


# CSC110 Lecture 3: Comprehensions and Introduction to Functions

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## Exercise 1: Practice with comprehension expressions

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Here is a summary of the three types of comprehensions, for your reference:

Comprehension type	Syntax
set comprehension	<code>{ &lt;expression&gt; for &lt;variable&gt; in &lt;collection&gt; }</code>
list comprehension	<code>[ &lt;expression&gt; for &lt;variable&gt; in &lt;collection&gt; ]</code>
dict comprehension	<code>{ &lt;key_expr&gt;: &lt;value_expr&gt; for &lt;variable&gt; in &lt;collection&gt; }</code>

1. Suppose we assign the variable `numbers = [1, 2, 3]`.
  - a. Fill in the table below.

Expression	Value
<code>numbers[0]</code>	
<code>numbers[1]</code>	
<code>numbers[2]</code>	
<code>numbers[0] ** 3</code>	
<code>numbers[1] ** 3</code>	

Expression	Value
<code>numbers[2] ** 3</code>	

- b. Write a comprehension that evaluates to the *list* of every integer in `numbers` cubed (i.e., raised to the power of 3).

```
>>>

[1, 8, 27]    # Evaluating your expression should produce this
```

- c. Write a comprehension that evaluates to a *dictionary* mapping every integer in `numbers` to three times that integer.

```
>>>

{1: 3, 2: 6, 3: 9}    # Evaluating your expression should produce
                       this
```

**Hint:** the *identity dictionary comprehension* has the following form:

```
>>> {x : x for x in numbers}
```

- d. Write a comprehension that evaluates to the given output dictionary shown.

```
>>>

{3: 1, 6: 2, 9: 3}    # Evaluating your expression should produce
                       this
```

- e. Write a comprehension that is a translation of the set builder expression

$$\left\{ \frac{x}{x+1} \mid x \in \text{numbers} \right\}.$$

## Exercise 2: Comprehensions and range

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1. Write down the integers that are contained in each of the following Python `range` expressions
  - a. `range(0, 5)`
  - b. `range(5, 10)`
2. For each of the following descriptions, write a comprehension that evaluates to the described collection.
  - a. The set of integers between 30 and 50, inclusive.
  - b. The list of integers between -30 and 30, inclusive (in ascending order).
  - c. The set of the squares of the natural numbers less than 2000.
  - d. A mapping from a number to its square, for the natural numbers less than 2000.

3. You are given a variable `s` that refers to a (very very long) string:

```
>>> s = 'nonsensenonsensenonsensenonsensenonsensenonsense'
```

Write a list comprehension expression that evaluates to a list containing the first 20 characters in the string, in the order they appear.

*Hint:* `s[19]` is the last character in `s` that should be included in the list.

## Exercise 3: Practice with built-in functions

Suppose we have assigned the following variables in the Python console:

```
>>> n = -5
>>> numbers_list = [1, 10, n]
>>> numbers_set = {100, n, 200}
```

1. Complete the following table showing the value of each variable.

Variable	Value
<code>n</code>	
<code>numbers_list</code>	
<code>numbers_set</code>	

2. Write down what each of the following expressions evaluate to. *Do this by hand first! (Then check your work in the Python console.)*

You may find it helpful to consult [Appendix A.1 Python Built-In Function Reference](https://www.teach.cs.toronto.edu/~csc110y/fall/notes/A-python-builtins/01-builtins.html) (<https://www.teach.cs.toronto.edu/~csc110y/fall/notes/A-python-builtins/01-builtins.html>).

```
>>> abs(n)

>>> sorted(numbers_list)

>>> sorted(numbers_set) + sorted(numbers_list)

>>> len(numbers_set)

>>> len(numbers_list) == n

>>> sum(numbers_set) - n
```

3. The variable `numbers` refers to a list that contains a mix of positive and negative integers (e.g. `[-1, 2, 3]`). Write a comprehension that evaluates to the set of the absolute values of every integer in `numbers`.

(Hint: the structure is the same as earlier problems on this worksheet. Use the `abs` function.)

## Additional exercises

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1. *Comprehension practice.* For each of the following mappings, write a Python dictionary expression that evaluates to the mapping.

- a. A mapping from a number to its square, for the first 50 natural numbers.
  - b. A mapping from input to output of the function  $f(x) = \frac{x}{x-1}$ , for integer inputs greater than 1 and less than 2000.
  - c. A mapping from a number to a list that contains the same number of items, where every item is the string 'Hello', for the first 50 natural numbers. (e.g., 3 maps to the list ['Hello', 'Hello', 'Hello'].)
  - d. A mapping from an integer to the set of integers between 0 and that integer inclusive, for integers 1 to 20, inclusive.
2. *Comprehensions with multiple variables.* Suppose you have the lists: `nums1 = [1, 2, 3]` and `nums2 = [4, 5, 6]`.
- a. Using both `nums1` and `nums2`, write a comprehension that evaluates to: `[[1, 4], [1, 5], [1, 6], [2, 4], [2, 5], [2, 6], [3, 4], [3, 5], [3, 6]]`.
  - b. Using both `nums1` and `nums2`, write a comprehension that evaluates to: `[[4, 1], [5, 1], [6, 1], [4, 2], [5, 2], [6, 2], [4, 3], [5, 3], [6, 3]]`.
  - c. Using both `nums1` and `nums2`, write a comprehension that evaluates to: `{5, 6, 7, 8, 9}`.
3. *Function practice.* Using the same variables defined in Exercise 3, determine the value of each of the following Python expressions.

```
>>> type(n)

>>> type(abs(n))

>>> type(numbers_list == n)

>>> type(numbers_list) == type(n)

>>> max(numbers_list + [5])

>>> max(numbers_list) + 5

>>> max(sorted(numbers_list)) == max(numbers_list)
```

4. *Interpreting errors.* Your friend is practicing in the Python console again, and is trying to add two numbers. They type in the following, and get an error:

```
>>> sum(3, 4)
Traceback (most recent call last):
... [some output omitted] ...
File "<stdin>", line 1, in <module>
TypeError: 'int' object is not iterable
```

Once again, explain this error to your friend, and how they can correctly add two numbers in Python. (*Hint:* treat “iterable” as another word for “collection”.)

