

Tutorial Sheet

Q1 Compute the Big Oh of the algorithm involving one for loop.

Ans:

Time complexity of a loop is considered as $O(n)$ if the loop variables are incremented / decremented by a constant amount.

Example

	Cost	times
int n=100	C_1	1
for (int i=0; i<n; i++)	C_2	$n+1$
{ cout << "Hello" ; }	C_3	n

Its Time Complexity will be

$$\begin{aligned}
 T_n &= C_1 * 1 + C_2 * (n+1) + C_3 * (n) \\
 &= C_1 * 1 + C_2 n + C_2 + C_3 n \\
 &= (C_2 + C_3) n + (C_1 + C_2)
 \end{aligned}$$

It is in the form of

$$T_n = an + b$$

So its Time complexity will be

$$\Rightarrow O(n)$$