CSC110 Lecture 24: Analyzing Built-In Data Type Operations

David Liu, Department of Computer Science

Navigation tip for web slides: press? to see keyboard navigation controls.

Announcements and Today's Plan

Announcements

- Assignment 4 has been posted
 - Check out the A4 FAQ (+ corrections)
 - Important simplifying precondition for Part 4b, find_collision_len_times_sum
 - Additional TA office hours
 - Review advice on academic integrity

Story so far

Up to this point, we've focused on running-time analysis where the complexity has been mainly due to **loops**.

The individual expressions/statements have been constant time (other than comprehensions):

- Arithmetic and comparison operations on numbers (+, <)
- Assignment statements (all data types)
- Calling print on numbers; calling len on collections
- Returning from a function

Today, we'll study the running time of individual operations on collection data types (list/set/dict) and data classes.

Today you'll learn to...

- 1. State the running times of operations on built-in collection data types and data classes.
- 2. Explain these running times for list operations based on how Python implements lists.
- 3. Analyze the running time of functions that use these operations.
- 4. Analyze the running time of functions that have multiple arguments (of different sizes).

Running time of list operations

Suppose we want to add an element to a list:

Add to the back:

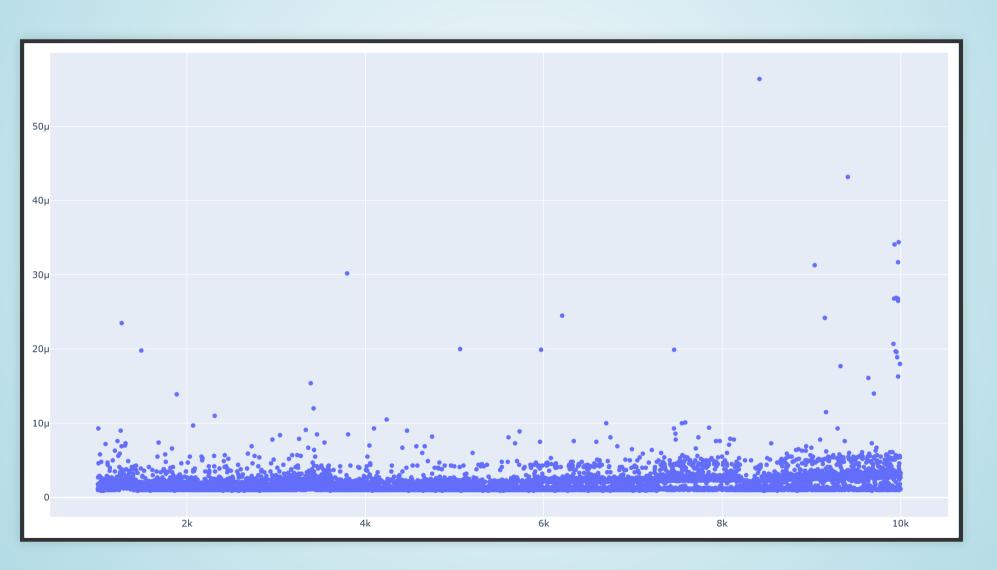
```
>>> lst = [0] * 10000000
>>> list.append(lst, 1234)
```

Add to the front:

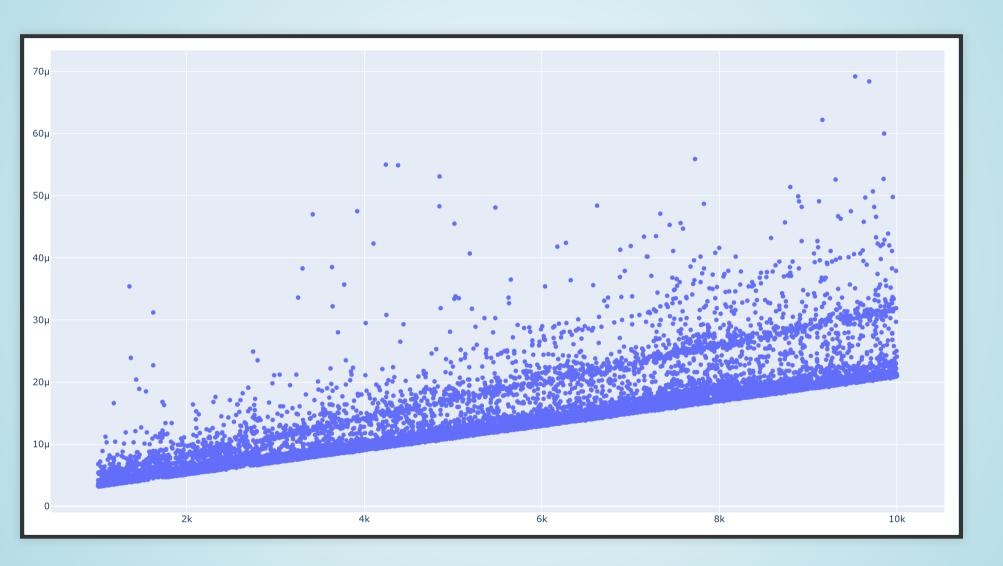
```
>>> lst = [0] * 10000000
>>> list.insert(lst, 0, 1234)
```

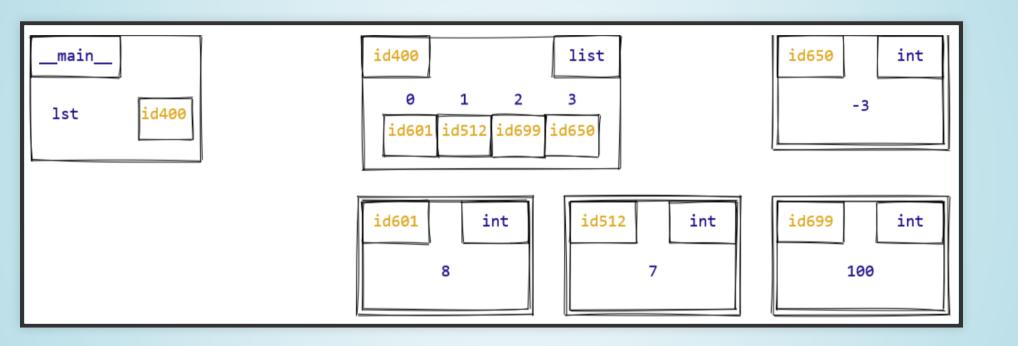
List length vs. time taken

list.append(lst, 1234)



list.insert(lst, 0, 1234)





Address	Memory	
:		
400	601	(list index 0)
401	512	
402	699	
403	650	
404		
:		
512	7	
:		
601	8	
:		
650	-3	
:		
699	100	
:		

How the Python interpreter stores lists

Each Python list has references to its elements stored in a contiguous block of memory.

(contiguous = consecutive memory locations with no gaps)

This is called an array-based list implementation.

Benefits: constant-time indexing!

To lookup the value of lst[i]:

- 1. Get the starting address of the list.
 - E.g., 400
- 2. Add i to the starting address. That block contains the reference to lst[i].
 - E.g., lst[3] is at address
 400 + 3 = 403.

List indexing (lst[i]) is $\Theta(1)$, independent of the size of the list or the index i.

Address	Memory	
:		
400	601	(list index 0)
401	512	
402	699	
403	650	
404		
:		
512	7	
:		
601	8	
:		
650	-3	
:		
699	100	
:		

Costs: insertion/deletion can be slow

All modifications to the list must preserve the contiguity of the list elements in memory.

When an element is inserted into a list, all elements after it must be shifted over to make room.

When an element is delected from a list, all elements after it must be shifted back to fill in the gap.

Address	Memory	
:		
400	601	(list index 0)
401	512	
402	699	
403	650	
404		
:		
512	7	
:		
601	8	
:		
650	-3	
:		
699	100	
:		
742	27	
:		

For a list of length n, insertion/deletion at index i takes $\Theta(n-i)$ time.

- When i = n 1 (end of the list), running time is $\Theta(1)$.
 - list.append(lst, item)
 - list.pop(lst)
- When i = 0, (front of list), running time is $\Theta(n)$.
 - list.insert(lst, 0, item)
 - list.pop(lst, 0)

Summary

Operation	Running time
List indexing (lst[i])	$\Theta(1)$
List index assignment (lst[i] =)	$\Theta(1)$
List insertion at index <i>i</i> (list.insert(lst, i,))	$\Theta(n-i)$
List deletion at index <i>i</i> (list.pop(lst, i))	$\Theta(n-i)$
List insertion at end (list.append(lst,))	$\Theta(1)$
List deletion at end (list.pop(lst))	$\Theta(1)$

Exercise 1: Running time of list operations

Analysing running time for functions with multiple parameters

```
def my_extend(lst1: list, lst2: list) -> None:
    """Add each element in lst2 to the end of lst1."""
    for item in lst2:
        list.append(lst1, item)
```

Analysis.

Let n_1 be the length of lst1 and n_2 be the length of lst2.

The loop iterates n_2 times, and each time takes constant time (1 step).

The total running time is $n_2 \cdot 1 = n_2$ steps, which is $\Theta(n_2)$.

Analysis. Let n_1 be the length of lst1 and n_2 be the length of lst2.

- The initial assignment statement takes 1 step.
- Loop 1 takes n_1 steps (n_1 iterations, 1 step per iteration)
- Loop 2 takes n_2 steps (n_2 iterations, 1 step per iteration)
- The return statement takes constant time.

The total running time is $1+n_1+n_2+1=n_1+n_2+2$, which is $\Theta(n_1+n_2)$.

Exercise 2: Running-time analysis with multiple parameters

Sets, dictionaries, and data classes

Sets

Set operations:

- x in my set
- set.add
- set.remove

Each of these operations take $\Theta(1)$ —constant time!

Sets are implemented in Python using hash tables, which are based on arrays.

Dictionaries

Dictionary operations:

- key search (k in my dict)
- key lookup/assignment (my_dict[k], my_dict[k] = ...)

Also $\Theta(1)$, very similar implementation to sets!

Data classes

Data class operations:

- attribute lookup (david.age)
- attribute assignment (david.age = ...)

Also $\Theta(1)$, very similar implementation to dictionaries (and sets)!

Exercise 3: Sets, dictionaries, and data classes (if time)

Some built-in aggregation functions

Most aggregation functions take $\Theta(n)$ time (where n is the size of the collection).

sum, max, min

len is special: it takes $\Theta(1)$ time—independent of the size of the collection!

Behind the scenes: a "hidden" size attribute stored by the Python interpreter for every collection object.

any/all are special, because they're implemented with an early return.

- any can stop as soon as it encounters a True
- all can stop as soon as it encounters a False

To be continued next class...

Summary

Today you learned to...

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Homework

- Readings:
 - Review: 9.5, 9.6
 - From today: 9.7
 - For tomorrow: 9.8
- Work on Assignment 4!

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