



(b) [4 marks] Consider the following function.

```
def f2(numbers: list[int], m: int) -> None:
    """Precondition: m >= 0"""
    for i in range(0, m):
        if i in numbers:
            print('Found')
        else:
            print('Not found')
```

Perform an **upper bound analysis of the worst-case running time** of this function, in terms of n , the length of `numbers`, and the input value m . The Big-O expression that you conclude should be *tight*, meaning that the worst-case running time should be Theta of this expression, but you are not required to show that. Use “at most” or \leq to explicitly indicate where a step count expression is an upper bound.

The inner if loop runs a maximum of m iterations, each iteration takes one step, thus the inner if loops runs at most m steps.

The outer for loop runs exactly m iterations, each iteration takes at most m steps, thus the function takes at most $m \cdot m$ steps to run.

$$\text{Thus } WC_{f_2} \in O(m \cdot m)$$

Lets say `numbers` is a list of n consecutive integers starting at m . For any i in `range(0, m)`, i will not be found in list `numbers`, causing the inner if loop to run m iterations of step always. The outer for loop runs m iterations for m steps each. Thus $WC_{f_2} \in \Omega(m \cdot m)$.

$$\text{Thus } WC_{f_2} \in \Theta(m \cdot m)$$