Anomaly Detection

Algorithms in Machine Learning, ISAE-SUPAERO

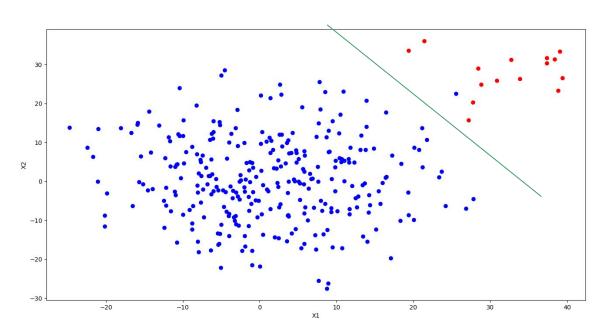
Fabrice Jimenez

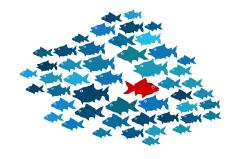
Data Scientist & Artificial Intelligence Engineer

Airbus Commercial Aircraft

Anomaly detection: intuition

Build a model to detect anomalies (labeled in red here)... what do you do?





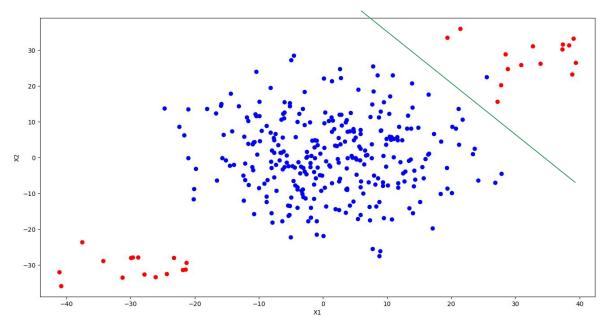
Supervised Learning?

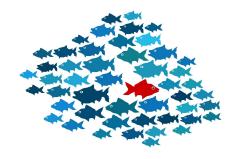
Naive bayes classifier, Random Forest, SVM...

- → Features = X1, X2
- → Label = Anomaly or not (0 or 1)

Anomaly detection: intuition

Build a model to detect anomalies (labeled in red here)... what do you do?



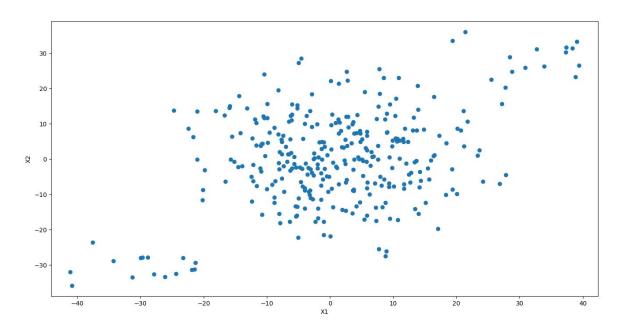


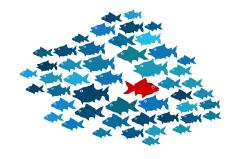
What if new anomalies?



Anomaly detection: intuition

Build a model to detect anomalies... what do you do?





What if no label?



Anomaly detection: definition and scope

What is an anomaly? 1/ Generally: a rare individual (row) in a dataset that differs significantly from the majority of the data 2/ Sometimes: anomalies are not so rare, and may not be so different from the majority of the data... **Anomalies** Normal during mid-season Normal during winter -20 **Normal during summer** -10 10 20

Anomaly detection: definition and scope

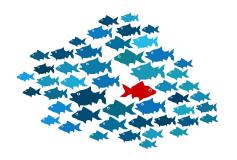
Why not using Supervised Learning with labeled dataset?

Very unbalanced dataset

5 anomalies given 100 000 normal points...

Lack of coverage of all anomaly types

Anomaly = something not expected, what if a new type happens...



We need other approaches...

Outlier detection: the dataset contains anomalies in the sense of statement 1/ (rare + statistically different)

→ Detect elements in this same dataset which differ from the majority of the data

Novelty detection: you have a clean dataset without anomalies (in the sense of 1/ or 2/)

→ Learn the normal behavior, to be able to check if a new item is normal or an anomaly

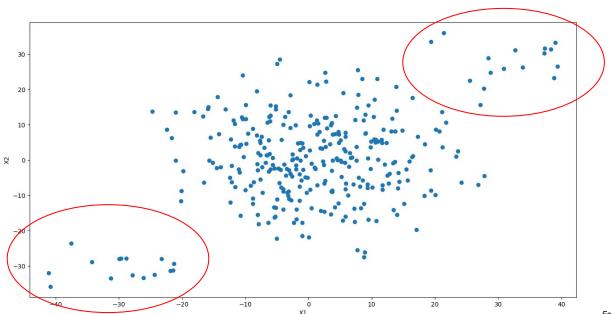
→ Some techniques can be used for both, but be aware of the approach you are using, and why...

Outlier detection

1/ Anomaly = a rare individual (row) in a dataset that differs significantly from the majority of the data

Outlier detection: the dataset contains anomalies in the sense of statement 1/

→ Detect elements in this same dataset which differ from the majority of the data



Example

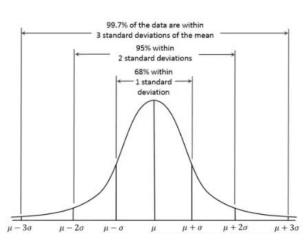
1 feature x



Х

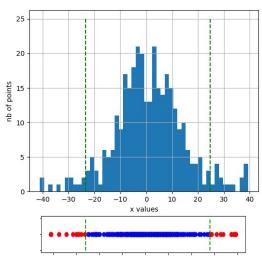
Univariate case: in 1 dimension (1 variable), how would you detect anomalies?





Remember your normal distribution!

→ Mean and Std help quantify density of data



→ outliers = points outside [mean - 2xstd, mean + 2xstd]

Are mean and std always reliable?

They quantify the data density in the case of normal distribution... It is not always the case!

Sensitive to outliers!

If too far outliers or many outliers → distorts estimation!

What is the alternative?

Let's go MAD!

Robustify mean? → median

Robustify standard deviation? → ...

MAD = Median Absolute Deviation = median(|x - median(x)|)



Robust thresholds

Example:

→ outliers = points outside [median - 3xMAD, median + 3xMAD]

What threshold to use? Why 3 x MAD?

- → there are relationships to quantify percentiles with median and MAD
- → they depend on the type of distribution...
- → Thresholds always need human intervention / fine-tuning!

Multivariate case: generalize what we saw in 1D?

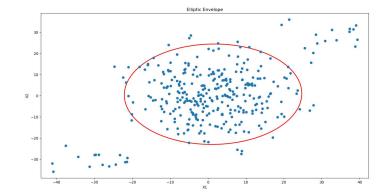
→ 1st approach: median and MAD on each of the variables (still univariate...)

It does not take at all into account relationship between x1 and x2...

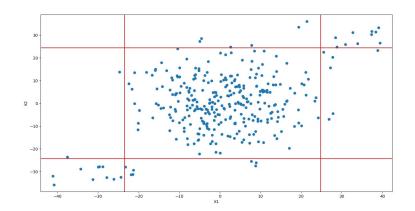
→ We can use covariance matrix!

$$\sum = \frac{1}{n} \times (M - \bar{M})^T \cdot (M - \bar{M})$$

We can use covariance matrix!
$$\sum = \frac{1}{n} \times \left(M - \bar{M} \right)^T \cdot \left(M - \bar{M} \right) \qquad M = \begin{bmatrix} X_{1\,1} & \dots & X_{1\,p} \\ \dots & \dots & \dots \\ X_{n\,1} & \dots & X_{n\,p} \end{bmatrix}$$



Elliptic envelope → Threshold to define!



Mahalanobis distance of a point to the distribution:

$$X = (X_1, X_2, ..., X_n)$$
$$D(X, M) = \sqrt{(X - \mu)^T \Sigma^{-1} (X - \mu)}$$

If scaled distribution, Euclidean distance to the center!

For more details on robust covariance estimator (FastMCD algorithm): A Fast Algorithm for the Minimum Covariance Determinant Estimator

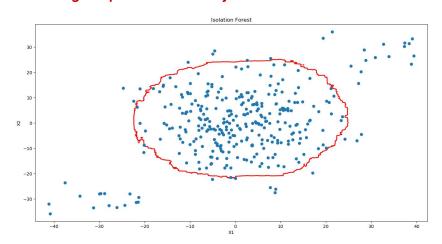
Peter J. Rousseeuw and Katrien Van Driessen

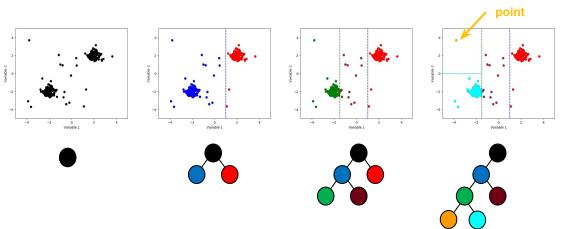
Other methods - Isolation Forest

- → 1/ Build Isolation Tree:

 Split entire dataset with random variables and random thresholds
- → 2/ Repeat with 100, 1000 trees...
- → 3/ Average depth of a point in the forest
- ≈ anomaly score*

Low depth = high anomaly score High depth = low anomaly score





Once again, threshold to define!

Advantages:

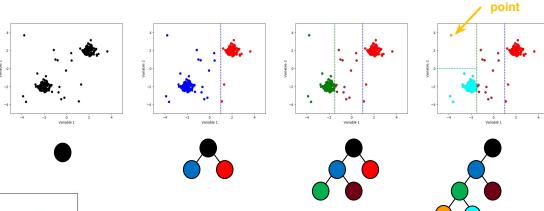
- → Few hyperparameters to tune
- → Linear complexity: time does not explode with volume!

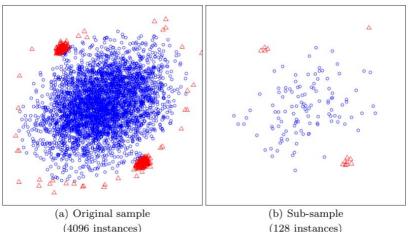
Isolated

^{*} Anomaly score = average depth normalized with average depth of unsuccessful searches in a binary search tree. For more details: *Isolation-based Anomaly Detection*, Fei Tony Liu and Kai Ming Ting

Other methods - Isolation Forest

Not exactly true... Each tree splits a subset of the data (max 256 points) to avoid swamping and masking





Swamping: predicting normal points as anomalies, because local density is lower

Masking: locally dense anomaly clusters, therefore predicting these anomalies as normal points

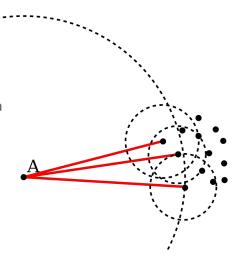
Subsampling reduces these 2 effects

Isolated

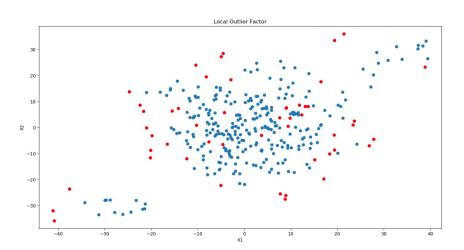
Other methods - Local Outlier Factor (LOF)

- → 1/ For each point A, compute the average distance to its' k nearest neighbors d
- → 2/ The inverse 1/d is the local reachability density Ird(A)
- → 3/ LOF: average(Ird(k-neighbors)) / Ird(A)

Point A has lower density than his neighbors with k=3



LOF <= 1: similar or higher density than neighbors = low anomaly score LOF > 1: lower density than neighbors = high anomaly score



Not exactly true... Not the average distance but the average k-distance = distance if point further than k-th neighbor, else distance to k-th neighbor

Once again, threshold to define!

Advantage:

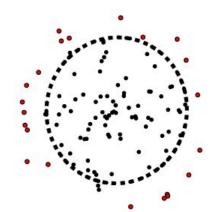
→ Locality aspect: points close to very dense cluster can still be anomalies, compared to "border"-based methods

For more details:

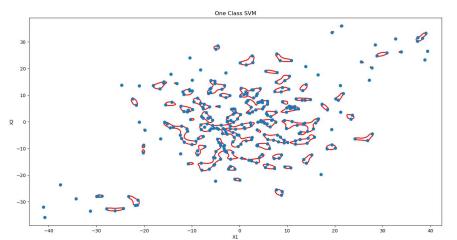
LOF: Identifying Density-Based Local Outliers
Markus M. Breunig, Hans-Peter Kriegel, Raymond T. Ng, Jörg Sander

Other methods - One Class SVM

- → Simple idea: draw a circle around your data points!
- → You allow a "soft-margin", tuned with parameter nu (contamination rate), because you have outliers in your dataset
- → With a kernel: projection of dataset in higher dimension, compute the circle, translate into a non-linear boundary in initial space!



Outside circle: outlier Inside circle: normal point



Kernel trick used as regular **SVM**: no need to know the projection, just the dot product...

Once again, threshold to define!

Advantage:

→ Complex boundary definition

Inconvenient:

→ Very sensitive to threshold and choice of kernel...

For more details:

Estimating the Support of a High-Dimensional Distribution Bernhard Scholkopf et al.

It's time to play with these methods with sklearn...

Main interest = play with parameters to see the impact on detection boundaries, and explain it through theory



Outlier detection: score VS decision

Be careful!

- → These unsupervised methods give only a relative measure of abnormality
 - → Elliptic envelope: mahalanobis distance
 - → iForest: average depth
 - → LOF: density ratio with neighbors

•••



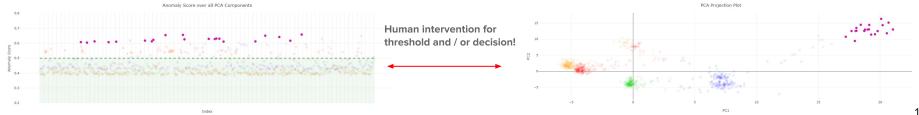
- → The decision itself (outlier or not) is proposed by default in those methods, but it always requires threshold tuning!
 - → Always need for human intervention, especially with complex interdependent systems!
 - → For example: cross the anomaly scores with manual cluster analysis with PCA, geometrical interpretation...

NOT because technology is not mature enough...

BUT because the problem is badly formulated!

Continuous scores

"Anomaly" is not clearly defined a priori, and statistics will never tell you what it is!

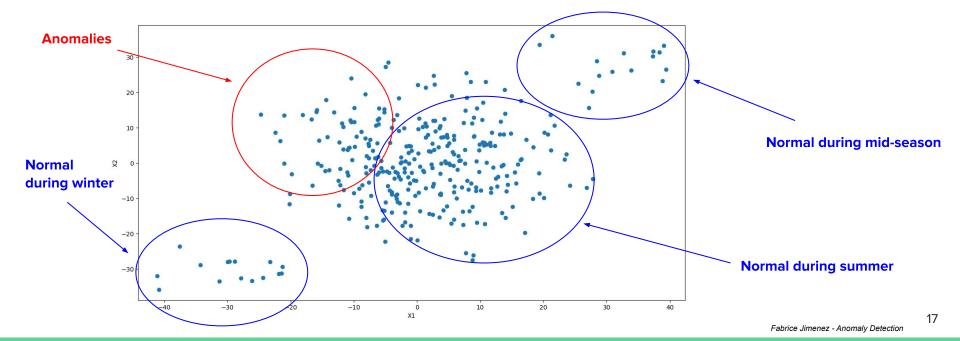


Novelty detection

2/ Anomalies = not so rare, and may not be so different from the majority of the data...

Novelty detection: you have a clean dataset without anomalies (in the sense of 1/ or 2/)

→ Learn the normal behavior, to be able to check if a new item is normal or an anomaly



Novelty detection

Basic principle

Clean dataset without anomalies: "learn" the normal behavior.

Predict the value / score of new points to find out if they match the normal behavior or not

→ Unsupervised methods we have seen can be used in this case (One Class SVM is even better at this than outlier detection!)

New possibilities

Why not using supervised learning to learn the normal behavior?

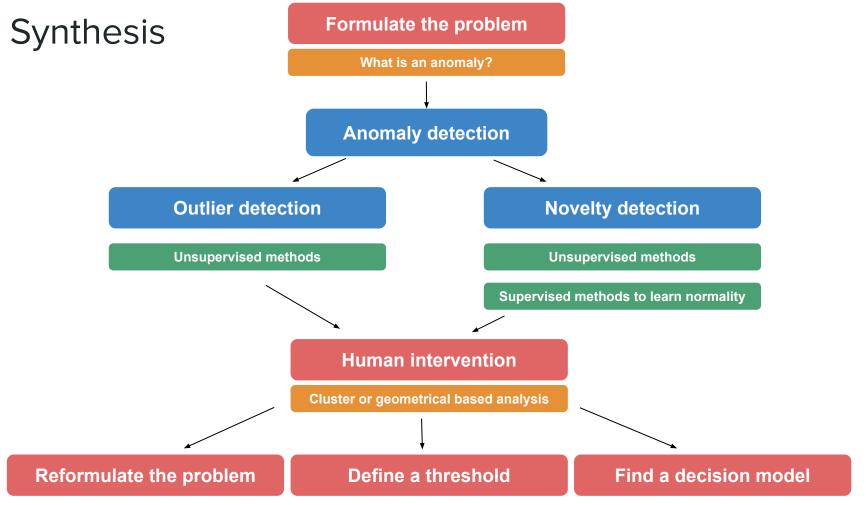
v1	v2	v3
8.4	15	2.2
9.1	10	5.1

Model 1: v1 = f(v2,v3)Model 2: v2 = f(v1,v3)Model 3: v3 = f(v1,v2) Predict each variable by using the others as features:

- → Linear regression
- → Random Forest
- → SVM...
- → A new point comes in: (x1,x2,x3)
- → Compute the predictions [x1] = f(x2,x3), [x2] = f(x1,x3), [x3] = f(x1,x2)
- → Compute the errors [xi] xi : squared error, absolute error...

High error = does not fit the "normal" model = high anomaly score

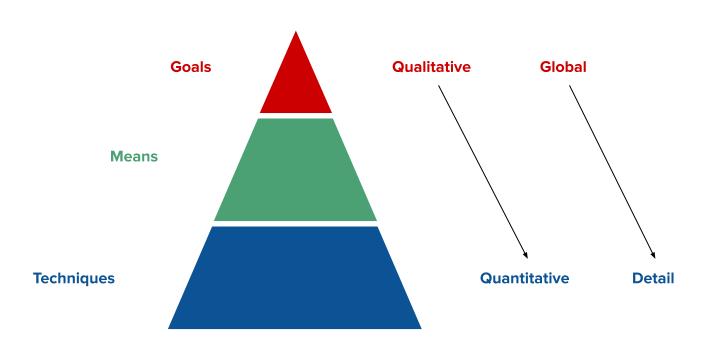




Quick piece of advice...

Machine Learning = complex field → a lot of: models, ideas, approaches, theories... every day!

How to keep up the rhythm? → Build your own understanding, from global to detail



Example:

Based on historical data, detect when behavior is changing

Novelty detection: learn normal past behavior, use prediction error as anomaly score

Random Forest regression to predict each feature in function of others, use mean squared error

Questions?

