

two_layer_net

September 26, 2019

1 Implementing a Neural Network

In this exercise we will develop a neural network with fully-connected layers to perform classification, and test it out on the CIFAR-10 dataset.

In [47]: *# A bit of setup*

```
import numpy as np
import matplotlib.pyplot as plt

%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# for auto-reloading external modules
# see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ipython
%load_ext autoreload
%autoreload 2

def rel_error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

The autoreload extension is already loaded. To reload it, use:

```
%reload_ext autoreload
```

The neural network parameters will be stored in a dictionary (model below), where the keys are the parameter names and the values are numpy arrays. Below, we initialize toy data and a toy model that we will use to verify your implementations.

In [48]: *# Create some toy data to check your implementations*

```
input_size = 4
hidden_size = 10
num_classes = 3
num_inputs = 5
```

```

def init_toy_model():
    model = {}
    model['W1'] = np.linspace(-0.2, 0.6, num=input_size*hidden_size).reshape(input_size, hidden_size)
    model['b1'] = np.linspace(-0.3, 0.7, num=hidden_size)
    model['W2'] = np.linspace(-0.4, 0.1, num=hidden_size*num_classes).reshape(hidden_size, num_classes)
    model['b2'] = np.linspace(-0.5, 0.9, num=num_classes)
    return model

def init_toy_data():
    X = np.linspace(-0.2, 0.5, num=num_inputs*input_size).reshape(num_inputs, input_size)
    y = np.array([0, 1, 2, 2, 1])
    return X, y

model = init_toy_model()
X, y = init_toy_data()

```

2 Forward pass: compute scores

Open the file `cs231n/classifiers/neural_net.py` and look at the function `two_layer_net`. This function is very similar to the loss functions you have written for the Softmax exercise in HW0: It takes the data and weights and computes the class scores, the loss, and the gradients on the parameters.

Implement the first part of the forward pass which uses the weights and biases to compute the scores for all inputs.

```

In [49]: from cs231n.classifiers.neural_net import two_layer_net

scores = two_layer_net(X, model)
print(scores)
correct_scores = [[-0.5328368, 0.20031504, 0.93346689],
                  [-0.59412164, 0.15498488, 0.9040914 ],
                  [-0.67658362, 0.08978957, 0.85616275],
                  [-0.77092643, 0.01339997, 0.79772637],
                  [-0.89110401, -0.08754544, 0.71601312]]

# the difference should be very small. We get 3e-8
print('Difference between your scores and correct scores:')
print(np.sum(np.abs(scores - correct_scores)))

[[-0.5328368  0.20031504  0.93346689]
 [-0.59412164  0.15498488  0.9040914 ]
 [-0.67658362  0.08978957  0.85616275]
 [-0.77092643  0.01339997  0.79772637]
 [-0.89110401 -0.08754544  0.71601312]]
Difference between your scores and correct scores:
3.848682303062012e-08

```

3 Forward pass: compute loss

In the same function, implement the second part that computes the data and regularization loss.

```
In [50]: reg = 0.1
         loss, _ = two_layer_net(X, model, y, reg)
         correct_loss = 1.38191946092

         # should be very small, we get 5e-12
         print('Difference between your loss and correct loss:')
         print(np.sum(np.abs(loss - correct_loss)))
```

```
Difference between your loss and correct loss:
4.6769255135359344e-12
```

4 Backward pass

Implement the rest of the function. This will compute the gradient of the loss with respect to the variables $W1$, $b1$, $W2$, and $b2$. Now that you (hopefully!) have a correctly implemented forward pass, you can debug your backward pass using a numeric gradient check:

```
In [54]: from cs231n.gradient_check import eval_numerical_gradient

         # Use numeric gradient checking to check your implementation of the backward pass.
         # If your implementation is correct, the difference between the numeric and
         # analytic gradients should be less than 1e-8 for each of W1, W2, b1, and b2.

         loss, grads = two_layer_net(X, model, y, reg)

         # these should all be less than 1e-8 or so
         for param_name in grads:
             param_grad_num = eval_numerical_gradient(lambda W: two_layer_net(X, model, y, reg)[0],
                                                         {param_name: grads[param_name]})
             print('%s max relative error: %e' % (param_name, rel_error(param_grad_num, grads[param_name])))
```

```
W2 max relative error: 1.401431e-09
b2 max relative error: 7.311059e-11
W1 max relative error: 4.426512e-09
b1 max relative error: 2.746125e-08
```

5 Train the network

To train the network we will use SGD with Momentum. Last assignment you implemented vanilla SGD. You will now implement the momentum update and the RMSProp update. Open the file `classifier_trainer.py` and familiarize yourself with the `ClassifierTrainer` class. It performs optimization given an arbitrary cost function data, and model. By default it uses vanilla SGD,

which we have already implemented for you. First, run the optimization below using Vanilla SGD:

```
In [55]: from cs231n.classifier_trainer import ClassifierTrainer

model = init_toy_model()
trainer = ClassifierTrainer()
# call the trainer to optimize the loss
# Notice that we're using sample_batches=False, so we're performing Gradient Descent
best_model, loss_history, _, _ = trainer.train(X, y, X, y,
                                              model, two_layer_net,
                                              reg=0.001,
                                              learning_rate=1e-1, momentum=0.0, learning_rate_decay=0.9,
                                              update='sgd', sample_batches=False,
                                              num_epochs=100,
                                              verbose=False)

print('Final loss with vanilla SGD: %f' % (loss_history[-1], ))

starting iteration  0
starting iteration 10
starting iteration 20
starting iteration 30
starting iteration 40
starting iteration 50
starting iteration 60
starting iteration 70
starting iteration 80
starting iteration 90
Final loss with vanilla SGD: 0.940686
```

Now fill in the **momentum update** in the first missing code block inside the train function, and run the same optimization as above but with the momentum update. You should see a much better result in the final obtained loss:

```
In [56]: model = init_toy_model()
trainer = ClassifierTrainer()
# call the trainer to optimize the loss
# Notice that we're using sample_batches=False, so we're performing Gradient Descent
best_model, loss_history, _, _ = trainer.train(X, y, X, y,
                                              model, two_layer_net,
                                              reg=0.001,
                                              learning_rate=1e-1, momentum=0.9, learning_rate_decay=0.9,
                                              update='momentum', sample_batches=False,
                                              num_epochs=100,
                                              verbose=False)

correct_loss = 0.494394
print('Final loss with momentum SGD: %f. We get: %f' % (loss_history[-1], correct_loss))
```

```

starting iteration 0
starting iteration 10
starting iteration 20
starting iteration 30
starting iteration 40
starting iteration 50
starting iteration 60
starting iteration 70
starting iteration 80
starting iteration 90
Final loss with momentum SGD: 0.494394. We get: 0.494394

```

The **RMSProp** update step is given as follows:

```

cache = decay_rate * cache + (1 - decay_rate) * dx**2
x += - learning_rate * dx / np.sqrt(cache + 1e-8)

```

Here, `decay_rate` is a hyperparameter and typical values are [0.9, 0.99, 0.999].

Implement the **RMSProp** update rule inside the `train` function and rerun the optimization:

```

In [57]: model = init_toy_model()
         trainer = ClassifierTrainer()
         # call the trainer to optimize the loss
         # Notice that we're using sample_batches=False, so we're performing Gradient Descent
         best_model, loss_history, _, _ = trainer.train(X, y, X, y,
                                                         model, two_layer_net,
                                                         reg=0.001,
                                                         learning_rate=1e-1, momentum=0.9, learning_rate_decay=0.9,
                                                         update='rmsprop', sample_batches=False,
                                                         num_epochs=100,
                                                         verbose=False)

         correct_loss = 0.439368
         print('Final loss with RMSProp: %f. We get: %f' % (loss_history[-1], correct_loss))

starting iteration 0
starting iteration 10
starting iteration 20
starting iteration 30
starting iteration 40
starting iteration 50
starting iteration 60
starting iteration 70
starting iteration 80
starting iteration 90
Final loss with RMSProp: 0.439368. We get: 0.439368

```

6 Load the data

Now that you have implemented a two-layer network that passes gradient checks, it's time to load up our favorite CIFAR-10 data so we can use it to train a classifier.

```
In [58]: from cs231n.data_utils import load_CIFAR10

def get_CIFAR10_data(num_training=49000, num_validation=1000, num_test=1000):
    """
    Load the CIFAR-10 dataset from disk and perform preprocessing to prepare
    it for the two-layer neural net classifier.
    """
    # Load the raw CIFAR-10 data
    cifar10_dir = 'cs231n/datasets/cifar-10-batches-py'
    X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)

    # Subsample the data
    mask = range(num_training, num_training + num_validation)
    X_val = X_train[mask]
    y_val = y_train[mask]
    mask = range(num_training)
    X_train = X_train[mask]
    y_train = y_train[mask]
    mask = range(num_test)
    X_test = X_test[mask]
    y_test = y_test[mask]

    # Normalize the data: subtract the mean image
    mean_image = np.mean(X_train, axis=0)
    X_train -= mean_image
    X_val -= mean_image
    X_test -= mean_image

    # Reshape data to rows
    X_train = X_train.reshape(num_training, -1)
    X_val = X_val.reshape(num_validation, -1)
    X_test = X_test.reshape(num_test, -1)

    return X_train, y_train, X_val, y_val, X_test, y_test

# Invoke the above function to get our data.
X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
print('Train data shape: ', X_train.shape)
print('Train labels shape: ', y_train.shape)
print('Validation data shape: ', X_val.shape)
print('Validation labels shape: ', y_val.shape)
print('Test data shape: ', X_test.shape)
```

```
print('Test labels shape: ', y_test.shape)
```

```
Train data shape: (49000, 3072)
Train labels shape: (49000,)
Validation data shape: (1000, 3072)
Validation labels shape: (1000,)
Test data shape: (1000, 3072)
Test labels shape: (1000,)
```

7 Train a network

To train our network we will use SGD with momentum. In addition, we will adjust the learning rate with an exponential learning rate schedule as optimization proceeds; after each epoch, we will reduce the learning rate by multiplying it by a decay rate.

```
In [59]: from cs231n.classifiers.neural_net import init_two_layer_model
```

```
model = init_two_layer_model(32*32*3, 50, 10) # input size, hidden size, number of classes
trainer = ClassifierTrainer()
best_model, loss_history, train_acc, val_acc = trainer.train(X_train, y_train, X_val,
                                                             model, two_layer_net,
                                                             num_epochs=5, reg=1.0,
                                                             momentum=0.9, learning_rate_decay = 0.95,
                                                             learning_rate=1e-5, verbose=True)
```

```
starting iteration 0
Finished epoch 0 / 5: cost 2.302593, train: 0.086000, val 0.088000, lr 1.000000e-05
starting iteration 10
starting iteration 20
starting iteration 30
starting iteration 40
starting iteration 50
starting iteration 60
starting iteration 70
starting iteration 80
starting iteration 90
starting iteration 100
starting iteration 110
starting iteration 120
starting iteration 130
starting iteration 140
starting iteration 150
starting iteration 160
starting iteration 170
starting iteration 180
starting iteration 190
starting iteration 200
```

starting iteration 210
starting iteration 220
starting iteration 230
starting iteration 240
starting iteration 250
starting iteration 260
starting iteration 270
starting iteration 280
starting iteration 290
starting iteration 300
starting iteration 310
starting iteration 320
starting iteration 330
starting iteration 340
starting iteration 350
starting iteration 360
starting iteration 370
starting iteration 380
starting iteration 390
starting iteration 400
starting iteration 410
starting iteration 420
starting iteration 430
starting iteration 440
starting iteration 450
starting iteration 460
starting iteration 470
starting iteration 480
Finished epoch 1 / 5: cost 2.279186, train: 0.172000, val 0.185000, lr 9.500000e-06
starting iteration 490
starting iteration 500
starting iteration 510
starting iteration 520
starting iteration 530
starting iteration 540
starting iteration 550
starting iteration 560
starting iteration 570
starting iteration 580
starting iteration 590
starting iteration 600
starting iteration 610
starting iteration 620
starting iteration 630
starting iteration 640
starting iteration 650
starting iteration 660
starting iteration 670

starting iteration 680
starting iteration 690
starting iteration 700
starting iteration 710
starting iteration 720
starting iteration 730
starting iteration 740
starting iteration 750
starting iteration 760
starting iteration 770
starting iteration 780
starting iteration 790
starting iteration 800
starting iteration 810
starting iteration 820
starting iteration 830
starting iteration 840
starting iteration 850
starting iteration 860
starting iteration 870
starting iteration 880
starting iteration 890
starting iteration 900
starting iteration 910
starting iteration 920
starting iteration 930
starting iteration 940
starting iteration 950
starting iteration 960
starting iteration 970
Finished epoch 2 / 5: cost 2.122511, train: 0.274000, val 0.237000, lr 9.025000e-06
starting iteration 980
starting iteration 990
starting iteration 1000
starting iteration 1010
starting iteration 1020
starting iteration 1030
starting iteration 1040
starting iteration 1050
starting iteration 1060
starting iteration 1070
starting iteration 1080
starting iteration 1090
starting iteration 1100
starting iteration 1110
starting iteration 1120
starting iteration 1130
starting iteration 1140

starting iteration 1150
starting iteration 1160
starting iteration 1170
starting iteration 1180
starting iteration 1190
starting iteration 1200
starting iteration 1210
starting iteration 1220
starting iteration 1230
starting iteration 1240
starting iteration 1250
starting iteration 1260
starting iteration 1270
starting iteration 1280
starting iteration 1290
starting iteration 1300
starting iteration 1310
starting iteration 1320
starting iteration 1330
starting iteration 1340
starting iteration 1350
starting iteration 1360
starting iteration 1370
starting iteration 1380
starting iteration 1390
starting iteration 1400
starting iteration 1410
starting iteration 1420
starting iteration 1430
starting iteration 1440
starting iteration 1450
starting iteration 1460
Finished epoch 3 / 5: cost 1.995343, train: 0.282000, val 0.292000, lr 8.573750e-06
starting iteration 1470
starting iteration 1480
starting iteration 1490
starting iteration 1500
starting iteration 1510
starting iteration 1520
starting iteration 1530
starting iteration 1540
starting iteration 1550
starting iteration 1560
starting iteration 1570
starting iteration 1580
starting iteration 1590
starting iteration 1600
starting iteration 1610

starting iteration 1620
starting iteration 1630
starting iteration 1640
starting iteration 1650
starting iteration 1660
starting iteration 1670
starting iteration 1680
starting iteration 1690
starting iteration 1700
starting iteration 1710
starting iteration 1720
starting iteration 1730
starting iteration 1740
starting iteration 1750
starting iteration 1760
starting iteration 1770
starting iteration 1780
starting iteration 1790
starting iteration 1800
starting iteration 1810
starting iteration 1820
starting iteration 1830
starting iteration 1840
starting iteration 1850
starting iteration 1860
starting iteration 1870
starting iteration 1880
starting iteration 1890
starting iteration 1900
starting iteration 1910
starting iteration 1920
starting iteration 1930
starting iteration 1940
starting iteration 1950
Finished epoch 4 / 5: cost 1.783637, train: 0.339000, val 0.333000, lr 8.145063e-06
starting iteration 1960
starting iteration 1970
starting iteration 1980
starting iteration 1990
starting iteration 2000
starting iteration 2010
starting iteration 2020
starting iteration 2030
starting iteration 2040
starting iteration 2050
starting iteration 2060
starting iteration 2070
starting iteration 2080

```
starting iteration 2090
starting iteration 2100
starting iteration 2110
starting iteration 2120
starting iteration 2130
starting iteration 2140
starting iteration 2150
starting iteration 2160
starting iteration 2170
starting iteration 2180
starting iteration 2190
starting iteration 2200
starting iteration 2210
starting iteration 2220
starting iteration 2230
starting iteration 2240
starting iteration 2250
starting iteration 2260
starting iteration 2270
starting iteration 2280
starting iteration 2290
starting iteration 2300
starting iteration 2310
starting iteration 2320
starting iteration 2330
starting iteration 2340
starting iteration 2350
starting iteration 2360
starting iteration 2370
starting iteration 2380
starting iteration 2390
starting iteration 2400
starting iteration 2410
starting iteration 2420
starting iteration 2430
starting iteration 2440
Finished epoch 5 / 5: cost 1.874293, train: 0.360000, val 0.363000, lr 7.737809e-06
finished optimization. best validation accuracy: 0.363000
```

8 Debug the training

With the default parameters we provided above, you should get a validation accuracy of about 0.37 on the validation set. This isn't very good.

One strategy for getting insight into what's wrong is to plot the loss function and the accuracies on the training and validation sets during optimization.

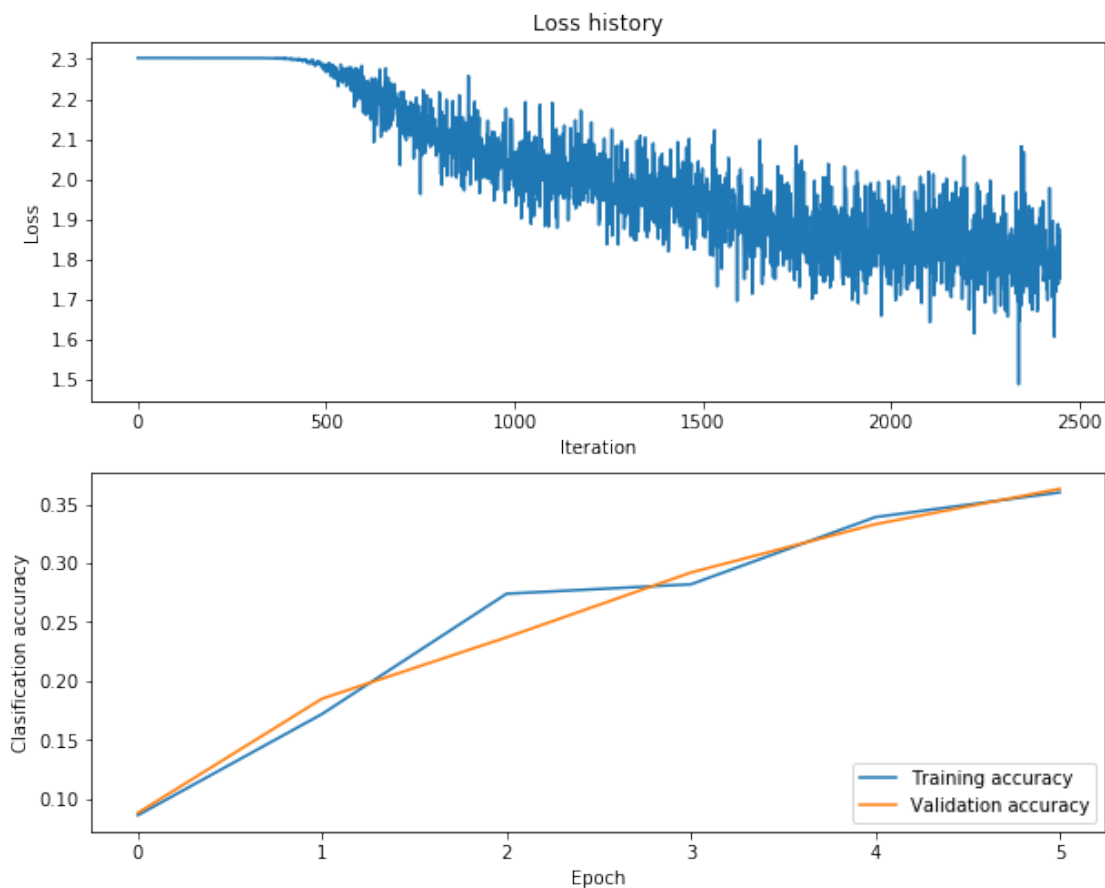
Another strategy is to visualize the weights that were learned in the first layer of the network.

In most neural networks trained on visual data, the first layer weights typically show some visible structure when visualized.

```
In [60]: # Plot the loss function and train / validation accuracies
plt.subplot(2, 1, 1)
plt.plot(loss_history)
plt.title('Loss history')
plt.xlabel('Iteration')
plt.ylabel('Loss')

plt.subplot(2, 1, 2)
plt.plot(train_acc)
plt.plot(val_acc)
plt.legend(['Training accuracy', 'Validation accuracy'], loc='lower right')
plt.xlabel('Epoch')
plt.ylabel('Clasification accuracy')

Out[60]: Text(0,0.5,'Clasification accuracy')
```

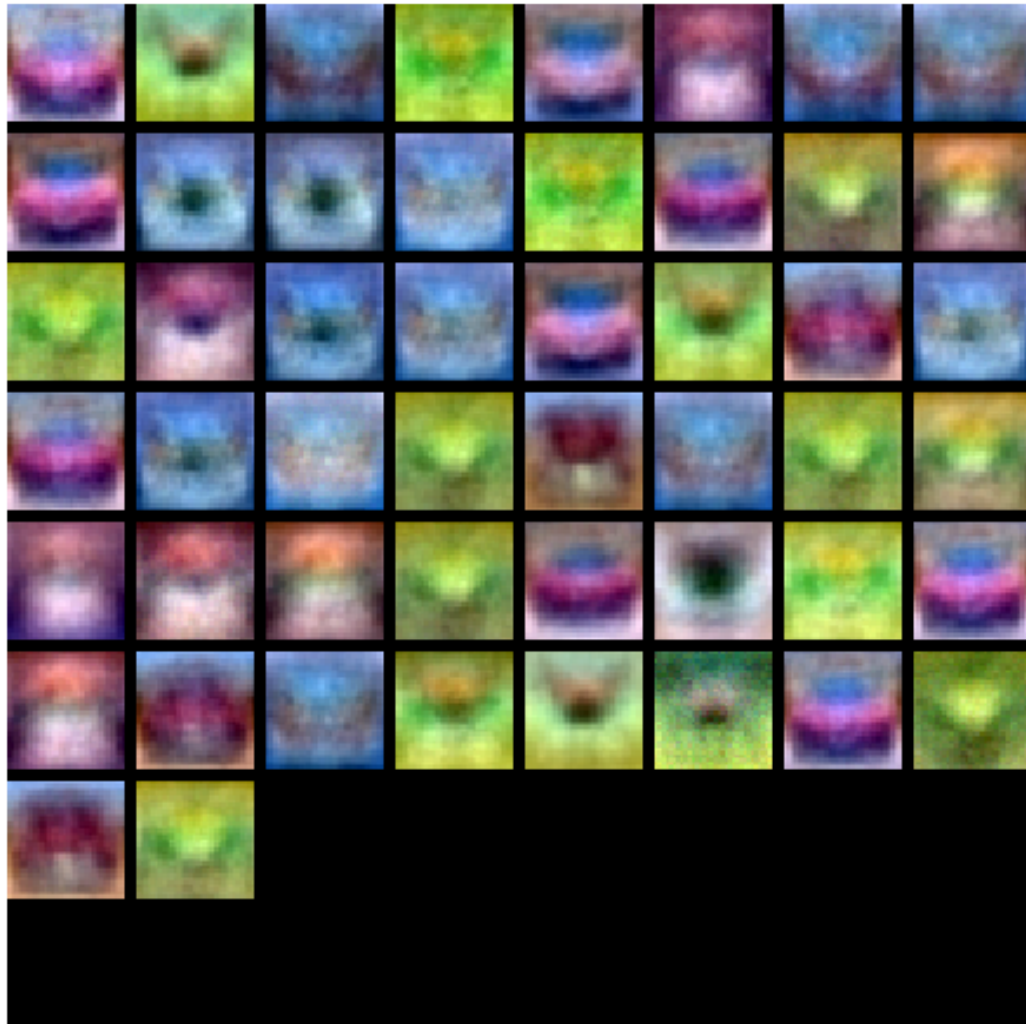


```
In [61]: from cs231n.vis_utils import visualize_grid
```

```
# Visualize the weights of the network

def show_net_weights(model):
    plt.imshow(visualize_grid(model['W1'].T.reshape(-1, 32, 32, 3), padding=3).astype
    plt.gca().axis('off')
    plt.show()

show_net_weights(model)
```



9 Tune your hyperparameters

What's wrong?. Looking at the visualizations above, we see that the loss is decreasing more or less linearly, which seems to suggest that the learning rate may be too low. Moreover, there is

no gap between the training and validation accuracy, suggesting that the model we used has low capacity, and that we should increase its size. On the other hand, with a very large model we would expect to see more overfitting, which would manifest itself as a very large gap between the training and validation accuracy.

Tuning. Tuning the hyperparameters and developing intuition for how they affect the final performance is a large part of using Neural Networks, so we want you to get a lot of practice. Below, you should experiment with different values of the various hyperparameters, including hidden layer size, learning rate, number of training epochs, and regularization strength. You might also consider tuning the momentum and learning rate decay parameters, but you should be able to get good performance using the default values.

Approximate results. You should be able to aim to achieve a classification accuracy of greater than 50% on the validation set. Our best network gets over 56% on the validation set.

Experiment: Your goal in this exercise is to get as good of a result on CIFAR-10 as you can, with a fully-connected Neural Network. For every 1% above 56% on the Test set we will award you with one extra bonus point. Feel free to implement your own techniques (e.g. PCA to reduce dimensionality, or adding dropout, or adding features to the solver, etc.).

```
In [1]: best_model = None # store the best model into this
```

```
#####
# TODO: Tune hyperparameters using the validation set. Store your best trained #
# model in best_model.                                                         #
#                                                                              #
# To help debug your network, it may help to use visualizations similar to the #
# ones we used above; these visualizations will have significant qualitative    #
# differences from the ones we saw above for the poorly tuned network.         #
#                                                                              #
# Tweaking hyperparameters by hand can be fun, but you might find it useful to #
# write code to sweep through possible combinations of hyperparameters        #
# automatically like we did on the previous assignment.                       #
#####
# input size, hidden size, number of classes
model = init_two_layer_model(32*32*3, 1000, 10)
trainer = ClassifierTrainer()
best_model, loss_history, train_acc, val_acc = trainer.train(X_train, y_train,
                                                             X_val, y_val,
                                                             model, two_layer_net,
                                                             num_epochs=10, reg=1e-3,
                                                             momentum=0.99,
                                                             learning_rate_decay=0.95,
                                                             learning_rate=3e-6, verbose=False)
#####
#                                     END OF YOUR CODE                         #
#####
```

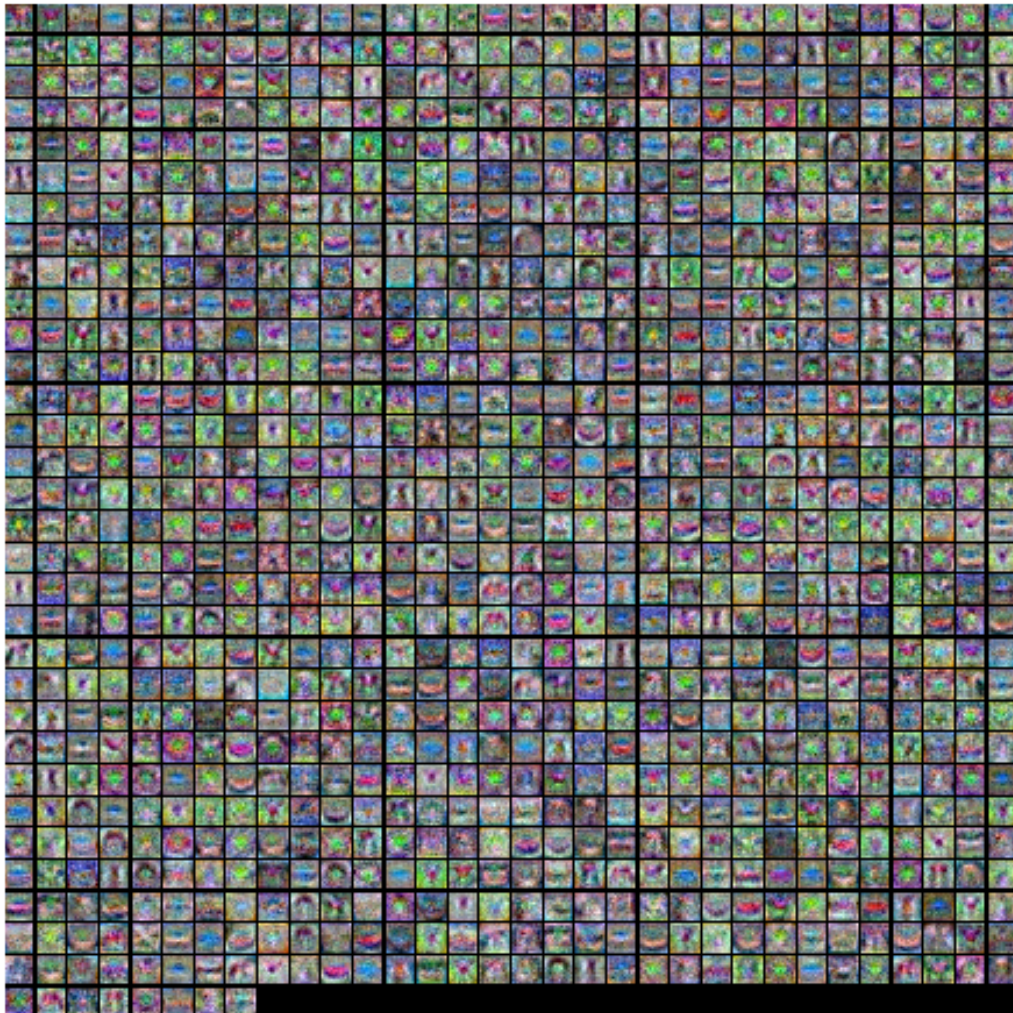
NameError

Traceback (most recent call last)

```
<ipython-input-1-97978f118412> in <module>()
 14 #####
 15 # input size, hidden size, number of classes
---> 16 model = init_two_layer_model(32*32*3, 1000, 10)
      17 trainer = ClassifierTrainer()
      18 best_model, loss_history, train_acc, val_acc = trainer.train(X_train, y_train,
```

NameError: name 'init_two_layer_model' is not defined

```
In [76]: # visualize the weights
show_net_weights(best_model)
```



10 Run on the test set

When you are done experimenting, you should evaluate your final trained network on the test set.

```
In [77]: scores_test = two_layer_net(X_test, best_model)
         print('Test accuracy: ', np.mean(np.argmax(scores_test, axis=1) == y_test))
```

```
Test accuracy:  0.516
```

```
In [ ]:
```