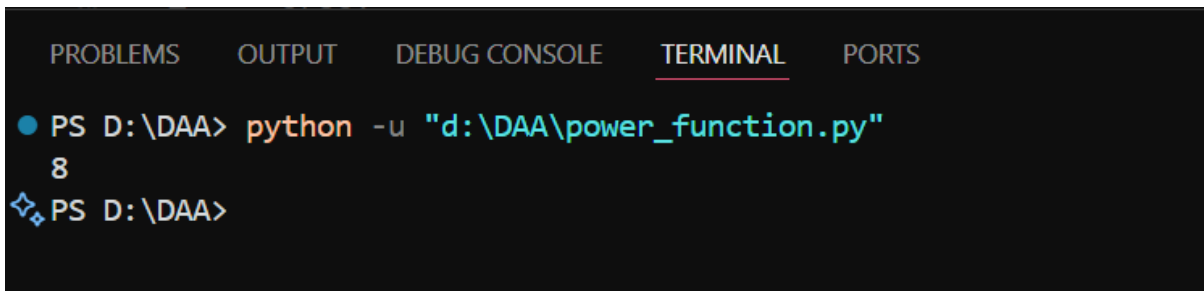
2) Exponential Function with $O(N)$ using Divide and Conquer Approach

Code:

```
#t(n)=o(n)
def power(x,n):
    if n==0:
        return 1
    elif n%2==0:
        return power(x,n//2) * power(x,n//2)
    else:
        return x * power(x,n//2) * power(x,n//2)



print(power(2,3))
```

Output:



```
PROBLEMS  OUTPUT  DEBUG CONSOLE  TERMINAL  PORTS

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8
❖ PS D:\DAA>
```

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Space complexity: $O(\log n)$

Justification: Each recursive call requires a separate location on the call stack when $n > 0$ in order to track variables and determine where to return once it is finished. It takes roughly $\log_2(n)$ steps to get to the base case because the function always reduces n by half. This indicates that the space complexity is $O(\log n)$, meaning that the call stack will never go deeper than roughly $\log_2(n)$ frames.



Time complexity:

Best case time complexity: $O(1)$

Justification: If it directly hit base case then it have $O(1)$ time complexity

Worst case time complexity: $O(n)$

Justification: When $n > 0$, the function always makes two new recursive calls for the same half-sized problem, instead of saving and reusing the result. This means the work doubles at each step of the recursion. Even though the recursion only goes about $\log_2(n)$ levels deep, the total number of calls adds up quickly like 1 call, then 2 calls, then 4, then 8, and so on until it reaches roughly 2^n calls. That's why, instead of being fast like $O(\log n)$, it ends up taking $O(n)$ time.

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3) Exponential Function with $O(\log N)$ using Divide and Conquer Approach

Code:

$T(n) = O(\log n)$

Using recursion with optimized approach

def power(x,n):

 temp=power(x,n//2)

if n==0:

return 1

elif n%2==0:

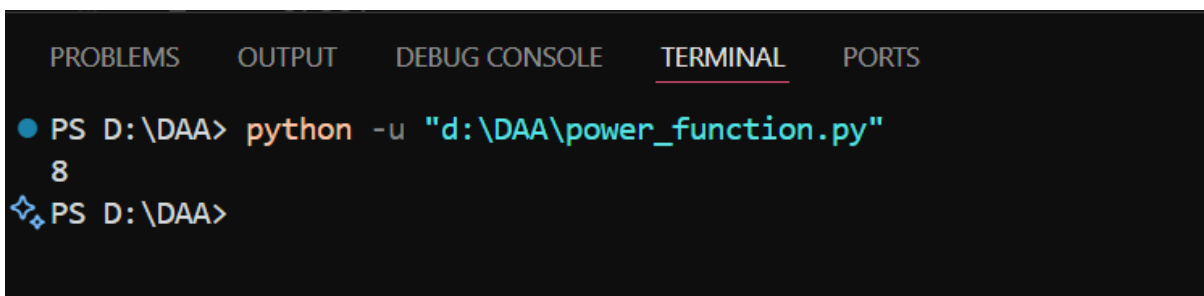
return temp * temp

else:

return x * temp * temp

print(power(2,3))

Output:




```

PROBLEMS  OUTPUT  DEBUG CONSOLE  TERMINAL  PORTS

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8
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```

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Time complexity:

Best case time complexity: $O(1)$

Justification: If it directly hit base case then it have $O(1)$ time complexity

Worst case time complexity: $O(\log n)$

Justification: In the worst scenario, the function calls $\text{power}(x, n/2)$ exactly once in each step when $n > 0$. Regardless of how big n is, it does a tiny, fixed amount of additional work after returning the recursive result just a few multiplications. It only takes roughly $\log_2(n)$ steps to get to the base case, where $n = 0$, because each recursive step cuts n in half. This indicates that the function's worst-case time complexity is $O(\log n)$, meaning that the total amount of work increases proportionately to $\log n$.