

Summary

General Principles

Kinematics describes motion in terms of position, velocity, and acceleration.

General kinematic relationships are given **mathematically** by:

Instantaneous velocity $v_s = ds/dt = \text{slope of position graph}$

Instantaneous acceleration $a_s = dv_s/dt = \text{slope of velocity graph}$

Final position $s_f = s_i + \int_{t_i}^{t_f} v_s dt = s_i + \left\{ \begin{array}{l} \text{area under the velocity} \\ \text{curve from } t_i \text{ to } t_f \end{array} \right.$

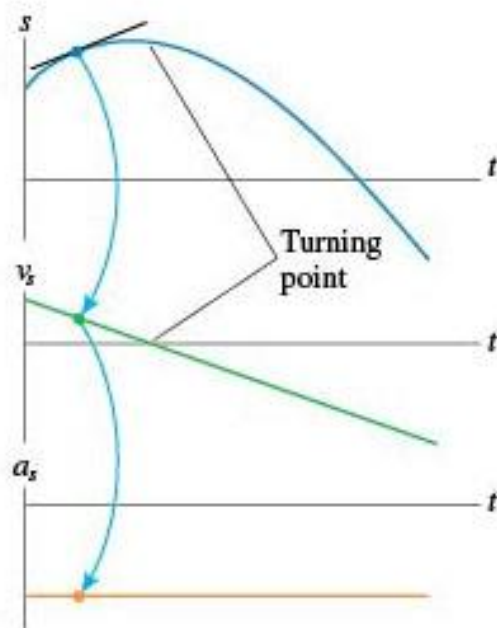
Final velocity $v_{fs} = v_{is} + \int_{t_i}^{t_f} a_s dt = v_{is} + \left\{ \begin{array}{l} \text{area under the acceleration} \\ \text{curve from } t_i \text{ to } t_f \end{array} \right.$

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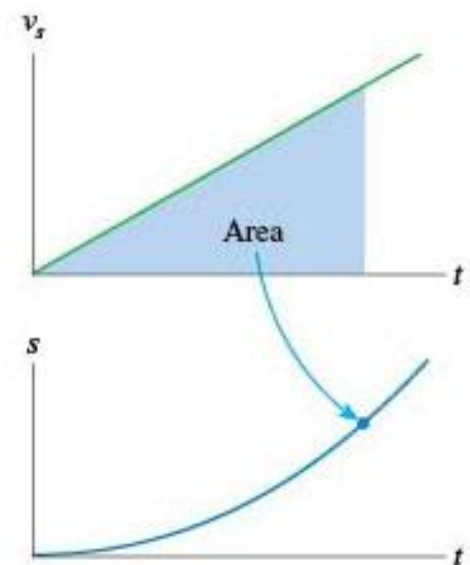
Important Concepts

Position, velocity, and acceleration are related graphically.

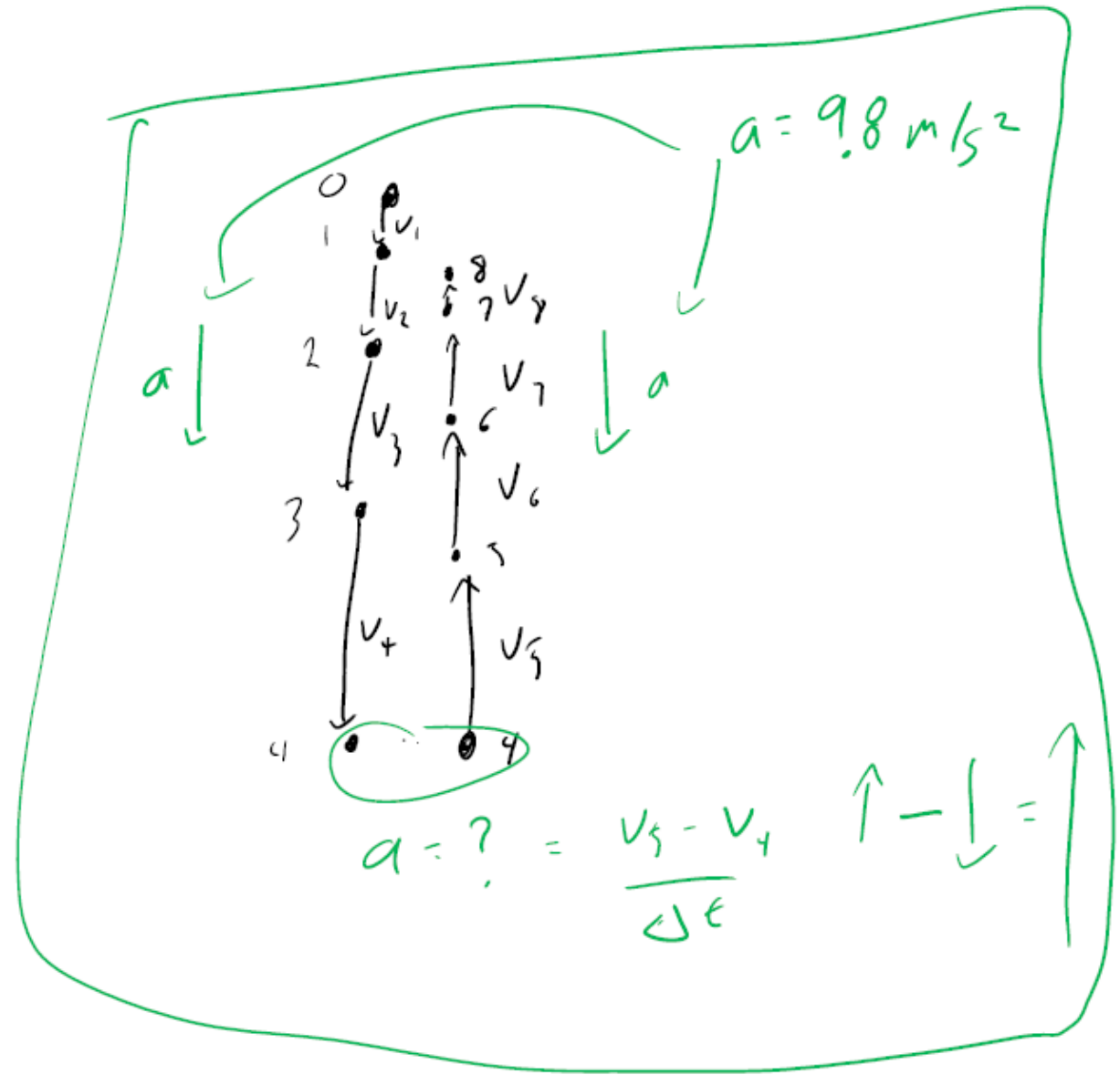
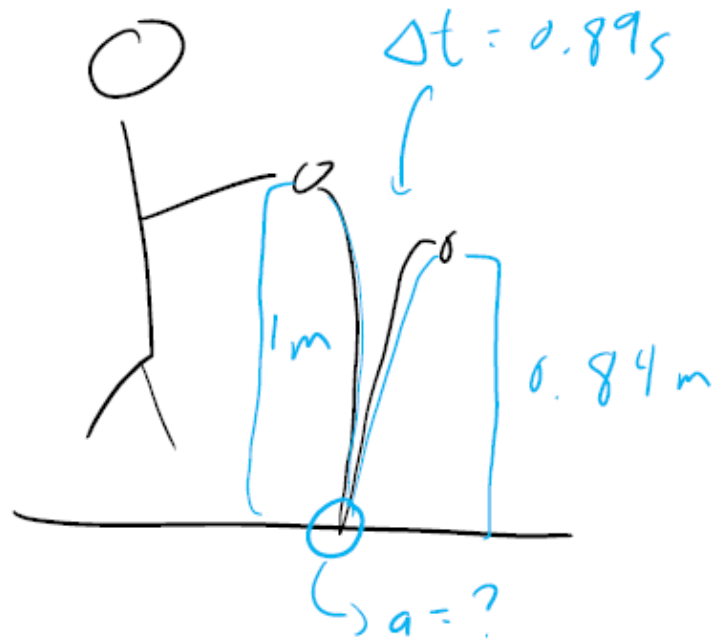
- The slope of the position-versus-time graph is the value on the velocity graph.
- The slope of the velocity graph is the value on the acceleration graph.
- s is a maximum or minimum at a turning point, and $v_s = 0$.



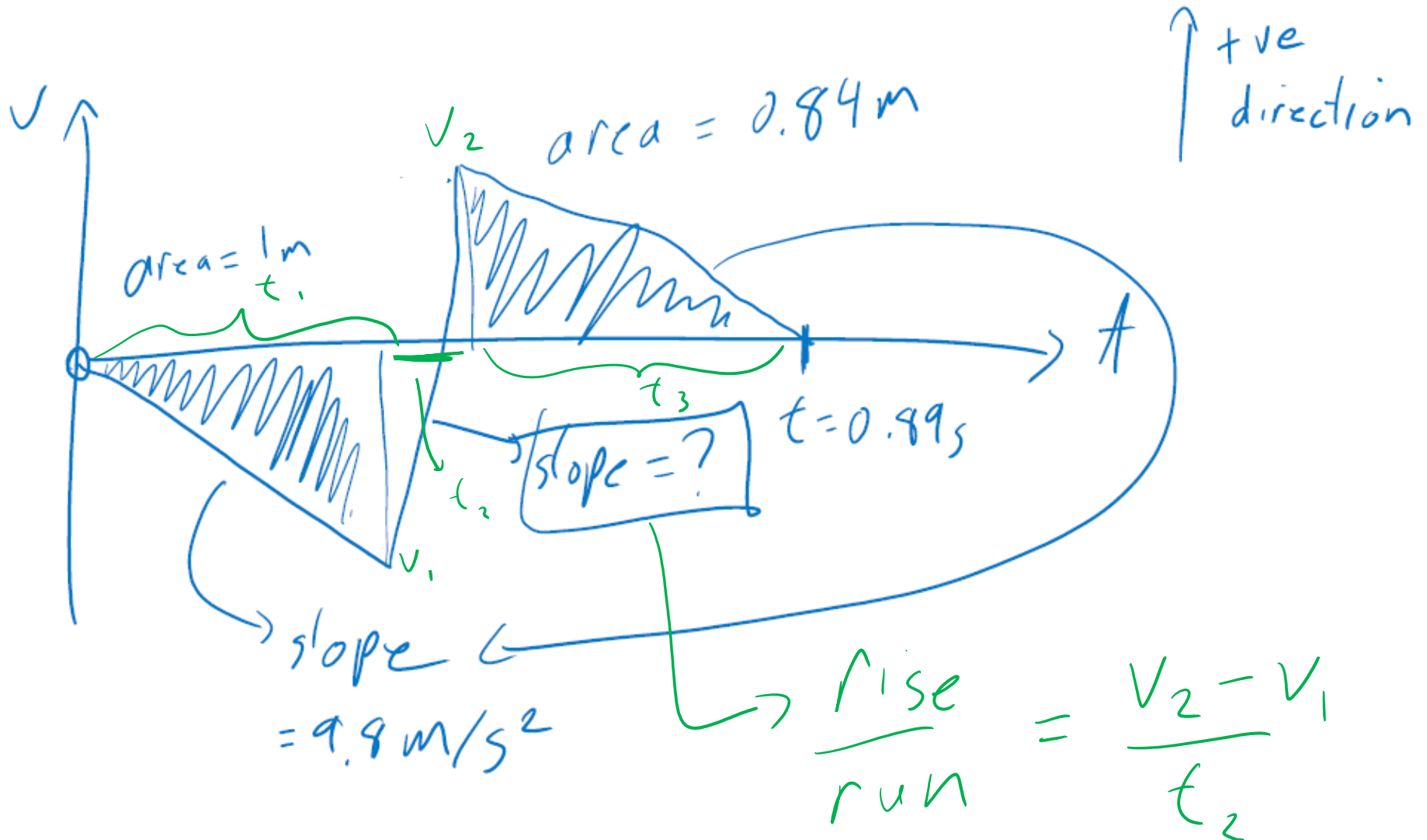
- Displacement is the area under the velocity curve.



You drop a ball from a height of 1.00 m. It bounces up to a height of 0.84 m after 0.89 s. What was the average acceleration of the ball when it was touching the ground?



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$$h_1 = -1\text{ m} = \frac{1}{2} v_1 t_1 \rightarrow t_1 = \frac{2h_1}{v_1}$$

$$a = \frac{v_2 - v_1}{t_2}$$

$$h_2 = 0.84\text{ m} = \frac{1}{2} v_2 t_3$$

$$g = 9.8 \frac{\text{m}}{\text{s}^2} = \frac{v_1}{t_1} = \frac{0 - v_2}{t_3}$$

$$350 \text{ m/s}^2$$

$$t_1 + t_2 + t_3 = 0.89\text{ s} \rightarrow t_2 = 0.89\text{ s} - t_1 - t_3$$

$$v_1^2 = 2gh_1 \rightarrow t_1 = \frac{2h_1}{\sqrt{2gh_1}}$$

$$v_2^2 = 2gh_2$$

$$a = \frac{|\sqrt{2gh_2}| + |\sqrt{2gh_1}|}{0.89\text{ s} - \sqrt{\frac{2h_1}{g}} - \sqrt{\frac{2h_2}{g}}}$$

Team Up Questions

$$S = \left(1 \frac{m}{s^4}\right) t^4$$