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AI1110: Probability and Random Variables Assignment 1

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12.13.5.9: Question: On a multiple-choice examination with three possible answers for each of the five questions, what is the probability that a candidate would get four or more correct answers just by guessing?

Solution:

- Let the probability of correct guess be **p** and incorrect be **q** which are $\frac{1}{3}$ and $\frac{2}{3}$ respectively
- X represents the number of correct answers by guessing in the set of 5 multiple choice questions.

The CDF of X is,

$$F(x) = \Pr(X \le x) = \sum_{k=0}^{x} {n \choose k} p^{x} q^{n-x}$$
 (1)

$$Pr(x >= 4) = 1 - Pr(x <= 3)$$
 (2)

$$=1-F(3)$$
 (3)

$$=1-(\binom{5}{0}(\frac{1}{3})^{0}(\frac{2}{3})^{5}+\binom{5}{1}(\frac{1}{3})^{1}(\frac{2}{3})^{4}+\tag{4}$$

$$\binom{5}{2} (\frac{1}{3})^2 (\frac{2}{3})^3 + \binom{5}{3} (\frac{1}{3})^3 (\frac{2}{3})^2) \tag{5}$$

$$=1-(\frac{232}{243})\tag{6}$$

$$=\frac{11}{243}$$
 (7)

 \therefore probability that a candidate would get 4 or more correct answers by guessing would be $\frac{11}{243}$