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Assignment-2

AI1110: Probability And Random Variables IIT Hyderabad

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Q7(b) Evaluate the given finite integral.

$$\int_{-6}^{3} |x+3| \, dx$$

Solution:-

$$|x+3| = \begin{cases} (x+3) \text{ if } x+3 \ge 0\\ -(x+3) \text{ if } x+3 < 0 \end{cases}$$
 (1)

$$|x+3| = \begin{cases} (x+3) \text{ if } x \ge -3\\ -(x+3) \text{ if } x < -3 \end{cases}$$

using the property $\int_a^b x \, dx = \int_a^c x \, dx + \int_c^b x \, dx$

$$I = \int_{-6}^{3} |x+3| \, dx \tag{3}$$

$$= \int_{-6}^{-3} |x+3| \, dx + \int_{-3}^{3} |x+3| \, dx \tag{4}$$

$$= \int_{-6}^{-3} -(x+3) \, dx + \int_{-3}^{3} (x+3) \, dx \tag{5}$$

$$= -\left[\frac{x^2}{2} + 3x\right]_{-6}^{-3} + \left[\frac{x^2}{2} + 3x\right]_{-3}^{3} \tag{6}$$

$$= -\left[\frac{(-3)^2 - (-6)^2}{2} + 3(-3 - (-6))\right]$$
 (7)

$$+\left[\frac{(3)^2-(-3)^2}{2}+3(3-(-6))\right]$$

$$= -\left[\frac{(9) - (36)}{2} + 3(3)\right] \tag{8}$$

 $+\left[\frac{(9)-(9)}{2}+3(3)\right]$

$$=\frac{27}{2}-9+0+18\tag{9}$$

$$=\frac{27}{2}+9\tag{10}$$

$$=\frac{45}{2}\tag{11}$$

$$=22\frac{1}{2}$$
 (12)

(13)

(2)
$$\implies \int_{-6}^{3} |x+3| \, dx = 22\frac{1}{2} \text{ unit.}$$