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D3ITA2

Tut-4

Q4 What do you know about Dijkstra's Algorithm?

Ans Dijkstra algorithm is a single-source shortest path algorithm. Here, single-source means that only one source is given, and we have to find the shortest path from the source to all the nodes.

In a graph,

$G(V, E) \rightarrow$ digraph

$v_0 =$ source

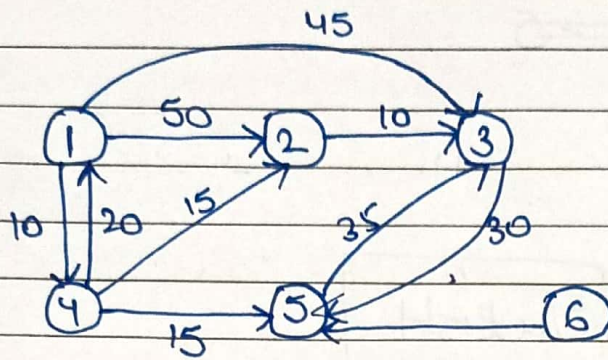
$C =$ weighting function

Time Complexity

$$O((n + E) \log n)$$

$n =$ ~~number of~~ nearest vertex
 $E =$ examine edge.

Eg



Single source shortest path
 we have to take paths from single start node
Path Length of path

1, 4
 1, 4, 5
 1, 4, 5, 2

10
 $10 + 15 = 25$
 $\times \boxed{50}$

direct edge will have length more than path so we will reject it

1, 3
 or
 1, 4, 5, 2, 3

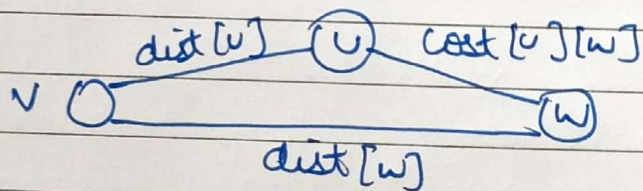
$\boxed{45}$

$10 + 15 + 20 + 10 = 55$
 Here path length is more than direct edge so we will choose direct edge

Limitation

→ It does not necessarily give the correct results on the digraph [directed graph] when some or all the edges have negative length.

Algorithm



Cost adjacency matrix

⇒ $cost[1:n][1:n]$

direct edge

$dist[i] = cost[v][i]$ for $i = 1$ to n

Boolean → $S[i] = false$
 array

For source

$v \rightarrow$
 source

⇒ $S[v] = true$
 $dist[v] = 0$

Start node will consider only 0; as no path will be defined

for rest of n nodes

for (num = 2 to num $\leq n$)

vertex ⇒ u

$S[u] = true$

↑
 $dist[u]$
 minimum

// Path to be find via nearest node

for ($w = 1$ to n)
 if ($s[w] == false$) && $dist[w] > dist[u] +$
 $cost[u][w]$)
 it will assign,
 $dist[w] = dist[u] + cost[u][w]$