1

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Question EC 31 2023

The signal-to-noise ratio (SNR) of an ADC with a full-scale sinusoidal input is given to be 61.96 dB. The resolution of the ADC is

GATE EC 2023

Solution: The mean power in a sinusoidal input signal with unit amplitude is simply

$$P_s = \frac{1}{N} \int_0^T \sin^2(\omega t) dt \tag{1}$$

Quantized to 2^n discrete levels, equivalent to n bits, one quantization step q has a size of

$$|e| \le \frac{q}{2}$$
 and therefore, $|e| \le 2^{-n}$ (2)

For a large enough number of quantization steps, the probability density function of the quantization error tends toward being flat 1. Its value within the quantization error bounds is

$$p_e \approx \frac{1}{q} \tag{3}$$

So, we can calculate its mean power or variance as the 2nd moment of its distribution:

$$P_e = \int_{-\frac{q}{2}}^{\frac{q}{2}} p(e)e^2 de \approx \frac{2^{-2n}}{3}$$
 (4)

Thus, an ideal ADC would have a signal-to-noise ratio

$$SNR = \frac{P_s}{P_e} = 1.5 \cdot 2^{2n} \tag{5}$$

or, expressed in decibels,

$$SNR = 1.76 + 6.02n \tag{6}$$

In this formula:

- SNR is the signal-to-noise ratio in dB, which is given as 61.96 dB in our case.
- 1.76 dB is a constant that accounts for quantization noise.
- 6.02 dB is the noise bandwidth factor for a sinusoidal input.

Plug in the values:

Resolution (in bits) =
$$\frac{61.96 \text{ dB} - 1.76 \text{ dB}}{6.02 \text{ dB}} \approx 10 \text{ bits}$$
 (7)

So, the resolution of the ADC is approximately 10 bits.