

ASSIGNMENT: 2

- ① Define relaxation time and drift velocity of electron in a semiconductor.

→ The average time between two successive collision is τ . This time is known as relaxation time.

DRIFT VELOCITY:- In absence of external field the random motion of free e^- is equally possible. It is defined as the average velocity attained by a charged particle in a material due to e^- field. The SI unit of drift velocity is m/s.

$$V = \frac{I}{neA}$$

- ② Define the expression of current density and mobility of charge carrier flowing carriers for semiconductor.

→ **CURRENT DENSITY:-** It is defined as the amount of electric current flowing per unit cross-section area of a material

$$J = \frac{I}{A} = \frac{NeAV_d}{A} = NeV_d$$

$$J = NeV_d$$

MOBILITY:- It is defined as the drift velocity of charge carrier per unit electric field.

$$\mu = \frac{V_d}{E_x}$$

$$V_d \rightarrow \mu E_x$$

$$\therefore E_H \rightarrow \frac{V_d B}{\mu}$$

$$V_d \rightarrow \frac{E_H}{B}$$

$$\frac{E_H}{B} \rightarrow \mu E_x$$

$$E_H = \mu E_x B$$

$$E_H = \frac{\mu J_x B}{\sigma}$$

$$\frac{E_H}{B J_x} = \frac{\mu}{\sigma}$$

$$R_H = \frac{\mu}{\sigma}$$

$$\mu = R_H \sigma$$

$$\tan \theta_H = \frac{E_H}{E_x}$$

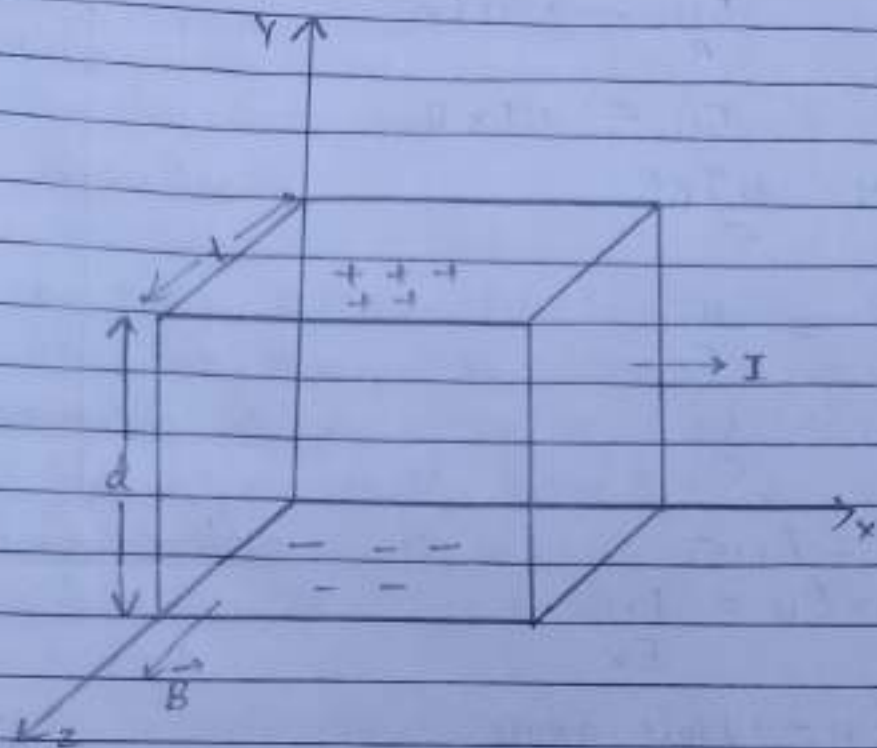
$\theta_H \rightarrow$ Hall angle

$$\mu = \frac{\sigma E_H}{B J_x}$$

$$\mu = \frac{\tan \theta_H}{B}$$

③ Discuss Hall effect with suitable diagram how can we calculate Hall effect, carrier density and mobility experimentally.

→ **HALL EFFECT:** If a current carrying conductor (or semiconductor) is placed in a magnetic field perpendicular to the direction of current, the magnetic field exerts a transverse force (LORENTZ FORCE) on the moving charge carriers which tends to push them to one side of the conductor. This magnetic influence, producing a measurable voltage is called Hall voltage (V_H) and the effect is called Hall effect.



CALCULATIONS:-

$$\text{Lorentz force} = F\vec{m} = q(\vec{V}d \times \vec{B})$$

$$q = -e, \quad \vec{V}d = -i Vd, \quad B = \hat{k} B$$

$$= -e (-i Vd \times \hat{k} B)$$

$$= e Vd B (\hat{i} \times \hat{k})$$

$$= -e Vd B \hat{j}$$

Hall effect at equilibrium

$$F_H = F_m$$

$$e E_H = e Vd B$$

$$E_H = Vd B \quad \text{--- (i)}$$

current density, $J_x = -ne Vd$

Hall coefficient

$$R_H = \frac{E_H}{BJ_x} = -\frac{V_d B}{ne V_d B} = -\frac{1}{ne}$$

$$\boxed{E_H = R_H BJ_x} \quad \text{--- (ii)}$$

$$\boxed{R_H = \frac{E_H}{BJ_x} = -\frac{1}{ne}} \quad \text{--- (iii)}$$

Mobility

Mobility, $\mu = \frac{V_d}{E_x} \Rightarrow V_d = \mu E_x$

$$E_H = V_d B \Rightarrow E_H = \mu E_x B$$

$$E_H = \frac{\mu J_x B}{\sigma} \quad [J_x = \sigma E_x]$$

$$R_H = \frac{E_H}{BJ_x} = \frac{\mu}{\sigma}$$

$$\boxed{\mu = R_H \sigma}$$

$$\tan \theta_H = \frac{E_H}{E_x}$$

$$\boxed{\mu = \frac{\sigma E_H}{BJ_x}}$$

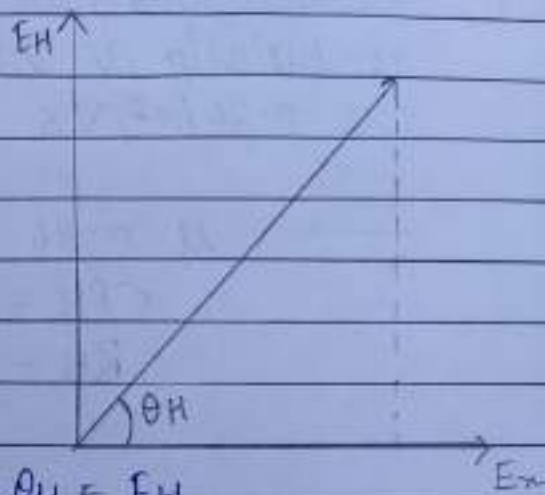
$$J_x = \sigma E_x$$

where, θ_H = Hall angle

$$\mu = \frac{\sigma E_H}{B \sigma E_x}$$

$$\mu = \frac{E_H}{B E_x}$$

$$\boxed{\mu = \frac{\tan \theta_H}{B}}$$



Determination of hall coefficient

$$E_H = \frac{V_H}{dB}, \quad J_x = \frac{I}{dt}$$

$$R_H = \frac{V_H}{dB} \times \frac{dt}{I} = \frac{V_H t}{BI}$$

- ④ Calculate the hall coefficient of a specimen whose electrical conductivity is 2.12 mho/m and charge carrier mobility are $0.36 \text{ m}^2/\text{V}\cdot\text{s}$

$$\rightarrow \mu = 0.36 \quad \sigma = 2.12 \text{ mho/m}$$

$$\sigma R_H = \mu$$

$$R_H = \frac{\mu}{\sigma} \Rightarrow R_H = \frac{0.36}{2.12}$$

$$= 0.169$$

- ⑤ The hall coefficient (R_H) of a semiconductor is $3.22 \times 10^{-4} \text{ m}^3/\text{C}$. If resistivity is $9 \times 10^{-3} \Omega\text{m}$. Calculate the mobility and the carrier concentration of the carrier ($e = 1.6 \times 10^{-19} \text{ C}$)

$$\rightarrow R_H = 3.22 \times 10^{-4} \text{ m}^3/\text{C}$$

$$e = 1.6 \times 10^{-19} \text{ C}$$

$$n = \frac{1}{R_H e}, \quad \mu = \sigma R_H$$

$$\mu = \frac{1}{\rho} R_H$$

n is carrier concentration

$$\eta = \frac{1}{3.22 \times 10^{-4} \times 1.6 \times 10^{-19}}$$

$$\eta = 1.94 \times 10^{22}$$

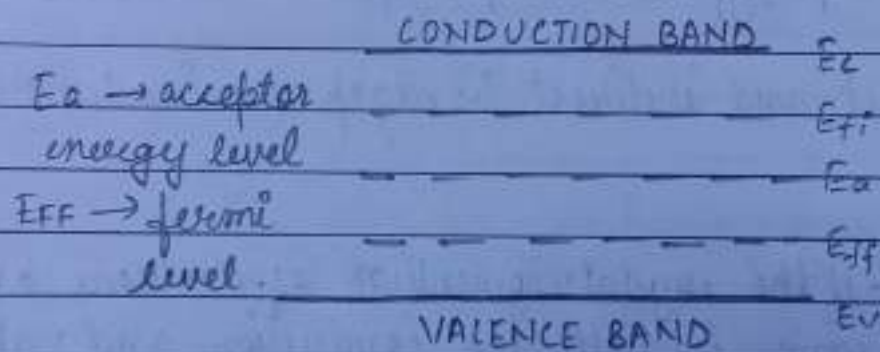
$$\mu = \frac{3.22 \times 10^{-4}}{9 \times 10^{-3}}$$

$$[\mu = 3.5]$$

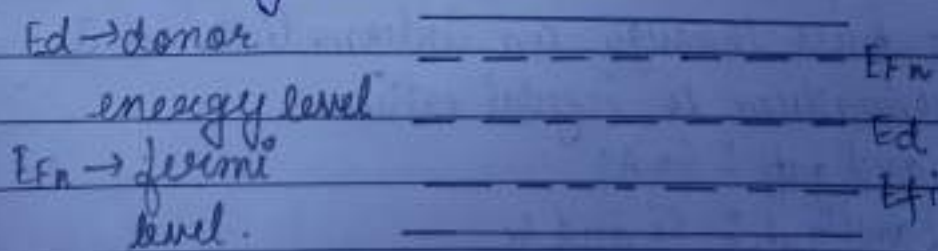
6) In a slab of specimen of width 4mm, electrons have drift velocity 3×10^3 m/s under the influence of externally applied electric field along the x-axis. Calculate the hall voltage if specimen is subjected to magnetic field of 4 Wb/m^2 along the z-axis.

7) Describe the P and N type semiconductor and indicate the fermi level and energy level of impurity atoms in band diagram.

→ P type semiconductor: The majority carriers are hole and minority carrier are electrons.



→ N type semiconductor: The majority are electrons and minority carrier are hole.



⑧ What are the charge carriers responsible for current conduction in pure semiconductor? Find the expression for conductivity of such semiconductor?

→ The more abundant charge carriers are called majority carriers which are primarily responsible for current transport in a piece of semiconductor. In n-type semiconductor they are electrons while in p-type semiconductor they are holes.

The conductivity of a semiconductor

$$\sigma = n_e e V_e + n_h e V_h$$

where

n_e is the number of electrons

e is the electronic charge

V_e and V_h is the mobility of e^- and hole

for n-type $\Rightarrow \sigma = n_e V_e$

for p-type $\Rightarrow \sigma = p_e V_h$

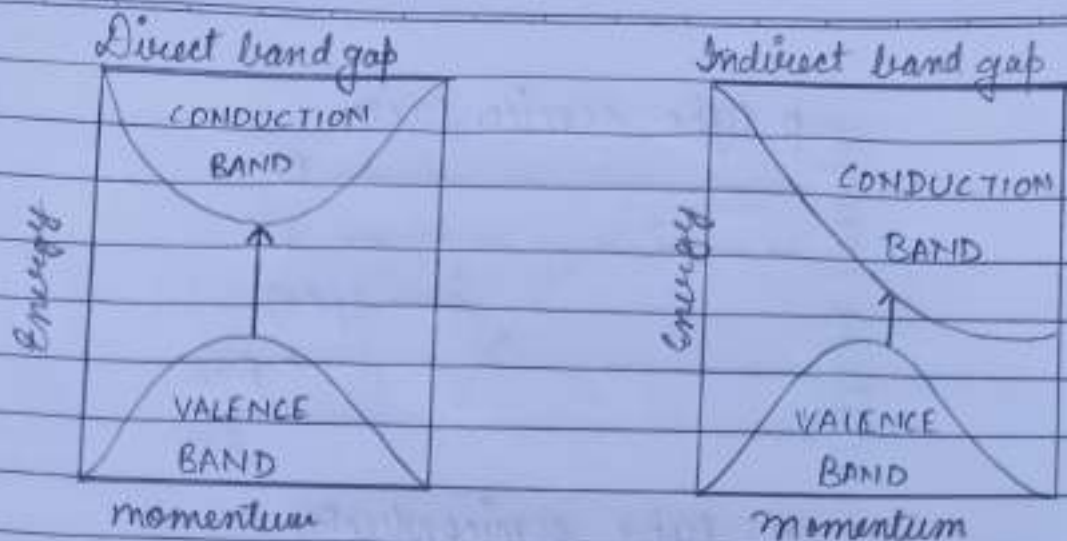
⑨ Explain the direct and indirect bandgap semiconductors with examples.

→ DIRECT BANDGAP:- If the crystal momentum of electrons and holes is the same in both the conduction and valence band.

INDIRECT BANDGAP:- A photon can be emitted because the electron must first pass through an intermediate state and transfer momentum to crystal lattice.

Eg. of direct band gap: GaAs

Eg. of indirect band gap: Si and Ge



- ⑩ Hall coefficient of a semiconductor is $3.22 \times 10^{-4} \text{ m}^3/\text{C}$. Its resistivity is $9 \times 10^{-3} \text{ ohm-meter}$. Calculate the mobility and carrier in the semiconductor.

$$\begin{aligned}
 \rightarrow \quad R_H &= 3.22 \times 10^{-4} \text{ m}^3/\text{C} \\
 \rho &= 9 \times 10^{-3} \text{ ohm-meter} \\
 \mu &= \frac{\sigma R_H}{\rho} = \frac{1}{\rho} R_H \\
 &= \frac{3.22 \times 10^{-4}}{9 \times 10^{-3}} = 3.5
 \end{aligned}$$

$$n = \frac{1}{R_H e} = \frac{1}{3.22 \times 10^{-4} \times 1.6 \times 10^{19}} = 1.94 \times 10^{22}$$

- ⑪ How does fermi level changes with increasing temperature in p-type semiconductor and n-type semiconductor? Sketch the diagram.

