

# Assignment-8

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## Question

### Papoulis book exercise 6

Q-39 The random variable  $x$  and  $y$  are independent,  $x$  is  $N(0, \sigma^2)$ . and  $y$  is uniform in the interval  $(0, \pi)$ . Show that if  $z = x + a \cos y$ , then

$$f_z(z) = \frac{1}{\pi \sigma 2\pi}$$



fig.jpg

# Solution

From the assumption it follows that

$$g'(-x) = -g'(x) \quad g''(x) \geq 0 \quad f(x - \eta) = f(\eta - x)$$

Hence, if  $I(a) = \int_{-\infty}^{\infty} g(x - a)f(x)dx$ , then

$$I'(a) = - \int_{-\infty}^{\infty} g'(x - a)f(x)dx \quad I'(\eta) = 0$$

$$I''(a) = \int_{-\infty}^{\infty} g''(x - a)f(x)dx \geq 0 \quad \text{all } a$$

Hence,  $I(a)$  is minimum for  $a = \eta$ .