# Literature Review: Selection, QTL Mapping and Statistical Models

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2025-09-08

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## 18 1 Introduction

- Selective breeding has been an important tool for agriculture for a long time. It helped to develop crop varieties and livestock breeds with higher productivity, better resilience, and improved quality to meet the global demand for food (Falconer & Mackay, 1996; Godfray et al., 2010). However, traditional methods such as phenotypic selection, progeny testing, and backcrossing are slow and require many resources. They depend on observable traits, which are often influenced by the environment, and therefore provide only an indirect and delayed measure of genetic potential (Collard et al., 2005). So we introduce marker-assisted analysis to detect traits more efficiently and accurately.
- In genetics, selection means choosing individuals with desirable traits as parents to produce the next generation, so that favourable alleles are passed on. Falconer and Mackay (Falconer & Mackay, 1996) defined selection as the unequal reproduction of genotypes, caused either by environmental pressures, which we call natural selection, or by human choices, which we call artificial selection.

  Natural selection depends on environmental effects on survival and reproduction, while artificial selection depends on human intervention to improve traits of agricultural or economic importance.
- In plant and animal breeding, artificial selection is implemented through traditional methods such as phenotypic selection, progeny testing, and backcross breeding. There are three main traditional breeding methods.
- <sup>36</sup> Phenotypic selection chooses individuals based on observable traits or performance, but its accuracy is reduced because environmental effects can hide genetic differences (Collard et al., 2005).
- <sup>38</sup> **Progeny testing** uses the performance of offspring to evaluate the genetic value of parents; while
  <sup>39</sup> more reliable, it is expensive and time-consuming (Foster, 2006).
- Backcross breeding introduces a favourable allele from a donor into an elite background through repeated backcrossing, but it requires many generations and can transfer unwanted linked alleles as well (Wu et al., 2007).
- Therefore, traditional methods such as phenotypic selection, progeny testing, and backcross breeding have supported crop and livestock improvement but remain limited by environmental noise,

- high costs, and the need for many generations (Collard et al., 2005; Foster, 2006; Wu et al., 2007).
- 46 These inefficiencies emphasise the need for more precise and efficient approaches, leading to the
- 47 development of marker-assisted selection (MAS), which uses molecular markers to accelerate and
- 48 improve breeding accuracy.
- 49 Marker-assisted selection (MAS) is a newer strategy that helps overcome the limits of these tra-
- oditional methods. MAS uses DNA markers that are closely linked to genes of interest to guide
- 51 breeding decisions, allowing selection at early growth stages and independent of environmental
- variation (Collard et al., 2005; Hasan et al., 2021). Collard et al. (Collard et al., 2005) showed
- that MAS is especially effective for traits with low heritability or late expression. It is more precise,
- 54 reliable, and cost-effective than traditional methods. Hasan et al. (Hasan et al., 2021) also showed
- 55 that MAS can be used to combine multiple favourable alleles, making it a powerful tool for crop
- <sup>56</sup> and livestock improvement. However, the success of MAS depends on first identifying markers
- 57 that are tightly linked to quantitative trait loci (QTL), which are genomic regions associated with
- variation in complex traits (Mackay et al., 2009).
- 59 Detecting QTL makes it possible to connect molecular markers with important phenotypes, but
- this requires careful statistical analysis. The following Methods section will provide a more detailed
- 61 discussion of how QTL are defined and how statistical models are used to detect them.
- 62 In this report, Section 2 reviews statistical methods for detecting QTL, highlighting their strengths
- and limitations, while Section 3 presents discussion and conclusion.

## 64 2 Method

- 65 This section introduces the statistical models that are commonly used to detect quantitative trait
- 66 loci (QTL). We begin with the single marker model, which tests the effect of one marker at a time,
- 67 and then turn to the multiple marker model, which incorporates several markers simultaneously
- to increase power. Multiple marker models, however, often face challenges such as collinearity,
- 69 where markers are strongly correlated, and high dimensionality, where the number of markers is

much larger than the number of samples. To address these issues, we also review model selection strategies, including stepwise procedures, Bayesian shrinkage, and penalised regression methods.

#### 72 Statistical method for detecting QTL

QTL analysis uses data that combine marker genotypes with phenotypic measurements. Genotypes are often coded numerically (for example, 0 = homozygous for one allele and 1 = homozygous for the other allele), which makes it possible to apply statistical models directly (Mackay et al., 2009).

Because the whole genome sequencing is very expensive, QTL are usually identified indirectly through linkage disequilibrium between observed markers and unobserved causal loci (Collard et al., 2005).

A quantitative trait locus (QTL) is formally defined as a chromosomal region containing one or more loci that contribute to variation in a quantitative trait (Mackay et al., 2009). QTL are not necessarily single genes; they are often larger genomic regions that contain multiple genes influencing complex traits such as yield or disease resistance (Collard et al., 2005). Since QTL cannot be observed directly, their effects must be inferred statistically by testing associations between marker genotypes and phenotypic outcomes in a mapping population. Statistical models provide the framework for this inference by decomposing the phenotype into genetic and environmental components and by quantifying how strongly marker genotypes predict trait values (Falconer & Mackay, 1996).

At their core, these models specify the relationship between a phenotypic response variable and explanatory variables that represent marker genotypes. A general form of the model is:

$$y_i = \beta_0 + \beta_G G_i + \beta_E E_i + \beta_{GE} (G_i \times E_i) + \epsilon_i,$$

90 where

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- $y_i$  is the phenotype of the *i*-th individual (for example, plant height or yield)
  - $\beta_0$  is the intercept, representing the overall mean of the phenotype

- $G_i$  is the genetic effect, and  $\beta_G$  is the regression coefficient for the genetic effect
- $E_i$  is the environmental effect, and  $\beta_E$  is the regression coefficient for the environmental effect
- $G_i \times E_i$  is the interaction between genotype and environment, and  $\beta_{GE}$  is the coefficient for this interaction
  - $\epsilon_i$  is the residual error term, which captures random variation not explained by the model
- For the purposes of this study, the model is simplified to focus only on the genetic contribution to phenotypic variation:

$$y_i = \beta_0 + \beta_G G_i + \epsilon_i.$$

This simplification assumes that environmental effects and genotype–environment interactions are negligible. As a result, the analysis considers only the phenotypic variance explained by genetic effects, while the residual term still accounts for unexplained variation.

## 2.1 Single Marker Model

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In this study, we focus on a backcross (BC) population, which is generated by crossing an F1 hybrid back to one of its parental lines. In the illustrated scheme, an individual homozygous for allele A (blue, with a star marker) is crossed with an individual homozygous for allele C (orange, with a star marker). The F1 generation inherits one allele from each parent and is then crossed again with the recurrent parent carrying allele C. The backcross design is introduced here because the single-marker model is formulated using the segregation pattern of this experimental population.

As shown in Figure 1, recombination between the marker locus and the putative QTL occurs with probability c, the recombination frequency. The resulting BC1 progeny segregate into four possible genotypes:

Probability	Genotype type	Genotypic value
$\frac{1}{2}(1-c)$	Non-recombinant	$\overline{d}$

Probability	Genotype type	Genotypic value
$\frac{1}{2}(1-c)$	Alternate non-recombinant	a
$\frac{1}{2}c$	Recombinant	a
$\frac{1}{2}c$	Recombinant	d

The expected phenotypes for the QTL genotypes are

$$\mu_{Qq} = d, \qquad \mu_{qq} = a,$$

where a is the mean for qq, and d is the mean for Qq. The difference (d-a) reflects the effect of the QTL.

#### 2.1.1 Mean Difference between Genotypes

In QTL analysis, the relationship between a marker and a QTL can be described using the recombi-117 nation frequency (c), which measures how often crossover occurs between loci. The recombination 118 frequency (c) not only shows how strong the linkage is between two loci, but it can also be used to 119 build a genetic map. By turning the recombination rate between markers into genetic distance mea-120 sured in centimorgans (cM), and using LOD scores to test if the linkage is significant, researchers 121 can place markers in order along the chromosome (Collard et al., 2005). When c=0, the loci 122 are completely linked; when c = 0.5, they segregate independently (Falconer & Mackay, 1996). In 123 practice, markers that are tightly linked to a QTL act as useful proxies because recombination 124 is rare (Mackay et al., 2009). Based on these recombination probabilities, we can calculate the 125 expected phenotypic mean for each genotype. Starting from the joint population frequencies shown 126 in the scheme (each haplotype has probability  $\frac{1}{2}(1-c)$  or  $\frac{1}{2}c$ ), where M represents for Marker AC 127 or CC. The conditional mean for the AC class is 128

$$\mu_{AC} = \mathbb{E}[Y \mid M = AC] = \frac{\frac{1}{2}(1-c)\,d + \frac{1}{2}c\,a}{\frac{1}{2}} = (1-c)\,d + c\,a.$$

## Formation of F1 and BC populations

Figure 1: Formation of F1 and backcross (BC) populations. Parents (P) are homozygous for different alleles (A with white star, C with yellow star). Their cross produces F hybrids (AC), which are then crossed back to the C parent to produce a BC population.

129 Similarly, for the CC class,

$$\mu_{CC} = \mathbb{E}[Y \mid M = \text{CC}] = \frac{\frac{1}{2}(1-c)\,a + \frac{1}{2}c\,d}{\frac{1}{2}} = (1-c)\,a + c\,d.$$

Hence the **mean difference** between the two marker classes is

$$\Delta = \mu_{AC} - \mu_{CC} = \left[ (1-c) \, d + c \, a \right] - \left[ (1-c) \, a + c \, d \right] = (d-a)(1-2c).$$

- where  $\Delta$  represents the expected phenotypic difference between the two genotypes.
- This shows that when (d-a)=0, there is no genetic effect, and when c=0.5, the marker and
- QTL are unlinked (Yang, 2019). The difference  $\Delta$  can also be written in a regression framework,
- which will be disscussed below.

#### 2.1.2 Univariate Regression

The difference  $\Delta$  is essentially the average effect of the marker on the phenotype. In statistical terms, this corresponds to the regression coefficient  $\beta$  in a simple linear regression model. Thus, the regression framework provides a formal way to test the same biological relationship.

In a BC population with only two genotypes (AC and CC), the single marker regression model is:

$$y_i = \mu + \beta G_i + \epsilon_i,$$

where  $G_i$  is coded as 0 for AC and 1 for CC, and  $\beta \equiv \Delta$ . This formulation allows us to test whether  $\beta$  ( $\Delta$ ) differs significantly from zero using a t-test (Foster, 2006), providing a straightforward way to evaluate marker–QTL association.

It shows how recombination frequency and genetic effects can be translated into a simple linear model that links marker genotype with phenotype.

#### 146 2.1.3 Mixture Distribution

While the regression model summarises genotype differences using mean values, it assumes normally distributed residuals within each genotype. In practice, phenotypic distributions may be more complex. To capture this, mixture models extend the analysis by modelling the full distribution of phenotypes conditional on marker genotypes.

In a BC1 population, we assume there is a single QTL linked to the marker with recombination frequency c. Because the BC design involves crossing an F1 heterozygote (Qq) with a homozygous recessive parent (qq), the possible QTL genotypes among the progeny are Qq and qq. Under this assumption (Figure 2), the conditional probabilities of QTL genotype given the observed marker genotype are:

Marker genotype	QTL genotype	Probability
AC	Qq	1-c
AC	qq	c
CC	Qq	c
CC	qq	1-c

156 (Foster, 2006, p. 15).

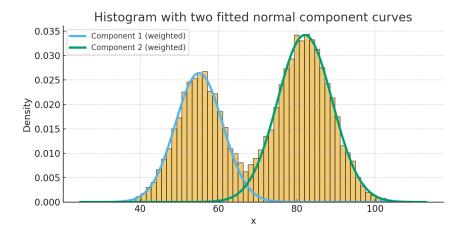


Figure 2: Density plot showing an example of two-state Gaussian mixture distribution. In the backcross experiemnt we demonstrated these two states corresponds to two hidden genotype of the QTL: Qq and qq.

The phenotype density conditional on marker genotype is defined as:

$$f(y\mid AC) = (1-c)\,\varphi\big(y;\mu_{Qq},\sigma^2\big) + c\,\varphi\big(y;\mu_{qq},\sigma^2\big)$$

$$f(y\mid CC) = c\,\varphi\big(y;\mu_{Qq},\sigma^2\big) + (1-c)\,\varphi\big(y;\mu_{qq},\sigma^2\big)\,.$$

Here, y denotes the observed phenotype of an individual (e.g., plant height or yield).  $\mu_{Qq}$  and  $\mu_{qq}$  are the expected phenotypic means for QTL genotypes Qq and qq, respectively.  $\sigma^2$  is the residual

variance, which captures variation not explained by genotype, such as environmental effects or measurement error. The function  $\varphi(y \mid \mu, \sigma^2)$  is the normal density:

$$\varphi(y \mid \mu, \sigma^2) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left(-\frac{(y-\mu)^2}{2\sigma^2}\right).$$

The overall phenotypic distribution is therefore a two-state normal mixture (Foster, 2006; Wu et al., 2007).

The single marker model provides a simple and intuitive framework for QTL detection. By comparing the phenotypic means of different marker classes in a backcross population, we can express
their difference as  $\Delta = (d-a)(1-2c)$  and reformulate this difference as the regression coefficient  $\beta$  in a univariate regression. This model is powerful for illustrating the basic relationship between
markers and QTL, and it can be tested statistically using a t-test. However, its main limitation is
that it considers one locus at a time and does not control for the effects of other loci. As a result,
spurious associations may occur and true QTL effects may be underestimated.

## 171 2.2 Multiple Marker Model

In contrast to single-marker analysis, which tests one locus at a time, the multiple marker model simultaneously incorporates information from several markers across the genome into a linear regression framework. This approach improves statistical power by accounting for background loci and reduces spurious associations that may arise when only one marker is analysed in isolation.

Formally, the model can be expressed as:

$$y_i = \mu + \sum_{j=1}^m \beta_j G_{ij} + \epsilon_i,$$

177 where

•  $y_i$  is the phenotypic value of the *i*-th individual

- $G_{ij}$  denotes the coded genotype of the j-th marker for the i-th individual (for example, 0/1 coding for backcross populations; 0/1/2 coding for  $F_2$  populations)
- $\beta_j$  represents the partial regression coefficient, capturing the effect of marker j conditional on the presence of other markers in the model
- $\mu$  is the overall mean
- $\epsilon_i \sim \mathcal{N}(0, \sigma^2)$  denotes the residual error term, assumed to follow an independent and identically distributed normal distribution.

In multiple marker models, traditional methods include stepwise regression and model choice based 186 on information criteria such as the Akaike Information Criterion (AIC) and the Bayesian Infor-187 mation Criterion (BIC). In recent years, penalised regression methods have become more common. 188 Ridge regression uses an  $\ell_2$  penalty to shrink coefficients and produce more stable results when 189 markers are highly correlated (Ogutu et al., 2012). The LASSO method applies an  $\ell_1$  penalty, 190 which both selects important variables and controls their size (Li & Sillanpää, 2012). The elastic 191 net combines  $\ell_1$  and  $\ell_2$  penalties. This gives a balance between variable selection and stability, and 192 works well in high-dimensional data where markers show strong correlation (Brault et al., 2021; 193 Zou & Hastie, 2005). 194

we will introduce each of these methods in details for the rest of the section.

#### 196 2.2.1 Stepwise Selection

A classical approach to variable selection is stepwise regression, in which markers are iteratively added or removed from the model according to predefined criteria. In practice, the AIC and BIC are widely used to select the model that minimises information loss:

$$AIC = -2 \log L + 2k$$
,  $BIC = -2 \log L + k \log n$ ,

where L is the likelihood of the model, which is a measure of how well the model fits the data, kthe number of parameters, and n the sample size. Stepwise procedures are computationally straightforward and interpretable. However, they are known to be unstable in high-dimensional genomic contexts and fail to account for model uncertainty, often leading to overconfident inference (Foster, 2006).

#### 5 2.2.2 Bayesian Shrinkage

A more flexible alternative is Bayesian shrinkage, in which regression coefficients are assigned hierarchical priors that adaptively control the degree of shrinkage for each marker. For marker effect  $\beta_j$ , a zero-mean normal prior is assumed:

$$\beta_j \sim \mathcal{N}\left(0, \frac{\sigma^2}{\lambda_j}\right),$$

where  $\lambda_j$  is a marker-specific precision parameter. To complete the hierarchy, a Gamma prior is placed on  $\lambda_j$ :

$$\lambda_i \sim \text{Gamma}(a, b).$$

where a and b are hyperparameters that control the shape of the Gamma prior.

In the normal–gamma prior, the size of  $\lambda_j$  controls the amount of shrinkage. A larger  $\lambda_j$  produces stronger shrinkage, which pulls  $\beta_j$  closer to zero, while a smaller  $\lambda_j$  allows  $\beta_j$  to take larger values. In this way, Bayesian shrinkage creates adaptive sparsity. In simple terms, adaptive sparsity means the method automatically removes many unimportant markers and keeps only the ones that really explain the trait. This makes the model simpler, more accurate, and especially useful for QTL mapping across the whole genome(Xu, 2003).

#### 2.2.3 Penalised Regression: Ridge, LASSO, and Elastic Net

Penalised regression provides a frequentist alternative to Bayesian shrinkage by adding penalty terms to the usual regression problem. The general form is:

$$\min_{\beta} \sum_{i=1}^{n} \left( y_i - \sum_{j=1}^{p} G_{ij} \beta_j \right)^2 + \lambda_1 \sum_{j=1}^{p} |\beta_j| + \lambda_2 \sum_{j=1}^{p} \beta_j^2,$$

221 where

- $y_i$ : the phenotype value of the *i*-th individual.
- $G_{ij}$ : the genotype code of the *i*-th individual at the *j*-th marker (for example, coded as 0/1 in a backcross population, or 0/1/2 in an  $F_2$  population).
- $\beta_j$ : the regression coefficient for the *j*-th marker, which shows the partial effect of that marker on the phenotype.
- $\sum_{i=1}^{n} \left(y_i \sum_{j=1}^{p} G_{ij}\beta_j\right)^2$ : the residual sum of squares. It measures how far the model predictions are from the observed phenotype values.
- $\lambda_1 \sum_{j=1}^p |\beta_j|$ : the L1 penalty (the LASSO part).
- $\lambda_1, \lambda_2$ : the hyperparameters that control the strength of the two penalties.
- p: the total number of markers in the dataset.
- n: the total number of individuals in the population.
- Ridge regression ( $\lambda_2 > 0, \lambda_1 = 0$ ): shrinks all coefficients toward zero but never exactly zero. It helps when markers are highly correlated (linkage disequilibrium), but it does not perform variable selection.

- LASSO ( $\lambda_1 > 0, \lambda_2 = 0$ ): uses the L1 penalty, which forces some coefficients to become exactly zero. This makes it useful for variable selection, but it can be unstable when markers are strongly correlated.
- Elastic net  $(\lambda_1 > 0, \lambda_2 > 0)$ : combines both penalties. The L2 part groups correlated markers together, while the L1 part keeps sparsity by removing irrelevant variables. Elastic net is especially suitable for genomic data where many markers are correlated in LD blocks (Wu et al., 2007).

In summary, stepwise selection, Bayesian shrinkage, and penalised regression represent complementary strategies for addressing the limitations of multiple marker models. Stepwise methods are simple but unstable; Bayesian shrinkage provides adaptive, marker-specific shrinkage; and penalised regression approaches offer computationally efficient solutions for high-dimensional problems, with the elastic net providing the most balanced performance in the presence of strong marker correlations.

## 50 3 Discussion and Conclusion

This review showed how breeding methods developed from selection that relies only on observable traits to MAS, and then to statistical models for QTL detection. The examples of the single marker and the multiple marker models show both progress and limits. The single marker model is simple and easy to follow, but it tests one locus at a time, so it has problems with noise from other loci and does not work well when loci are linked. The multiple marker model uses several loci together, which solves part of this problem, but it also creates new issues such as strong correlation between markers and too many variables when the number of markers is large.

These issues are not only theory, when we put them into practice. For traits with low heritability,
the signal of a QTL is weak and often hidden by effects from the environment. This makes the
average difference between genotypes very small and increases false negatives in QTL studies. In
this case, using the same number of individuals as for traits with high heritability is not enough.

Future studies should ask how many individuals are needed to detect QTL with enough power under different levels of heritability. For some traits, it may be necessary to use multiple times more individuals to separate weak genetic signals from environmental effects.

For methods, one possible improvement is to extend the multiple marker model beyond simple 265 regression. Compared with simple regression models, mixture models are more useful for traits that are controlled by many loci. In polygenic traits, most loci only have very small effects, while a 267 few loci may have larger effects. In such cases, we may consider using genetic selection, which is a 268 method that selects individuals mainly based on their observed phenotype and pedigree information. A simple regression model forces all loci to follow one type of effect, which can hide this difference. 270 Mixture models allow different effect sizes across loci, so they give a picture that is closer to the 271 real biology of polygenic traits. Penalised regression is also important when many markers are 272 strongly correlated, which happens in linkage disequilibrium (LD) blocks. In these blocks, markers 273 carry similar information and simple regression can become unstable. By adding penalty terms, 274 penalised regression can shrink or remove some effects while keeping groups of correlated markers 275 together. This makes the model more stable and better suited for high-dimensional genetic data. By linking the choice of model and the design of sample size to the biological reality of traits with 277 low heritability, QTL studies can move beyond general frameworks and give stronger guidance for 278 modern breeding research.

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