

**Opened:** Saturday, 11 February 2023, 12:00 AM

**Due:** Friday, 1 March 2024, 11:59 PM

**This assignment is worth 9% of the overall weight.**

**Submission guidelines:**

For this assignment, you have to implement your code in the [provided template scripts](#). These scripts include code to load images and plot the outputs. Make sure you complete all of the TODO statements, and that your output matches the expected.

**In this assignment, you will perform color image reconstruction using Bayer pattern and color reproduction using Dithering.**

**(I) BasicBayer (25%):** In this part, you will reconstruct [this RGB color image](#) (this original color image is only for your reference, you will not use it inside your code) given a corresponding [Bayer pattern image](#) (your code takes the [Bayer pattern](#) as input). The Bayer pattern used is GRBG.

Your task is to reconstruct green, red and blue channels from the Bayer pattern image using these [Green](#), [Red](#), and [Blue](#) image masks, where black and white vertices respectively represent valid and empty entries. These masks together form the Bayer color pattern, viz., GRBG.

You should complete [the provided template python script](#) to interpolate the empty entries in the reconstructed green, red and blue channels independently of each other. Next, combine these channels into a full RGB color image and display this image.

Details about Bayer filter and the reconstruction process are provided in the presentation [Bayer Filter and Demosaicing.pdf](#). You can also refer to the Wikipedia pages on [Bayer filter](#) and [demosaicing](#).

In case you are interested in even more details, here's a nice reference: <http://www.site.uottawa.ca/~edubois/lsld/>

**Note:** This assignment requires you to implement a modified version of the interpolation algorithm, where values from **all** valid neighbours (shaded pixels in the mask) are averaged.

**As a simple scheme of pixel interpolation, you can follow these rules:**

- For reconstruction of the green channel IG with respect to the pattern [Green](#), the values at empty locations can be interpolated as:
  - $B = (A+C+F)/3$
  - $D = (C+H)/2$
  - $G = (F+C+H+K)/4$ , etc.
- For reconstruction of the red channel IR with respect to the pattern [Red](#), use these rules:
  - $C = (B+D)/2$
  - $F = (B+J)/2$
  - $G = (B+D+L+J)/4$ , etc.

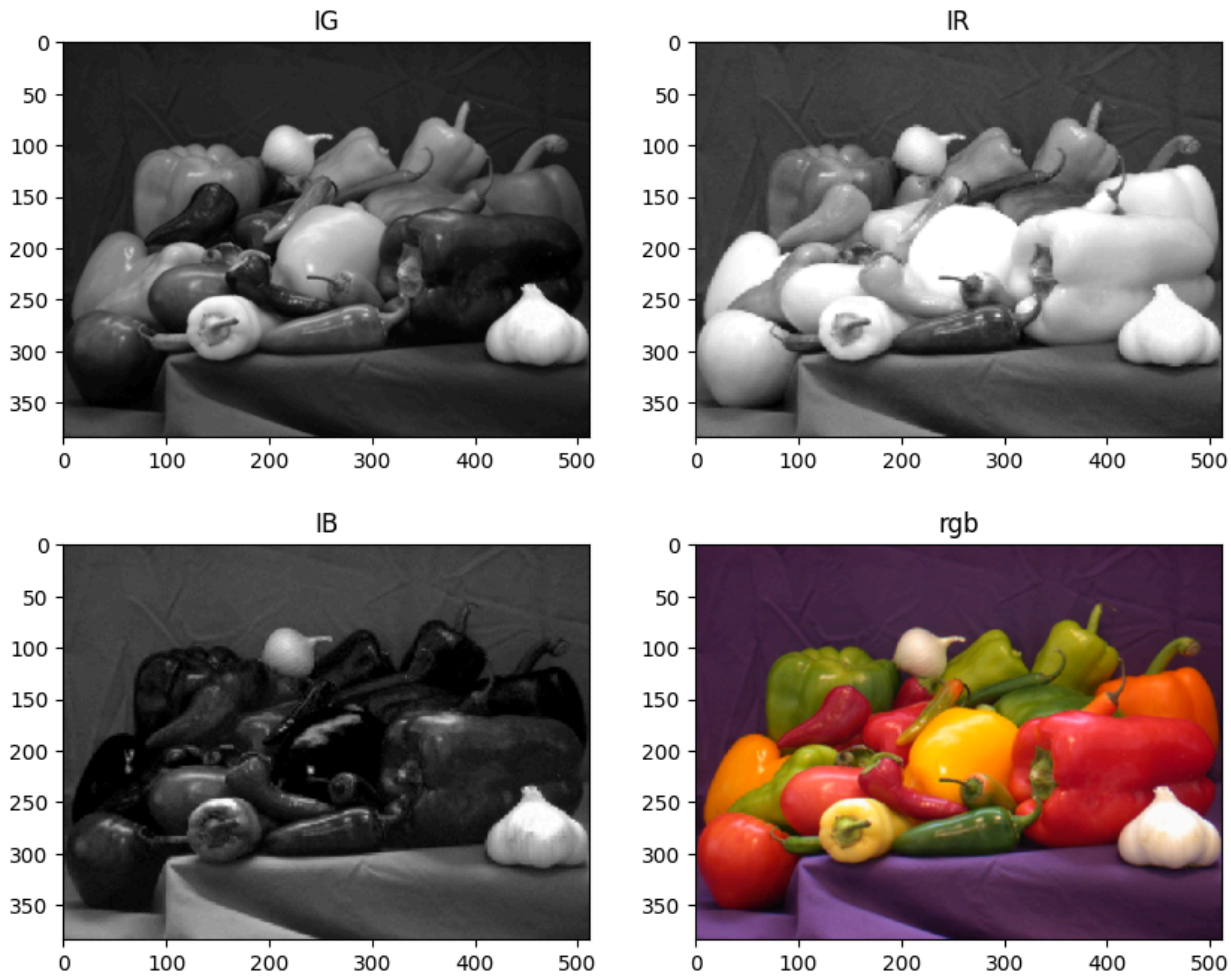
Note that the first column and the last row are entirely empty. You need to fill them in by copying the second column and the second last row, respectively.

- For reconstruction of the blue channel IB with respect to the pattern [Blue](#), use these rules:
  - $F = (E+G)/2$
  - $I = (E+M)/2$
  - $J = (E+G+O+M)/4$ , etc.

Note that here the last column and the first row are entirely empty. You need to fill them by copying the second row and the second last column respectively.

?

**Expected output:**



## (II) Floyd-Steinberg dithering (25%):

Complete [the provided template python script](#) to read [this RGB image](#) and implement [Floyd-Steinberg dithering](#) algorithm to change the representation of this image.

The original algorithm uses the error distribution on the left, **but you need to implement the one on the right**:

x	x	x
x	@	7/16
3/16	5/16	1/16

x	x	x
x	@	11/26
5/26	7/26	3/26

The template script:

- Dynamically calculates an N-colour palette for the given image (in the notebook the variable nColours determines the number of colours in the palette).
- Uses the KMeans clustering algorithm to determine the best colors.
- Makes a kd-tree palette from the provided list of colors.
- Applies [the Floyd-Steinberg](#) method to change the representation of the image.

More details about Dithering techniques can be found in the Wikipedia pages on [Dither](#) and [Palette](#).

### Hints:

- Check if x and y are within the image bounds for each pixel location

- Perform the action on each colour channel.

**Expected output:**

colours:

[[0.91219912 0.3257617 0.21832768]

[0.70676912 0.72203413 0.68072663]

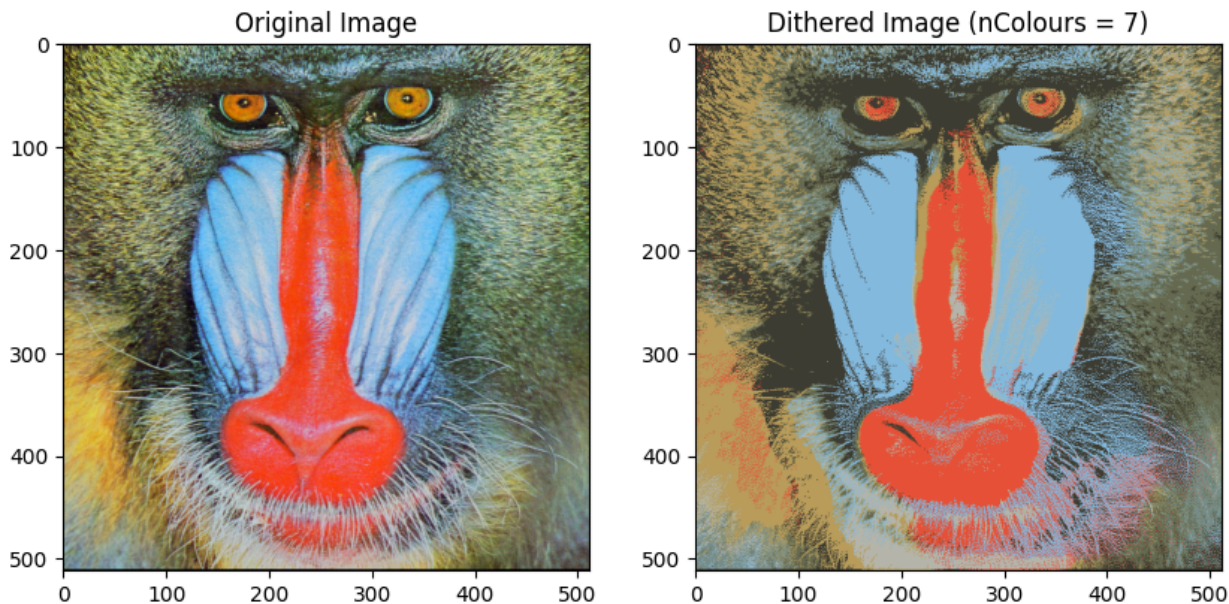
[0.41088001 0.42779406 0.31911404]

[0.52587285 0.73030921 0.87671832]

[0.24926086 0.24574098 0.20012105]

[0.47650788 0.56045069 0.53032372]

[0.7265762 0.62201352 0.36742985]]



Note that you need to adjust the parameters of [sklearn.cluster.KMeans](#) till you get the colors given above. Also, the colours found by K-Means depend on the version of scikit-learn so if you are running the code on your own machine, make sure that it has a same python version as colab (1.2.2). You can install it by running: `pip install scikit-learn==1.2.2`

**(III) Affine Transformation (25%):**

In this part, you will perform image rotation, scaling, and skewing which are specializations of affine transformation.

You should complete [the provided template python script](#).

In parts 1 - 4 you are required to create and apply the transformations using your own code. **You are not allowed to use built-in functions like [skimage.transform.warp](#) for this purpose.**

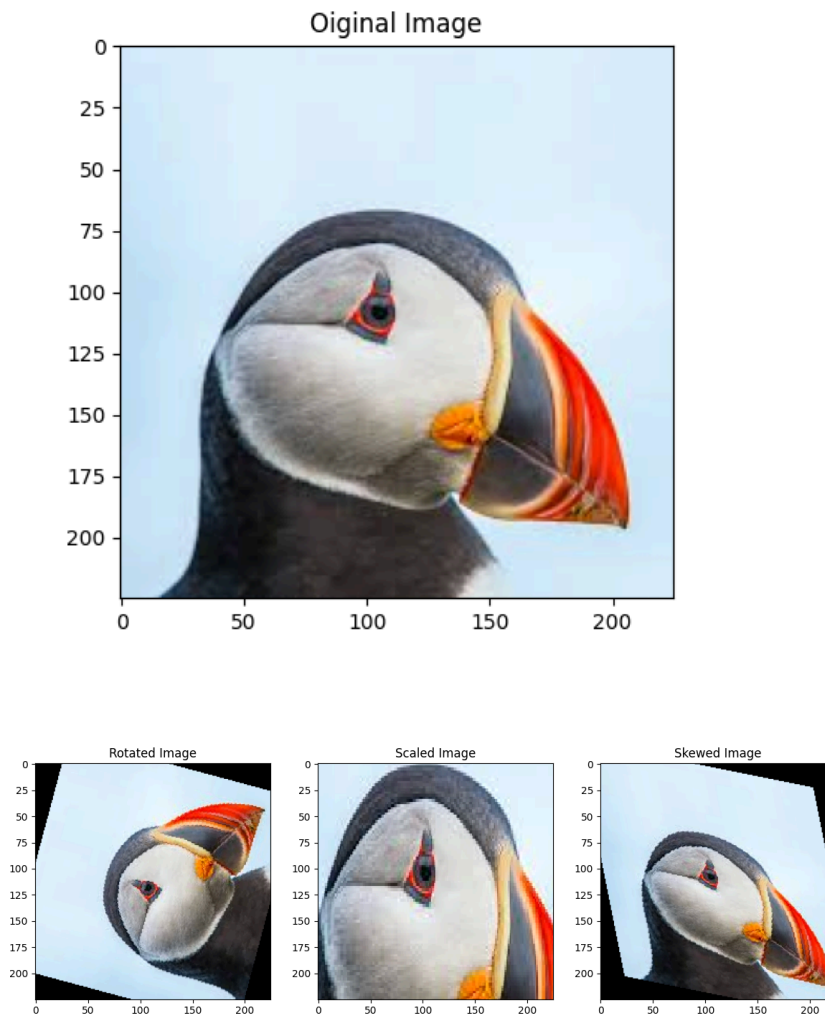
You need to iterate over the pixel locations of the output image ( $[x_{out}, y_{out}]$ ), find the corresponding location in the input image using the inverse transform ( $[x_{in}, y_{in}] = \text{inverse-transform}(x_{out}, y_{out})$ ), and fill in that pixel value in the output image ( $\text{output}[x_{out}, y_{out}] = \text{input}[x_{in}, y_{in}]$ ).

Note that the obtained  $[x_{in}, y_{in}]$  are likely floating point values so you can simply take the floor of the obtained values ( $[\text{int}(x_{in}), \text{int}(y_{in})]$ ).

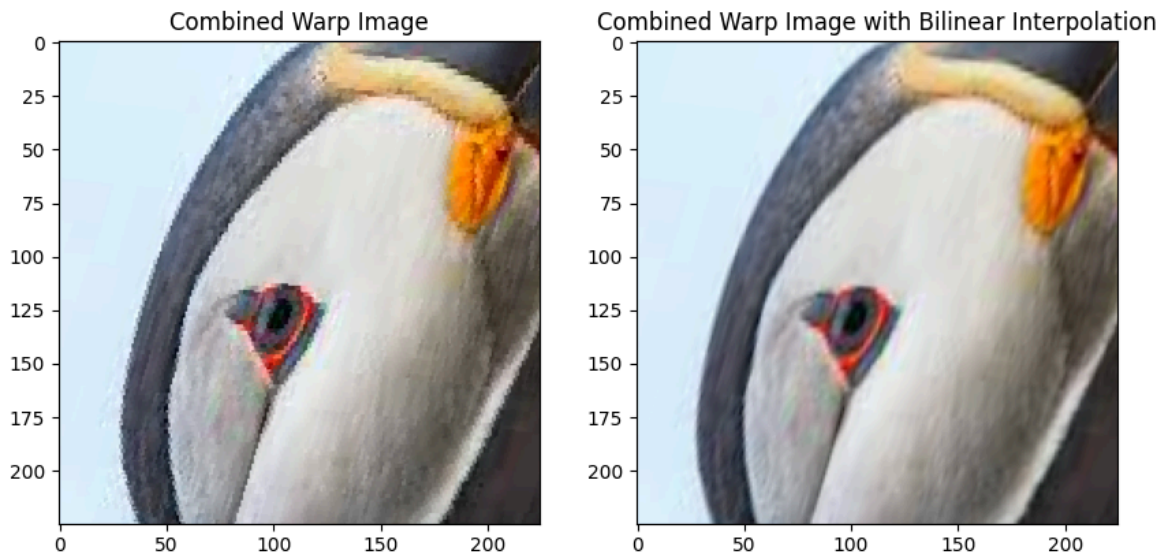
In part 5, you will use [skimage.transform.warp](#) to obtain the pixel values at the exact floating point coordinates  $[x_{in}, y_{in}]$  using [bilinear interpolation](#) over the neighbouring pixels rather than simply taking the pixel value at  $[\text{int}(x_{in}), \text{int}(y_{in})]$ .

Read [this](#) color image as the input image, and apply the following transformations to the input image independently (not sequentially).

1. A [Rotation transformation](#) matrix  $T_r$  (75 degrees counter-clockwise).
2. A [Scale transformation](#) matrix  $T_s$  which scales the placement of the points by 1.5 times in the x-direction and 2.5 times in the y-direction.
3. A Skew transformation with parameter = 0.2 in both directions.
4. Combination of the transformations in 1, 2, and 3: Affine transformation is equivalent to a linear transformation (i.e. multiplying the vectors in [homogeneous coordinates](#) by the [augmented matrix](#)). So to combine different affine transformations one can multiply the 3x3 matrices of each transformation to arrive at a single 3x3 matrix that corresponds to the combination of the transformations. To demonstrate this, apply the dot product (matrix multiplication) of the previous three transformation matrices to the input image.
5. The above implementation of backwards mapping diminishes the quality of the original image due to the rounding off errors in the floating point coordinates, To address this, apply the combined transformation of part 4 to the input image using [skimage.transform.warp](#) through **bilinear interpolation**. To choose between different interpolation methods, you can pass the argument 'order' to [skimage.transform.warp](#).

**Expected outputs:**





#### (IV) Image stitching by feature-matching (25%):

In this part, you will perform image stitching by completing [this template code](#) and using the images [im1](#) and [im2](#) as inputs. The resulting stitched image should look similar to [this](#).

The feature-matching algorithm for image stitching that you need to implement can be briefly summarized as follows:

**Step 1)** Detect local features with [BRISF](#) or [ORB](#) in the two images  $I_1$  and  $I_2$ . You can also use any other feature extractors like [SIFT](#) or [SURE](#).

**Step 2)** Perform feature matching between  $I_1$  and  $I_2$ , based on (approximate) nearest neighbour search, to generate a set of putative matching feature pairs. Usually, the similarity or distance between two feature descriptors is considered as the metric for matching. For this step you should use [skimage.feature.match\\_descriptors](#). This function allows for basic heuristics to better handle ambiguous matches and potentially discard outliers. In particular, when calling [skimage.feature.match\\_descriptors](#) you should set the argument `'cross_check'` to True and the argument `'max_distance'` to a proper value that you can find by hand-tuning. In any case a lot of outliers (i.e. wrong matches) will be selected in this step and step 3 will handle them.

**Step 3)** A [homography matrix](#) is a 3-by-3 matrix that defines the transformation between the two images, i.e.,

$$H_{12} * [x_1, y_1, 1]^T = w * [x_2, y_2, 1]^T$$

where  $(x_1, y_1)$  and  $(x_2, y_2)$  are the image coordinates of the matching features in the two images,  $H_{12}$  is the homography matrix and  $w$  is a scalar.

Compute the homography matrix between  $I_1$  and  $I_2$  based on the matches found in step 2 using the [RANSAC](#) algorithm implemented by [skimage.measure.ransac](#). The [RANSAC](#) algorithm is a good choice to find the homography matrix because there are a lot of outlier matches and [RANSAC](#) can handle a lot of outliers. In this step, you may need to hand-tune the parameters of [skimage.measure.ransac](#) so the output of your code becomes consistent and stable.

**Step 4)** Perform image stitching based on the homography matrix found in step 3. For this, you will need to calculate the new image coordinates for every pixel in  $I_1$ , with respect to  $I_2$  coordinate system. If  $H_{12}$  is calculated correctly, you should expect that after transformation, the features in  $I_1$  now have the same coordinates to their corresponding features in  $I_2$ , i.e., they are translated to the matching places.

The resulting stitched image should look similar to [this](#).

Finally, randomly select 10 of the found inlier matches (as returned by the RANSAC algorithm in step 3), and show them using [skimage.feature.plot\\_matches](#). The expected output is provide below at the end.

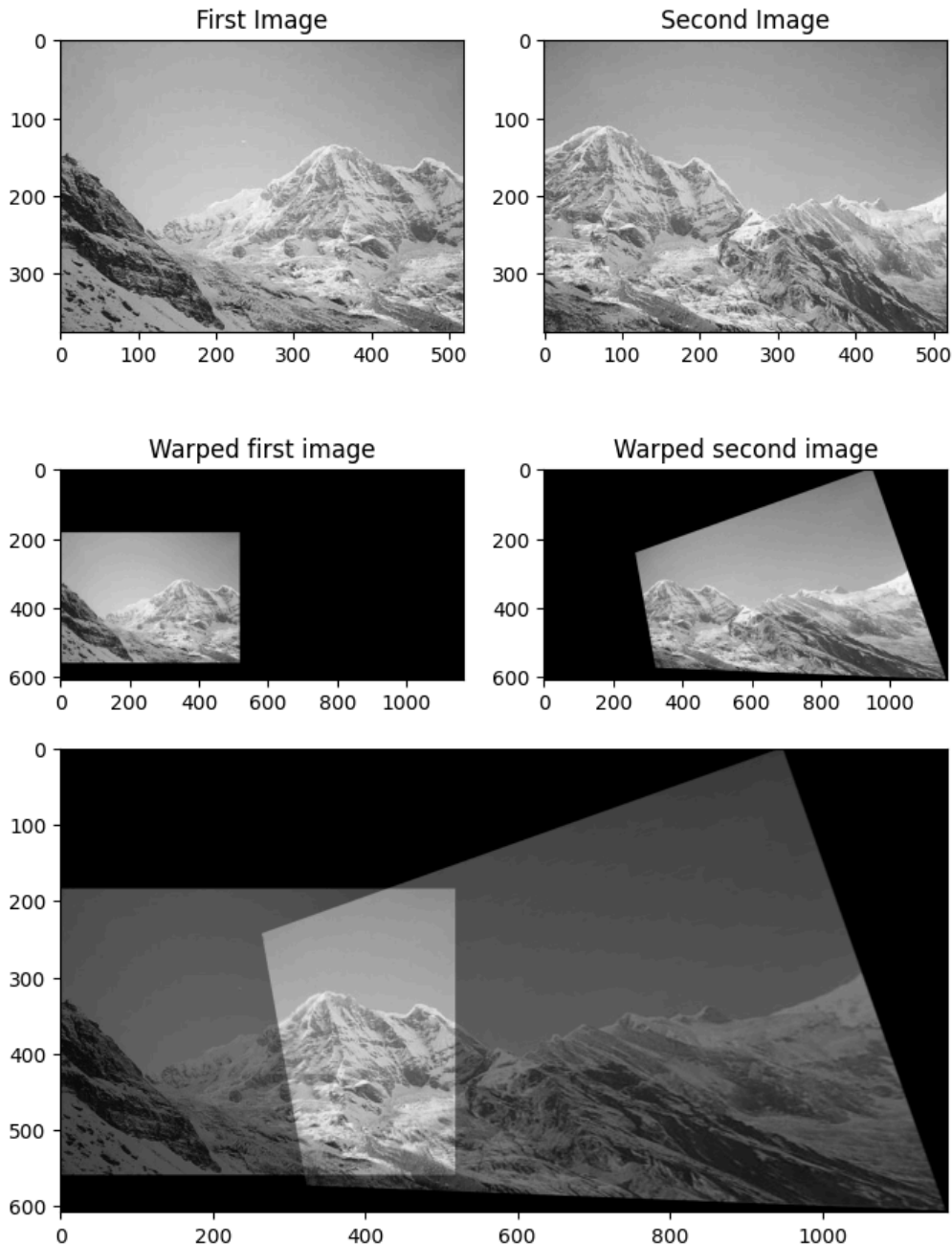
Note that steps 3) and 4) could be correlated. To decide the inliers, we need a model  $H$  to see if the matches fit it. On the other hand, to obtain  $H$ , we need sufficient true matches to complete the estimation. This is a chicken-egg problem. Refer to [RANSAC](#) if you are interested.

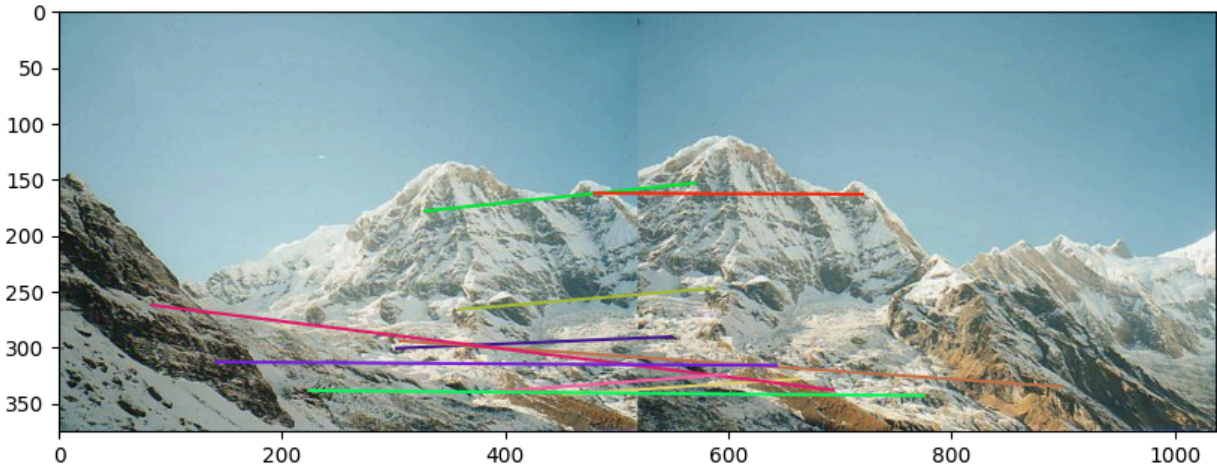
When calculating the new image coordinates, try to avoid using loops to access every pixel since matrix operations are usually much faster than loops.

To make this step easier you time, a reference implementation of stitching with detailed comments is available in the provided code. You can use it in your code (but may need to modify a bit). You are also welcome to develop your own implementation too.

**Note, you need to run your implementation multiple times to make sure the results of ransac are consistent. If they are not, tweak the parameters so that the results become consistent.**

**Expected output:**





Add submission

Submission status

Attempt number	This is attempt 1.
Submission status	No submissions have been made yet
Grading status	Not graded
Time remaining	2 days 18 hours remaining
Last modified	-
Submission comments	<div>► <a href="#">Comments (0)</a></div>